

Problem 1:

- (A) Functional dependency is a statement that describes the relation between two attributes in a table. The relationship is there when one attribute is dependent on the other attribute. Denoted such as  $A \rightarrow B$  where attribute B is dependent of A.
- (B) A trivial functional dependency is when the right side (dependent attribute) is a subset of the other attribute
- (C) These functional dependencies determine only part of a row because there are two partial dependencies
- $ABC \rightarrow D$  // D is dependent on C
  - $B \rightarrow D$  // D is dependent on B
  - $A \rightarrow C$
- (D) What makes a table not 3NF is that there are transitive dependencies. In the cases below,  $D \rightarrow C$  is a transitive dependency on AB.
- $AB \rightarrow C$
  - $AB \rightarrow D$
  - $D \rightarrow C$  // This is transitive where  $AB \rightarrow D \rightarrow C$
- (E) Given two functional dependencies,  $A \rightarrow C$  and  $B \rightarrow D$ , it can be said that  $R(A, B, C, D)$  with key AB is in BCNF because the super key AB determined one or more of other attributes. In our case, the attributes are C & D.
- (F) The relation can be decomposed into two relations R1 and R2 where  
R1:  $S(A, B, C)$  with the functional dependency of FD:  $A \rightarrow ABC$   
R2:  $T(C, D)$  with the functional dependency of FD:  $C \rightarrow D$   
Both relations satisfy conditions of 3NF, there are no transitive dependencies
- (G) Assuming the \* means multiplication of the two attributes A and D from the relation, such a SQL statement can look like
- `SELECT R1.A*R2.D FROM R1 INNER JOIN R2 ON R1.C = R2.C`

Problem 2:

Given the schema  $S(A, B, C, D)$  with FD's  $A \rightarrow B$ ,  $B \rightarrow C$ , and  $B \rightarrow D$

(A) What are all the nontrivial FD's that follow the from given FD's?

To calculate the FD's, we need to compute the closure of the attributes

For one attribute, we have:

- $A^+ = \{ A, B, C, D \}$
- $B^+ = \{ B, C, D \}$
- $C^+ = \{ C \}$
- $D^+ = \{ D \}$

For two attributes, we have:

- $AB^+ = \{ A, B, C, D \}$
- $AC^+ = \{ A, B, C, D \}$
- $BC^+ = \{ B, C, D \}$
- $BD^+ = \{ B, C, D \}$
- $CD^+ = \{ C, D \}$
- $DA^+ = \{ D, A, B, C \}$

For three attributes, we have:

- $ABC^+ = \{ A, B, C, D \}$
- $ABD^+ = \{ A, B, C, D \}$
- $ACD^+ = \{ A, B, C, D \}$
- $BCD^+ = \{ B, C, D \}$

And so, the FD's are

One Attributes:  $A \rightarrow C$ ,  $A \rightarrow D$ ,

Two Attributes:  $AB \rightarrow D$ ,  $AC \rightarrow B$ ,  $AC \rightarrow D$ ,  $BC \rightarrow D$ ,  $DA \rightarrow B$ ,  $DA \rightarrow C$ ,

Three Attributes:  $ABC \rightarrow D$ ,  $ABD \rightarrow C$ ,  $ACD \rightarrow B$

(B) What are all the keys of R?

$A$ ,  $AB$ ,  $AC$ ,  $DA$  are all keys because the other functional dependencies do not contain the entire relation  $S(A, B, C, D)$  as its closure.

(C) A super key contains the keys listed above but cannot be a key. Since all keys share attribute  $A$ , all super keys need to contain attribute  $A$ . And so, all the super keys in relation  $S$  are  $ABC$ ,  $ACD$ ,  $ABD$ ,  $ABCD$ .

Problem 3:

Given  $R(A,B,C,D,E)$  and FD's  $A \rightarrow B$ ,  $BC \rightarrow E$ ,  $DE \rightarrow A$

To start of this problem, the definition of a candidate key is a column or a set of columns which uniquely defines a table (the basis of a super key). Given the functional dependencies listed above, ABCDE, ABCD, and BDE are not candidate keys but rather super keys. This is because, the functional dependencies still exist even when one or more attributes are removed.

However, if we look at ACD, removing either attribute will make the functional dependencies listed above void. Because the FD's are preserved given this set of attributes as a super key, ACD is considered the candidate key since it is the basis of all super keys in the relation.

Problem 4:

- (A) HS is the key for the relation Courses. The key contains all attributes in its closure
- (B) The functional dependencies for the relation are verifiable. Since the right side of every dependency contains only a single attribute, the functional dependency cannot be removed. In addition, neither can the attributes on left side of the dependency be altered, or else redundancy can occur and/or dependencies violated.
- (C) If we decompose courses into separate relations to satisfy 3NF to remove any redundancies and transitive dependencies, we get

R1( C,T )            with FD:  $C \rightarrow T$

R2( H, R, C )    with FD:  $HR \rightarrow C$

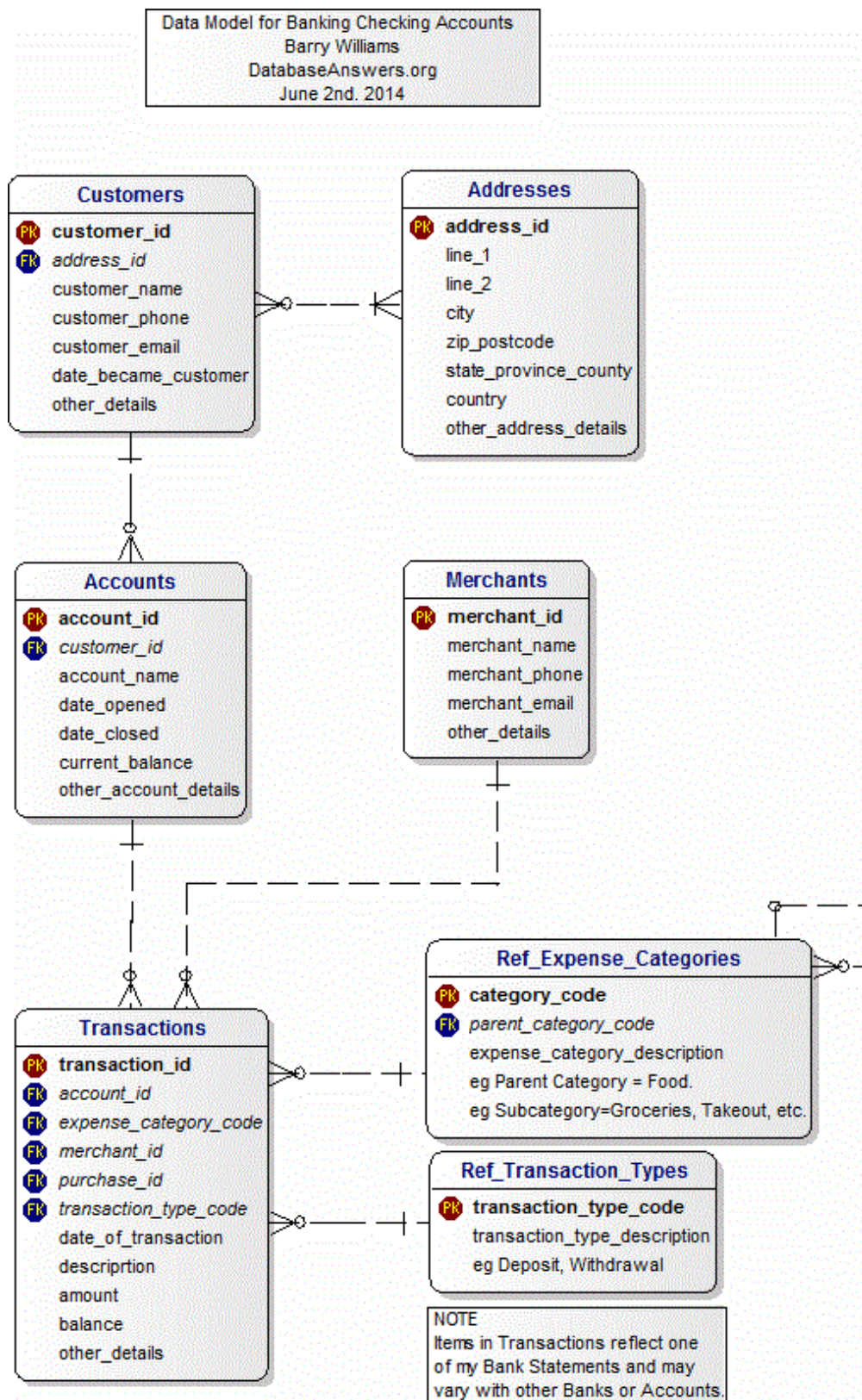
R3( H, T, R )    with FD:  $HT \rightarrow R$

R4( H, S, R )    with FD:  $HS \rightarrow R$

R5( C, S, G )    with FD:  $CS \rightarrow G$

All are in BCNF. This is because, as verified above, each relation is a minimal basis and are part of a super key which contains one or more of the following attributes in the courses relation.

Problem 5:



Problem 6:

- (A) 

```
CREATE TABLE Valid_Answers (  
    Valid_Answer_ID int NOT NULL,  
    Question_ID int NOT NULL,  
    Valid_Answer_Text varchar(255),  
    PRIMARY KEY(Valid_Answer_ID),  
    FOREIGN KEY(Question_ID) REFERENCES Questions(Question_ID)  
);
```
- (B) The professor would use several tables. These tables include the Ref\_Type\_of\_Question, Questions, Valid\_Answers, Questions\_in\_Exams, Exams, Ref\_Subjects tables.
- (C) The application would modify the Questions, Exams, and Valid\_Answers tables.
- (D) The application would query the Student, Student\_Answers, Student\_Assessments, and Valid\_Answers to administer the exam.
- (E) The application will update the Student\_Answers and Student\_Assessments tables while a student works through the exam

An aggie does not lie cheat, steal, or tolerate those who do