

1. Veak integration Feynman diagram

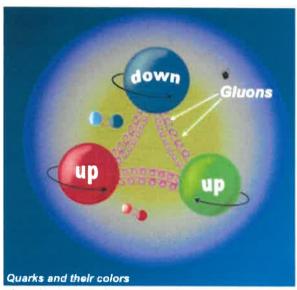
2. Decays 2 Conservation laws

3. Unification

9 chapter 3. Relativistic Kinematics

# New approach merges theoretical fundamentals with experimental studies of the proton's structure

by US Department of Energy



Artist's depiction of a proton's interior. In quantum chromodynamics, the constituent quarks come in three "colors," along with up and down "flavors." Also shown are virtual quark-antiquark pairs and the gluons that bind the quarks together. Credit: Ted Rogers

Protons and other subatomic particles that are subject to the strong nuclear force have a complex structure that involves even more fundamental constituents called quarks and gluons. These quarks and gluons bind under the influence of quantum chromodynamics (QCD). QCD is the theory of strong interaction of quarks and the role of color symmetry.

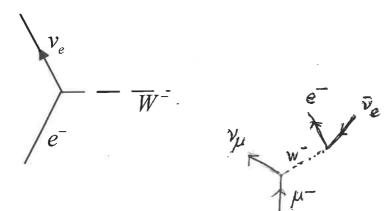
However, the mechanisms that lead to <u>quarks</u> and <u>gluons</u> combining to form the particles we see in nature are very mysterious and poorly understood. For example, virtual quarks and gluons constantly appear and disappear within

#### (c) Weak Interaction

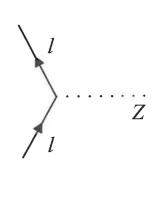
#### Two kinds, charged and neutral vertices

Leptons: primitive vertices connect members of the <u>same</u> generation Lepton number is separately conserved for each Lepton generation, that is,  $L_e$ ,  $L_\mu$ ,  $L_\tau$  separately conserved.

Charged vertex



**Neutral vertex** 



e.g.

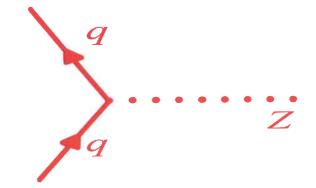
#### Quarks

Flavour not conserved in weak interaction.

#### **Charged Vertex.**



#### **Neutral vertex**



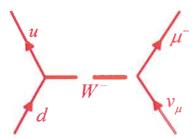
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#### Quarks

### Flavour not conserved in weak interaction **Charged Vertex**.



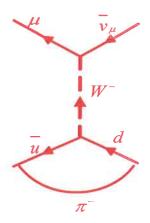
Semileptonic process  $d + v_{\mu} \rightarrow u + \mu^{-}$ 



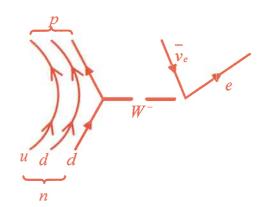
Not observable due to quark confinement

#### But can be observed in

Decay of 
$$\pi^- \rightarrow \mu^- + \overline{\nu}_\mu$$

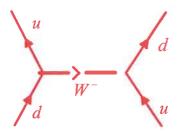


and neutron decay  $n \rightarrow p + e^- + \overline{v_e}$ 



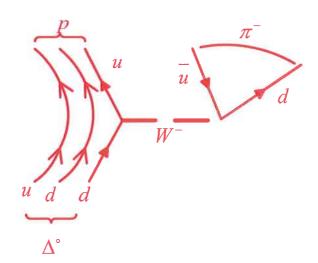
Two quarks u, d in neutron n not participating are called spectator quarks.

#### Hadronic decays

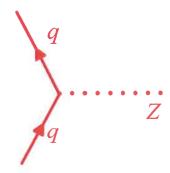


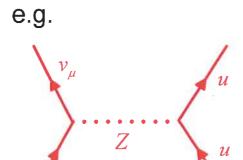
#### observed in

$$\Delta^{\circ}(udd)$$
  
 $\Delta^{\circ} \to p + \pi^{-}$ 



#### **Neutral vertex**

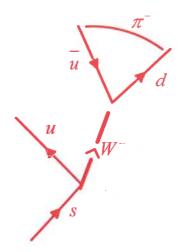




observed in  $v_{\mu} + p \rightarrow v_{\mu} + p$ 

Decays of quark by weak interaction can involve members of different generations

e.g. a strange quark can decay into an u-quark



The weak force not just couples members of the same generation

$$\binom{u}{d}$$
 or  $\binom{c}{s}$  or  $\binom{t}{b}$ 

but couples also members of different generations

$$\begin{pmatrix} u \\ d \end{pmatrix} or \begin{pmatrix} c \\ s \end{pmatrix} or \begin{pmatrix} t \\ b \end{pmatrix} \qquad \text{where} \qquad \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

#### Cabibbo

#### Kobayashi – Maskawa matrix

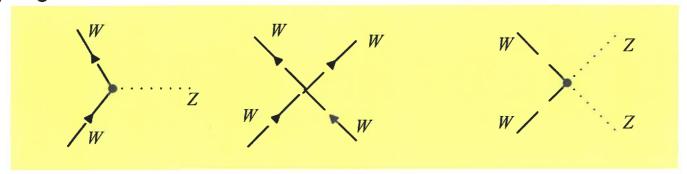
$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 0.9747 - 0.9759, & 0.218 - 0.224, & 0.001 - 0.007 \\ 0.218 - 0.224, & 0.9734 - 0.9752, & 0.030 - 0.058 \\ 0.003 - 0.019, & 0.029 - 0.058, & 0.9983 - 0.9996 \end{pmatrix}$$

$$V_{ud}$$
 = coupling of  $u$  to  $d$ 

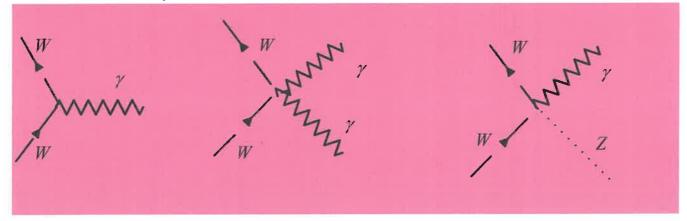
$$V_{us}$$
 = coupling of  $u$  to  $s$ 

#### (d) wk and em couplings of $W^{\pm}$ and Z

#### Weak couplings



#### Couplings involve photon $\gamma$



#### **Summary**

#### 1.5 Decay & Conservation Laws

#### 1.5.1 Decay

(a) Every particle decays into lighter particles unless prevented by some conservation law

Stable particles:  $e^{-}$  (lightest lepton, conservation of lepton number),

p (lightest baryon, conservation of baryon number), neutrinos, photons (massless particles)

(b) Most particles exhibit several different decay modes e.g.

#### Branching ratio

Each unstable species has a characteristic mean life time  $\tau$ 

e.g. 
$$\tau_{\mu} = 2.2 \times 10^{-6} \text{ s}$$
 
$$\tau_{\pi^+} = 2.6 \times 10^{-8} \text{ s}$$
 
$$\tau_{\pi^\circ} = 8.3 \times 10^{-17} \text{ s}$$

Note:  $I = I_0 e^{-t/\tau}$ ,

 $\tau$  = time taken for I to decrease from  $I_0$  to  $I_0$   $e^{-1}$ 

 $t_{1/2}$  = time taken for I to reduce to  $\frac{1}{2}I_o$ ,

$$\frac{1}{2}I_o = I_o e^{-(t_{1/2}/\tau)} \Rightarrow ln2 = (t_{1/2}/\tau)$$

#### (c) Three Fundamental Decays:

Strong decay e.g. 
$$\Delta^{++} \rightarrow p + \pi^{+}$$
  $\tau = 10^{-23} s$  **em** decay e.g.  $\pi^{\circ} \rightarrow \gamma + \gamma$   $\tau = 10^{-16} s$  **wk** decay e.g.  $\Sigma^{-} \rightarrow n + e^{-} + v_{e}$   $\tau \sim 10^{-13} s$  Neutron decay  $n \rightarrow p + e^{-} + v_{e}$  ( $\tau = 15 \, \mathrm{min}$ )  $(d \rightarrow u + e^{-} + v_{e})$ 

- (d) Kinematic Effect: the larger the mass difference between the original particle and the decay products, the more rapidly the decay occurs.
  - This is also known as phase space factor. It accounts for the enormous range of mean life time  $\tau$  in **wk** decays.

#### 1.5.2 CONSERVATION LAWS

(i) Spacetime symmetry

Homogeneity of space time  $\rightarrow$  laws of physics are invariant under time and space translations  $\rightarrow$ 

Conservation of spatial momentum p, Conservation of energy  $E/c=p^0$ 

Isotropy of space time  $\rightarrow$  laws of physics are invariant under rotations in space time.

In particular laws of physics are invariant under rotations in space → Conservation of angular momentum.

Invariant under rotation in space and time (Lorentz transformation), Lorentz Symmetry

**Discrete Symmetry** 

Space inversion → conservation of parity

Time inversion T, no quantum number associated.

T represented by anti-unitary operator.

$$T^+ = T^{-1}$$
 (unitary)  
 $T(c_1|\psi_1\rangle + c_2|\psi_2\rangle) = c_1^*T|\psi_1\rangle + c_2^*T|\psi_2\rangle$  (antilinear)  
and  $c_1^*$  is the complex conjugate of  $c_i$ ,  $i=1$ , 2

#### (ii) Internal Symmetry

(1) U(1) symmetry
A physical state of a physical system is represented by a vector  $|\psi\rangle$  in Hilbert space up to a phase factor (assume normalization)

i.e. if  $|\psi\rangle$  represents a physical state then  $e^{i\alpha}|\psi\rangle$  represents the same physical state, where  $\alpha$ =constant, phase whereas exp( $i\alpha$ ) is known as phase factor.

 $\left\{e^{i\alpha_1},e^{i\alpha_2}...\right\}$  form a group, an Abelian group U(1)

Conservations of electric charge, baryon number and lepton number are due to the U(1) phase invariance.

For the electric charge case, can also let phase  $\alpha$  be dependent on spacetime point  $x^u$ , namely  $\alpha = \alpha(\underline{x})$  and one gets local gauge invariance

(2) The QCD Lagrangian is invariant under local SU(3) transformations. i.e. QCD has a local SU(3) symmetry. An SU(3) transformation is represented by a unitary 3 x 3 matrix with determinant=1.

$$SU(3)$$
 = special unitary group in three dimensions

(3) Approximate conservation of flavour. Quark flavour is conserved at a strong or electromagnetic vertex, but <u>not</u> at a weak vertex.

#### OZI (Okubo, Zweig and lizuka ) rule Some <u>strong</u> decays are suppressed

e.g.

 $J/\psi = c\overline{c}$  bound state of charmed quarks has anomalously long lifetime

$$\varphi$$
 Meson  $(s\bar{s})$ ,  $I^G(J^{pc})=0^-(1^{--})$  mass = 1020 MeV, Full width  $\Gamma=4$ MeV,  $(\tau\Gamma=\hbar)$   $\tau=1.6$  x  $10^{-22}$ s

#### Decay modes

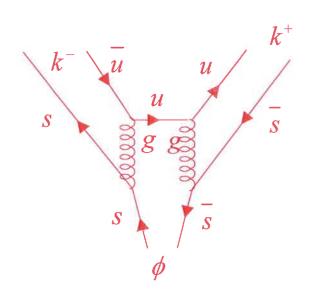
$$K^{+}K^{-}$$
 50%  $K_{l}^{0}K_{s}^{0}$  34%  $\rho\pi$  13%  $\pi^{+}\pi^{-}\pi^{o}$  2%  $\eta\gamma$  1%

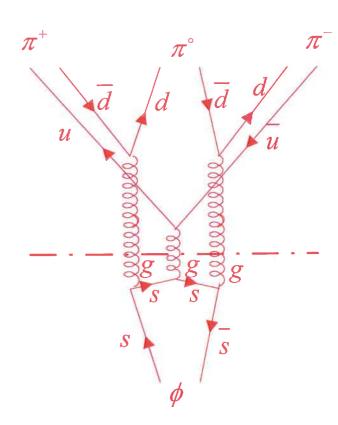
Clearly,  $\phi$  meson decays more often into  $K^+K^-$ 

$$\phi \to K^+ + K^-$$
 mass of  $(K^+ + K^-) = 990 \,\text{MeV/c}^2$ 

than into  $3\pi$ 's

$$\phi \to \pi^+ + \pi^- + \pi^0$$
 mass of  $(\pi^+ + \pi^- + \pi^0) = 415 MeV/c^2$ 





#### **OZI rule:**

If the diagram can be cut in two by slicing only gluon lines (and not cutting open any external lines), the process is suppressed.

Qualitatively OZI rule is related to the asymptotic freedom.

In an OZI suppressed diagram the gluons have higher energy than those in the OZI - allowed diagram. (More gluons imply higher energy, higher energy so strong interaction coupling constant is smaller, meaning process less likely to occur).

$$J/\psi$$
  $I^G(J^p) = 0^-(1^-)$  mass = 3100 MeV/c²,  $\Gamma$ =0.093 MeV

#### Decay modes

$e^+e^-$	6.0%
$\mu^+\mu^-$	6.0%
hadrons	88%

$$J/\psi \to 3\pi$$
 OZI - suppressed  $J/\psi \to D^+ + D^-(D^\circ + \overline{D}^\circ)$  charmed nonstrange Mesons mass of D  $\approx$  1869 MeV/c². D+ (c  $\overline{d}$ ); D0 (c  $\overline{u}$ ) Kinematically forbidden since a pair of two charmed D mesons has larger total mass than the J particle. Hence this J particle has a longer life time than the  $\phi$  meson.

#### **Planck Scale**

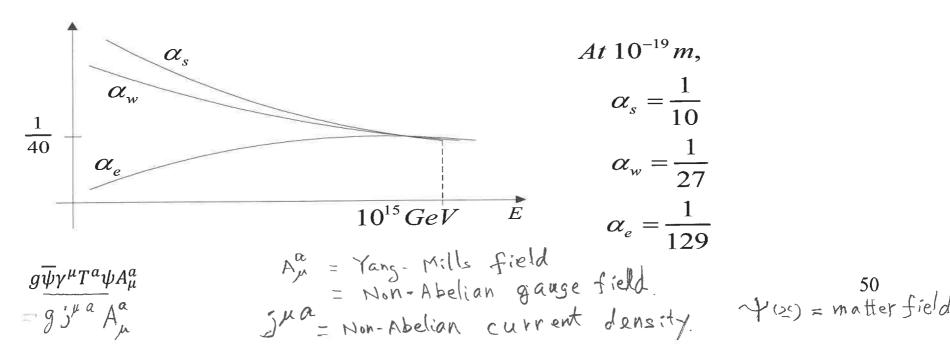
Strong coupling constant  $\alpha_s$  decreases at short distances (very high energy collisions)

Weak coupling  $\alpha_{_{\mathcal{W}}}$  also decreases but at a slower rate.

Electromagnetic coupling constant  $\alpha_{\scriptscriptstyle e}$  increases as energy increases

[Note: the relative weakness of the weak force is due to the large mass of  $W^{\pm}$ , Z; its intrinsic strength is greater than that of the **em** force.]

From the present functional form of the running coupling constants,  $\alpha_{\rm s,}$   $\alpha_{\rm w,}$  and  $\alpha_{\rm e}$  converge at around 10<sup>15</sup> GeV (Planck energy scale).



# Our Universe according to Wilkison Microwave Anistropy Probe (WMAP) 2003

- Age: 13.7 billion years
- Shape: Flat
- Age when first light appeared:200 Million years
- Contents: 4% ordinary matter, 23% dark matter, nature unknown; 73% dark energy, nature unknown
- Hubble constant (expansion rate):71km/sec/megaparsec

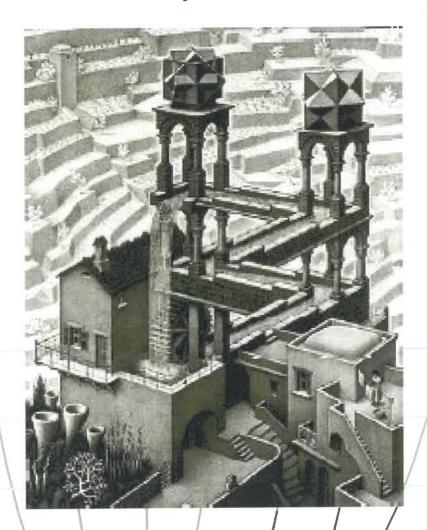
# To see a World in a Grain of Sand And a Heaven in A Wild Flower Hold Infinity in the palm of your hand And Eternity in an hour

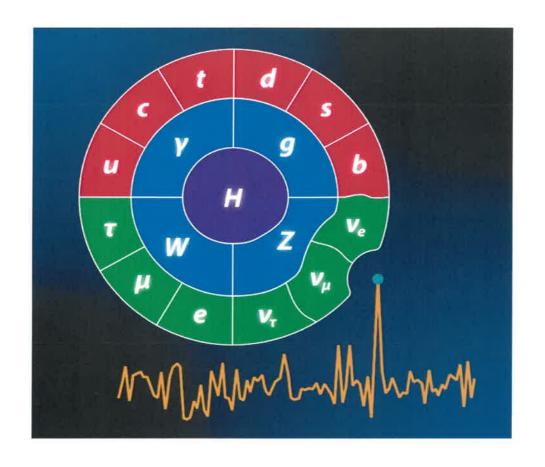
W. Blake (1757-1827)



## M.C. Escher

(Dutch graphic artist, 1898- 1972)





#### APS/Alan Stonebraker

The colored circle represents the standard model of particle physics, which describes the Higgs boson (purple), the force-carrying particles (blue), the quarks (red), and the leptons (green). Particle physicists hope that an anomaly (shown as a data peak) will pierce through the standard model's long-standing dominance, so that a new, more comprehensive theory can develop.

#### Relativistic Kinematics.

In particle physics, particle reactions involve high energy, e.g in the collider, violent

outgoing particles
incoming beam
incoming beam
outgoing particles

collisions. Thus the readions are relativistic

We review special relativity in 4-vector notations and study simple examples in high energy collisions.

Special Relativity:

Frames of reference

Postulates of special Relativity

Galilean and Loventz transformations