

New Experiments

June 8, 2018

Vary Warm Start + Effective end of game

Here we vary the size of the warm start (the number of observations given to the principals before the competing bandits game begins). We also track a new quantity - the “effective end of game” which we define as the last round where there is a “switch” in the decision of the agent. So, for instance, if in $t - 1$ the agent picks principal 1 and in t the agent picks principal 2 then this is a “switch.” The last time this happens in a simulation is defined as effective end of game (EEOG).

Below we report the results of running on the same priors we have been considering, but varying the warm start and recording market share + EEOG.

Results for Needle In Haystack - 0.5 HardMax K=10

	WS = 1	WS = 5	WS = 10	WS = 15	WS = 20	WS = 50	WS = 100
TS vs DG	0.54 (0.02) <u>eeog</u> avg: 49 med: 0	0.62 (0.02) <u>eeog</u> avg: 140 med: 1	0.64 (0.02) <u>eeog</u> avg: 180 med: 7	0.66 (0.02) <u>eeog</u> avg: 190 med: 15	0.64 (0.02) <u>eeog</u> avg: 210 med: 24	0.64 (0.02) <u>eeog</u> avg: 240 med: 62.5	0.61 (0.02) <u>eeog</u> avg: 250 med: 26
TS vs DEG	0.53 (0.03) <u>eeog</u> avg: 37 med: 0	0.58 (0.02) <u>eeog</u> avg: 80 med: 0	0.59 (0.02) <u>eeog</u> avg: 100 med: 0	0.61 (0.02) <u>eeog</u> avg: 130 med: 4	0.6 (0.02) <u>eeog</u> avg: 150 med: 10	0.58 (0.02) <u>eeog</u> avg: 180 med: 31	0.53 (0.02) <u>eeog</u> avg: 240 med: 17
DG vs DEG	0.5 (0.02) <u>eeog</u> avg: 130 med: 3	0.47 (0.02) <u>eeog</u> avg: 240 med: 10	0.47 (0.02) <u>eeog</u> avg: 300 med: 47	0.44 (0.02) <u>eeog</u> avg: 300 med: 61	0.46 (0.02) <u>eeog</u> avg: 350 med: 114	0.44 (0.02) <u>eeog</u> avg: 470 med: 194	0.45 (0.02) <u>eeog</u> avg: 570 med: 303.5

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Results for Heavy Tail HardMax K=10

	WS = 1	WS = 5	WS = 10	WS = 15	WS = 20	WS = 50	WS = 100
TS vs DG	0.46 (0.03) <u>eeog</u> avg: 11 med: 0	0.37 (0.02) <u>eeog</u> avg: 40 med: 0	0.32 (0.02) <u>eeog</u> avg: 44 med: 0	0.31 (0.02) <u>eeog</u> avg: 53 med: 0	0.33 (0.02) <u>eeog</u> avg: 57 med: 0	0.43 (0.02) <u>eeog</u> avg: 85 med: 0	0.51 (0.02) <u>eeog</u> avg: 120 med: 0
TS vs DEG	0.45 (0.03) <u>eeog</u> avg: 6.2 med: 0	0.35 (0.02) <u>eeog</u> avg: 12 med: 0	0.32 (0.02) <u>eeog</u> avg: 23 med: 0	0.3 (0.02) <u>eeog</u> avg: 23 med: 0	0.32 (0.02) <u>eeog</u> avg: 44 med: 0	0.44 (0.02) <u>eeog</u> avg: 83 med: 0	0.6 (0.02) <u>eeog</u> avg: 170 med: 0
DG vs DEG	0.53 (0.02) <u>eeog</u> avg: 130 med: 2	0.56 (0.02) <u>eeog</u> avg: 200 med: 1	0.57 (0.02) <u>eeog</u> avg: 270 med: 2	0.61 (0.02) <u>eeog</u> avg: 330 med: 3	0.6 (0.02) <u>eeog</u> avg: 400 med: 7	0.64 (0.02) <u>eeog</u> avg: 540 med: 181.5	0.62 (0.02) <u>eeog</u> avg: 650 med: 390

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Results for Uniform HardMax K=10

	WS = 1	WS = 5	WS = 10	WS = 15	WS = 20	WS = 50	WS = 100
TS vs DG	0.5 (0.03) <u>eeog</u> avg: 48 med: 0	0.47 (0.02) <u>eeog</u> avg: 120 med: 0	0.45 (0.02) <u>eeog</u> avg: 180 med: 0	0.44 (0.02) <u>eeog</u> avg: 220 med: 0	0.42 (0.02) <u>eeog</u> avg: 270 med: 0	0.4 (0.02) <u>eeog</u> avg: 410 med: 26.5	0.42 (0.02) <u>eeog</u> avg: 550 med: 260
TS vs DEG	0.48 (0.03) <u>eeog</u> avg: 33 med: 0	0.46 (0.02) <u>eeog</u> avg: 94 med: 0	0.44 (0.02) <u>eeog</u> avg: 140 med: 0	0.41 (0.02) <u>eeog</u> avg: 170 med: 0	0.43 (0.02) <u>eeog</u> avg: 220 med: 0	0.38 (0.02) <u>eeog</u> avg: 390 med: 11.5	0.39 (0.02) <u>eeog</u> avg: 530 med: 239
DG vs DEG	0.48 (0.02) <u>eeog</u> avg: 120 med: 2	0.49 (0.02) <u>eeog</u> avg: 270 med: 7	0.5 (0.02) <u>eeog</u> avg: 390 med: 15	0.5 (0.02) <u>eeog</u> avg: 450 med: 27	0.5 (0.02) <u>eeog</u> avg: 500 med: 72.5	0.51 (0.02) <u>eeog</u> avg: 720 med: 584.5	0.5 (0.02) <u>eeog</u> avg: 890 med: 915.5

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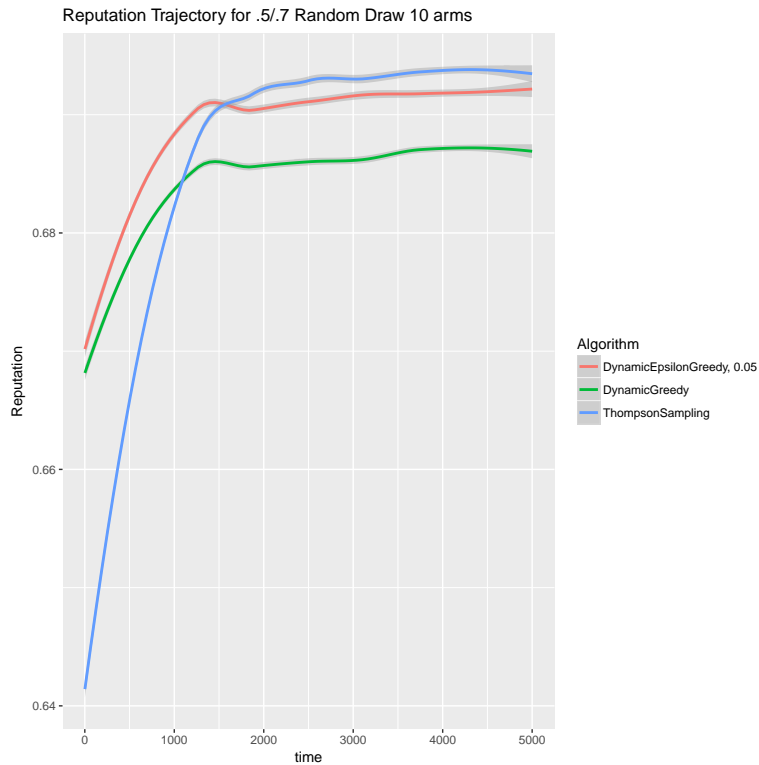
Results for .5/.7 Random Draw HardMax K=10

	WS = 1	WS = 5	WS = 10	WS = 15	WS = 20	WS = 50	WS = 100
TS vs DG	0.52 (0.06) <u>eeog</u> avg: 600 med: 0	0.52 (0.05) <u>eeog</u> avg: 1500 med: 3.5	0.45 (0.05) <u>eeog</u> avg: 2200 med: 5	0.46 (0.05) <u>eeog</u> avg: 3000 med: 26.5	0.5 (0.05) <u>eeog</u> avg: 3800 med: 1021	0.44 (0.05) <u>eeog</u> avg: 5700 med: 5800.5	0.4 (0.04) <u>eeog</u> avg: 7100 med: 7655.5
TS vs DEG	0.53 (0.06) <u>eeog</u> avg: 570 med: 0	0.49 (0.06) <u>eeog</u> avg: 1700 med: 3	0.42 (0.05) <u>eeog</u> avg: 2500 med: 3	0.46 (0.05) <u>eeog</u> avg: 3100 med: 26	0.45 (0.05) <u>eeog</u> avg: 4400 med: 1440.5	0.42 (0.05) <u>eeog</u> avg: 5900 med: 5360	0.43 (0.04) <u>eeog</u> avg: 7100 med: 7606.5
DG vs DEG	0.47 (0.05) <u>eeog</u> avg: 990 med: 2	0.48 (0.05) <u>eeog</u> avg: 3000 med: 67	0.47 (0.05) <u>eeog</u> avg: 4000 med: 246.5	0.46 (0.05) <u>eeog</u> avg: 4700 med: 1648	0.52 (0.05) <u>eeog</u> avg: 4600 med: 2472.5	0.52 (0.04) <u>eeog</u> avg: 6600 med: 7155	0.49 (0.04) <u>eeog</u> avg: 7800 med: 9041

.5/.7 Instance

This is an instance where the arms are uniformly either 0.5 or 0.7 (as opposed to Needle in a Haystack where 9 arms have mean 0.5 and 1 arm has mean 0.7).

This is what the preliminary calibration for this instance looks like:



The results of the simulations:

Results for t= 15000 .5/.7 Random Draw Warm Start= 1 K= 10

	TS vs DEG	TS vs DG	DG vs DEG	TS vs TS	DEG vs DEG	DG vs DG
HM	0.53 +/- 0.06 Var: 0.24 Share: 96 %	0.53 +/- 0.06 Var: 0.24 Share: 97 %	0.46 +/- 0.05 Var: 0.23 Share: 92 %			
HMR	0.5 +/- 0.02 Var: 0.027 Share: 1.3 %	0.52 +/- 0.02 Var: 0.047 Share: 11 %	0.49 +/- 0.02 Var: 0.04 Share: 11 %			
SM	0.5 +/- 0.007 Var: 0.0037 Share: 0 %	0.51 +/- 0.01 Var: 0.017 Share: 0 %	0.48 +/- 0.01 Var: 0.017 Share: 0 %			

Results for t= 15000 .5/.7 Random Draw Warm Start= 5 K= 10

	TS vs DEG	TS vs DG	DG vs DEG	TS vs TS	DEG vs DEG	DG vs DG
HM	0.52 +/- 0.06 Var: 0.24 Share: 94 %	0.54 +/- 0.05 Var: 0.23 Share: 91 %	0.49 +/- 0.05 Var: 0.21 Share: 81 %			
HMR	0.53 +/- 0.02 Var: 0.032 Share: 4.3 %	0.51 +/- 0.02 Var: 0.043 Share: 9 %	0.49 +/- 0.02 Var: 0.038 Share: 9.3 %			
SM	0.5 +/- 0.007 Var: 0.0034 Share: 0 %	0.5 +/- 0.01 Var: 0.011 Share: 0 %	0.5 +/- 0.01 Var: 0.014 Share: 0 %			

Results for t= 15000 .5/.7 Random Draw Warm Start= 10 K= 10

	TS vs DEG	TS vs DG	DG vs DEG	TS vs TS	DEG vs DEG	DG vs DG
HM	0.43 +/- 0.05 Var: 0.21 Share: 86 %	0.48 +/- 0.05 Var: 0.22 Share: 88 %	0.46 +/- 0.05 Var: 0.18 Share: 66 %			
HMR	0.52 +/- 0.02 Var: 0.029 Share: 2.3 %	0.49 +/- 0.02 Var: 0.043 Share: 9.7 %	0.51 +/- 0.02 Var: 0.036 Share: 7.3 %			
SM	0.5 +/- 0.006 Var: 0.0032 Share: 0 %	0.5 +/- 0.01 Var: 0.014 Share: 0.33 %	0.5 +/- 0.01 Var: 0.011 Share: 0 %			

Results for t= 15000 .5/.7 Random Draw Warm Start= 15 K= 10

	TS vs DEG	TS vs DG	DG vs DEG	TS vs TS	DEG vs DEG	DG vs DG
HM	0.49 +/- 0.05 Var: 0.21 Share: 78 %	0.47 +/- 0.05 Var: 0.21 Share: 81 %	0.42 +/- 0.05 Var: 0.17 Share: 67 %			
HMR	0.5 +/- 0.02 Var: 0.031 Share: 2.7 %	0.51 +/- 0.02 Var: 0.042 Share: 9.3 %	0.48 +/- 0.02 Var: 0.035 Share: 7.7 %			
SM	0.5 +/- 0.008 Var: 0.0045 Share: 0 %	0.5 +/- 0.01 Var: 0.014 Share: 0 %	0.49 +/- 0.01 Var: 0.013 Share: 0.33 %			

Results for t= 15000 .5/.7 Random Draw Warm Start= 20 K= 10

	TS vs DEG	TS vs DG	DG vs DEG	TS vs TS	DEG vs DEG	DG vs DG
HM	0.48 +/- 0.05 Var: 0.19 Share: 72 %	0.53 +/- 0.05 Var: 0.2 Share: 76 %	0.51 +/- 0.05 Var: 0.17 Share: 61 %			
HMR	0.5 +/- 0.02 Var: 0.025 Share: 2 %	0.5 +/- 0.02 Var: 0.042 Share: 9.7 %	0.49 +/- 0.02 Var: 0.036 Share: 9.3 %			
SM	0.5 +/- 0.007 Var: 0.0033 Share: 0 %	0.5 +/- 0.01 Var: 0.013 Share: 0.33 %	0.51 +/- 0.01 Var: 0.01 Share: 0 %			

Results for t= 15000 .5/.7 Random Draw Warm Start= 50 K= 10

	TS vs DEG	TS vs DG	DG vs DEG	TS vs TS	DEG vs DEG	DG vs DG
HM	0.47 +/- 0.04 Var: 0.16 Share: 53 %	0.51 +/- 0.05 Var: 0.16 Share: 59 %	0.48 +/- 0.04 Var: 0.14 Share: 46 %			
HMR	0.51 +/- 0.02 Var: 0.024 Share: 2.7 %	0.51 +/- 0.02 Var: 0.044 Share: 11 %	0.49 +/- 0.02 Var: 0.04 Share: 10 %			
SM	0.5 +/- 0.008 Var: 0.0047 Share: 0 %	0.49 +/- 0.01 Var: 0.012 Share: 0 %	0.48 +/- 0.01 Var: 0.016 Share: 0 %			

Results for t= 15000 .5/.7 Random Draw Warm Start= 100 K= 10

	TS vs DEG	TS vs DG	DG vs DEG	TS vs TS	DEG vs DEG	DG vs DG
HM	0.49 +/- 0.04 Var: 0.14 Share: 47 %	0.47 +/- 0.04 Var: 0.14 Share: 50 %	0.5 +/- 0.04 Var: 0.13 Share: 41 %			
HMR	0.5 +/- 0.02 Var: 0.024 Share: 2.3 %	0.5 +/- 0.02 Var: 0.035 Share: 7.3 %	0.5 +/- 0.02 Var: 0.037 Share: 9.7 %			
SM	0.5 +/- 0.007 Var: 0.0042 Share: 0 %	0.5 +/- 0.01 Var: 0.014 Share: 0.67 %	0.5 +/- 0.01 Var: 0.012 Share: 0 %			

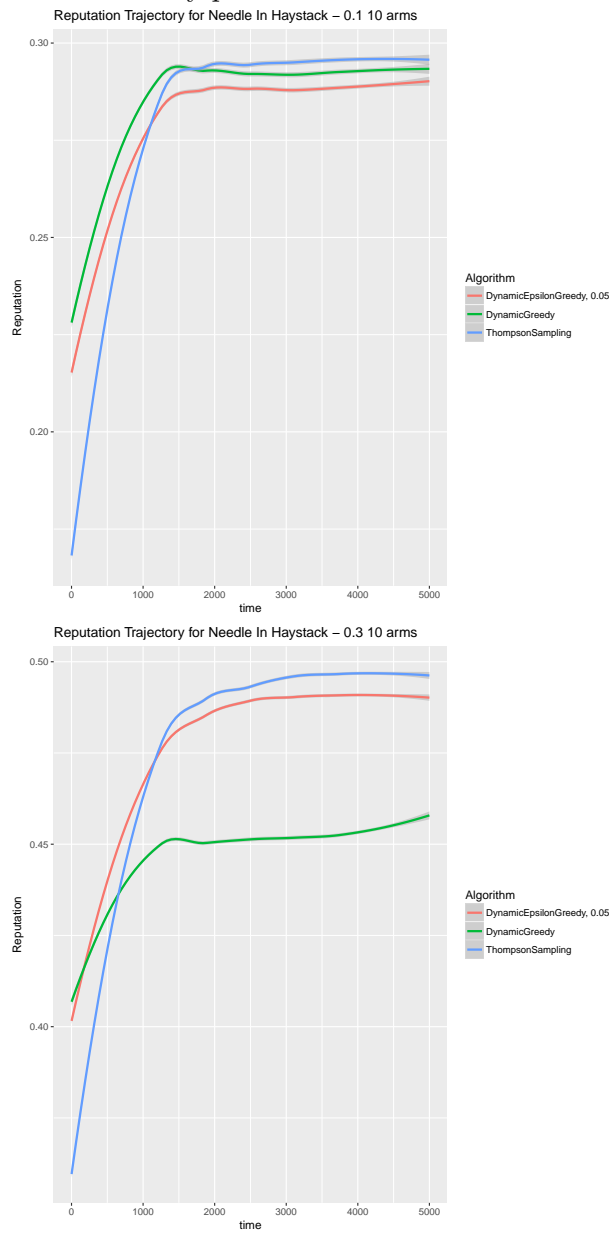
Various Needles in a Haystack

In this set of experiments we simply shift the needle in a haystack distribution.

We consider the following instances:

1. Needle In Haystack 0.1 - 9 arms with mean 0.1, 1 arm with mean 0.3
2. Needle In Haystack 0.3 - 9 arms with mean 0.3, 1 arm with mean 0.5
3. Needle In Haystack 0.5 - 9 arms with mean 0.5, 1 arm with mean 0.7
4. Needle In Haystack 0.7 - 9 arms with mean 0.5, 1 arm with mean 0.7

Preliminary plots for 0.1 and 0.3:



Results for Needle In Haystack - 0.7 HardMax K=10

	WS = 1	WS = 5	WS = 10	WS = 15	WS = 20	WS = 50	WS = 100
TS vs DG	0.58 (0.02) <u>eeog</u> avg: 50 med: 1	0.66 (0.02) <u>eeog</u> avg: 170 med: 4	0.75 (0.02) <u>eeog</u> avg: 170 med: 9	0.79 (0.02) <u>eeog</u> avg: 170 med: 9	0.82 (0.02) <u>eeog</u> avg: 190 med: 9.5	0.93 (0.01) <u>eeog</u> avg: 120 med: 0	0.96 (0.007) <u>eeog</u> avg: 75 med: 0
TS vs DEG	0.56 (0.02) <u>eeog</u> avg: 32 med: 1	0.63 (0.02) <u>eeog</u> avg: 74 med: 1	0.67 (0.02) <u>eeog</u> avg: 79 med: 1.5	0.73 (0.02) <u>eeog</u> avg: 93 med: 2	0.73 (0.02) <u>eeog</u> avg: 93 med: 2	0.83 (0.02) <u>eeog</u> avg: 86 med: 0	0.81 (0.02) <u>eeog</u> avg: 82 med: 0
DG vs DEG	0.46 (0.02) <u>eeog</u> avg: 160 med: 2	0.44 (0.02) <u>eeog</u> avg: 390 med: 39	0.42 (0.02) <u>eeog</u> avg: 500 med: 244	0.37 (0.02) <u>eeog</u> avg: 530 med: 279.5	0.36 (0.02) <u>eeog</u> avg: 560 med: 335.5	0.34 (0.02) <u>eeog</u> avg: 660 med: 495	0.29 (0.02) <u>eeog</u> avg: 650 med: 464

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Results for Needle In Haystack - 0.5 HardMax K=10

	WS = 1	WS = 5	WS = 10	WS = 15	WS = 20	WS = 50	WS = 100
TS vs DG	0.55 (0.02) <u>eeog</u> avg: 50 med: 0	0.62 (0.02) <u>eeog</u> avg: 130 med: 1	0.63 (0.02) <u>eeog</u> avg: 170 med: 5	0.66 (0.02) <u>eeog</u> avg: 180 med: 11	0.64 (0.02) <u>eeog</u> avg: 200 med: 26	0.63 (0.02) <u>eeog</u> avg: 220 med: 64	0.61 (0.02) <u>eeog</u> avg: 240 med: 29
TS vs DEG	0.53 (0.03) <u>eeog</u> avg: 33 med: 0	0.56 (0.02) <u>eeog</u> avg: 76 med: 0	0.59 (0.02) <u>eeog</u> avg: 120 med: 1	0.6 (0.02) <u>eeog</u> avg: 130 med: 7	0.6 (0.02) <u>eeog</u> avg: 140 med: 7	0.56 (0.02) <u>eeog</u> avg: 200 med: 18.5	0.53 (0.02) <u>eeog</u> avg: 230 med: 15
DG vs DEG	0.49 (0.02) <u>eeog</u> avg: 100 med: 3	0.44 (0.02) <u>eeog</u> avg: 240 med: 12	0.47 (0.02) <u>eeog</u> avg: 290 med: 36	0.45 (0.02) <u>eeog</u> avg: 340 med: 89	0.45 (0.02) <u>eeog</u> avg: 360 med: 130.5	0.44 (0.02) <u>eeog</u> avg: 470 med: 174	0.44 (0.02) <u>eeog</u> avg: 540 med: 235.5

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Results for Needle In Haystack - 0.3 HardMax K=10

	WS = 1	WS = 5	WS = 10	WS = 15	WS = 20	WS = 50	WS = 100
TS vs DG	0.53 (0.03) <u>eeog</u> avg: 22 med: 0	0.56 (0.02) <u>eeog</u> avg: 110 med: 0	0.49 (0.02) <u>eeog</u> avg: 120 med: 2	0.49 (0.02) <u>eeog</u> avg: 170 med: 1	0.5 (0.02) <u>eeog</u> avg: 210 med: 8	0.45 (0.02) <u>eeog</u> avg: 240 med: 13.5	0.45 (0.02) <u>eeog</u> avg: 250 med: 4.5
TS vs DEG	0.54 (0.03) <u>eeog</u> avg: 21 med: 0	0.53 (0.02) <u>eeog</u> avg: 77 med: 0	0.48 (0.02) <u>eeog</u> avg: 90 med: 1	0.48 (0.02) <u>eeog</u> avg: 140 med: 2.5	0.49 (0.02) <u>eeog</u> avg: 170 med: 2.5	0.43 (0.02) <u>eeog</u> avg: 220 med: 15	0.41 (0.02) <u>eeog</u> avg: 280 med: 17
DG vs DEG	0.47 (0.02) <u>eeog</u> avg: 62 med: 2	0.5 (0.02) <u>eeog</u> avg: 150 med: 6	0.47 (0.02) <u>eeog</u> avg: 170 med: 9	0.5 (0.02) <u>eeog</u> avg: 300 med: 27	0.5 (0.02) <u>eeog</u> avg: 380 med: 65	0.5 (0.02) <u>eeog</u> avg: 460 med: 152.5	0.5 (0.02) <u>eeog</u> avg: 570 med: 197

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Results for Needle In Haystack - 0.1 HardMax K=10

	WS = 1	WS = 5	WS = 10	WS = 15	WS = 20	WS = 50	WS = 100
TS vs DG	0.53 (0.03) <u>eeog</u> avg: 10 med: 3	0.53 (0.03) <u>eeog</u> avg: 26 med: 0	0.47 (0.02) <u>eeog</u> avg: 60 med: 0	0.48 (0.02) <u>eeog</u> avg: 75 med: 0	0.46 (0.02) <u>eeog</u> avg: 69 med: 0	0.37 (0.02) <u>eeog</u> avg: 110 med: 0	0.28 (0.02) <u>eeog</u> avg: 130 med: 0
TS vs DEG	0.52 (0.03) <u>eeog</u> avg: 8.5 med: 3	0.53 (0.03) <u>eeog</u> avg: 30 med: 0	0.47 (0.02) <u>eeog</u> avg: 56 med: 0	0.48 (0.02) <u>eeog</u> avg: 62 med: 0	0.43 (0.02) <u>eeog</u> avg: 81 med: 0	0.37 (0.02) <u>eeog</u> avg: 120 med: 0	0.31 (0.02) <u>eeog</u> avg: 170 med: 0
DG vs DEG	0.49 (0.03) <u>eeog</u> avg: 23 med: 5	0.49 (0.02) <u>eeog</u> avg: 46 med: 5	0.52 (0.02) <u>eeog</u> avg: 120 med: 14.5	0.52 (0.02) <u>eeog</u> avg: 140 med: 12	0.5 (0.02) <u>eeog</u> avg: 150 med: 11	0.51 (0.02) <u>eeog</u> avg: 280 med: 9	0.53 (0.02) <u>eeog</u> avg: 460 med: 12.5

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