## **Competing Bandits**

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#### Introduction

- Focused on a "Competing Bandits" model similar to Mansour, Slivkins, Wu (2017) where we have two principals that compete for agents
- Principals can only learn if the agents select them and aim to maximize the number of agents which select them
- We look at this model from a simulation perspective and run several experiments asking how certain variants of the setup change the results

#### Model Setup

- Agents choose between two competing principals (who can be thought of as firms). Agents seek to maximize their reward. In our implementation, an agent's beliefs are based on the realized rewards that prior agents received.
- 2. Before the beginning of the game, each principal selects a bandit algorithm to use, and starts with some prior beliefs on the distributions of the K arms. Each time the principal is chosen by an agent, the principal runs its bandit algorithm and selects an arm. Each principal seeks to maximize its market share, and can do so by choosing arms with high rewards so that agents will choose them.
- 3. At each t=1,...,T, a single agent enters (and lives only for one period) and selects a principal according to the Agent algorithm and the agent's beliefs.
- 4. The chosen principal runs its bandit algorithm to select an arm. The reward generated by the arm is given to the agent. The principal not chosen is not aware of the (arm, reward) pair.

## Algorithm Preliminaries

- Principals:
  - 1. Adaptive Exploration
    - ▶ UCB1
    - Thompson Sampling
  - 2. Non-Adaptive Exploration
    - ▶ Dynamic  $\epsilon$ -greedy
    - Explore Then Exploit
  - 3. Greedy
    - Bayesian Greedy
    - Static Greedy
- Agents:
  - HardMax Perfect expected utility maximizers based on beliefs over principals
  - 2. HardMaxWithRandom With probability  $\epsilon$  play random actions, otherwise play HardMax chosen actions
  - SoftMax The principals are chosen randomly according to a logistic function (higher scores ⇒ higher probability of being chosen)

#### Simulation Details

- ► Considered only Bernoulli rewards with Beta Priors
- ▶ Simulations have K = 10
- Reputation score generated by a sliding window average (fix memory sufficiently high except for limited memory experiment)

## Experiments - Overview

- ► In our simulations we considered the following five experiments:
  - 1. Competing algorithms
  - 2. Limited memory
  - 3. Tuning SoftMax
  - 4. Prior or Algorithm?
  - 5. Effects of "Warm start"

## Experiment 1 - Competing Algorithms

- ▶ In this experiment, we ran several competing algorithms against each other.
- results

### Experiment 2 - Limited Memory

- ▶ In this experiment we consider what happens when agents are perfect expected utility maximizers, but have limited memory.
- The driving question is can you get sufficient exploration in any given simulation simply by limiting how much agents remember?

 ${\bf Agent:\ HardMax}$  Principals: Thompson Sampling vs Thompson Sampling

	Memory Size	Principal 1 MS	Principal 2 MS	Principal 1 Avg Regret	Principal 2 Avg Regret
ĺ	1	0.498	0.502	0.021	0.021
	5	0.566	0.433	0.041	0.068
	10	0.540	0.460	0.062	0.080
	50	0.480	0.520	0.109	0.103
	100	0.320	0.680	0.130	0.067

# Experiment 3 - Tuning SoftMax

► SoftMax is great!

## Experiment 4 - Prior or Algorithm

- ▶ The purpose of this experiment was to attempt to figure out if it's better to use a better learning algorithm matters more or have better initial information.
- Ran simulations competing StaticGreedy (with almost correct beliefs) vs Thompson Sampling (with perverse beliefs) with K=10
- StaticGreedy had highest expected mean on the 2nd best arm, but Thompson Sampling had priors that thought the worst arms

were the best and that the best arms were very bad. Who wins?

Agent: HardMax, $T = 5000$								
Mean of Arm A	Principal 1 Alg	Principal 1 MS	Principal 2 MS	P1 Avg Regret	P2 Avg Regret			
0.55	ThompsonSampling	0.440	0.560	0.049	0.000			
0.65	ThompsonSampling	0.647	0.353	0.057	0.100			
0.75	ThompsonSampling	0.710	0.291	0.059	0.200			
0.55	Dynamic $\epsilon$ -greedy	0.298	0.656	0.057	0.000			
0.65	Dynamic $\epsilon$ -greedy	0.335	0.664	0.138	0.100			
0.75	Dynamic $\epsilon$ -greedy	0.442	0.558	0.154	0.200			

## Experiment 4 - Prior or Algorithm Cont'd

What if we drastically reduce the number of periods in the simulation?

Agent: HardMax, $T = 500$								
Mean of Arm A	Principal 1 Alg	Principal 1 MS	Principal 2 MS	P1 Avg Regret	P2 Avg Regret			
0.55	ThompsonSampling	0.181	0.812	0.088	0.0			
0.65	ThompsonSampling	0.287	0.712	0.178	0.100			
0.75	ThompsonSampling	0.274	0.723	0.244	0.200			
0.55	Dynamic $\epsilon$ -greedy	0.183	0.817	0.100	0.000			
0.65	Dynamic $\epsilon$ -greedy	0.169	0.831	0.190	0.100			
0.75	Dynamic $\epsilon$ -greedy	0.297	0.703	0.251	0.200			

 Given enough time, the algorithms that explore will catch up, but if we have sufficiently few periods then better initial information seems to win (according to our parameterization)

#### Additional Considerations

- What if we gave the principals free information at the start by giving them N agents? Some simulations showed that there was no difference.
- ▶ What if we made the rewards of the agents separate from the rewards of the principals?