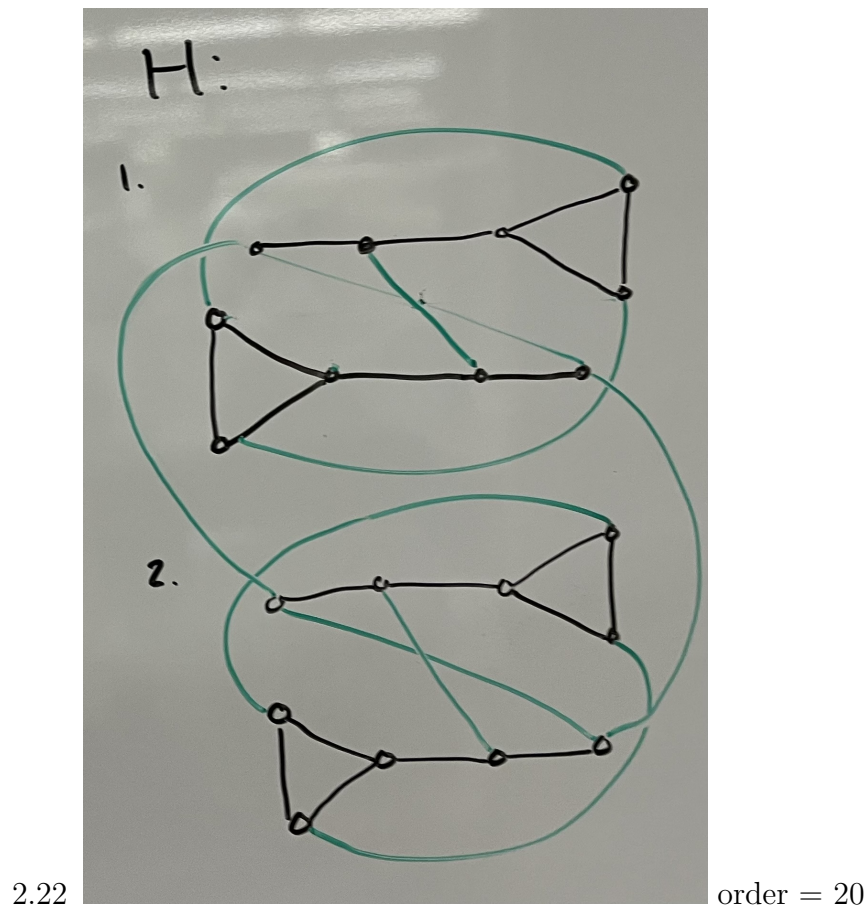


2.20 Show that if  $G$  is a connected graph that is not regular, then  $G$  contains adjacent vertices  $u$  and  $v$  such that  $\deg(u) > \deg(v)$ .



2.26

2.32 Determine if the following sequences are graphic. If so, construct a graph.

b Start: 6,3,3,3,3,2,2,2,1,1

Remove 6 and subtract 1 from the first 6 remaining numbers: 2,2,2,2,1,1,1,1,1,1

Remove 2 and subtract 1 from the first 2 remaining numbers: 1,1,2,1,1,1,1,1,1,1

Remove 2 and subtract 1 from the first 2 remaining numbers: 1,1,1,1,1,1,1,1,1,1

Remove 1 and subtract 1 from the first remaining number: 1,1,1,1,0

Remove 1 and subtract 1 from the first remaining number: 1,1,0,0,0

Remove 1 and subtract 1 from the first remaining number: 0,0,0,0,0

All zeros, so the sequence is graphic.

d Start: 7,5,4,4,4,3,2,1

Remove 7 and subtract 1 from the first 7 remaining numbers: 4,3,3,3,2,1,0

Remove 4 and subtract 1 from the first 4 remaining numbers: 2,2,2,1,0,0

Remove 2 and subtract 1 from the first 2 remaining numbers: 1,1,1,0,0,0

Remove 1 and subtract 1 from the first remaining number: 1,1,0,0,0

Remove 1 and subtract 1 from the first remaining number: 1,0,0,0,0

Remove 1 and subtract 1 from the first remaining number: 0,0,0,0

All zeros, so the sequence is graphic.

2.33