

Individual Quiz #07 (17/12/2013)
(15 Mins)

Name _____ ID _____ Group _____

Part I: True (T) | False (F) questions. (1 mark each.)

1. _____ In any vector space, a sequence of vectors is a basis of the vector space if and only if each vector in the space can be expressed as a linear combination of vectors in that sequence.
2. _____ The trivial space $\{\vec{0}\}$ has only one basis which is the $\langle \vec{0} \rangle$.
3. _____ No 2 vectors can span \mathbb{R}^3 .
4. _____ The dimension of the vector space of matrices $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$ where $a + d = 0$ is 4.

Part II: Answer the questions and show how to solve the questions. (2 marks each.)

5. Determine whether $\langle \begin{pmatrix} 1 \\ -2 \end{pmatrix}, \begin{pmatrix} 3 \\ 1 \end{pmatrix}, \begin{pmatrix} -1 \\ 1 \end{pmatrix} \rangle$ is a basis for \mathbb{R}^2 .
6. What is the dimension of the vector space $M_{3 \times 5}$ of 3x5 matrices?
7. Find the rank of this matrix $\begin{bmatrix} 1 & 3 & 2 \\ 5 & 1 & 1 \\ 6 & 4 & 3 \end{bmatrix}$