Name: Solanki Ravi

Course: Data Science

Sem: 7

Subject: Image Processing

- 1. Implement functions for encoding and decoding an image using the following methods:
 - A. Transform Coding (using DCT for forward transform)
 - B. Huffman Encoding
 - C. LZWEncoding
 - D. Run-Length Encoding
 - E. Arithmetic Coding

For each method, display the Compression Ratio and calculate the Root Mean Square Error (RMSE) between the original and reconstructed image to quantify any loss of information

```
import numpy as np
import cv2
from scipy.fftpack import dct, idct
import heapq
import collections
from sklearn.metrics import mean_squared_error
import math
```

```
In [13]: # Helper function for RMSE calculation
    def calculate_rmse(original, reconstructed):
        return np.sqrt(mean_squared_error(original.flatten(), reconstructed.flatten()))
# Helper function for compression ratio
    def calculate_compression_ratio(original_size, compressed_size):
        return original_size / compressed_size
```

A. Transform Coding (DCT Based)

```
In [14]: # DCT encoding
def dct_encode(image, block_size=8):
    h, w = image.shape
    dct_blocks = np.zeros((h, w), dtype=np.float32)
    for i in range(0, h, block_size):
        for j in range(0, w, block_size):
            block = image[i:i+block_size, j:j+block_size]
            dct_blocks[i:i+block_size, j:j+block_size] = dct(dct(block, axis=0, norm='
            return dct_blocks
```

```
# DCT decoding
         def dct_decode(dct_blocks, block_size=8):
             h, w = dct_blocks.shape
             reconstructed = np.zeros((h, w), dtype=np.float32)
             for i in range(0, h, block size):
                 for j in range(0, w, block size):
                     block = dct_blocks[i:i+block_size, j:j+block_size]
                     reconstructed[i:i+block_size, j:j+block_size] = idct(idct(block, axis=0, r
              return np.clip(reconstructed, 0, 255).astype(np.uint8)
In [23]: # Example 8x8 grayscale image (pixel values between 0-255)
         original image = np.array([
              [50, 55, 61, 66, 70, 61, 64, 73],
              [67, 55, 66, 90, 109, 85, 69, 52],
             [25, 59, 68, 113, 184, 104, 46, 73],
              [63, 59, 71, 122, 144, 126, 50, 69],
             [67, 61, 68, 104, 146, 88, 68, 70],
             [79, 67, 60, 90, 57, 68, 58, 75],
              [85, 78, 84, 59, 55, 61, 65, 83],
             [87, 49, 49, 68, 65, 76, 78, 94]
         ], dtype=np.uint8)
         # Perform DCT encoding
         dct encoded = dct encode(original image)
         # Perform DCT decoding to reconstruct the image
         dct_decoded = dct_decode(dct_encoded)
         # Calculate Compression Ratio and RMSE
         original size = original image.size * original image.itemsize
         compressed_size = dct_encoded.size * dct_encoded.itemsize # Can adjust based on quant
         compression_ratio = calculate_compression_ratio(original_size, compressed_size)
         rmse = calculate_rmse(original_image, dct_decoded)
         print("Original Image:\n", original_image)
         print("DCT Encoded (Frequency Domain):\n", dct_encoded)
         print("Reconstructed Image:\n", dct_decoded)
         print(f"Compression Ratio: {compression_ratio:.2f}")
         print(f"RMSE: {rmse:.2f}")
```

```
Original Image:
 [[ 50 55 61 66 70 61 64 73]
 [ 67 55 66 90 109 85 69 52]
 [ 25 59 68 113 184 104 46 73]
 [ 63 59 71 122 144 126
                         50
                             69]
  67 61 68 104 146 88 68
                            70]
 [ 79 67 60 90 57 68 58
                             75]
 [ 85 78 84 59 55 61
                         65
                             83]
 [ 87 49 49 68 65 76 78 94]]
DCT Encoded (Frequency Domain):
 [[ 6.0387500e+02 -3.1663446e+01 -8.4772408e+01 2.7025295e+01
  5.9625000e+01 -2.6122663e+01 6.0245891e+00 -1.2159461e+00]
 [ 4.6301618e+00 -1.6079477e+01 -7.3930679e+01 1.1386600e+01
  6.1034756e+00 -2.3492607e+01 -1.0829472e+01 1.1151272e+01]
 [-5.4891235e+01 3.4339614e+00 8.6425331e+01 -2.1633005e+01
 -2.7345310e+01 2.8754131e+01 3.0528545e+00 3.1543176e+00]
 [-3.4095802e+01 2.6057545e+01 5.3000034e+01 -2.4241652e+01
  -1.9311680e+01 2.5285940e+01 -4.3974919e+00 -5.3044448e+00]
 [ 6.6250000e+00 -1.6961658e+01 -1.7011949e-01 1.2130071e+01
  8.8750000e+00 4.8020830e+00 3.1823435e+00 -1.8482486e+00]
 [-1.6967047e+00 6.0731049e+00 5.2455964e+00 -1.7033865e+01
  -1.1872666e+01 -1.3257085e+01 1.3392779e+01 -8.0334454e+00]
 [-1.0682165e+01 -1.8022390e+01 -9.9471455e+00 -7.7026505e+00
  1.3356283e+01 -1.1073159e+01 -5.6753292e+00 -1.0066974e+01]
 [ 7.2609630e+00 -1.0168533e+01 -1.8489538e+01 -7.4164028e+00
  5.6928830e+00 -2.6382061e+01 -1.2942762e+01 2.8078215e+01]]
Reconstructed Image:
 [[ 49 54 60 65 69 60 63 72]
 [ 66 54 65 89 108 84 68 51]
 [ 25 59 68 113 184 104 46 73]
  63 59 71 122 144 126 50 69]
  66 60 67 103 146 87
                         67
                             69]
 [ 79 67 60 90 57 68 58
                             75]
 [ 85 78 84 59 55 61 65 83]
 [ 86 48 48 67 64 75 77 93]]
Compression Ratio: 0.25
RMSE: 0.70
```

B. Huffman Encoding

```
In [24]:
         # Huffman encoding and decoding functions
          class HuffmanNode:
              def __init__(self, symbol, frequency):
                  self.symbol = symbol
                  self.frequency = frequency
                  self.left = None
                  self.right = None
              def lt (self, other):
                  return self.frequency < other.frequency</pre>
          def build huffman tree(frequency dict):
              heap = [HuffmanNode(symbol, freq) for symbol, freq in frequency dict.items()]
              heapq.heapify(heap)
              while len(heap) > 1:
                  left = heapq.heappop(heap)
                  right = heapq.heappop(heap)
                  merged = HuffmanNode(None, left.frequency + right.frequency)
```

```
def build_huffman_codes(node, prefix="", code_dict={}):
             if node.symbol is not None:
                  code_dict[node.symbol] = prefix
             else:
                 build_huffman_codes(node.left, prefix + "0", code_dict)
                 build huffman codes(node.right, prefix + "1", code dict)
             return code dict
         def huffman_encode(image):
             frequency dict = collections.Counter(image.flatten())
             huffman tree = build huffman tree(frequency dict)
             huffman codes = build huffman codes(huffman tree)
             encoded_image = ''.join(huffman_codes[pixel] for pixel in image.flatten())
             return encoded image, huffman codes
         # Function to decode Huffman encoded image
         def huffman_decode(encoded_image, huffman_codes, shape):
             reverse codes = {v: k for k, v in huffman codes.items()}
             current_code = ""
             decoded pixels = []
             for bit in encoded_image:
                  current code += bit
                 if current code in reverse codes:
                      decoded_pixels.append(reverse_codes[current_code])
                     current_code = ""
              return np.array(decoded pixels).reshape(shape)
In [25]:
         # Example 4x4 image for simplicity
         example_image = np.array([
             [45, 45, 255, 255],
              [45, 45, 255, 255],
             [45, 200, 200, 255],
             [45, 200, 200, 255]
          ], dtype=np.uint8)
         # Huffman Encode the image
         encoded_image, huffman_codes = huffman_encode(example_image)
         # Decode the encoded image
         decoded_image = huffman_decode(encoded_image, huffman_codes, example_image.shape)
         # Calculate Compression Ratio
         original_size = example_image.size * 8 # 8 bits per pixel in original image
          compressed size = len(encoded image)
         compression ratio = original size / compressed size
         # Display results
         print("Original Image:\n", example_image)
         print("Huffman Codes:", huffman codes)
         print("Encoded Image:", encoded_image)
         print("Decoded Image:\n", decoded_image)
```

print(f"Compression Ratio: {compression ratio:.2f}")

merged.left = left
merged.right = right

return heap[0]

heapq.heappush(heap, merged)

```
Original Image:
    [[ 45     45     255     255]
    [ 45     45     255     255]
    [ 45     200     200     255]
    [ 45     200     200     255]]
Huffman Codes: {45: '0', 200: '10', 255: '11'}
Encoded Image: 0011110011111010110101011
Decoded Image:
    [[ 45     45     255     255]
    [ 45     45     255     255]
    [ 45     200     200     255]
    [ 45     200     200     255]]
Compression Ratio: 4.92
```

C. LZW Encoding

```
In [26]: # LZW encoding function
         def lzw encode(image):
             image = image.flatten()
             dictionary = {bytes([i]): i for i in range(256)}
             current_sequence = bytes([image[0]])
             encoded data = []
             code = 256
             for pixel in image[1:]:
                  sequence_plus_pixel = current_sequence + bytes([pixel])
                  if sequence plus pixel in dictionary:
                      current_sequence = sequence_plus_pixel
                  else:
                      encoded data.append(dictionary[current sequence])
                      dictionary[sequence_plus_pixel] = code
                      code += 1
                      current_sequence = bytes([pixel])
             encoded_data.append(dictionary[current_sequence])
             return encoded data
         # Function to perform LZW Decoding
         def lzw_decode(encoded_data):
             # Initialize the dictionary for decoding
             dictionary = {i: bytes([i]) for i in range(256)}
             code = 256 # Start codes for sequences longer than one byte
             # Decode the first value
             current_sequence = dictionary[encoded_data[0]]
             decoded_image = [current_sequence]
             for code_value in encoded_data[1:]:
                  if code_value in dictionary:
                      entry = dictionary[code_value]
                  elif code value == code:
                      entry = current sequence + current sequence[:1]
                  # Append decoded sequence
                 decoded image.append(entry)
                  # Add new sequence to the dictionary
                  dictionary[code] = current_sequence + entry[:1]
                  code += 1
                  current sequence = entry
```

```
decoded_image = b''.join(decoded_image)
             return np.frombuffer(decoded_image, dtype=np.uint8)
In [27]: # Example 4x4 grayscale image for simplicity
         example image = np.array([
             [45, 45, 45, 255],
              [45, 45, 255, 255],
             [200, 200, 45, 45],
             [200, 200, 255, 255]
          ], dtype=np.uint8)
         # Step 1: LZW Encode the image
         encoded data = lzw encode(example image)
         # Step 2: LZW Decode the encoded image
         decoded_image = lzw_decode(encoded_data).reshape(example_image.shape)
         # Calculate Compression Ratio
         original_size = example_image.size * 8 # 8 bits per pixel in the original image
         compressed_size = len(encoded_data) * 16 # Assuming each encoded entry takes 16 bits
         compression_ratio = original_size / compressed_size
         # Display results
         print("Original Image:\n", example_image)
         print("Encoded Data:", encoded_data)
         print("Decoded Image:\n", decoded_image)
         print(f"Compression Ratio: {compression ratio:.2f}")
         Original Image:
          [[ 45 45 45 255]
```

D. Run-Length Encoding

[45 45 255 255] [200 200 45 45] [200 200 255 255]]

Decoded Image:
[[45 45 45 255]
[45 45 255 255]
[200 200 45 45]
[200 200 255 255]]
Compression Ratio: 0.73

Convert to a 1D array of pixel values

```
import numpy as np

# Function to perform RLE Encoding
def rle_encode(image):
    # Flatten the image to treat it as a 1D sequence
    image = image.flatten()
    encoded_data = []
    i = 0

# Traverse through the image pixels
    while i < len(image):
        count = 1
        while i + 1 < len(image) and image[i] == image[i + 1]:</pre>
```

Encoded Data: [45, 256, 255, 257, 255, 200, 200, 256, 261, 255, 255]

```
count += 1
            i += 1
        # Store the pixel value and its count
        encoded_data.append((image[i], count))
        i += 1
    return encoded data
# Function to perform RLE Decoding
def rle_decode(encoded_data, shape):
    decoded_image = []
    # Expand each (value, count) pair
    for value, count in encoded data:
        decoded_image.extend([value] * count)
    # Convert list to a numpy array and reshape to original image shape
    return np.array(decoded_image, dtype=np.uint8).reshape(shape)
# Example 4x4 grayscale image for simplicity
example image = np.array([
    [45, 45, 45, 255],
    [45, 45, 255, 255],
    [200, 200, 45, 45],
    [200, 200, 255, 255]
], dtype=np.uint8)
# Step 1: RLE Encode the image
encoded data = rle encode(example image)
# Step 2: RLE Decode the encoded image
decoded_image = rle_decode(encoded_data, example_image.shape)
# Calculate Compression Ratio
original_size = example_image.size * 8 # 8 bits per pixel in the original image
compressed_size = sum(len(bin(value)[2:]) + 8 for value, count in encoded_data) # con
compression_ratio = original_size / compressed_size
# Display results
print("Original Image:\n", example_image)
print("RLE Encoded Data:", encoded_data)
print("Decoded Image:\n", decoded_image)
print(f"Compression Ratio: {compression_ratio:.2f}")
Original Image:
[[ 45 45 45 255]
 [ 45 45 255 255]
[200 200 45 45]
[200 200 255 255]]
RLE Encoded Data: [(45, 3), (255, 1), (45, 2), (255, 2), (200, 2), (45, 2), (200, 2),
(255, 2)
Decoded Image:
[[ 45 45 45 255]
 [ 45 45 255 255]
[200 200 45 45]
[200 200 255 255]]
Compression Ratio: 1.05
```

E. Arithmetic Coding

```
In [29]: from collections import Counter
         import numpy as np
         # Function to calculate probability ranges for each pixel value
         def calculate prob ranges(sequence):
             total_pixels = len(sequence)
             freq = Counter(sequence)
             prob ranges = {}
             current low = 0.0
             # Calculate cumulative probability ranges for each pixel value
             for pixel value, count in sorted(freq.items()):
                 probability = count / total pixels
                  current_high = current_low + probability
                  prob ranges[pixel value] = (current low, current high)
                  current_low = current_high
             return prob ranges
         # Arithmetic encoding function
         def arithmetic encode(sequence, prob ranges):
             low, high = 0.0, 1.0
             for pixel in sequence:
                 pixel_low, pixel_high = prob_ranges[pixel]
                  range = high - low
                 high = low + range_ * pixel_high
                 low = low + range_ * pixel_low
             return (low + high) / 2 # Encoded as a single value within the final range
         # Arithmetic decoding function
         def arithmetic_decode(encoded_value, prob_ranges, sequence_length):
             low, high = 0.0, 1.0
             decoded sequence = []
             for _ in range(sequence_length):
                  range_ = high - low
                  for pixel, (pixel_low, pixel_high) in prob_ranges.items():
                      pixel_range_low = low + range_ * pixel_low
                      pixel_range_high = low + range_ * pixel_high
                      if pixel_range_low <= encoded_value < pixel_range_high:</pre>
                          decoded_sequence.append(pixel)
                          low, high = pixel range low, pixel range high
                          break
             return decoded_sequence
         # Example image represented as a 4x4 grayscale image
         example_image = np.array([
             [45, 45, 45, 255],
              [45, 45, 255, 255],
             [200, 200, 45, 45],
             [200, 200, 255, 255]
          ], dtype=np.uint8)
         # Flatten the image to create a sequence
          sequence = example_image.flatten()
```

```
# Step 1: Calculate probability ranges for each pixel value
prob_ranges = calculate_prob_ranges(sequence)
# Step 2: Encode the sequence using Arithmetic Encoding
encoded value = arithmetic encode(sequence, prob ranges)
# Step 3: Decode the sequence to retrieve the original image
decoded_sequence = arithmetic_decode(encoded_value, prob_ranges, len(sequence))
decoded_image = np.array(decoded_sequence, dtype=np.uint8).reshape(example_image.shape
# Calculate Compression Ratio
original_size = example_image.size * 8 # 8 bits per pixel in the original image
compressed_size = len(bin(int(encoded_value * (2 ** 32)))) - 2 # Approx. bits for end
compression_ratio = original_size / compressed_size
# Display results
print("Original Image:\n", example_image)
print("Encoded Value:", encoded_value)
print("Decoded Image:\n", decoded_image)
print(f"Compression Ratio: {compression ratio:.2f}")
Original Image:
[[ 45 45 45 255]
 [ 45 45 255 255]
[200 200 45 45]
[200 200 255 255]]
Encoded Value: 0.06236219020966758
Decoded Image:
[[ 45 45 45 255]
 [ 45 45 255 255]
[200 200 45 45]
[200 200 255 255]]
Compression Ratio: 4.57
```

In []: