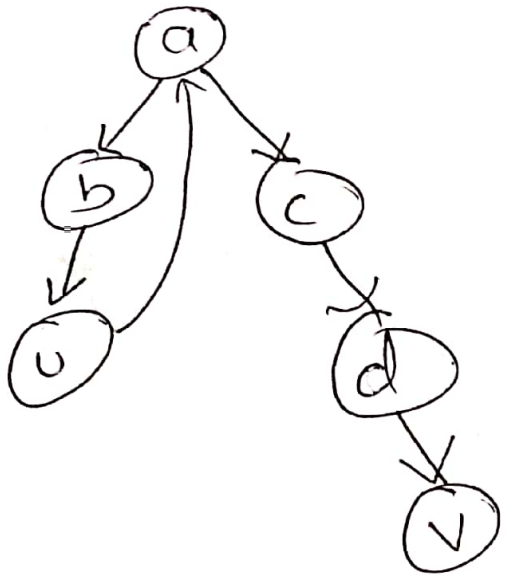
Q1

(a)



From (a)

$d[u] = 2$

$d[v] = 3$

but u is not descendent of v

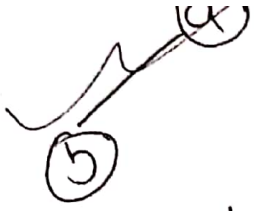
(b) ~~Maybe, when graph is~~ ~~Didn't understand~~

$|E| < |V|^2 \Rightarrow \lg|E| = O(\lg V)$ if there are no multiedges.

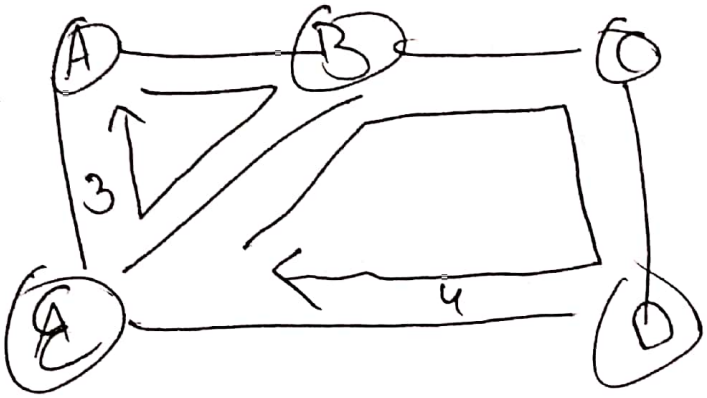
(c) No, idea

Q2: Store discovery time and finishing time using dfs, u will be ancestor of v if and only if u discovery time is earlier and finishing time is later than that of v.

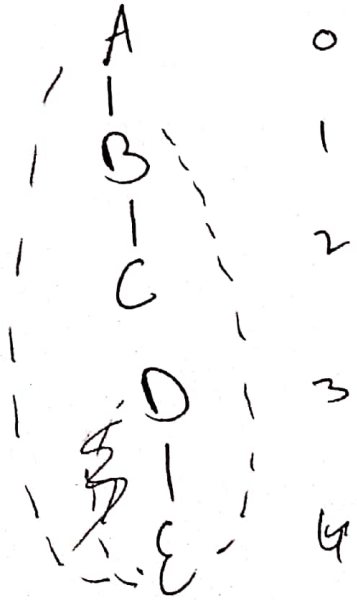
Q3.



Counter example



DFS Tree



~~4-3+1=2~~

4-1+1 = 4 - loop 1

4-0+1 = 5 - loop 2

Q4. For adjacency_list:

square (G) :

1. $G_1 = G_2$
2. For v in G.V :
3. For u in adj[v] :
4. For w in adj[u] :
5. G_1.adj[v].add(w)
6. Remove duplicates in G_1
7. return G_1

→ This routine will work in $O(VE)$.

Adjacency matrix :

we can convert adjacency matrix in adjacency list in $O(V^2)$ and run the same sub routine

Q6. coincharge (coins[], target) :

1. n = coins.size
2. dp[0.... target] initialized to $+\infty$
2.1. dp[0] = 0
3. for (int i = 0 ; i <= target ; i++)
for (int j = 0 ; j <= n ; j++)
4. if (coin[j] <= i)
5. dp[i] = min (dp[i], dp[i - coin[j]])
6.
7. return dp[target]