

## Computational Physics - Assignment 4

### 4 a)

In this problem, a one-dimensional cellular automata was implemented. The user can select an N number of sites, whether to implement the finite grids or periodic boundary conditions and the number of cycles for which the process goes on for.

Here, an initial array with randomized 0s and 1s is generated. Next, the possible neighbour combinations are determined and a specific rule assigns a 0 or a 1 to each combination of neighbours. Considering boundary conditions, the finite grids method assumes an extra 0 at each end of the array to determine the neighbours and the periodic boundary condition assumes that the left neighbour of the first element is the last element of the array and that the right neighbor of the last element is the first element of the array. (each element has only 2 neighbours since this is one-dimensional) Finally, each element of the original array is assigned a new value depending on the neighbours it had and a new array is generated with these new values. This process repeats itself to give us the desired automata.

In my code, as an example, Rule 30 is implemented and an output is generated accordingly using N=25, finite grids and 50 cycles.

The code is explained in detail in the attached python file for this problem (4a.py).

The corresponding output is shown below:

original random data: [1 1 0 1 1 1 0 1 1 1 0 1 1 0 1 0 1 1 1 0 1 0 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [0 0 0 1 1 1 1 0]

generated array with finite bound:

```
[1 1 1 1 0 1 1 1 0 1 1 1 1 0 1 0 1 1 0 1 0]
[1 0 0 1 1 1 0 1 1 1 0 0 0 1 1 0 1 1 1 1 1 0 1]
[0 1 0 1 0 1 1 1 0 1 1 0 0 1 1 1 1 0 0 0 0 1 1 0]
[0 0 1 0 1 1 0 1 1 1 1 1 0 1 0 0 1 1 0 0 0 1 1 1]
[0 0 0 1 1 1 1 1 0 0 0 1 1 0 1 0 1 1 1 0 0 0 1 0 1]
[0 0 0 1 0 0 0 1 1 0 0 1 1 1 0 1 1 0 1 1 0 0 0 1 0]
[0 0 0 0 1 0 0 1 1 1 0 1 0 1 1 1 1 1 1 1 1 0 0 0 1]
[0 0 0 0 0 1 0 1 0 1 1 0 1 1 0 0 0 0 0 0 1 1 0 0 0]
```

[illegible]



[illegible]

[1010001010001010000010000000000000000000  
0000000000000000000000000000000010100010001010  
00101100100111100111101101]  
[0100100100100100100111000111111111111111  
11111111111111111111111111111001001000100100  
10011100000100100100111110]  
[00000000000000000000101010100000000000000  
000000000000000000000000000000001000000010000000  
0001010111000000000000100010]  
[1111111111111111100101010011111111111111  
111111111111111111111111100011111000111111  
11001011010111111110001000]  
[100000000000000000001000101000100000000000  
000000000000000000000000101010001010100000  
01000111101100000010100011]  
[0011111111111110001001001000111111111111  
11111111111111111111111110010100100101001111  
00010100111101111001001011]  
[10100000000000101000000000001010000000000  
00000000000000000000000010001000000010001001  
01001000100111001000000111]  
[010011111110010011111110010011111111111  
111111111111111111111000100011111000100000  
10000010000101000011110101]  
[00001000001000001000001000001000001000000  
000000000000000000001010001010001010001110  
00111000110010011010011010]  
[111000111000111000111000111000111000111111  
1111111111111111100100100100100100101010  
10101010110000011100011100]  
[101010101010101010101010101010101010100000  
0000000000000000100000000000000000000010101  
01010101110111010101010101]  
[010101010101010101010101010101010101001111  
1111111111111000111111111111111111111001010  
10101011011101101010101010]  
[001010101010101010101010101010101010001000  
000000000000101010000000000000000000001000101  
01010111110111110101010100]  
[1001010101010101010101010101010101001000111

11111111110010100111111111111100010010  
10101100011100011010101001]  
[00001010101010101010101010000010100  
0000000001000100010000000000101000001  
01011101010101011101010000]  
[1110010101010101010101010100111001001  
1111111100010001000111111110010011100  
10110110101010110110100111]  
[1010001010101010101010101000101000001  
0000000101000100010100000010000010100  
011111110101011111111000101]  
[0100100101010101010101010010010011100  
0111110010010001001001111000111001001  
01000001101011000001010010]  
[0000000010101010101010100000000010101  
01000100000001000000010010101000000  
10011101110111011100100000]  
[1111111001010101010101001111111001010  
1001000111110001111100000101010011110  
00010111011101110100001111]  
[1000001000101010101010001000001000101  
0000010100010101000101110010100010010  
11001101110111011001101001]  
[0011100010010101010100100011100010010  
0111001001001010010011010001001000001  
11001111011101111001110000]  
[1010101000001010101000001010101000000  
0101000000000100000011100100000011101  
01001001110111001001010111]  
[0101010011100101010011100101010011111  
0010011111110001111010100001111010110  
10000001011101000000101101]  
[0010100010100010100010100010100010001  
0000010000010101001101001101001101111  
00111100110110011110011110]  
[1001001001001001001001001001001000100  
0111000111001010001110001110001111001  
00100100111110010010010010]  
[0000000000000000000000000000000000000  
0101010101000100101010101010101001000

[illegible]

Using periodic boundary conditions,  $N=100$  and 50 cycles:

[illegible]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [1 0 0 1 0 1 1 0]

generated array with periodic bound

```
[1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1  
1 1 1 1 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
```

```
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0  
0 0 0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
```

```
[1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1  
1 1 0 0 1 0 1 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
```

```
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0  
0 1 0 0 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
```

```
[1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1  
0 0 0 1 0 0 0 1 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
```

[illegible]

```
[1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0  
1 0 0 1 0 0 0 1 0 0 1 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
```

[illegible]



0001000100011111000100010001111111111  
111111111111111111111111111111111]  
[0000000000000000000010100010001010001  
0100010001010001010001010001000101000000000  
000000000000000000000000000000000]  
[11111111111111111111001001000100100100  
1001000100100100100100100010010011111111  
111111111111111111111111111111111]  
[00000000000000000000100000001000000000  
000001000000000000000001000000010000000  
000000000000000000000000000000000]  
[1111111111111111111100011111000111111111  
111100011111111111111100011111000111111  
111111111111111111111111111111111]  
[00000000000000000010101000101010000000  
00010101000000000000101010001010100000  
000000000000000000000000000000000]  
[111111111111111110010100100101001111111  
11001010011111111110010100100101001111  
111111111111111111111111111111111]  
[000000000000000010001000000010001000000  
0100010001000000010001000000010001000  
000000000000000000000000000000000]  
[1111111111111111000100011111000100011111  
0001000100011111000100011111000100011  
111111111111111111111111111111111]  
[000000000000001010001010001010001010001  
0100010001010001010001010001010001010  
000000000000000000000000000000000]  
[111111111111100100100100100100100100100  
1001000100100100100100100100100100100  
111111111111111111111111111111111]  
[00000000000100000000000000000000000000  
0000010000000000000000000000000000000  
100000000000000000000000000000000]  
[11111111111000111111111111111111111111  
1111000111111111111111111111111111110  
001111111111111111111111111111111]  
[00000000101010000000000000000000000000  
00010101000000000000000000000000000010

[illegible]



```

[1 0 0 1 0 1 0 1 0 0 1 0 0 1 0 1 0 1 0 1 0 1 0]
[0 0 0 0 1 0 1 0 0 0 0 0 0 0 1 0 1 0 1 0 1 0 0]
[1 1 1 0 0 1 0 0 1 1 1 1 1 0 0 1 0 1 0 1 0 1 0 0 1]
[1 0 1 0 0 0 0 0 1 0 0 0 1 0 0 0 1 0 1 0 1 0 0 0 0]
[0 1 0 0 1 1 1 0 0 0 1 0 0 0 1 0 0 1 0 1 0 0 1 1 1]
[0 0 0 0 1 0 1 0 1 0 0 0 1 0 0 0 0 0 1 0 0 0 1 0 1]
[1 1 1 0 0 1 0 1 0 0 1 0 0 0 1 1 1 0 0 0 1 0 0 1 0]
[1 0 1 0 0 0 1 0 0 0 0 0 1 0 1 0 1 0 1 0 0 0 0 0 0]
[0 1 0 0 1 0 0 0 1 1 1 0 0 1 0 1 0 1 0 0 1 1 1 1 1]
[0 0 0 0 0 0 1 0 1 0 1 0 0 0 1 0 1 0 0 0 1 0 0 0 1]
[1 1 1 1 1 0 0 1 0 1 0 0 1 0 0 1 0 0 1 0 0 0 1 0 0]
[1 0 0 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 1]
[0 0 1 0 0 0 1 0 0 0 1 1 1 1 1 1 1 1 1 1 0 0 0 1 0 0]
[1 0 0 0 1 0 0 0 1 0 1 0 0 0 0 0 0 0 0 1 0 1 0 0 0 1]
[0 0 1 0 0 0 1 0 0 1 0 0 1 1 1 1 1 0 0 1 0 0 1 0 0]
[1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0 1]
[0 0 1 0 0 0 1 1 1 1 1 0 0 0 1 0 0 0 1 1 1 1 1 0 0]
[1 0 0 0 1 0 1 0 0 0 1 0 1 0 0 0 1 0 1 0 0 0 1 0 1]
[0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0]
[1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1]
[0 1 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0]
[0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1]
[1 1 1 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 0]
[1 0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0]
[0 1 0 1 0 1 0 0 1 1 1 1 1 1 1 1 1 1 1 0 0 0 1 1 1]
[0 0 1 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 1 0 1 0 1 0 1]
[1 0 0 1 0 0 1 0 0 0 1 1 1 1 1 1 1 0 0 1 0 1 0 1 0]
[0 0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 1 0 1 0 0]

```

Periodic Boundary conditions, N=25 and 50 cycles:

original data: [1, 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [1 0 0 1 0 1 1 0]

generated array with periodic bound

```
[0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0]
```

[1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0]  
[0 1 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1]  
[1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0]  
[0 0 1 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 0 1 0]  
[1 0 0 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0]  
[0 0 1 0 0 1 0 0 1 1 1 1 1 1 1 1 1 1 0 0 1 0 0 1 0]  
[1 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0]  
[0 0 1 1 1 1 1 0 0 0 1 1 1 1 1 1 0 0 0 1 1 1 1 1 0]  
[1 0 1 0 0 0 1 0 1 0 1 0 0 0 0 1 0 1 0 1 0 0 0 1 0]  
[0 1 0 0 1 0 0 1 0 1 0 0 1 1 0 0 1 0 1 0 0 1 0 0 1]  
[1 0 0 0 0 0 0 0 1 0 0 0 1 1 0 0 0 1 0 0 0 0 0 0]  
[0 0 1 1 1 1 1 0 0 0 1 0 1 1 0 1 0 0 0 1 1 1 1 1 0]  
[1 0 1 0 0 0 1 0 1 0 0 1 1 1 1 0 0 1 0 1 0 0 0 1 0]  
[0 1 0 0 1 0 0 1 0 0 0 1 0 0 1 0 0 0 1 0 0 1 0 0 1]  
[1 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 0 0 0]  
[0 0 1 1 1 1 1 1 0 0 0 1 1 1 1 0 0 0 1 1 1 1 1 1 0]  
[1 0 1 0 0 0 0 1 0 1 0 1 0 0 1 0 1 0 1 0 0 0 0 1 0]  
[0 1 0 0 1 1 0 0 1 0 1 0 0 0 0 1 0 1 0 0 1 1 0 0 1]  
[1 0 0 0 1 1 0 0 0 1 0 0 1 1 0 0 1 0 0 0 1 1 0 0 0]  
[0 0 1 0 1 1 0 1 0 0 0 0 1 1 0 0 0 0 1 0 1 1 0 1 0]  
[1 0 0 1 1 1 1 0 0 1 1 0 1 1 0 1 1 0 0 1 1 1 1 0 0]  
[0 0 0 1 0 0 1 0 0 1 1 1 1 1 1 1 1 1 0 0 1 0 0 1 0 0]  
[1 1 0 0 0 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 0 0 0 1]  
[0 1 0 1 1 1 1 1 0 0 0 1 1 1 1 0 0 0 1 1 1 1 1 0 1]  
[1 0 1 1 0 0 0 1 0 1 0 1 0 0 1 0 1 0 1 0 0 0 1 1 0]  
[0 1 1 1 0 1 0 0 1 0 1 0 0 0 0 1 0 1 0 0 1 0 1 1 1]  
[1 1 0 1 1 0 0 0 0 1 0 0 1 1 0 0 1 0 0 0 0 1 1 0 1]  
[0 1 1 1 1 0 1 1 0 0 0 0 1 1 0 0 0 0 1 1 0 1 1 1 1]  
[1 1 0 0 1 1 1 1 0 1 1 0 1 1 0 1 1 0 1 1 1 1 0 0 1]  
[0 1 0 0 1 0 0 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 0 0 1]  
[1 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0]  
[0 0 1 1 1 1 0 0 0 1 1 1 1 1 1 1 1 1 0 0 0 1 1 1 1 0]  
[1 0 1 0 0 1 0 1 0 1 0 0 0 0 0 0 1 0 1 0 1 0 0 1 0]  
[0 1 0 0 0 0 1 0 1 0 0 1 1 1 1 0 0 1 0 1 0 0 0 0 1]  
[1 0 0 1 1 0 0 1 0 0 0 1 0 0 1 0 0 0 1 0 0 1 1 0 0]  
[0 0 0 1 1 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 1 1 0 0]  
[1 1 0 1 1 0 1 1 0 0 0 1 1 1 1 0 0 0 1 1 0 1 1 0 1]  
[0 1 1 1 1 1 1 1 0 1 0 1 0 0 1 0 1 0 1 1 1 1 1 1 1]  
[1 1 0 0 0 0 0 1 1 0 1 0 0 0 0 1 0 1 1 0 0 0 0 0 1]  
[0 1 0 1 1 1 0 1 1 1 0 0 1 1 0 0 1 1 1 0 1 1 1 0 1]

```
[1 0 1 1 0 1 1 1 0 1 0 0 1 1 0 0 1 0 1 1 1 0 1 1 0]
[0 1 1 1 1 1 0 1 1 0 0 0 1 1 0 0 0 1 1 0 1 1 1 1 1]
[1 1 0 0 0 1 1 1 1 0 1 0 1 1 0 1 0 1 1 1 1 0 0 0 1]
[0 1 0 1 0 1 0 0 1 1 0 1 1 1 1 0 1 1 0 0 1 0 1 0 1]
[1 0 1 0 1 0 0 0 1 1 1 1 0 0 1 1 1 1 0 0 0 1 0 1 0]
[0 1 0 1 0 0 1 0 1 0 0 1 0 0 1 0 0 1 0 1 0 0 1 0 1]
[1 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 1 0]
[0 1 0 0 1 1 0 0 0 1 1 1 1 1 1 1 1 0 0 0 1 1 0 0 1]
[1 0 0 0 1 1 0 1 0 1 0 0 0 0 0 0 1 0 1 0 1 1 0 0 0]
```

#### **4 c)**

A randomized array was used.

#### Rule 90

Finite grids, N=25 and 50 cycles

original random data: [0 1 1 1 1 1 1 1 1 0 0 1 0 0 0 1 1 0 1 0 0 0 0 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [0 1 0 1 1 0 1 0]

generated array with finite bound:

```
[1 1 0 0 0 0 0 0 0 1 1 1 0 1 0 1 1 1 0 0 1 0 0 0 0]
[1 1 1 0 0 0 0 0 1 1 0 1 0 0 0 1 0 1 1 1 0 1 0 0 0]
[1 0 1 1 0 0 0 1 1 1 0 0 1 0 1 0 0 1 0 1 0 0 1 0 0]
[0 0 1 1 1 0 1 1 0 1 1 1 0 0 0 1 1 0 0 0 1 1 0 1 0]
[0 1 1 0 1 0 1 1 0 1 0 1 1 0 1 1 1 1 0 1 1 1 0 0 1]
[1 1 1 0 0 0 1 1 0 0 0 1 1 0 1 0 0 1 0 1 0 1 1 1 0]
[1 0 1 1 0 1 1 1 1 0 1 1 1 0 0 1 1 0 0 0 0 1 0 1 1]
[0 0 1 1 0 1 0 0 1 0 1 0 1 1 1 1 1 1 0 0 1 0 0 1 1]
[0 1 1 1 0 0 1 1 0 0 0 0 1 0 0 0 0 1 1 1 0 1 1 1 1]
[1 1 0 1 1 1 1 1 1 0 0 1 0 1 0 0 1 1 0 1 0 1 0 0 1]
[1 1 0 1 0 0 0 0 1 1 1 0 0 0 1 1 1 1 0 0 0 0 1 1 0]
[1 1 0 0 1 0 0 1 1 0 1 1 0 1 1 0 0 1 1 0 0 1 1 1 1]
[1 1 1 1 0 1 1 1 1 1 0 1 1 0 1 1 1 1 1 1 1 1 1 0 0 1]
[1 0 0 1 0 1 0 0 1 0 1 1 0 1 0 0 0 0 0 0 0 1 1 1 0]
[0 1 1 0 0 0 1 1 0 0 1 1 0 0 1 0 0 0 0 0 1 1 0 1 1]
[1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 0 1 0 0 0 1 1 1 0 1 1]
[1 0 0 1 0 1 0 0 0 0 0 0 0 1 0 0 1 0 1 1 0 1 0 1 1]
[0 1 1 0 0 0 1 0 0 0 0 0 1 0 1 1 0 0 1 1 0 0 0 1 1]
```

[1 1 1 1 0 1 0 1 0 0 0 1 0 0 1 1 1 1 1 1 0 1 1 1]  
[1 0 0 1 0 0 0 0 1 0 1 0 1 1 1 0 0 0 0 0 1 0 1 0 1]  
[0 1 1 0 1 0 0 1 0 0 0 0 1 0 1 1 0 0 0 1 0 0 0 0 0]  
[1 1 1 0 0 1 1 0 1 0 0 1 0 0 1 1 1 0 1 0 1 0 0 0 0]  
[1 0 1 1 1 1 1 0 0 1 1 0 1 1 1 0 1 0 0 0 0 1 0 0 0]  
[0 0 1 0 0 0 1 1 1 1 1 0 1 0 1 0 0 1 0 0 1 0 1 0 0]  
[0 1 0 1 0 1 1 0 0 0 1 0 0 0 0 1 1 0 1 1 0 0 0 1 0]  
[1 0 0 0 0 1 1 1 0 1 0 1 0 0 1 1 1 0 1 1 1 0 1 0 1]  
[0 1 0 0 1 1 0 1 0 0 0 0 1 1 1 0 1 0 1 0 1 0 0 0 0]  
[1 0 1 1 1 1 0 0 1 0 0 1 1 0 1 0 0 0 0 0 0 1 0 0 0]  
[0 0 1 0 0 1 1 1 0 1 1 1 1 0 0 1 0 0 0 0 1 0 1 0 0]  
[0 1 0 1 1 1 0 1 0 1 0 0 1 1 1 0 1 0 0 1 0 0 0 1 0]  
[1 0 0 1 0 1 0 0 0 0 1 1 1 0 1 0 0 1 1 0 1 0 1 0 1]  
[0 1 1 0 0 0 1 0 0 1 1 0 1 0 0 1 1 1 1 0 0 0 0 0 0]  
[1 1 1 1 0 1 0 1 1 1 1 0 0 1 1 1 0 0 1 1 0 0 0 0 0]  
[1 0 0 1 0 0 0 1 0 0 1 1 1 1 0 1 1 1 1 1 1 0 0 0 0]  
[0 1 1 0 1 0 1 0 1 1 1 0 0 1 0 1 0 0 0 0 1 1 0 0 0]  
[1 1 1 0 0 0 0 0 1 0 1 1 1 0 0 0 1 0 0 1 1 1 1 0 0]  
[1 0 1 1 0 0 0 1 0 0 1 0 1 1 0 1 0 1 1 1 0 0 1 1 0]  
[0 0 1 1 1 0 1 0 1 1 0 0 1 1 0 0 0 1 0 1 1 1 1 1 1]  
[0 1 1 0 1 0 0 0 1 1 1 1 1 1 1 0 1 0 0 1 0 0 0 0 1]  
[1 1 1 0 0 1 0 1 1 0 0 0 0 0 1 0 0 1 1 0 1 0 0 1 0]  
[1 0 1 1 1 0 0 1 1 1 0 0 0 1 0 1 1 1 1 0 0 1 1 0 1]  
[0 0 1 0 1 1 1 1 0 1 1 0 1 0 0 1 0 0 1 1 1 1 1 0 0]  
[0 1 0 0 1 0 0 1 0 1 1 0 0 1 1 0 1 1 1 0 0 0 1 1 0]  
[1 0 1 1 0 1 1 0 0 1 1 1 1 1 1 0 1 0 1 1 0 1 1 1 1]  
[0 0 1 1 0 1 1 1 1 1 0 0 0 0 1 0 0 0 1 1 0 1 0 0 1]  
[0 1 1 1 0 1 0 0 0 1 1 0 0 1 0 1 0 1 1 1 0 0 1 1 0]  
[1 1 0 1 0 0 1 0 1 1 1 1 1 0 0 0 0 1 0 1 1 1 1 1 1]  
[1 1 0 0 1 1 0 0 1 0 0 0 1 1 0 0 1 0 0 1 0 0 0 0 1]  
[1 1 1 1 1 1 1 1 1 0 1 0 1 1 1 1 1 0 1 1 0 1 0 0 1 0]  
[1 0 0 0 0 0 0 1 0 0 0 1 0 0 0 1 0 1 1 0 0 1 1 0 1]

### Periodic Boundary Conditions, N=25 and 50 cycles

original random data: [0 0 0 1 1 1 0 1 0 1 0 1 1 0 1 0 1 1 1 0 1 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [0 1 0 1 1 0 1 0]

generated array with periodic bound

[0 0 1 1 0 1 0 0 0 0 0 1 1 0 1 1 0 0 0 1 0 1 0 0 1]  
[1 1 1 1 0 0 1 0 0 0 1 1 1 0 1 1 1 0 1 0 0 0 1 1 0]  
[1 0 0 1 1 1 0 1 0 1 1 0 1 0 1 0 1 0 0 1 0 1 1 1 0]  
[0 1 1 1 0 1 0 0 0 1 1 0 0 0 0 0 0 1 1 0 0 1 0 1 0]  
[1 1 0 1 0 0 1 0 1 1 1 1 0 0 0 0 1 1 1 1 1 0 0 0 1]  
[0 1 0 0 1 1 0 0 1 0 0 1 1 0 0 1 1 0 0 0 1 1 0 1 1]  
[0 0 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 0 1 1 1 0 1 1]  
[1 1 1 0 0 0 0 1 0 1 0 0 0 0 0 0 0 1 0 1 0 1 0 1 1]  
[0 0 1 1 0 0 1 0 0 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 0]  
[0 1 1 1 1 1 0 1 0 1 0 1 0 0 0 1 0 1 0 0 0 0 1 0 1]  
[0 1 0 0 0 1 0 0 0 0 0 0 1 0 1 0 0 0 1 0 0 1 0 0 0]  
[1 0 1 0 1 0 1 0 0 0 0 1 0 0 0 1 0 1 0 1 1 0 1 0 0]  
[0 0 0 0 0 0 0 1 0 0 1 0 1 0 1 0 0 0 0 1 1 0 0 1 1]  
[1 0 0 0 0 0 1 0 1 1 0 0 0 0 0 1 0 0 1 1 1 1 1 1 1]  
[1 1 0 0 0 1 0 0 1 1 1 0 0 0 1 0 1 1 1 0 0 0 0 0 0]  
[1 1 1 0 1 0 1 1 1 0 1 1 0 1 0 0 1 0 1 1 0 0 0 0 1]  
[0 0 1 0 0 0 1 0 1 0 1 1 0 0 1 1 0 0 1 1 1 0 0 1 1]  
[1 1 0 1 0 1 0 0 0 0 1 1 1 1 1 1 1 1 1 0 1 1 1 1 1]  
[0 1 0 0 0 0 1 0 0 1 1 0 0 0 0 0 0 0 1 0 1 0 0 0 0]  
[1 0 1 0 0 1 0 1 1 1 1 1 0 0 0 0 0 1 0 0 0 1 0 0 0]  
[0 0 0 1 1 0 0 1 0 0 0 1 1 0 0 0 1 0 1 0 1 0 1 0 1]  
[1 0 1 1 1 1 1 0 1 0 1 1 1 1 0 1 0 0 0 0 0 0 0 0 0]  
[0 0 1 0 0 0 1 0 0 0 1 0 0 1 0 0 1 0 0 0 0 0 0 0 1]  
[1 1 0 1 0 1 0 1 0 1 0 1 1 0 1 1 0 1 0 0 0 0 0 1 0]  
[1 1 0 0 0 0 0 0 0 0 0 1 1 0 1 1 0 0 1 0 0 0 1 0 0]  
[1 1 1 0 0 0 0 0 0 0 0 1 1 1 0 1 1 1 1 0 1 0 1 0 1]  
[0 0 1 1 0 0 0 0 0 0 1 1 0 1 0 1 0 0 1 0 0 0 0 0 1 0]  
[0 1 1 1 1 0 0 0 0 1 1 1 0 0 0 0 1 1 0 1 0 0 0 1 0 1]  
[0 1 0 0 1 1 0 1 1 0 1 1 0 0 1 1 1 0 0 1 0 1 0 0 0]  
[1 0 1 1 1 1 0 1 1 0 1 1 1 1 1 0 1 1 1 0 0 0 1 0 0]  
[0 0 1 0 0 1 0 1 1 0 1 0 0 0 1 0 1 0 1 1 0 1 0 1 1]  
[1 1 0 1 1 0 0 1 1 0 0 1 0 1 0 0 0 0 1 1 0 0 0 1 1]  
[0 1 0 1 1 1 1 1 1 1 1 0 0 0 1 0 0 1 1 1 1 0 1 1 0]  
[1 0 0 1 0 0 0 0 0 0 0 1 1 0 1 0 1 1 1 0 0 1 0 1 1]  
[1 1 1 0 1 0 0 0 0 0 1 1 1 0 0 0 1 0 1 1 1 0 0 1 0 0]  
[1 0 1 0 0 1 0 0 1 1 0 1 1 0 1 0 0 1 0 1 1 1 0 1 1]  
[1 0 0 1 1 0 1 1 1 1 0 1 1 0 0 1 1 0 0 1 0 1 0 1 0]  
[0 1 1 1 1 0 1 0 0 1 0 1 1 1 1 1 1 1 1 1 0 0 0 0 0 0]  
[1 1 0 0 1 0 0 1 1 0 0 1 0 0 0 0 0 0 1 1 0 0 0 0 0]  
[1 1 1 1 0 1 1 1 1 1 1 0 1 0 0 0 0 1 1 1 1 0 0 0 1]



```
[0 0 0 1 0 1 0 0 0 0 1 0 0 1 0 0 1 1 0 1 1]
[1 0 1 0 0 0 1 0 0 1 0 1 1 1 1 1 1 1 1 0 1 1]
[1 0 0 1 0 1 0 1 1 0 0 1 1 0 1 0 0 0 0 0 1 0 1 0]
[0 1 1 0 0 0 0 1 1 1 1 1 1 0 0 1 0 0 0 0 1 0 0 0 0]
[1 1 1 1 0 0 1 1 0 0 0 0 1 1 1 0 1 0 0 1 0 1 0 0 0]
[1 0 0 1 1 1 1 1 1 0 0 1 1 0 1 0 0 1 1 0 0 0 1 0 1]
[1 1 1 1 0 0 0 0 1 1 1 1 1 0 0 1 1 1 1 1 0 1 0 0 1]
[0 0 0 1 1 0 0 1 1 0 0 0 1 1 1 1 0 0 0 1 0 0 1 1 1]
[1 0 1 1 1 1 1 1 1 1 0 1 1 0 0 1 1 0 1 0 1 1 1 0 1]
[1 0 1 0 0 0 0 0 0 1 0 1 1 1 1 1 1 0 0 0 1 0 1 0 1]
```

### Rule 150

#### Finite grids, N=25 and 50 cycles

original random data: [1 1 1 0 0 0 0 0 1 1 0 1 1 0 1 1 1 1 0 1 0 1 0 1 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [1 0 0 1 0 1 1 0]

generated array with finite bound:

```
[1 0 1 0 1 1 1 0 1 1 1 1 1 1 1 0 0 1 1 0 1 0 1 0 0]
[0 1 0 1 1 0 1 1 1 0 0 0 0 0 1 0 0 1 1 1 0 1 0 0 1]
[0 0 1 1 1 1 1 0 1 0 1 1 1 0 0 0 0 1 0 1 1 0 0 0 0]
[1 0 1 0 0 0 1 1 0 1 1 0 1 0 1 1 0 0 1 1 1 0 1 1 1]
[0 1 0 0 1 0 1 1 1 1 1 1 0 1 1 1 0 0 1 0 1 1 1 0 1]
[0 0 0 0 0 1 1 0 0 0 0 1 1 1 0 1 0 0 0 1 1 0 1 1 0]
[1 1 1 1 0 1 1 0 1 1 0 1 0 1 1 0 0 1 0 1 1 1 1 1 0]
[1 0 0 1 1 1 1 1 1 1 1 0 1 1 1 0 0 0 1 1 0 0 0 1 0]
[0 0 0 1 0 0 0 0 0 0 1 1 1 0 1 0 1 0 1 1 0 1 0 0 0]
[1 1 0 0 0 1 1 1 1 0 1 0 1 1 0 1 0 1 1 1 1 0 0 1 1]
[1 1 0 1 0 1 0 0 1 1 0 1 1 1 1 0 1 1 0 0 1 0 0 1 1]
[1 1 1 0 1 0 0 0 1 1 1 1 0 0 1 1 1 1 0 0 0 0 0 1 1]
[1 0 1 1 0 0 1 0 1 0 0 1 0 0 1 0 0 1 0 1 1 1 0 1 1]
[0 1 1 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 1 1 0 1 1 1 1]
[0 1 0 1 0 1 0 0 0 1 1 1 1 1 1 1 1 0 1 1 1 1 0 0 1]
[0 0 1 0 1 0 0 1 0 1 0 0 0 0 0 0 1 1 1 0 0 1 0 0 0]
[1 0 0 1 0 0 0 0 1 0 0 1 1 1 1 0 1 0 1 0 0 0 0 1 1]
[0 0 0 0 0 1 1 0 0 0 0 1 0 0 1 1 0 1 0 0 1 1 0 1 1]
[1 1 1 1 0 1 1 0 1 1 0 0 0 0 1 1 1 0 0 0 1 1 1 1 1]
[1 0 0 1 1 1 1 1 1 1 0 1 1 0 1 0 1 0 1 0 1 0 0 0 1]
[0 0 0 1 0 0 0 0 0 1 1 1 1 1 0 1 0 1 0 1 0 0 1 0 0]
```

```

[1 1 0 0 0 1 1 1 0 1 0 0 0 1 1 0 1 0 1 0 0 0 0 0 1]
[1 1 0 1 0 1 0 1 1 0 0 1 0 1 1 1 0 1 0 0 1 1 1 0 0]
[1 1 1 0 1 0 1 1 1 0 0 0 1 1 0 1 1 0 0 0 1 0 1 0 1]
[1 0 1 1 0 1 1 0 1 0 1 0 1 1 1 1 1 0 1 0 0 1 0 1 0]
[0 1 1 1 1 1 1 1 0 1 0 1 1 0 0 0 1 1 0 0 0 0 1 0 0]
[0 1 0 0 0 0 0 1 1 0 1 1 1 0 1 0 1 1 0 1 1 0 0 0 1]
[0 0 0 1 1 1 0 1 1 1 1 0 1 1 0 1 1 1 1 1 1 0 1 0 0]
[1 1 0 1 0 1 1 1 0 0 1 1 1 1 1 1 0 0 0 0 1 1 0 0 1]
[1 1 1 0 1 1 0 1 0 0 1 0 0 0 0 1 0 1 1 0 1 1 0 0 0]
[1 0 1 1 1 1 1 0 0 0 0 0 1 1 0 0 1 1 1 1 1 1 0 1 1]
[0 1 1 0 0 0 1 0 1 1 1 0 1 1 0 0 1 0 0 0 0 1 1 1 1]
[0 1 1 0 1 0 0 1 1 0 1 1 1 1 0 0 0 0 1 1 0 1 0 0 1]
[0 1 1 1 0 0 0 1 1 1 1 0 0 1 0 1 1 0 1 1 1 0 0 0 0]
[0 1 0 1 0 1 0 1 0 0 1 0 0 0 1 1 1 1 1 0 1 0 1 1 1]
[0 0 1 0 1 0 1 0 0 0 0 0 1 0 1 0 0 0 1 1 0 1 1 0 1]
[1 0 0 1 0 1 0 0 1 1 1 0 0 1 0 0 1 0 1 1 1 1 1 1 0]
[0 0 0 0 1 0 0 0 1 0 1 0 0 0 0 0 0 1 1 0 0 0 0 1 0]
[1 1 1 0 0 0 1 0 0 1 0 0 1 1 1 1 0 1 1 0 1 1 0 0 0]
[1 0 1 0 1 0 0 0 0 0 0 0 1 0 0 1 1 1 1 1 1 1 0 1 1]
[0 1 0 1 0 0 1 1 1 1 1 0 0 0 0 1 0 0 0 0 0 1 1 1 1]
[0 0 1 0 0 0 1 0 0 0 1 0 1 1 0 0 0 1 1 1 0 1 0 0 1]
[1 0 0 0 1 0 0 0 1 0 0 1 1 1 0 1 0 1 0 1 1 0 0 0 0]
[0 0 1 0 0 0 1 0 0 0 0 1 0 1 1 0 1 0 1 1 1 0 1 1 1]
[1 0 0 0 1 0 0 0 1 1 0 0 1 1 1 1 0 1 1 0 1 1 1 0 1]
[0 0 1 0 0 0 1 0 1 1 0 0 1 0 0 1 1 1 1 1 1 0 1 1 0]
[1 0 0 0 1 0 0 1 1 1 0 0 0 0 0 1 0 0 0 0 1 1 1 1 0]
[0 0 1 0 0 0 0 1 0 1 0 1 1 1 0 0 0 1 1 0 1 0 0 1 0]
[1 0 0 0 1 1 0 0 1 0 1 1 0 1 0 1 0 1 1 1 0 0 0 0 0]
[0 0 1 0 1 1 0 0 0 1 1 1 1 0 1 0 1 1 0 1 0 1 1 1 1]

```

### Periodic Boundary Conditions, N=25 and 50 cycles

original random data: [0 0 0 0 1 1 0 0 1 1 1 0 0 0 0 0 0 1 1 0 0 1 1 1 1]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [1 0 0 1 0 1 1 0]

generated array with periodic bound

```

[0 1 1 0 1 1 0 0 1 0 1 0 1 1 1 1 0 1 1 0 0 1 0 0 1]
[1 1 1 1 1 1 0 0 0 1 0 1 1 0 0 1 1 1 1 0 0 0 0 0 0]
[1 0 0 0 0 1 0 1 0 0 1 1 1 0 0 1 0 0 1 0 1 1 1 1 0]
[0 0 1 1 0 0 1 0 0 0 1 0 1 0 0 0 0 0 0 1 1 0 0 1 1]

```

[0 0 1 1 0 0 0 0 1 0 0 1 0 0 1 1 1 1 0 1 1 0 0 1 1]  
[0 0 1 1 0 1 1 0 0 0 0 0 0 0 1 0 0 1 1 1 1 0 0 1 1]  
[0 0 1 1 1 1 1 0 1 1 1 1 1 0 0 0 0 1 0 0 1 0 0 1 1]  
[0 0 1 0 0 0 1 1 1 0 0 0 1 0 1 1 0 0 0 0 0 0 0 1 1]  
[0 0 0 0 1 0 1 0 1 0 1 0 0 1 1 1 0 1 1 1 1 1 0 1 1]  
[0 1 1 0 0 1 0 1 0 1 0 0 0 1 0 1 1 1 0 0 0 1 1 1 1]  
[1 1 1 0 0 0 1 0 1 0 0 1 0 0 1 1 0 1 0 1 0 1 0 0 1]  
[0 0 1 0 1 0 0 1 0 0 0 0 0 0 1 1 1 0 1 0 1 0 0 0 1]  
[0 0 0 1 0 0 0 0 0 1 1 1 1 0 1 0 1 1 0 1 0 0 1 0 0]  
[1 1 0 0 0 1 1 1 0 1 0 0 1 1 0 1 1 1 1 0 0 0 0 0 1]  
[0 1 0 1 0 1 0 1 1 0 0 0 1 1 1 1 0 0 1 0 1 1 1 0 1]  
[1 0 1 0 1 0 1 1 1 0 1 0 1 0 0 1 0 0 0 1 1 0 1 1 0]  
[0 1 0 1 0 1 1 0 1 1 0 1 0 0 0 0 0 1 0 1 1 1 1 1 1]  
[1 0 1 0 1 1 1 1 1 1 1 0 0 1 1 1 0 0 1 1 0 0 0 0 1]  
[1 1 0 1 1 0 0 0 0 0 1 0 0 1 0 1 0 0 1 1 0 1 1 0 1]  
[0 1 1 1 1 0 1 1 1 0 0 0 0 0 1 0 0 0 1 1 1 1 1 1 1]  
[1 1 0 0 1 1 1 0 1 0 1 1 1 0 0 0 1 0 1 0 0 0 0 0 1]  
[0 1 0 0 1 0 1 1 0 1 1 0 1 0 1 0 0 1 0 0 1 1 1 0 1]  
[1 0 0 0 0 1 1 1 1 1 1 1 0 1 0 0 0 0 0 0 0 1 0 1 1 0]  
[0 0 1 1 0 1 0 0 0 0 0 1 1 0 0 1 1 1 1 0 0 1 1 1 1]  
[0 0 1 1 1 0 0 1 1 1 0 1 1 0 0 1 0 0 1 0 0 1 0 0 1]  
[0 0 1 0 1 0 0 1 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0]  
[1 0 0 1 0 0 0 0 1 1 0 0 1 0 1 1 1 1 1 1 1 1 1 1 1]  
[1 0 0 0 0 1 1 0 1 1 0 0 0 1 1 0 0 0 0 0 0 0 0 0 0]  
[0 0 1 1 0 1 1 1 1 1 0 1 0 1 1 0 1 1 1 1 1 1 1 1 0]  
[1 0 1 1 1 1 0 0 0 1 1 0 1 1 1 1 1 0 0 0 0 0 0 1 0]  
[0 1 1 0 0 1 0 1 0 1 1 1 1 0 0 0 1 0 1 1 1 1 0 0 1]  
[1 1 1 0 0 0 1 0 1 1 0 0 1 0 1 0 0 1 1 0 0 1 0 0 0]  
[1 0 1 0 1 0 0 1 1 1 0 0 0 1 0 0 0 1 1 0 0 0 0 1 0]  
[0 1 0 1 0 0 0 1 0 1 0 1 0 0 0 1 0 1 1 0 1 1 0 0 1]  
[1 0 1 0 0 1 0 0 1 0 1 0 0 1 0 0 1 1 1 1 1 1 0 0 0]  
[0 1 0 0 0 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 1 0 1 0]  
[0 0 0 1 1 1 1 1 0 0 0 1 1 1 1 0 0 0 1 1 0 0 1 0 0]  
[1 1 0 1 0 0 0 1 0 1 0 1 0 0 1 0 1 0 1 1 0 0 0 0 1]  
[0 1 1 0 0 1 0 0 1 0 1 0 0 0 0 1 0 1 1 1 0 1 1 0 1]  
[1 1 1 0 0 0 0 0 0 1 0 0 1 1 0 0 1 1 0 1 1 1 1 1 0]  
[1 0 1 0 1 1 1 1 0 0 0 0 1 1 0 0 1 1 1 1 0 0 0 1 1]  
[1 1 0 1 1 0 0 1 0 1 1 0 1 1 0 0 1 0 0 1 0 1 0 1 0]  
[1 1 1 1 1 0 0 0 1 1 1 1 1 1 0 0 0 0 0 0 1 0 1 0 1]  
[0 0 0 0 1 0 1 0 1 0 0 0 0 1 0 1 1 1 1 0 0 1 0 1 1]



[illegible]

### Periodic Boundary Conditions, N=25 and 50 cycles

original random data: [1 0 1 1 1 0 0 0 0 0 0 1 0 0 0 1 0 1 1 1 0 0 1 1 1]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [0 0 0 1 0 0 1 0]

generated array with periodic bound

[illegible]

[illegible]

[0 0]  
[0 0]

### Rule 73

#### Finite grids, N=25 and 50 cycles

original random data: [0 1 0 0 0 0 1 0 0 1 0 0 1 1 1 0 1 1 0 0 0 1 1 0 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [0 1 0 0 1 0 0 1]

generated array with finite bound:

[1 0 1 0 0 1 0 1 1 0 1 1 0 1 0 0 0 0 1 0 1 0 0 1 0]  
[0 0 0 1 1 0 0 0 0 0 0 0 0 0 1 0 0 1 0 0 0 1 1 0 1]  
[0 0 1 0 0 1 0 0 0 0 0 0 0 0 1 0 1 1 0 1 0 1 0 0 0 0]  
[0 1 0 1 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 1 0 0 0]  
[1 0 0 0 0 0 0 1 0 0 0 1 0 1 0 0 0 0 0 0 1 0 1 0 0]  
[0 1 0 0 0 0 1 0 1 0 1 0 0 0 1 0 0 0 0 1 0 0 0 1 0]  
[1 0 1 0 0 1 0 0 0 0 0 1 0 1 0 1 0 0 1 0 1 0 1 0 1]  
[0 0 0 1 1 0 1 0 0 0 1 0 0 0 0 0 1 1 0 0 0 0 0 0 0]  
[0 0 1 0 0 0 0 1 0 1 0 1 0 0 0 1 0 0 1 0 0 0 0 0 0]  
[0 1 0 1 0 0 1 0 0 0 0 0 1 0 1 0 1 1 0 1 0 0 0 0 0]  
[1 0 0 0 1 1 0 1 0 0 0 1 0 0 0 0 0 0 0 0 1 0 0 0 0]  
[0 1 0 1 0 0 0 0 1 0 1 0 1 0 0 0 0 0 0 1 0 1 0 0 0]  
[1 0 0 0 1 0 0 1 0 0 0 0 0 1 0 0 0 0 1 0 0 0 1 0 0]  
[0 1 0 1 0 1 1 0 1 0 0 0 1 0 1 0 0 1 0 1 0 1 0 1 0]  
[1 0 0 0 0 0 0 0 0 1 0 1 0 0 0 1 1 0 0 0 0 0 0 0 1]  
[0 1 0 0 0 0 0 0 1 0 0 0 1 0 1 0 0 1 0 0 0 0 0 1 0]  
[1 0 1 0 0 0 0 1 0 1 0 1 0 0 0 1 1 0 1 0 0 0 1 0 1]  
[0 0 0 1 0 0 1 0 0 0 0 0 1 0 1 0 0 0 0 1 0 1 0 0 0]  
[0 0 1 0 1 1 0 1 0 0 0 1 0 0 0 1 0 0 1 0 0 0 1 0 0]  
[0 1 0 0 0 0 0 0 1 0 1 0 1 0 1 0 1 1 0 1 0 1 0 1 0]  
[1 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1]  
[0 0 0 1 0 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0]  
[0 0 1 0 1 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1]  
[0 1 0 0 0 0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 0 1 0 0 0]  
[1 0 1 0 0 1 0 0 0 0 0 1 0 0 0 0 0 0 0 0 1 0 1 0 0]  
[0 0 0 1 1 0 1 0 0 0 1 0 1 0 0 0 0 0 0 1 0 0 0 1 0]  
[0 0 1 0 0 0 0 1 0 1 0 0 0 1 0 0 0 0 1 0 1 0 1 0 1]  
[0 1 0 1 0 0 1 0 0 0 1 0 1 0 1 0 0 1 0 0 0 0 0 0 0]  
[1 0 0 0 1 1 0 1 0 1 0 0 0 0 0 1 1 0 1 0 0 0 0 0 0]  
[0 1 0 1 0 0 0 0 0 0 1 0 0 0 1 0 0 0 0 1 0 0 0 0 0]

```
[1 0 0 0 1 0 0 0 0 1 0 1 0 1 0 1 0 0 1 0 1 0 0 0 0]
[0 1 0 1 0 1 0 0 1 0 0 0 0 0 0 0 1 1 0 0 0 1 0 0 0]
[1 0 0 0 0 0 1 1 0 1 0 0 0 0 0 1 0 0 1 0 1 0 1 0 0]
[0 1 0 0 0 1 0 0 0 0 1 0 0 0 1 0 1 1 0 0 0 0 0 1 0]
[1 0 1 0 1 0 1 0 0 1 0 1 0 1 0 0 0 0 1 0 0 0 1 0 1]
[0 0 0 0 0 0 0 1 1 0 0 0 0 0 1 0 0 1 0 1 0 1 0 0 0]
[0 0 0 0 0 0 1 0 0 1 0 0 0 1 0 1 1 0 0 0 0 0 1 0 0]
[0 0 0 0 0 1 0 1 1 0 1 0 1 0 0 0 0 1 0 0 0 1 0 1 0]
[0 0 0 0 1 0 0 0 0 0 0 0 0 1 0 0 1 0 1 0 1 0 0 0 1]
[0 0 0 1 0 1 0 0 0 0 0 0 1 0 1 1 0 0 0 0 0 1 0 1 0]
[0 0 1 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 1 0 0 0 1]
[0 1 0 1 0 1 0 1 0 0 1 0 1 0 0 1 0 1 0 1 0 1 0 1 0]
[1 0 0 0 0 0 0 0 1 1 0 0 0 1 1 0 0 0 0 0 0 0 0 0 1]
[0 1 0 0 0 0 0 1 0 0 1 0 1 0 0 1 0 0 0 0 0 0 0 1 0]
[1 0 1 0 0 0 1 0 1 1 0 0 0 1 1 0 1 0 0 0 0 0 1 0 1]
[0 0 0 1 0 1 0 0 0 0 1 0 1 0 0 0 0 1 0 0 0 1 0 0 0]
[0 0 1 0 0 0 1 0 0 1 0 0 0 1 0 0 1 0 1 0 1 0 1 0 0]
[0 1 0 1 0 1 0 1 1 0 1 0 1 0 1 1 0 0 0 0 0 0 0 1 0]
[1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 1 0 1]
[0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0 1 0 0 0]
```

### Periodic Boundary Conditions, N=25 and 50 cycles

original random data: [0 0 1 0 1 1 0 1 1 0 0 0 0 0 0 1 0 0 0 1 0 1 1 1 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [0 1 0 0 1 0 0 1]

generated array with periodic bound

```
[0 1 0 0 0 0 0 0 0 1 0 0 0 0 1 0 1 0 1 0 0 0 1 0 1]
[0 0 1 0 0 0 0 0 1 0 1 0 0 1 0 0 0 0 0 1 0 1 0 0 0]
[0 1 0 1 0 0 0 1 0 0 0 1 1 0 1 0 0 0 1 0 0 0 1 0 0]
[1 0 0 0 1 0 1 0 1 0 1 0 0 0 0 1 0 1 0 1 0 1 0 1 0]
[0 1 0 1 0 0 0 0 0 0 0 1 0 0 1 0 0 0 0 0 0 0 0 0 0]
[1 0 0 0 1 0 0 0 0 0 1 0 1 1 0 1 0 0 0 0 0 0 0 0 0]
[0 1 0 1 0 1 0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 0 0 0 1]
[0 0 0 0 0 0 1 0 1 0 1 0 0 0 0 1 0 1 0 0 0 0 0 1 0]
[0 0 0 0 0 1 0 0 0 0 0 1 0 0 1 0 0 0 1 0 0 0 1 0 1]
[1 0 0 0 1 0 1 0 0 0 1 0 1 1 0 1 0 1 0 1 0 1 0 0 0]
[0 1 0 1 0 0 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1]
[0 0 0 0 1 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 1 0 0]
[0 0 0 1 0 0 0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 1 0 1 0]
```



[0 0 1 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0 1 0]  
[0 1 0 0 0 0 0 1 0 0 0 1 0 1 0 0 0 0 1 0 1 0 1 0 1]  
[0 0 1 0 0 0 1 0 1 0 1 0 0 0 1 0 0 1 0 0 0 0 0 0 0]  
[0 1 0 1 0 1 0 0 0 0 0 1 0 1 0 1 1 0 1 0 0 0 0 0 0]  
[1 0 0 0 0 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 1 0 0 0 0]  
[0 1 0 0 0 1 0 1 0 1 0 1 0 0 0 0 0 0 0 1 0 1 0 0 0 1]  
[0 0 1 0 1 0 0 0 0 0 0 0 0 1 0 0 0 0 0 1 0 0 0 1 0 1 0]  
[0 1 0 0 0 1 0 0 0 0 0 0 1 0 1 0 0 1 0 1 0 1 0 0 0 1]  
[0 0 1 0 1 0 1 0 0 0 1 0 0 0 0 1 1 0 0 0 0 0 1 0 1 0]  
[0 1 0 0 0 0 0 1 0 1 0 1 0 1 0 0 1 0 0 0 1 0 0 0 1]  
[0 0 1 0 0 0 1 0 0 0 0 0 0 0 0 1 1 0 1 0 1 0 1 0 1 0]  
[0 1 0 1 0 1 0 1 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 1]  
[0 0 0 0 0 0 0 0 0 1 0 0 0 1 0 1 0 0 0 0 0 0 0 0 0 1 0]  
[0 0 0 0 0 0 0 0 1 0 1 0 1 0 0 0 0 1 0 0 0 0 0 0 0 1 0 1]  
[1 0 0 0 0 0 0 1 0 0 0 0 0 0 1 0 1 0 1 0 0 0 0 0 1 0 0 0]  
[0 1 0 0 0 1 0 1 0 0 0 0 1 0 0 0 0 0 0 1 0 0 1 0 1 0 1]  
[0 0 1 0 1 0 0 0 0 1 0 1 0 1 0 0 0 0 1 0 1 1 0 0 0 0 0]  
[0 1 0 0 0 1 0 1 0 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0]  
[1 0 1 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 1 0 1 0 0 0]  
[0 0 0 0 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 1 0 0 0 0 1 0 1]  
[1 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0]  
[0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 1 0 1]  
[0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 1 0 0]  
[0 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 1 0 0]  
[0 0 0 0 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0 0 1 0 0]  
[0 0 0 0 1 0 1 0 1 0 1 0 0 0 0 0 1 0 0 0 0 1 0 1 0 0 0 0 1]  
[1 0 1 0 0 0 0 0 0 0 0 0 0 1 0 0 0 1 0 1 0 1 0 0 0 0 1 0 1 0]  
[0 0 0 0 1 0 0 0 0 0 0 0 0 0 1 0 1 1 0 0 0 0 0 0 1 0 1 0 0 0 0]  
[0 0 1 0 1 0 0 0 0 1 0 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0]  
[0 1 0 0 0 1 0 1 0 1 0 1 0 0 0 1 0 1 0 1 0 1 0 1 0 1 0 0]  
[1 0 1 0 1 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0]  
[0 0 0 0 0 0 1 0 0 0 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 1 0 0]  
[0 0 0 0 0 1 0 1 0 1 0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 1 0 1 0]  
[0 0 0 0 1 0 1 0 0 0 1]  
[1 0 1 0 1 0 1 0 1 0 1 0]  
[0 0 0 0 0 0 1 0]  
[0 0 0 0 0 1 0 1 0]

Rule 136

Finite grids, N=25 and 50 cycles

```
original random data: [0 0 1 0 1 0 1 1 0 1 0 1 0 1 1 1 0 1 1 0 0 0]
combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']
```

rule applied to each combination in order: [1 0 0 0 1 0 0 0]

generated array with finite bound:

[illegible]

```
[1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
```

### Periodic Boundary Conditions, N=25 and 50 cycles

original random data: [0 1 1 0 0 1 0 1 0 0 0 0 0 1 1 0 1 0 1 1 1 0 1 1 1]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [1 0 0 0 1 0 0 0]

generated array with periodic bound

```
[0 0 0 1 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[1 1 0 0 1 1 1 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[0 0 1 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[1 0 0 1 1 1 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[0 1 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 1 1 1 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]
[1 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 1 1 1 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0]
[0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1]
[1 1 1 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0]
[0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0]
[1 1 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1]
[0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0]
[1 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 1]
[0 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0]
[0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 1 1]
[1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0]
[0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 1 1 0]
```

[illegible]

The sensitivity to the boundary conditions depend on the rule used. For some rules, there is no major difference between the patterns produced while for others, the pattern changes completely.

Taking this fact into consideration, yes, the nature of patterns depends on the use and non-use of periodic boundary conditions.

4 d)

Rule 184 was implemented with periodic boundary conditions.

First test with 50 cycles:

random position where we have 1s: [56, 42, 14, 96, 74, 94, 75, 13, 7, 69, 36, 23]

original random data: [1, 1, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0,  
0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [1 0 1 1 1 0 0 0]

generated array with periodic bound

```
[1 0 0 0 0 0 0 1 1 1 1 1 0 1 0 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 0 1  
1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 0  
1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 0 1 1 1 1 0]
```

```
[1 1 1 1 1 1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1  
0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0  
1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0]
```

```
[1 0 0 0 0 0 0 1 1 1 1 1 0 1 0 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 0 1  
1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 0  
1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 0 1 1 1 1 0]
```

```
[1 1 1 1 1 1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1  
0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0  
1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0]
```

```
[1 0 0 0 0 0 0 1 1 1 1 1 0 1 0 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1  
1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 1 0  
1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 0 1 1 1 1 0]
```

```
[1 1 1 1 1 1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 1  
0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0  
1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0]
```

```
[1 0 0 0 0 0 0 1 1 1 1 1 0 1 0 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 0 1  
1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 0  
1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 0 1 1 1 1 0]
```

```
[1 1 1 1 1 1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 1
0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0
1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0]
```

[1 0 0 0 0 0 1 1 1 1 0 1 0 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 0 1]

[illegible]

[illegible]

[illegible]



```
1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 0
1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 0 1 1 1 1 0]
[1 1 1 1 1 1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1
0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0
1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0]
```

### Second test with 50 cycles:

random position where we have 1s: [97, 20, 72, 23, 15, 48, 35, 31, 42, 50, 83, 36, 33, 69, 37, 81, 63, 29, 27, 57, 56, 98, 13, 52, 96, 58, 43, 89, 70, 44]

original random data: [1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1, 1, 1, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 0, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [1 0 1 1 1 0 0 0]

generated array with periodic bound

```
[1 0 0 0 0 0 1 1 1 1 1 1 0 1 0 1 1 1 1 0 1 1 0 1 1 1 0 1 0 1 0 1 0 1 0 1 0
0 1 1 1 0 1 0 0 1 1 0 1 0 1 0 1 1 1 0 1 0 0 1 1 1 0 1 1 1 1 1 0 1 0 0 1 1
1 1 1 1 1 1 0 1 0 1 1 1 1 1 0 1 1 1 1 1 1 0 1 0 0 0]
[1 1 1 1 1 1 0 1 0 0 0 0 0 0 1 0 1 0 0 0 0 1 0 0 1 0 0 0 1 0 1 0 1 0 1 0 1 1
0 1 0 0 0 1 1 0 1 0 0 1 0 1 0 1 0 0 0 1 1 0 1 0 0 0 1 0 0 0 0 0 1 1 0 1 0
0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 1 1 0]
[1 0 0 0 0 0 1 1 1 1 1 1 0 1 0 1 1 1 1 0 1 1 0 1 1 1 0 1 0 1 0 1 0 1 0 1 0
0 1 1 1 0 1 0 0 1 1 0 1 0 1 0 1 1 1 0 1 0 0 1 1 1 0 1 1 1 1 1 0 1 0 0 1 1
1 1 1 1 1 1 0 1 0 1 1 1 1 1 0 1 1 1 1 1 1 0 1 0 0 0]
[1 1 1 1 1 1 0 1 0 0 0 0 0 0 1 0 1 0 0 0 0 1 0 0 1 0 0 0 1 0 1 0 1 0 1 0 1 1
0 1 0 0 0 1 1 0 1 0 0 1 0 1 0 1 0 0 0 1 1 0 1 0 0 0 1 0 0 0 0 0 1 1 0 1 0
0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 1 1 0]
[1 0 0 0 0 0 1 1 1 1 1 1 0 1 0 1 1 1 1 0 1 1 0 1 1 1 0 1 0 1 0 1 0 1 0 1 0
0 1 1 1 0 1 0 0 1 1 0 1 0 1 0 1 1 1 0 1 0 0 1 1 1 0 1 1 1 1 1 0 1 0 0 1 1
1 1 1 1 1 1 0 1 0 1 1 1 1 1 0 1 1 1 1 1 1 0 1 0 0 0]
[1 1 1 1 1 1 0 1 0 0 0 0 0 0 1 0 1 0 0 0 0 1 0 0 1 0 0 0 1 0 1 0 1 0 1 0 1 1
0 1 0 0 0 1 1 0 1 0 0 1 0 1 0 1 0 0 0 1 1 0 1 0 0 0 1 0 0 0 0 0 1 1 0 1 0
0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 1 1 0]
[1 0 0 0 0 0 1 1 1 1 1 1 0 1 0 1 1 1 1 0 1 1 0 1 1 1 0 1 0 1 0 1 0 1 0 1 0
```

[illegible]

[illegible]

[illegible]

```

0 1 1 1 0 1 0 0 1 1 0 1 0 1 0 1 1 1 0 1 0 0 1 1 1 0 1 1 1 1 0 1 0 0 1 1
1 1 1 1 1 1 0 1 0 1 1 1 1 1 0 1 1 1 1 1 1 0 1 0 0 0]
[1 1 1 1 1 0 1 0 0 0 0 0 0 1 0 1 0 0 0 0 1 0 0 1 0 0 0 1 0 1 0 1 0 1 1
0 1 0 0 0 1 1 0 1 0 0 1 0 1 0 1 0 0 0 1 1 0 1 0 0 0 1 0 0 0 0 0 1 1 0 1 0
0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 1 1 0]
[1 0 0 0 0 0 1 1 1 1 1 1 0 1 0 1 1 1 1 0 1 1 0 1 1 1 0 1 0 1 0 1 0 1 0 1 0
0 1 1 1 0 1 0 0 1 1 0 1 0 1 0 1 1 1 0 1 0 0 1 1 1 0 1 1 1 1 1 0 1 0 0 1 1
1 1 1 1 1 1 0 1 0 1 1 1 1 1 0 1 1 1 1 1 1 1 0 1 0 0 0]
[1 1 1 1 1 0 1 0 0 0 0 0 0 1 0 1 0 0 0 0 1 0 0 1 0 0 0 1 0 1 0 1 0 1 0 1 1
0 1 0 0 0 1 1 0 1 0 0 1 0 1 0 1 0 0 0 1 1 0 1 0 0 0 1 0 0 0 0 0 1 1 0 1 0
0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 0 0 1 1 1 0]

```

### Third test with 50 cycles:

random position where we have 1s: [45, 38, 77, 88, 92, 61, 82, 25, 81, 84, 42, 95, 54, 35, 26, 55, 80, 73, 22, 79, 72, 78, 47, 53, 44, 57, 8, 27, 87, 86, 23, 68, 74, 83, 59, 7, 91, 41, 6, 37, 70, 11, 65, 69, 63, 29, 34, 14]

original random data: [1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 1, 0, 1, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 1, 0, 1, 0, 1, 0, 0, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0]

combinations possible for input: ['000', '001', '010', '011', '100', '101', '110', '111']

rule applied to each combination in order: [1 0 1 1 1 0 0 0]

generated array with periodic bound

```

[1 0 0 0 0 0 0 0 0 1 0 1 1 0 1 1 1 1 1 1 0 1 0 0 1 0 0 0 1 1 1 1 0 1 0 0
1 0 1 0 1 0 0 1 0 0 1 1 1 1 1 0 1 0 0 0 1 0 1 0 1 0 1 0 1 1 0 1 0 0 0 1 0
0 1 0 1 0 0 0 0 0 0 0 0 0 1 0 0 1 0 1 0 1 0 1 1 1 1 0]
[1 1 1 1 1 1 1 1 1 0 1 0 1 0 0 1 0 0 0 0 0 0 0 1 1 0 1 1 1 0 1 0 0 0 0 1 1 0
1 0 1 0 1 1 0 1 1 0 1 0 0 0 0 0 1 1 1 0 1 0 1 0 1 0 1 0 1 0 0 1 1 1 0 1 1
0 1 0 1 1 1 1 1 1 1 1 0 1 1 0 1 0 1 0 1 0 1 0 0 0 0]
[1 0 0 0 0 0 0 0 0 1 0 1 1 0 1 1 1 1 1 1 1 0 1 0 0 1 0 0 0 1 1 1 1 0 1 0 0
1 0 1 0 1 0 0 1 0 0 1 1 1 1 1 0 1 0 0 0 1 0 1 0 1 0 1 0 1 1 0 1 0 0 0 1 0
0 1 0 1 0 0 0 0 0 0 0 0 0 1 0 0 1 0 1 0 1 0 1 1 1 1 0]
[1 1 1 1 1 1 1 1 1 0 1 0 1 0 0 1 0 0 0 0 0 0 0 1 1 0 1 1 1 0 1 0 0 0 0 1 1 0
1 0 1 0 1 1 0 1 1 0 1 0 0 0 0 0 1 1 1 0 1 0 1 0 1 0 1 0 1 0 0 1 1 1 0 1 1
0 1 0 1 1 1 1 1 1 1 1 0 1 1 0 1 0 1 0 1 0 1 0 0 0 0]
[1 0 0 0 0 0 0 0 0 1 0 1 1 0 1 1 1 1 1 1 1 0 1 0 0 1 0 0 0 1 1 1 1 0 1 0 0

```

[illegible]

[illegible]

[illegible]



1010100100111110100010101010110100010  
01010000000010010101011110]  
[1111111101010010000000110111010000110  
1010110110100000111010101010100111011  
01011111111011010101010000]  
[1000000001011011111110100100011110100  
1010100100111110100010101010110100010  
01010000000010010101011110]  
[1111111101010010000000110111010000110  
1010110110100000111010101010100111011  
010111111111011010101010000]  
[1000000001011011111110100100011110100  
1010100100111110100010101010110100010  
01010000000010010101011110]  
[1111111101010010000000110111010000110  
1010110110100000111010101010100111011  
010111111111011010101010000]