How to test whether parity is conserved?

Do experiment.

27

- (1) Prepare a physical system (object) or a reaction which has a handedness (chirality)
- (2) Investigate the mirror image of this chiral object or neadion. Thus a LH reaction occurs as a RH reaction in the mirror world LH = beft hand, RH = right hand.
- (3) If mirror events = physical events (events in physical world), then parity is conserved
- (4) If mirror event & physical event, then, as a phenomenon, parity is not conserved (i.e. broken).
- (5) However the nonconservation of parity in the events (phenomena) may be due to the initial choice of solutions, or it may be due to dynamics
- (6) If it can be attributed to the initial choice of solutions, we can still claim parity is conserved.

  (E.g. human heart position on the left side of the chest.)

  Otherwise, the nonconservation is due the dynamics

Otherwise, the nonconservation is all the agranics

and we say parity is broken

Discuss. downfall of parity conservation in reflection symmetry broken.

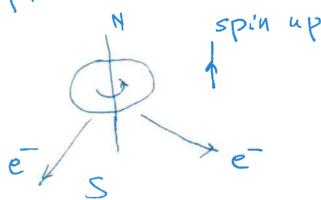
C.S. Wu experiment 1956

$$60_{27} 0 \rightarrow 60_{Ni} + e^- + \overline{\nu}_e$$

(basically,  $n \rightarrow p + e^- + \overline{\nu}_e$ )

or  $d \rightarrow u + e^- + \overline{\nu}_e$ )

The cobalt 60 nuclei were coolled to very low temperature so that their spins were aligned up

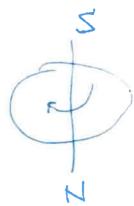


9 8. 1 9

the electrons were detected in the southerly' direction, opposite to the 60 spin up direction.

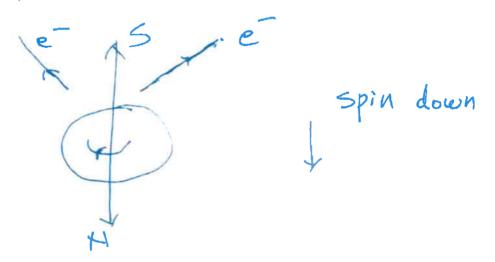
Repeat the experiment.

Invert spins of the 60 co nuclei to the down direction. Spin



Spindown

Again the electrons were emitted opposite to the nuclear spin direction



The image process as shown

was not detected.

+ spin down

+ spin down

| without

| process,

-> Parity is broken

Preferential emission of electrons in direction opp Cobalt-60 nuclear spin thus contradicting the expectation of parity conservation.

If the image process (e emitted in the same direction as the nuclear spin) were observed, then in physical world both original process and image process occur.

that means one cannot differentiate between the physical world and the mirror world. That would mean parity would be conserved.

CS Wa experiment clearly indicates parity. is broken.

Note that we did point out before mirror reflection can be done with a notation in a higher dimensional space. E. g. reflection in 2-dim. can be realized as notation in 3-dim doject & image 2-dim.

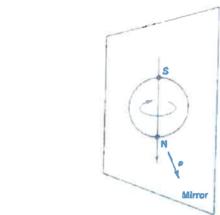
9 H:moli

P can be rotated to 9 in 3-dimensional space.

$$\begin{array}{c} 60 \\ 27 \\ \downarrow \\ Nucleus \end{array}$$

$$\begin{array}{c} 60 \\ 28 \\ \downarrow \\ (n \rightarrow P + e^- + \frac{1}{4}e \\ or d \rightarrow u + e^- + \frac{1}{4}e \end{array})$$
Nucleus

4.4 Discrete Symmetries 137



The asymmetric

distribution of the

electrons emitted

in the 60CD de cays indicates parity is not

conservad.

electrons are emitted in the direction oppo-electrons are emitted parallel to the nuclear side to the nuclear spin.

4.7 in the beta decay of cobalt 60, most Fig. 4.8 Mirror Image of Figure 4.7: Most

see in Chapter 9, it is in fact 'maximal'. Nor is it limited to beta decay in cobalt: once you look for it, parity violation is practically the signature of the weak force. It is most dramatically revealed in the behavior of the neutrino. In the theory of angular momentum, the axis of quantization is, by convention, the z axis. Of course, the orientation of the z axis is completely up to us, but if we are dealing with a particle traveling through the laboratory at velocity v. a natural choice suggests itself: why not pick the direction of motion as the z axis? The value of ma/s for this axis is called the helicity of the particle. Thus a particle of spin  $\frac{1}{2}$  can have a helicity of  $+1(m_1=\frac{1}{2})$  or  $-2(m_1=-\frac{1}{2})$ ; we call the former 'right-handed' and the latter 'left-handed'." The difference is not terribly profound, however, because it is not Lorentz-invariant. Suppose I have a right-handed electron going to the right (Figure 4.9a), and someone else looks at it from an inertial system traveling to the right at a speed greater than v. From his perspective, the electron is going to the left (Figure 4.9b); but it is still spinning the same way, so this observer will say it's a left-handed electron. In other words, you can convert a right-handed electron into a left-handed one simply by changing your frame of reference. That's what I mean, when I say the distinction is not Lorentz-invariant.

But what if we applied that same reasoning to a neutrino - taken, for the moment, to be massless, so it travels at the speed of light, and hence there is no observer traveling faster? It is impossible to 'reverse the direction of motion' of a (massless) neutrino by getting into a faster-moving reference system, and therefore the helicity

Read: scientific American, April 1957, volume 196, Number 4, pages 45-53 (1957): The Overthrow of parity

<sup>•</sup> In Chapter 9, I shall introduce a technical distinction between 'handedness' and helicity, but for the moment I will use the terms interchangealty.

Further discussion on Parity

Our physical right hand (RH) becomes a Left hand (LH) in the mirror world.

If in our physical world, we all have only one hand, the RH, then we can use hand to differentiate between a physical world and a mirror world. As soon as we see only RH human beings we immediately know we are in physical world whereas if we see only LH human beings, we are in the mirror world. Because we can distinguish RH and LH distindly, we say space inversion (mirror reflection) is not a symmetry.

However in our physical world, we have both RH and It equally. In other words, RH and its image LH by LH and its image RH, both appear in our physical world (and hence also equally in the mirror world). We therefore cannot use our hand to say whether we are in the physical world or in the mirror world. As far as hands are concerned, physical world and mirror world are the same. We say space inversion is a



perfect symmetry (symmetry = 1055 of information)

On the other hand, we can use the position of a human heart in a human being to differentiate a physical world and a mirror world because in the physical world almost all human hearts are on the left hand side of the chest, whereas the other way in the mirror world. So phenomenologically human heart indicates that space inversion is a broken symmetry. However human heart is based on the electromagnetic interaction which is described by the Maxwell equation. Maxwell's equation remains the same under space inversion. So although as a phenomenon human heart breaks space inversion symmetry its dynamics still obeys space inversion symmetry

CS Wa experiment involves a physical process the weak decay of  $co^6$  to Hi60 ( $n \rightarrow p + e^- + V_e$  or  $d \rightarrow u + e^- + V_e$ ). As a physical process (the decay of  $co^{60}$ ), the  $e^-$  is detected in a direction opposite to the nudeus ( $co^{60}$ ) spin direction (momentum of

the electron e, P, and the spin & of the Co in opposite directions) The mirror process in which I and & same directions. are hardly seen in our physical world. 50 the decay process of co60 is an indicator of broken space inversion symmetry. This broken space inversion symmetry is not only as a phenomenon, but also dynamical. This is because de cay process involves weak interaction. so We say wed suteraction breaks the space inversion symmetry. We own use weak interaction process as an indicator whether we are in a physical world ( 2 & opposite) or in a mirror world ( P & same direction).

Perfect symmetry implies loss of information But to discuss physics, we still needs to assign convention to break the symmetry. Consider a sphere. We need to assign its Thorth (N) or south (s) to describe the sphere fully. That is, N,S is a convention. N, s convention can be assigned rigidly (globely) or non-rigidly (Hexibly, or locally) However it appears that space inversion symmetry, supposed is a perfect symmetry, the convention of left hand (L) or right hand (R) can only assigned rigidly (globally). Theoretically we still do not how to assign L, R convention

locally.



Handedness is a property of a physical system or a physical process under mirror reflection or space inversion. If under mirror reflection, the physical system or physical process remains the same, we say the system has no handedness, otherwise, it is either left or right handed. E. g. sphere has no handedness, a screw is right-handed.

Helicity is defined as the projection of the spin of the physical system along its momentum direction.

For a spin  $\frac{1}{2}$  particle, its helicity is defined as

$$h(\vec{p}) = \frac{\vec{\Sigma} \cdot \vec{p}}{\vec{p}}$$

where  $\frac{\hbar}{2}\vec{\Sigma}$  is spin operator of the particle.

Helicity is a kinematic property for a system in motion, this system must also have a nonzero spin.

Chirality is defined as an intrinsic property of an elementary particle. For a spin  $\frac{1}{2}$  particle, chirality is given by the Dirac matrix  $\gamma^5$ 

Conceptually the two are different, helicity not the same as chirality.

However it is often stated that the two are the same if they are massless. This is easy to prove for spin 1/2 system by using the Dirac equation.

Handedness as a term is applicable to helicity and chirality, by usage convention.

charge conjugation

Originally charge conjugation means the electric charge changes to be electric charge and vice versa charge conjugation C is a symmetry transformation for the Maxwell equations

speed of light  $\rightarrow C^2 (\nabla \wedge B) = \frac{\partial B}{\partial C} + \frac{\partial E}{\partial C}$   $\nabla \cdot B = 0$ 

Under C, P - - P, 2 - - j

E - - E & - B: F = 9 (E + Y AB)

Maxwell's equations remain unchanged. invariant

Extend Charge conjugation to flip sign of all internal quantum numbers e.g. Isospin Basically, particles -> anti-particles

Apply Charge conjugation C to elementary particles

Few particles are eigenstates of C

To be eigenstate of C, the particle must be neutral. Yet neutron is not an eigenstate of C, neutron + antineutron

Table 4.6 Quantum numbers of some meson nonets

Orbital angular momentum	Net spin		Observed Nonet			4
		JPC	1=1	$l=\frac{1}{2}$	1-0	. Average mass (MeV/c²)
l = 0	s == 0	0-+	л	K	η, η'	400
	s = 1	1	P	K*	φ, ω	900
l = 1	s == 0	1+-	$b_1$	K <sub>1 H</sub>	$h_1, h_1$	1200
	s = 1	0++	20	K.	fo.fo	1100
	s = 1	1++	aı	K <sub>1.4</sub>	$f_1,f_1$	1300
	s == 1	2++	a2	K <sub>1,A</sub> K <sub>2</sub> *	$f'_2,f_2$	1400

It seemed peculiar that two otherwise identical particles should carry different parity. The alternative, suggested by Lee and Yang in 1956 was that  $\tau$  and  $\theta$  are really the same particle (now known as the  $K^+$ ), and parity is simply not conserved in one of the decays. This idea prompted their search for evidence of parity invariance in the weak interactions and, when they found none, to their proposal for an experimental test.

#### 4.4.2 Charge Conjugation

Toda .

Classical electrodynamics is invariant under a change in the sign of all electric charges; the potentials and fields reverse their signs, but there is a compensating charge factor in the Lorentz law, so the forces still come out the same. In elementary particle physics, we introduce an operation that generalizes this notion of 'changing the sign of the charge'. It is called *charge conjugation*, C, and it converts each particle into its antiparticle:

$$C|p\rangle = |\overline{p}\rangle$$
 (4.54)

'Charge conjugation' is something of a misnomer, for C can be applied to a neutral particle, such as the neutron (yielding an antineutron), and it changes the sign of all the 'internal' quantum numbers - charge, baryon number, lepton number, strangeness, charm, beauty, truth - while leaving mass, energy, momentum, and spin untouched.

As with P, application of C twice brings us back to the original state:

$$C^2 = I (4.55)$$

and hence the eigenvalues of C are  $\pm 1$ . Unlike P, however, most of the particles in nature are clearly not eigenstates of C. For if  $|p\rangle$  is an eigenstate of C, it follows that

$$C|p\rangle = \pm |p\rangle = |\vec{p}\rangle \tag{4.56}$$

so  $|p\rangle$  and  $|\bar{p}\rangle$  differ at most by a sign, which means that they represent the same physical state. Thus, only those particles that are their own antiparticles can be eigenstates of C. This leaves us the photon, as well as all those mesons that lie at the center of their Eightfold-Way diagrams:  $\pi^0$ ,  $\eta$ ,  $\eta'$ ,  $\rho^0$ ,  $\phi$ ,  $\omega$ ,  $\psi$ , and so on. Because the photon is the quantum of the electromagnetic field, which changes sign under C, it makes sense that the photon's 'charge conjugation number' is -1. It can be shown [19] that a system consisting of a spin- $\frac{1}{2}$  particle and its antiparticle, in a configuration with orbital angular momentum l and total spin s, constitutes an eigenstate of C with eigenvalue  $(-1)^{l+s}$ . According to the quark model, the mesons in question are of precisely this form: for the pseudoscalars, l=0 and s=0, so C=+1; for the vectors, l=0 and s=1, so C=-1. (Often, as in Table 4.6, C is listed as though it were a valid quantum number for the entire supermultiplet; in fact it pertains only to the central members.)

Charge conjugation is a multiplicative quantum number, and, like parity, it is conserved in the strong and electromagnetic interactions. Thus, for example, the  $\pi^0$  decays into two photons:

$$\pi^0 \to \gamma + \gamma \tag{4.57}$$

(for n photons  $C=(-1)^n$ , so in this case C=+1 before and after), but it cannot decay into three photons. Similarly, the  $\omega$  goes to  $\pi^0+\gamma$ , but never to  $\pi^0+2\gamma$ . In the strong interactions, charge conjugation invariance requires, for example, that the energy distributions of the charged pions in the reaction

$$p + \overline{p} \rightarrow \pi^+ + \pi^- + \pi^0 \tag{4.58}$$

should (on average) be identical [20]. On the other hand, charge conjugation is not a symmetry of the weak interactions: when applied to a neutrino (left-handed, remember), C gives a left-handed antineutrino, which does not occur. So the charge-conjugated version of any process involving neutrinos is not a possible physical process. And purely hadronic weak interactions also show violations of C as well as P.

Because so few particles are eigenstates of C, its direct application in elementary particle physics is rather limited. Its power can be somewhat extended, if we confine our attention to the strong interactions, by combining it with an appropriate isospin transformation. Rotation by 180° about the number 2 axis in isospin space\* will carry  $I_3$  into  $-I_3$ , converting, for instance, a  $\pi^+$  into a  $\pi^-$ . If we then apply the charge conjugation operator, we come back to  $\pi^+$ . Thus the charged pions are eigenstates of this combined operator, even though they are not eigenstates of C alone. For some reason the product transformation is called 'G-parity':

$$G = CR_2$$
, where  $R_2 = e^{i\pi l_2}$  (4.59)

 $\omega$ -meson is a vector meson  $\omega = -\omega$ 

71 - Meson is

a pseudoscalar

C π°= π°

<sup>\*</sup> Some authors use the number 1 axis. Obviously, any axis in the 1-2 plane will do the job.

144 4 Symmetries

All mesons that carry no strangeness (or charm, beauty, or truth) are eigenstates of G;\* for a multiplet of isospin I the eigenvalue is given (Problem 4.36) by

$$G = (-1)^{T}C (4.60)$$

where C is the charge conjugation number of the neutral member. For a single pion, G = -1, and for a state with n pions

$$G = (-1)^n \tag{4.61}$$

This is a very handy result, for it tells you how many pions can be emitted in a particular decay. For example, the  $\rho$  mesons, with I=1, C=-1, and hence G=+1, can go to two pions, but not to three, whereas the  $\phi$ , the  $\omega$ , and the  $\psi$  (all I=0) can go to three, but not to two.

4.4.3 CP

As we have seen, the weak interactions are not invariant under the parity transformation P; the cleanest evidence for this is the fact that the antimuon emitted in pion decay

$$\pi^+ \to \mu^+ + \nu_\mu \tag{4.62}$$

always comes out left-handed. Nor are the weak interactions invariant under C, for the charge-conjugated version of this reaction would be

$$\pi^- \to \mu^- + \overline{\nu}_{\mu} \tag{4.63}$$

with a left-handed muon, whereas in fact the muon always comes out right-handed. However, if we combine the two operations we're back in business: CP turns the left-handed antimuon into a right-handed muon, which is exactly what we observe in nature. Many people who had been shocked by the fall of parity were consoled by this realization; perhaps, it was the combined operation that our intuition had been talking about all along — maybe what we should have meant by the 'mirror image' of a right-handed electron was a left-handed positron.\(^{\frac{1}{2}}\) If we had defined parity from the start to be what we now call CP, the trauma of parity violation might have been avoided (or at least postponed). It is too late to change the terminology

muon always comes out righthanded in the chargeconjugated version

## Note:

Charge conjugation C is Hermitian and thus an observable Spatial inversion P is Hermitian and thus an observable Time inversion T is NOT Hermitian, NOT observable Similarly, rotation operator not an observable

<sup>\*</sup> K<sup>+</sup>, for example, is not an eigenstate of G, for R<sub>2</sub> takes it to K<sup>0</sup>, and C takes that to K<sup>0</sup>. The idea could be extended to the K's, by using an appropriate SU(3) transformation in place of R<sub>2</sub>, but since SU(3) is not a very good symmetry of the strong forces, there is little percentage in doing so.

brough so.

Incidentally, we could perfectly well take electric charge to be a pseudoscalar in classical electrodynamics; E becomes a pseudovector and B a vector, but the results are all the same. It is really a matter of taste whether you say the mirror image of a plus charge is positive or negative. But it seems simplest to say the charge does not change, and this is the standard convention.

(15)

Photon and all those mesons that lie at the center of their Eightfold-way diagrams: 70, 11, 11'
e°, 4, w, 4... are eigenstates of charge

Neutral particles (except the neutron) are eigenstates of C

Conjugation opeator C

l'or mesons, ligenvalue of  $C = (-1)^{l+s}$ l= orbital angular momentum, s = spin

For pseudoscalar mesons, l=0 and s=0 :: C=1e.g C  $\pi^{\circ}=\pi^{\circ}$ 

For vector mesons, l=0, s=1, ... c=-1

e.g c w = - w

Not many hadrons are eigenstates of C.

Consider G-parity for hadrons,

combining C with isospin rotation

Ce TII2

Consider week decays, e.g. pion decay

· Pion decay violates charge conjugation Consider the weak decay of IT: T- + Vi In the frame at which the TT is at rest, Apply Π, expect to see this but reality is you'll NEVER SEE LEFT-HANDED anti-neutrinos (P violated) RH antineutrino helicity +1 muon helicity +1 (right-handed) (1) (right-handed) Under charge conjugation C, We expect to get  $\pi^+ \longrightarrow \mu^+ + \nu_{\mu}$ C changes internal quantum numbers only, C does

not change angular momentum (spin polarization). 50

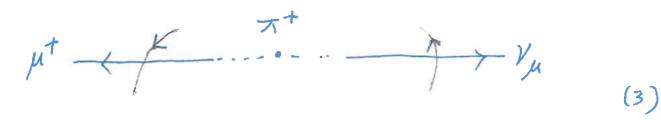
Fig(1) becomes

# **EXPECTATION**

The Year (z)

But in nature, we observe

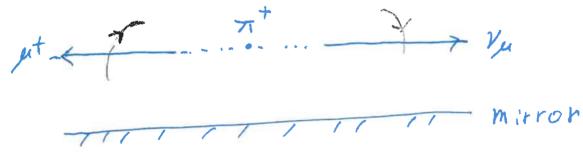
### REALITY



this means the decay of Ti Violates the charge conjugation since fig(2) = fig (3).

If we apply parity operator II to fig (2),
We can get fig (3).

Place a mirror beneath fig (2)



we then get fig (3)



So applying C and P jointly ie CP, fig(1) becomes fig (3) which is realized in nature. CP is a symmetry obeyed by  $\pi$ - decay

# Discuss CP violation

All reactions obey CP symmetry (e.g. in the decay of To as illustrated in the previous figures) except the Kaons (containing strange quarks Ko = ds) decays, the B (B° = db, containing b quark) decays and possibly the D decay (containing equark, D=cu) (d)(s)(t) Kaons K° (strangeness +1), K° (strangeness -1) are produced in strong interaction processes, e.g.

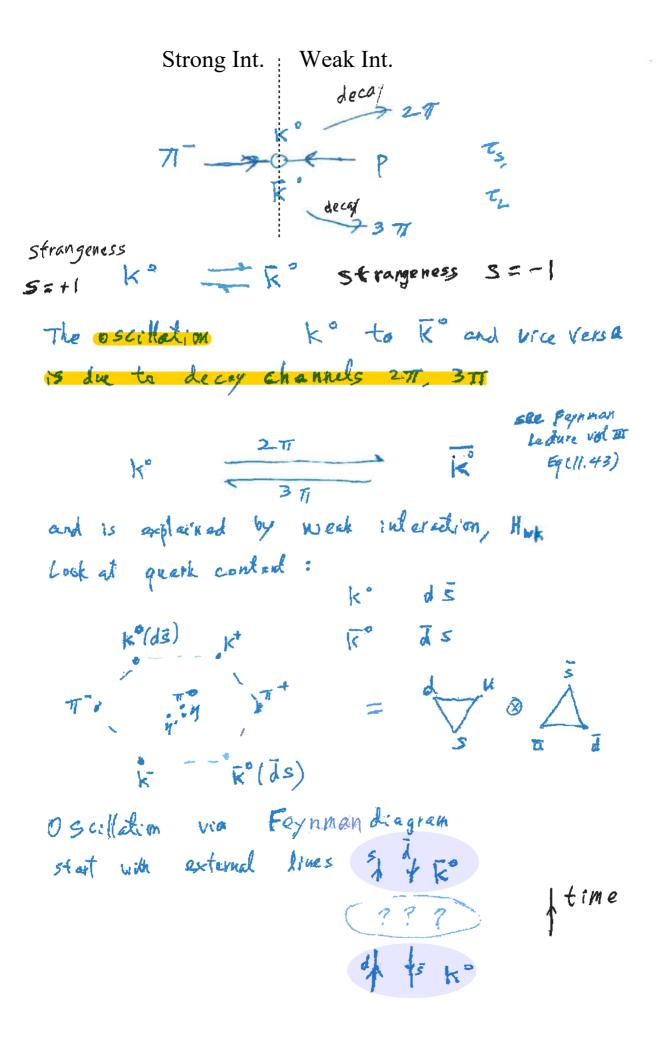
K°= ds  $\pi^{\dagger} P \rightarrow P + k^{\dagger} + \overline{k}^{\circ}$ 

(see Faynman Lecture Vol3, p. 11-12 to 11-20)

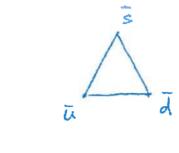
Ko and Ro are eigenstates of Hst (strong interaction Hamiltonian). Let Ho = Hot + Hem & electromagnetic Ho IKO> = EO IKO> = EO IKO>

Experimentally (i) ko oscillates to Ko and they decay into or 3 Th via weak interaction The decays have 2 different life times

TS = 0. 89 X 10 S, TL = 5.2 X 10 S



-



d s

u š

dā.

dd., uū ss

• ud

s ū ·

sid Ko

Fet the relevant week interaction vertex (see 2nd lecture

PowerPoint)

Y

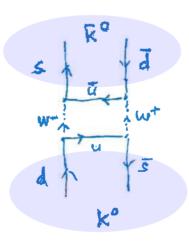
= intermediate bosons

9

Insert vertices to complete the dragram,

an example is

Similarly



Line

The above two diagrams illustrates the oscillations of  $K^{\circ} \rightrightarrows \overline{K}^{\circ}$ 

We now proceed to explain the two decay modes:  $2\pi$ 's and  $3\pi$ 's  $K^0 \to 2\pi$  and also two lifetimes  $\tau_s$ ,  $\tau_s$ 

k", k" are produced by strong interaction. Immediately they decay by weak interaction. One can say the kaons appear as particles Ko, Ko when interact strongly, but appear as particles Ks, KL when interact weakly Gellman & Pais (1955) Proposed to use linearly superposed states, Ks, KL are linearly superposed from Ko Ko 1Ks> ~ 1k°> - 1K°> 1KL> ~ 1K°> + 1K°>

Applying charge conjugation C and parity operato P

CP 1Ks> ~ CP (1Ke> - 1Fe>)

Note: Previously we denote parity operator (space inversion operator) by Jr.

Now 
$$CP|K_0\rangle = C(-)|K_0\rangle = -C|K_0\rangle = -|K_0\rangle$$

hence

$$HWCPIK_s > - + |k_s\rangle$$

$$CPIK_h > - |K_h\rangle$$

$$egin{aligned} \mathcal{CP}\ket{K_s} &\sim \mathcal{CP}(\ket{K^{\mathrm{o}}} - \ket{ar{K}^{\mathrm{o}}})) \ &= \mathcal{C}(-)\ket{K^{\mathrm{o}}} - \mathcal{C}(-)\ket{ar{K}^{\mathrm{o}}}) \ &= -\ket{ar{K}^{\mathrm{o}}} + \ket{K^{\mathrm{o}}} \ &= \ket{K_s} \ \mathcal{CP}\ket{K_L} &\sim \mathcal{CP}(\ket{K^{\mathrm{o}}} + \ket{ar{K}^{\mathrm{o}}})) \ &= \mathcal{C}(-)\ket{K^{\mathrm{o}}} + \mathcal{C}(-)\ket{ar{K}^{\mathrm{o}}} \ &= -\ket{ar{K}^{\mathrm{o}}} - \ket{K^{\mathrm{o}}} \ &= -\ket{K_L} \end{aligned}$$

1ks > eigenstate of CP with eigenvalue +1 TK eigenstate of CP with eigenvalue -1

With the introduction of kaons as ks, k, in weak decay, we can account for the 2 Tis and 3 The decays.

For 2 Pions, CPIT° T°> = C (-1) (-1) 1x° T°> = c \10° T° > = \17° T°>  $CP | \pi^+ \pi^- \rangle = C (4) (-1) | \pi^+ \pi^- \rangle = C | \pi^+ \pi^- \rangle = | \pi^- \pi^+ \pi^- \rangle$  Similarly for 3 pions, Cp = (-1)(-1)(-1) = -1.

Tf CP is conserved in weak decay, then

Ks -> 2 pions and K\_ -> 3 pions

To check CP conservation, the Kaons after production can be separated out as ks and KL particles

1964 Cronin- Fitch

source

57 ft away ≈ 17.4 m

K, K's
are produced

only K\_ remained (no more Ks)

found 45 2-pion decays among 22700 decays.

If cp is conserved, Ki can only decay to 3 pions. So this experiment indicates CP is not conserved in Kaon decays.

(24)

However the violation of CP conservation is very small

$$\frac{45}{22700}$$
 2 × 10<sup>-3</sup>

We proceed to account for  $K^{\circ} = \overline{K^{\circ}}$ 0 scillation and CP violation of kaon decays

by treating the kaon as a 2-state

System, see Feynman Lecture vol 3,

Chapter 11.

1