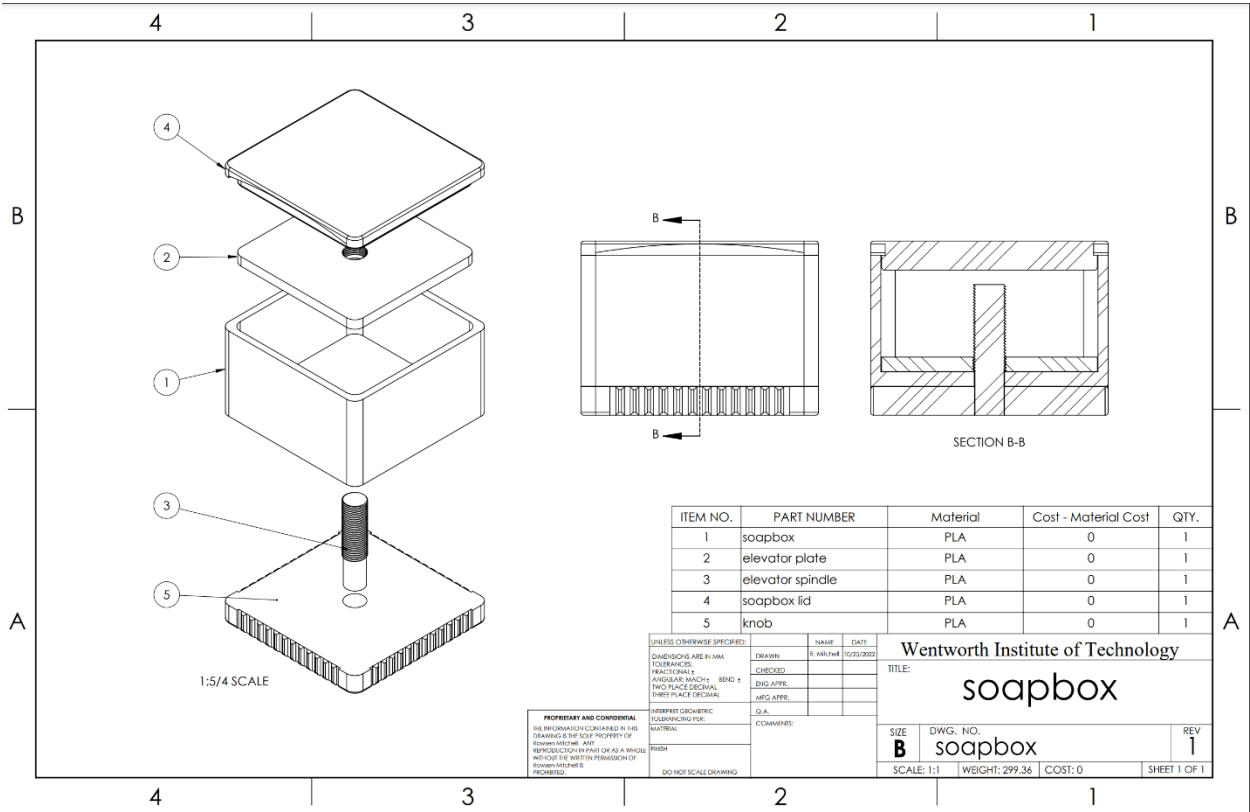
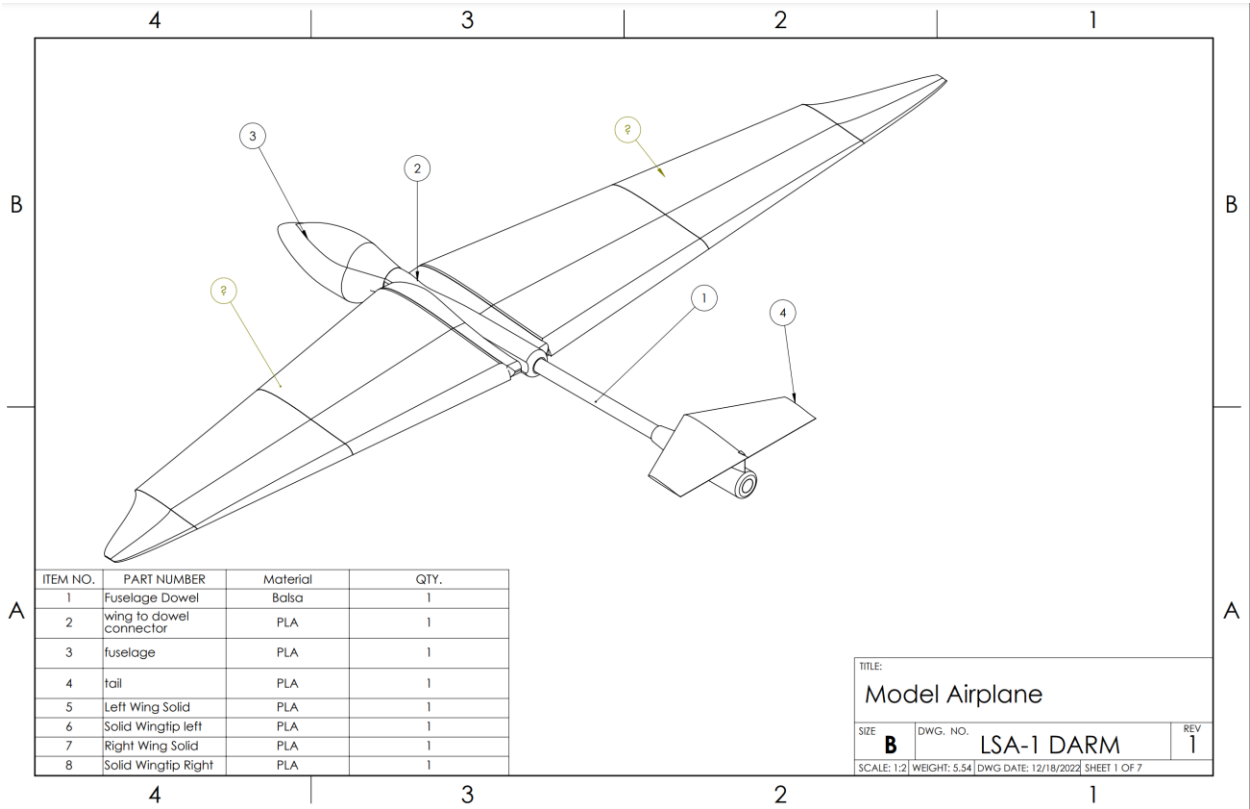
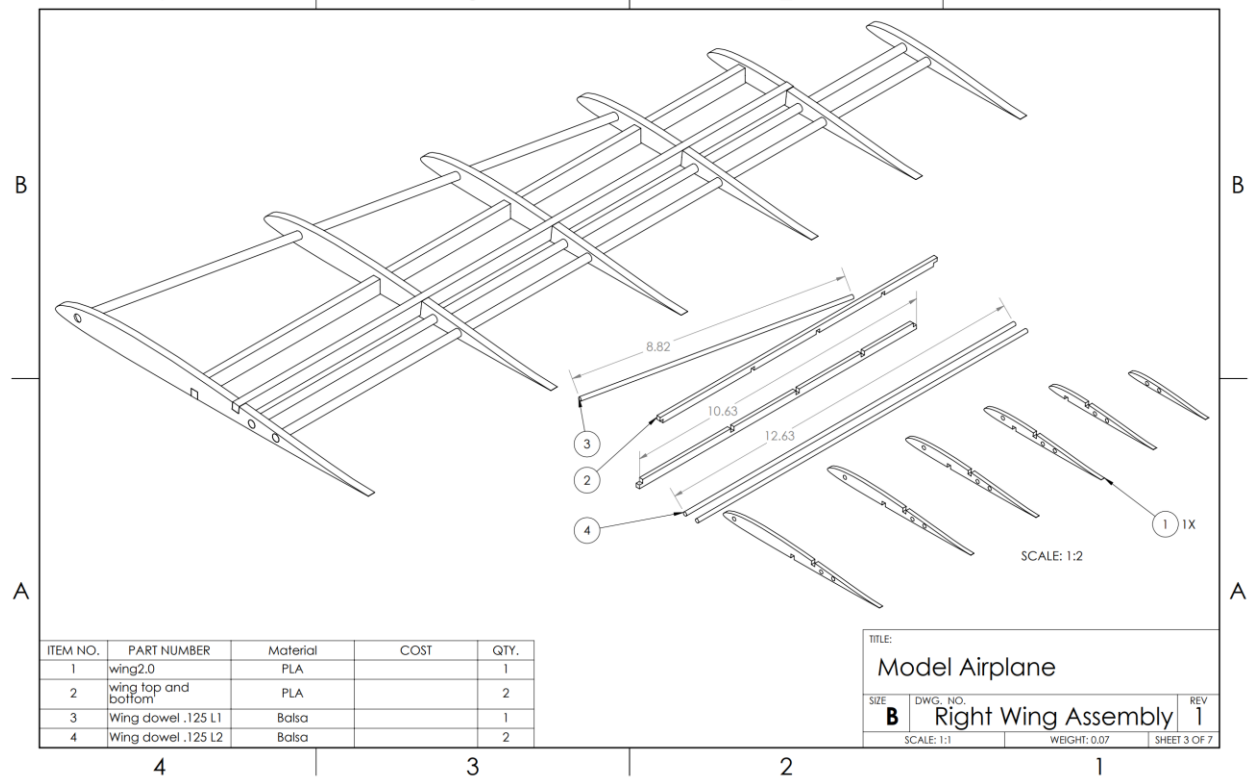
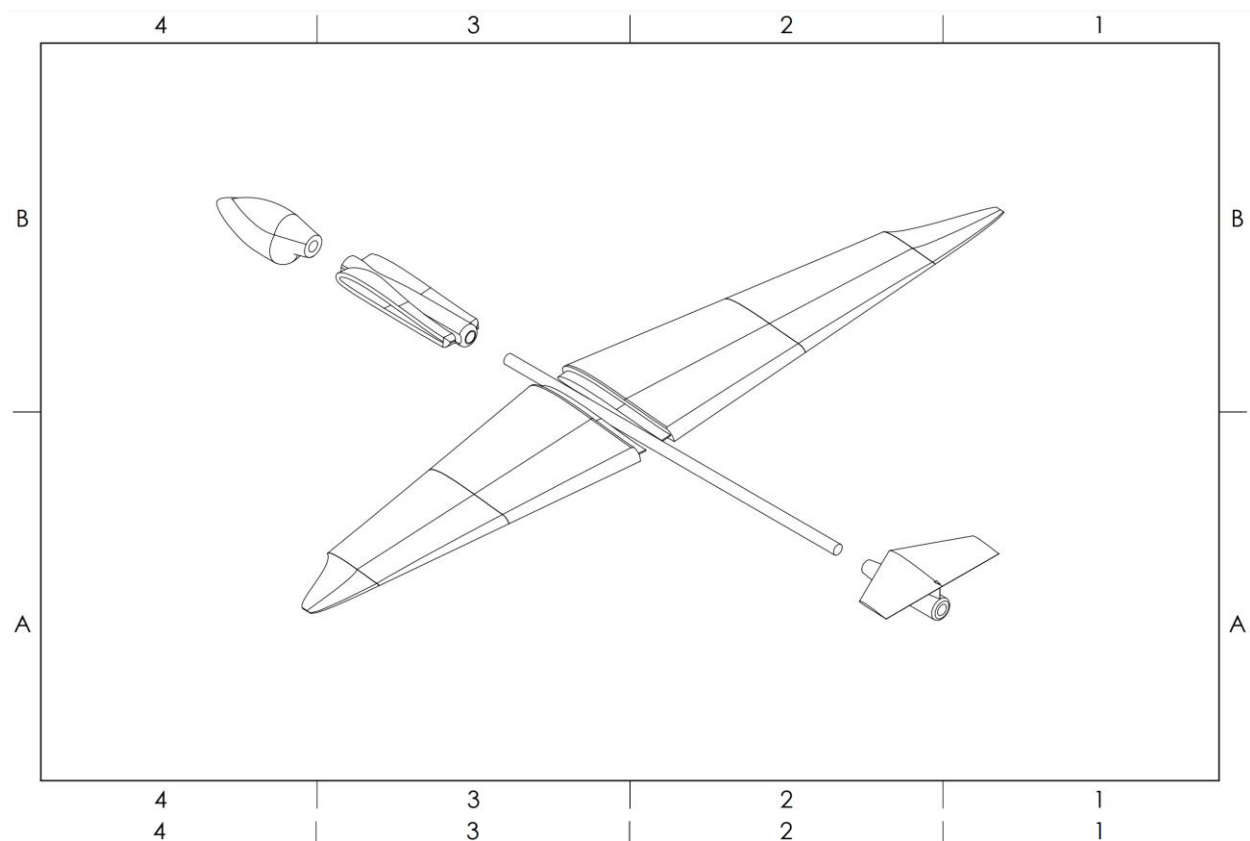


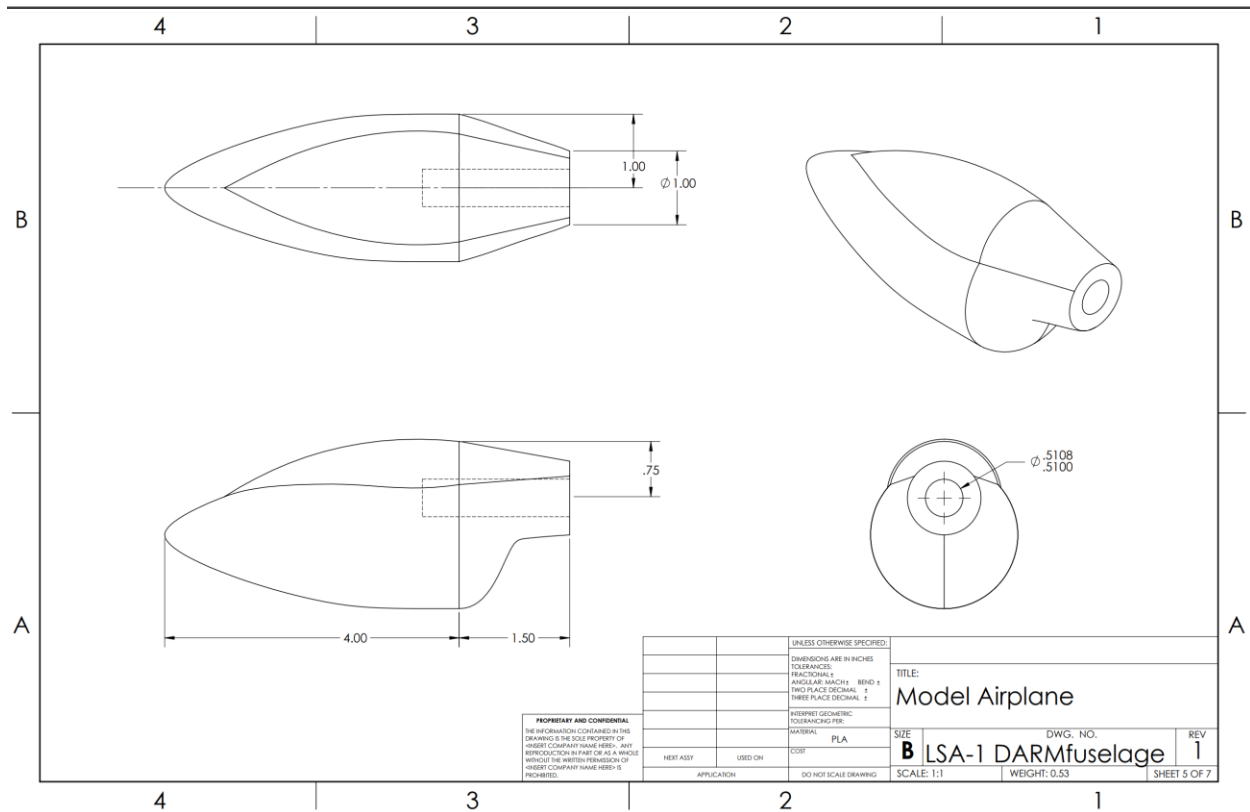
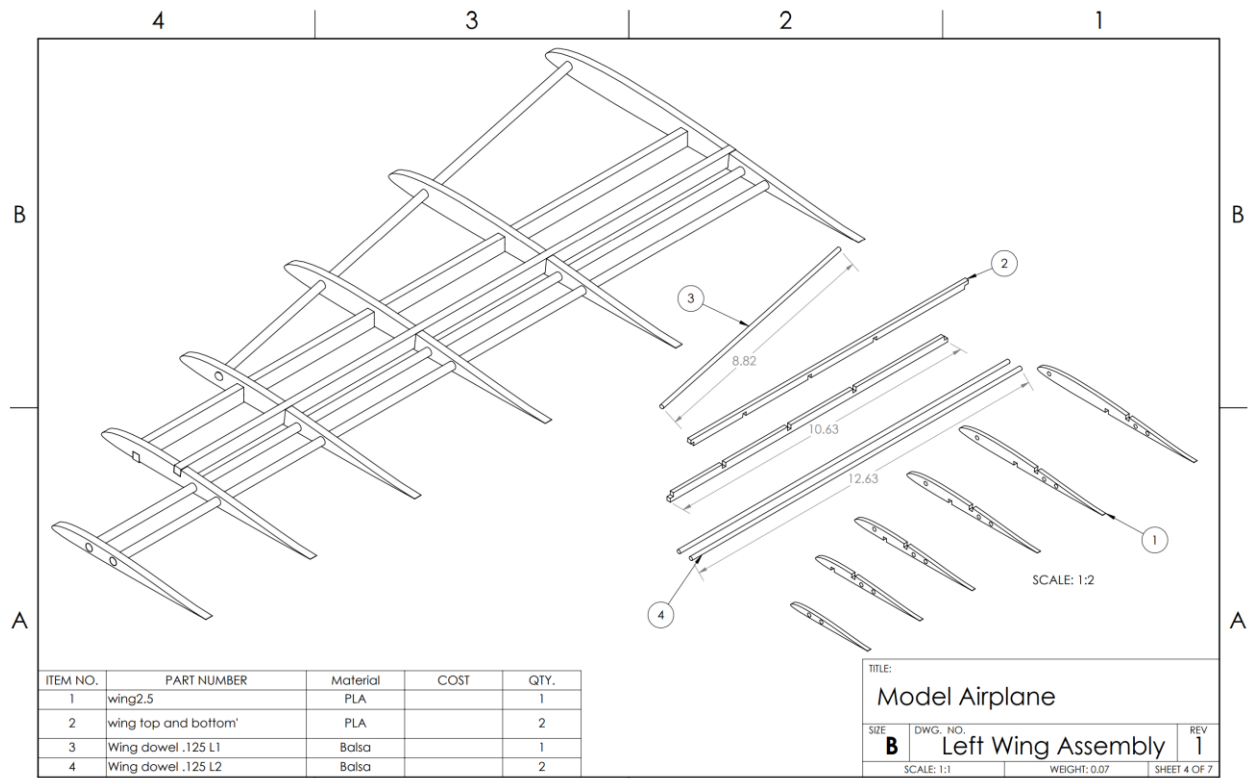
Reusable Soap Box

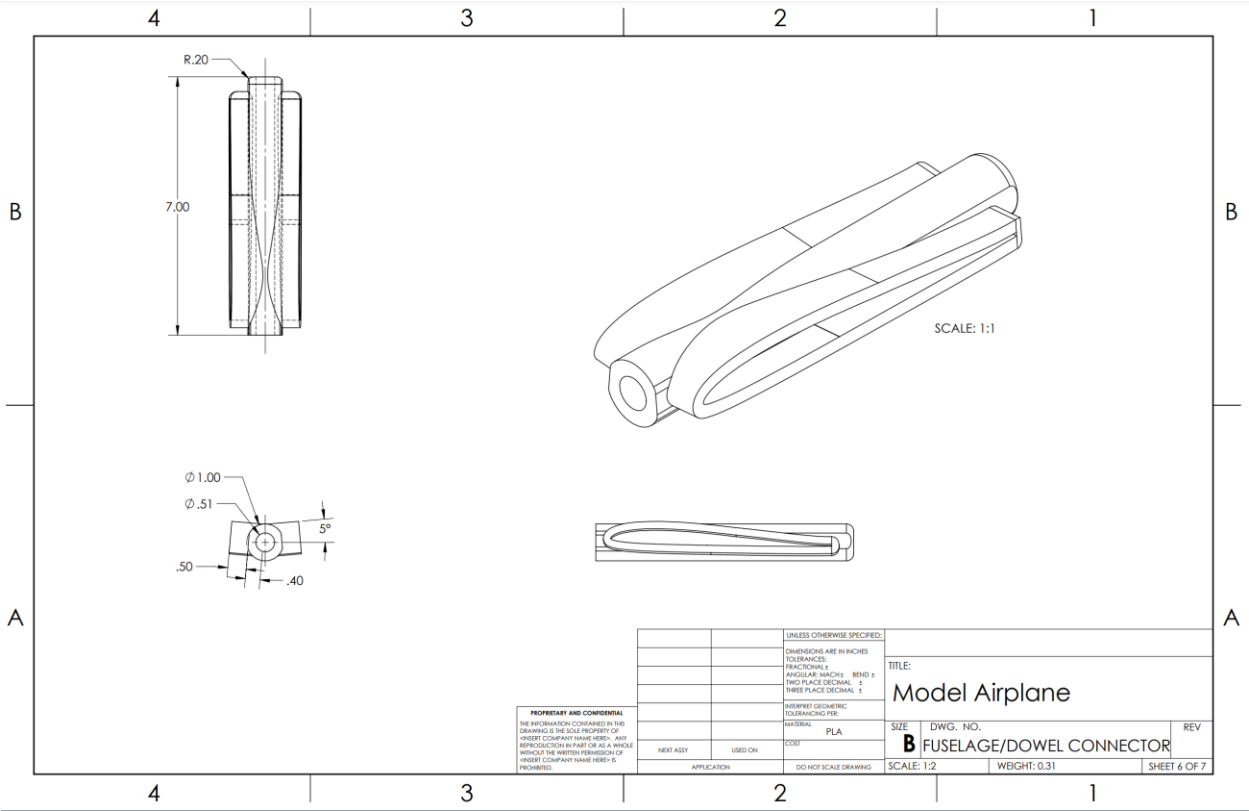


Modular Model Airplane









## Using Excel to integrate with multiple methods

Rawsen Mitchell  
Cournoyer  
CALC II

THQ Area by Midpoint Rule

$i$	$x_i$	$f(x_i)$	$\Delta x$	$A_i$
1	1.5	1.991862	1	1.991862
2	2.5	1.949199	1	1.949199
3	3.5	2.703302	1	2.703302
4	4.5	4.44529	1	4.44529
Sum of areas =				11.08965
Exact Area =				
Error =				11.08965
% Error =				#DIV/0!

I was not able to find an exact value due to it not having an antiderivative, so I will base my observations off of this estimation.

$i$	$x_i$	$f(x_i)$	$\Delta x$	$A_i$
1	1.25	2.233819	0.5	1.11691
2	1.75	1.879054	0.5	0.939527
3	2.25	1.874121	0.5	0.93706
4	2.75	2.068447	0.5	1.034224
5	3.25	2.441689	0.5	1.220844
6	3.75	3.023721	0.5	1.511861
7	4.25	3.881269	0.5	1.940634
8	4.75	5.122849	0.5	2.561425
Sum of areas =				11.26248
Exact Area =				
Error =				11.26248
% Error =				#DIV/0!

This value is higher than when we used 4 rectangles, which is expected of the rectangle/midpoint method.

$i$	$x_i$	$f(x_i)$	$\Delta x$	$A_i$
1	1.125	2.433752	0.25	0.608438
2	1.375	2.091941	0.25	0.522985
3	1.625	1.923188	0.25	0.480797
4	1.875	1.854811	0.25	0.463703
5	2.125	1.854206	0.25	0.463551
6	2.375	1.905997	0.25	0.476499
7	2.625	2.003385	0.25	0.500846
8	2.875	2.144475	0.25	0.536119
9	3.125	2.330613	0.25	0.582653
10	3.375	2.565644	0.25	0.641411
11	3.625	2.855627	0.25	0.713907
12	3.875	3.208837	0.25	0.802209
13	4.125	3.635941	0.25	0.908985
14	4.375	4.150326	0.25	1.037582
15	4.625	4.768574	0.25	1.192143
16	4.875	5.511075	0.25	1.377769
Sum of areas =				11.3096
Exact Area =				
Error =				11.3096
% Error =				#DIV/0!

This value is rising, but in smaller increments. It seems to run towards the 11.32+005 range.

As we divide the area into smaller rectangles, the value rises closer to 11.32+01. On a separate sheet, I performed the approximation with 64 and 128 intervals. The value continued to rise, but the values increased substantially less than the previous three sums. The average area calculated by 64 intervals and 128 intervals respectively were 11.325 and 11.3256. From my observations, the value 11.326 would be a reasonable average. A reasonable number of decimal places would be to the ten thousandths (11.3256).

Rawsen Mitchell  
CALC II  
Cournoyer

Simpsons Rule THQ

i	$x_i$	$f(x_i)$	$x_{mid}$	$f(x_{mid})$	$\Delta x$	M	T	S
0	0	0						
1	0.5	1.96875	0.25	0.499023	0.5	0.249512	0.492188	0.330404
2	1	7	0.75	4.262695	0.5	2.131348	2.242188	2.168294
3	1.5	10.40625	1.25	9.448242	0.5	4.724121	4.351563	4.599935
4	2	0	1.75	8.086914	0.5	4.043457	2.601563	3.562826
Sum of areas = 10.66146								
Exact Area = 10.66667								
Error = 0.005212								
% Error = 0.048859								

i	$x_i$	$f(x_i)$	$x_{mid}$	$f(x_{mid})$	$\Delta x$	M	T	S
0								
1	0.25	0.499023	0.125	0.124969	0.25	0.031242	0.062378	0.041621
2	0.5	1.96875	0.375	1.117584	0.25	0.279396	0.308472	0.289088
3	0.75	4.262695	0.625	3.029633	0.25	0.757408	0.778931	0.764582
4	1	7	0.875	5.612091	0.25	1.403023	1.407837	1.404627
5	1.25	9.448242	1.125	8.322968	0.25	2.080742	2.05603	2.072505
6	1.5	10.40625	1.375	10.21011	0.25	2.552528	2.481812	2.528956
7	1.75	8.086914	1.625	9.794037	0.25	2.448509	2.311646	2.402888
8	2	0	1.875	4.950714	0.25	1.237679	1.010864	1.162074
Sum of areas = 10.66634								
Exact Area = 10.66667								
Error = 0.000329								
% Error = 0.003083								

Summaries

4 intervals:  
The approximate area is 10.66146. This value is much closer to the exact area than the trapezoid and midpoint formulas.

8 intervals:  
The approximate area is 10.66634, which is rising closer to the exact value.

16 intervals:  
The approximate area is 10.66665, which is practically the exact area.

Overall, using Simpson's Rule proved to be much more accurate than the midpoint or trapezoid formulas. The percentage error at 4 intervals was .048859%, which is well under the percent error for the previous two approximation methods.

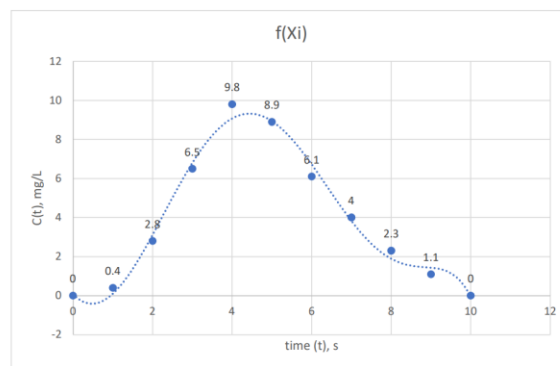
i	$x_i$	$f(x_i)$	$x_{mid}$	$f(x_{mid})$	$\Delta x$	M	T	S
0								
1	0.125	0.124969	0.0625	0.031249	0.125	0.003906	0.007810593	0.005208
2	0.25	0.499023	0.1875	0.281018	0.125	0.035127	0.038999557	0.036418
3	0.375	1.117584	0.3125	0.77827	0.125	0.097284	0.101037979	0.098535
4	0.5	1.96875	0.4375	1.515222	0.125	0.189403	0.192895889	0.190567
5	0.625	3.029633	0.5625	2.474936	0.125	0.309367	0.312398911	0.310378
6	0.75	4.262695	0.6875	3.62766	0.125	0.453457	0.455770493	0.454228
7	0.875	5.612091	0.8125	4.927157	0.125	0.615895	0.617174149	0.616321
8	1	7	0.9375	6.307054	0.125	0.788382	0.788255692	0.78834
9	1.125	8.322968	1.0625	7.677169	0.125	0.959646	0.957685471	0.958993
10	1.25	9.448242	1.1875	8.919858	0.125	1.114982	1.110700607	1.113555
11	1.375	10.21011	1.3125	9.886348	0.125	1.235793	1.228647232	1.233411
12	1.5	10.40625	1.4375	10.39307	0.125	1.299134	1.28852272	1.295597
13	1.625	9.794037	1.5625	10.21802	0.125	1.277253	1.262517929	1.272341
14	1.75	8.086914	1.6875	9.097066	0.125	1.137133	1.117559433	1.130609
15	1.875	4.950714	1.8125	6.720294	0.125	0.840037	0.814851761	0.831642
16	2	0	1.9375	2.728364	0.125	0.341045	0.309419632	0.330504
Sum of areas = 10.66665								
Exact Area = 10.66667								
Error = 2.37E-05								
% Error = 0.000222								

Rawsen Mitchell  
Cournoyer CALC II

DYE-DILUTION THQ

November 28th, 2022

i	$x_i$	$f(x_i)$	$\Delta x$	$A_i$
0	0	0		
1	1	0.4	1	0.2
2	2	2.8	1	1.6
3	3	6.5	1	4.65
4	4	9.8	1	8.15
5	5	8.9	1	9.35
6	6	6.1	1	7.5
7	7	4	1	5.05
8	8	2.3	1	3.15
9	9	1.1	1	1.7
10	10	0	1	0.55
Sum of areas (mg/L•s) = 41.9				
Amount of Dye (mg) = 5				
Flow Rate/Cardiac Output (L/s) = 0.12				
Flow Rate/Cardiac Output (L/min) = 7.16				
Flow Rate/Cardiac Output (L/hr) = 429.59				



The sum of the area under the curve is approximately 41.9 mg/L•s. This is found by taking the time (t) values given and putting them in the  $x_i$  column to represent the amount of intervals (and rectangles) under the graph. The concentration of dye in the atrium ( $C(t)$ ) is inserted into the  $f(x_i)$  column because it is the value presented by the function at a time (t). With the relationship between A (amount of dye) and F (flow rate/cardiac output) being  $A = F \int_0^t C(t) dt$ , we can rearrange the formula to find  $F$ ,  $F = A / (\int_0^t C(t) dt)$ . Once we solve for the area using the trapezoid rule, we can use the resulting value in the derived equation to solve for  $F$ . With the numbers plugged in, it looks like this:  $F = (5\text{mg}) / (41.9\text{mg/L}\cdot\text{s})$ . We cancel out the mg for our units to find L/s and compute the numbers, resulting in .12 L/s. This is a very small number, so I took it upon myself to include the Cardiac Output in minutes and hours as well.