

Birla Institute of Technology & Science, Pilani  
Work-Integrated Learning Programmes Division  
Second Semester 2020-2021  
M.Tech (Data Science and Engineering)  
Mid-Semester Test (Makeup)

Course No. : DSECLZG525

Course Title : Natural Language Processing

Nature of Exam : Open Book

Weightage : 30%

No. of Pages	= 3
No. of Questions	= 3

Note: Assumptions made if any, should be stated clearly at the beginning of your answer.

**Question 1. [3+5=8 Marks]**

- a) Explain which type of ambiguity exist in following sentences. **[3 marks]**
- i. I saw someone on the hill with a telescope. (Answer : structural)
  - ii. She is walking towards a bank. (Answer: Lexical)
  - iii. The running race was wonderful to watch. (Answer: Grammatical – race and watch has both noun and verb sense)

- b) Given is the following toy corpus. Calculate all the bigram probabilities. **[2 marks]**

<s> I love NLP </s>  
<s> NLP is interesting</s>  
<s> I am learning NLP </s>

$$P(I|<s>)=2/3=0.67$$

$$P(\text{love}|I)=1/3$$

$$P(NLP|\text{love}) = 1/3$$

$$P(</s>|NLP)=2/3$$

$$P(NLP|<s>)=1/3$$

$$P(\text{is}|NLP)=1/3$$

$$P(\text{interesting}|\text{is})=1/3$$

$$P(</s>|\text{interesting})=1/3$$

$$P(I|<s>)=2/3=0.67$$

$$P(\text{am}|I)=1/3$$

$$P(\text{learning}|\text{am})=1/3$$

$$P(NLP|\text{learning})=1/3$$

$$P(</s>|NLP)=2/3$$

- c) Calculate the probability of sentence <s> I am studying NLP</s> using raw bigram probabilities and using Laplace smoothing. **[1+2=3 marks]**

**Without smoothing**

$$P(I|<s>)=2/3=0.67$$

$$P(\text{am}|I)=1/3$$

$$P(\text{studying}|\text{am})=0$$

$P(\text{NLP} | \text{studying}) = 0$

$P(</s> | \text{NLP}) = 2/3$

Unique words=7

With smoothing

Word	Bigram with smoothing
$P(I   <s>)$	$2+1 / 3+7$
$P(\text{am}   I)$	$1+1 / 3+7$
$P(\text{studying}   \text{am})$	$0+1 / 3+7$
$P(\text{NLP}   \text{studying})$	$0+1 / 3+7$

Question 2. [6+4 =10 Marks]

- a) Let the input sentence be “Bank upon me”. Possible Tags are {T1, T2, T3, T4}. Assume all the POS tags are equally likely to be at the starting of the sequence

Table 1: Transition probabilities

	T1	T2	T3	T4
T1	0.18	0.01	0.8	0.01
T2	0.9	0	0.05	0.05
T3	0.4	0.5	0.05	0.05
T4	0.4	0.5	0.05	0.05

Table 2: Emission probabilities

	Bank	Upon	Me
T1	0.1	0.1	0.8
T2	0.8	0.1	0.1
T3	0.2	0.2	0.6
T4	0.8	0.1	0.1

- a) Calculate  $P(x_1=\text{Bank}, x_2=\text{Upon}, y_1=\text{T1}, y_2=\text{T2})$  [1 Mark]  
b) Which is the most probable POS tag sequence out of these sequences for the given input sentence: I) T4 T1 T3  
II) T2 T1 T3  
III) T2 T2 T1

IV) T3 T2 T1

[4 Marks]

- c) Compute the joint probable sequence of most probable sequence above. [1 Mark]

**Solution**

$$\begin{aligned} \text{i. } P(x_1=\text{Bank}, x_2=\text{Upon}, y_1=T_1, y_2=T_2) &= P(T_1) * P(x_1|T_1) * P(T_2|T_1) * P(x_2|T_2) \\ &= 0.25 * 0.1 * 0.1 * 0.01 \\ &= 0.000025 \end{aligned}$$

- ii. Here we have to find out the most probable tag sequence

for I) **T4 T1 T3**

$$\begin{aligned} P(x_1=\text{Bank}, x_2=\text{Upon}, x_3=\text{me}, y_1=T_4, y_2=T_1, y_3=T_3) \\ &= P(T_4) * P(x_1|T_4) * P(T_1|T_4) * P(x_2|T_1) * P(x_3|T_3) * P(T_3|T_1) \\ &= 0.25 * 0.8 * 0.4 * 0.1 * 0.6 * 0.4 = 0.0019 \end{aligned}$$

for II) **T2 T1 T3**

$$\begin{aligned} P(x_1=\text{Bank}, x_2=\text{Upon}, x_3=\text{me}, y_1=T_2, y_2=T_1, y_3=T_3) \\ &= P(T_2) * P(x_1|T_2) * P(T_1|T_2) * P(x_2|T_1) * P(x_3|T_3) * P(T_3|T_1) \\ &= 0.25 * 0.8 * 0.9 * 0.1 * 0.6 * 0.8 = 0.0086 \end{aligned}$$

for III) **T2 T2 T1**

$$P(x_1=\text{Bank}, x_2=\text{Upon}, x_3=\text{me}, y_1=T_2, y_2=T_2, y_3=T_1) = 0$$

For IV) **T3 T2 T1**

$$\begin{aligned} P(x_1=\text{Bank}, x_2=\text{Upon}, x_3=\text{me}, y_1=T_3, y_2=T_2, y_3=T_1) \\ &= P(T_3) * P(x_1|T_3) * P(T_2|T_3) * P(x_2|T_2) * P(x_3|T_1) * P(T_1|T_2) \\ &= 0.25 * 0.2 * 0.2 * 0.1 * 0.8 * 0.9 = 0.0007 \end{aligned}$$

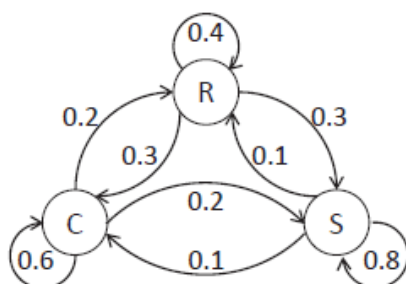
Maximum of all these sequences correspond to T2 T1 T3.

Hence the most probable sequence is **T2 T1 T3**

The joint probability for the most probable sequence is 0.0086

- b) Once a day, weather is observed as one of the states: [4 marks]

state 1: Rainy (R), state 2: cloudy (C), state 3: Sunny (S)



- A) Given that model is in state  $i$ , what is the probability that it stays in the state  $i$  for exactly  $d$  days.
- B) What is the expected duration in the state  $i$ . (Also conditioned on starting in the state  $i$ ).

**13 TUESDAY**

Soln (A)  $O = \{s_1, s_2, s_3, \dots, s_i, s_{j+1}\}$   
 $1 \quad 2 \quad 3 \quad \dots \quad d \quad d+1$

let  $a_{ii}$  be transition probability from state  $i$  to  $i$

$a_{11} = 0.4$   
 $a_{22} = 0.6$   
 $a_{33} = 0.8$

It is given that the starting state is  $i$   
 so the probability that the model is in state  $i$  for exactly  $d$  days is

$(a_{ii})^{d-1} (1 - a_{ii})$

if  $i=1$  then ans is  $(0.4)^{d-1} \cdot 0.6$   
 if  $i=2$  " ans is  $(0.6)^{d-1} \cdot (0.4)$   
 if  $i=3$  " ans is  $(0.8)^{d-1} \cdot 0.2$

**14 WEDNESDAY**

(B) let  $p = 1 - a_{ii}$  is the probability of success (exiting state  $i$ ) & there are  $(d-1)$  failures before first success

then  $E(X) = \sum_{k=1}^{\infty} k (1-p)^{k-1} p$

$= p \sum_{k=1}^{\infty} k (1-p)^{k-1}$

$= \frac{p}{(1 - (1-p))^2} = \frac{p}{p^2} = \frac{1}{p}$

$E(X) = \frac{1}{p}$

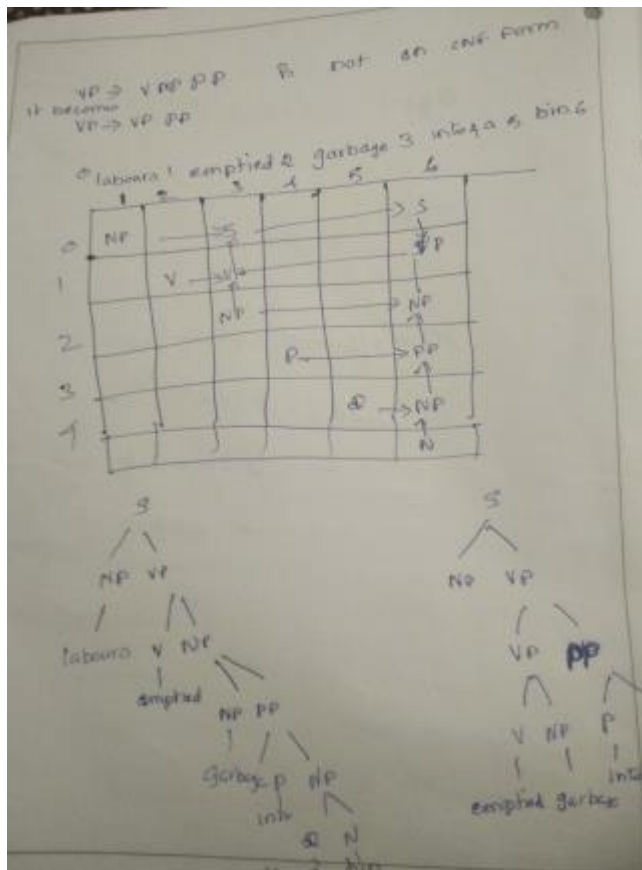
for rainy  $E(X) = \frac{1}{0.6} = 1.67$   
 for cloudy  $E(X) = \frac{1}{0.4} = 2.5$   
 for sunny  $E(X) = \frac{1}{0.2} = 5$

Question 3. [Marks 5+2+5=12 marks]

- a) Find the following the context free grammar is in Chomsky normal form. Justify your answer [1 Marks]
- b) Create a CKY table for parsing the sentence "labours emptied garbage into a bin" with the grammar  $G$  and make all possible parse trees. [4 Marks]

$S \rightarrow NP VP$   
 $PP \rightarrow P NP$   
 $VP \rightarrow V NP PP$   
 $VP \rightarrow V NP$   
 $NP \rightarrow D N$   
 $NP \rightarrow NP PP$   
 $NP \rightarrow NP CNP$   
 $N \rightarrow A N$

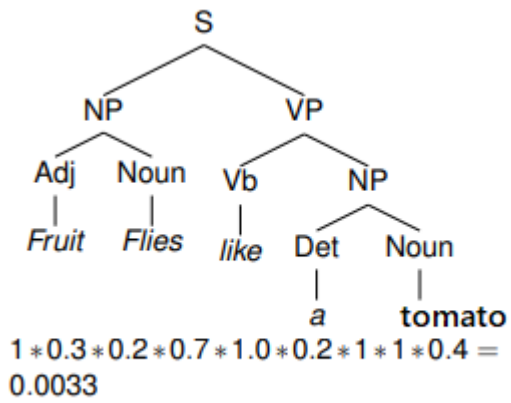
$CNP \rightarrow C NP$   
 $NP \rightarrow \text{"labours"} \mid \text{"sacks"} \mid \text{"garbage"} \mid \text{"junk"}$   
 $N \rightarrow \text{"worker"} \mid \text{"bin"} \mid \text{"sack"}$   
 $V \rightarrow \text{"dumped"} \mid \text{"emptied"}$   
 $P \rightarrow \text{"of"} \mid \text{"into"}$   
 $D \rightarrow \text{"a"} \mid \text{"the"}$   
 $C \rightarrow \text{"and"}$   
 $A \rightarrow \text{"big"} \mid \text{"small"}$



- c) Find the probability of the sentence "Fruits flies like a tomato" using PCFG parsing method  
[2 Marks]

1.0  $S \rightarrow NP VP$   
 0.3  $NP \rightarrow Adj Noun$   
 0.7  $NP \rightarrow Det Noun$   
 1.0  $VP \rightarrow Vb NP$   
 -  
 0.2  $Adj \rightarrow fruit$   
 0.2  $Noun \rightarrow flies$   
 1.0  $Vb \rightarrow like$   
 1.0  $Det \rightarrow a$   
 0.4  $Noun \rightarrow banana$   
 0.4  $Noun \rightarrow tomato$   
 0.8  $Adj \rightarrow angry$

**Solution:**



d) Find the dependency parse tree using Chu Liu Edmonds algorithm [5 marks]

