

mlcam 310 Hw2

① Naive Bayes

Senior	High	High School	Yes	?
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$$P(\text{Age} = \text{Senior}) = 3/11$$

$$P(\text{Income} = \text{High}) = 4/11$$

$$P(\text{Edu} = \text{High School}) = 4/11$$

$$P(\text{Prior} = \text{Yes}) = 5/11$$

$$P(\text{Buy PC} = \text{Yes}) = 5/11$$

$$P(\text{Buy PC} = \text{NO}) = 6/11$$

Frequency Tables

		BUY PC?		
		Yes	No	
Income	Low	1/4	3/4	4/11
	Medium	1/3	2/3	3/11
	High	3/4	1/4	4/11

		BUY PC?		
		YES	NO	
Education	College	4/7	3/7	7/11
	High School	1/4	3/4	4/11

		BUY PC?		
		Yes	No	
Prior Purchase	YES	4/5	1/5	5/11
	NO	1/6	5/6	6/11

		BUY PC?		
		YES	NO	
Age	Young Adult	3/4	1/4	4/11
	Middle Age	1/4	3/4	4/11
	Senior	1/3	2/3	3/11

1.2 Naive Bayes

Y = Senior, High, HighSchool, Yes
 1 44 Y = Senior | Age = Senior

$$P(Y | \text{Buy PC} = \text{Yes}) = P(\text{Age} = \text{Senior} | \text{Buy} = \text{Yes})$$

$$* P(\text{Income} = \text{High} | \text{Buy} = \text{Yes})$$

$$* P(\text{Edu} = \text{HighSchool} | \text{Buy} = \text{Yes})$$

$$* P(\text{Prior} = \text{Yes} | \text{Buy} = \text{Yes})$$

$$= 1/3 * 3/4 * 1/4 * 4/5$$

$$P(\text{Buy PC} = \text{YES} | Y) \approx P(Y | \text{Buy} = \text{Yes}) P(\text{Buy} = \text{Yes})$$

$$= 1/3 * 2/4 * 1/4 * 4/5 * 7/11$$

$$\approx 1/44$$

$$P(\text{Buy PC} = \text{NO} | Y) \approx P(Y | \text{Buy} = \text{NO}) P(\text{Buy} = \text{NO})$$

$$\approx 2/3 * 1/4 * 2/4 * 1/5 * 6/11$$

$$P(\text{Buy PC} = \text{NO} | Y)$$

$$> P(\text{Buy PC} = \text{YES} | Y)$$

$$\approx \frac{2 * 6^3}{4 * 4 * 5} = \frac{18}{20}$$