



UNIVERSITY of **HOUSTON**

DEPARTMENT OF COMPUTER SCIENCE

COSC 4370 Fall 2023

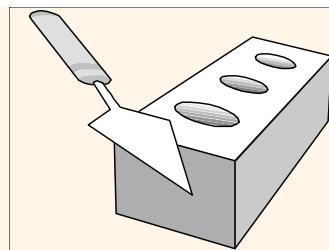
Interactive Computer Graphics

M & W 5:30 to 7:00 PM

Prof. Victoria Hilford

PLEASE TURN your webcam ON

NO CHATTING during LECTURE



COSC 4370

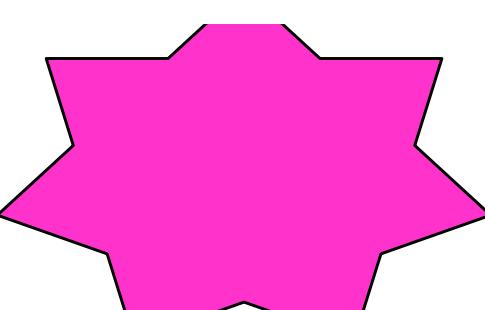
5:30 to 7

**PLEASE
LOG IN
CANVAS**

Please close all other windows.

NEXT.

10.02.2023 (M 5:30 to 7) (12)	Homework 5	Lecture 6
10.04.2023 (W 5:30 to 7) (13)	Homework 6	Lecture 7
10.09.2023 (M 5:30 to 7) (14)		PROJECT 2
10.11.2023 (W 5:30 to 7) (15)		EXAM 2 REVIEW
10.16.2023 (M 5:30 to 7) (16)		EXAM 2



CLASS PARTICIPATION - 15%

15% of Total + :

Class APRTICIPATION on Lecture 6
Not available until Oct 2 at 5:30pm | Due Oct 2 at 7pm | 100 pts

VH, publish

LECTURES

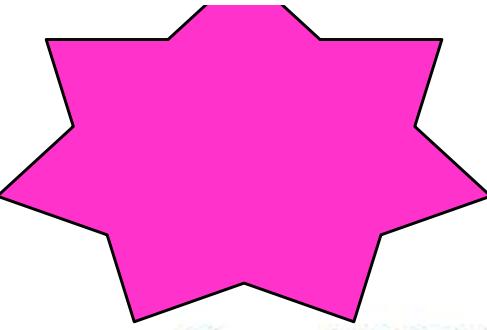
LECTURE 6 CLASS PARTICIPATION

Class Participation on Lecture 6.docx

SphereShading.c

VH, publish

VH, publish



Class APRTICIPATION on Lecture 6 

 Publish

 Edit

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Download and complete this word document.

Class Participation on Lecture 6.doc

SphereShading.c ↓

You will be prompted when to Upload completed document to CANVAS as **score.doc** (example 100.doc).

Warning:

TA, at random, will inspect the Uploaded document.

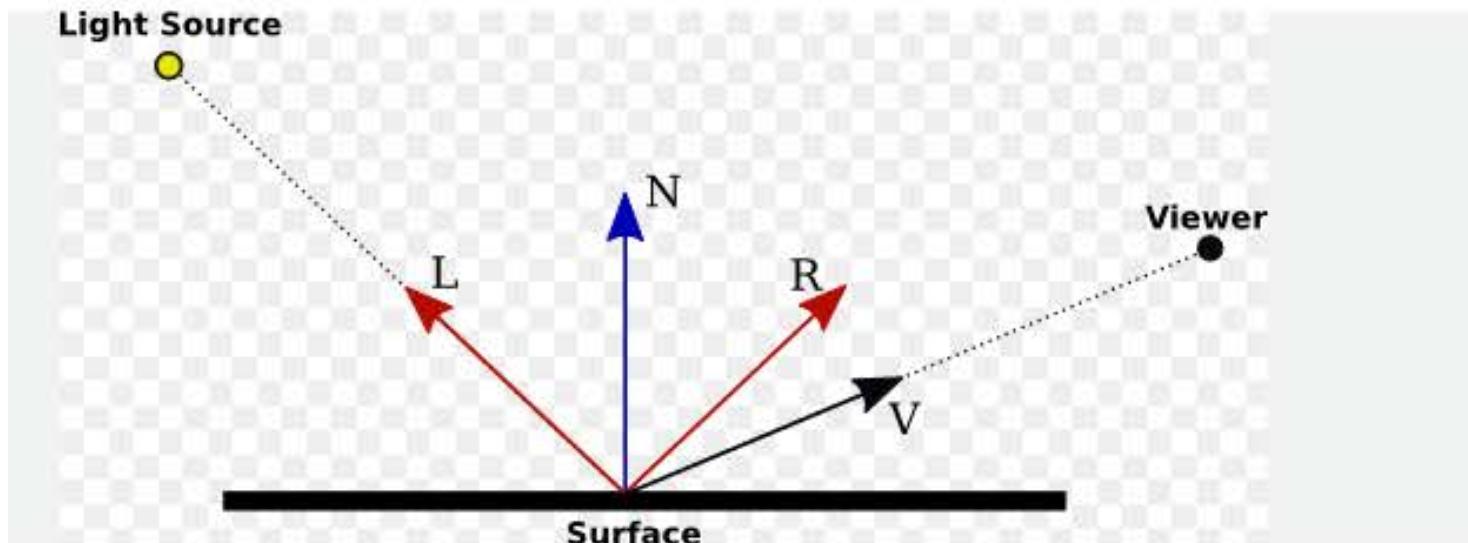
If your score is not honestly entered, you will get a zero.

For the Grader: if the student did not submit, please skip and do not assign a ZERO (MISSING).

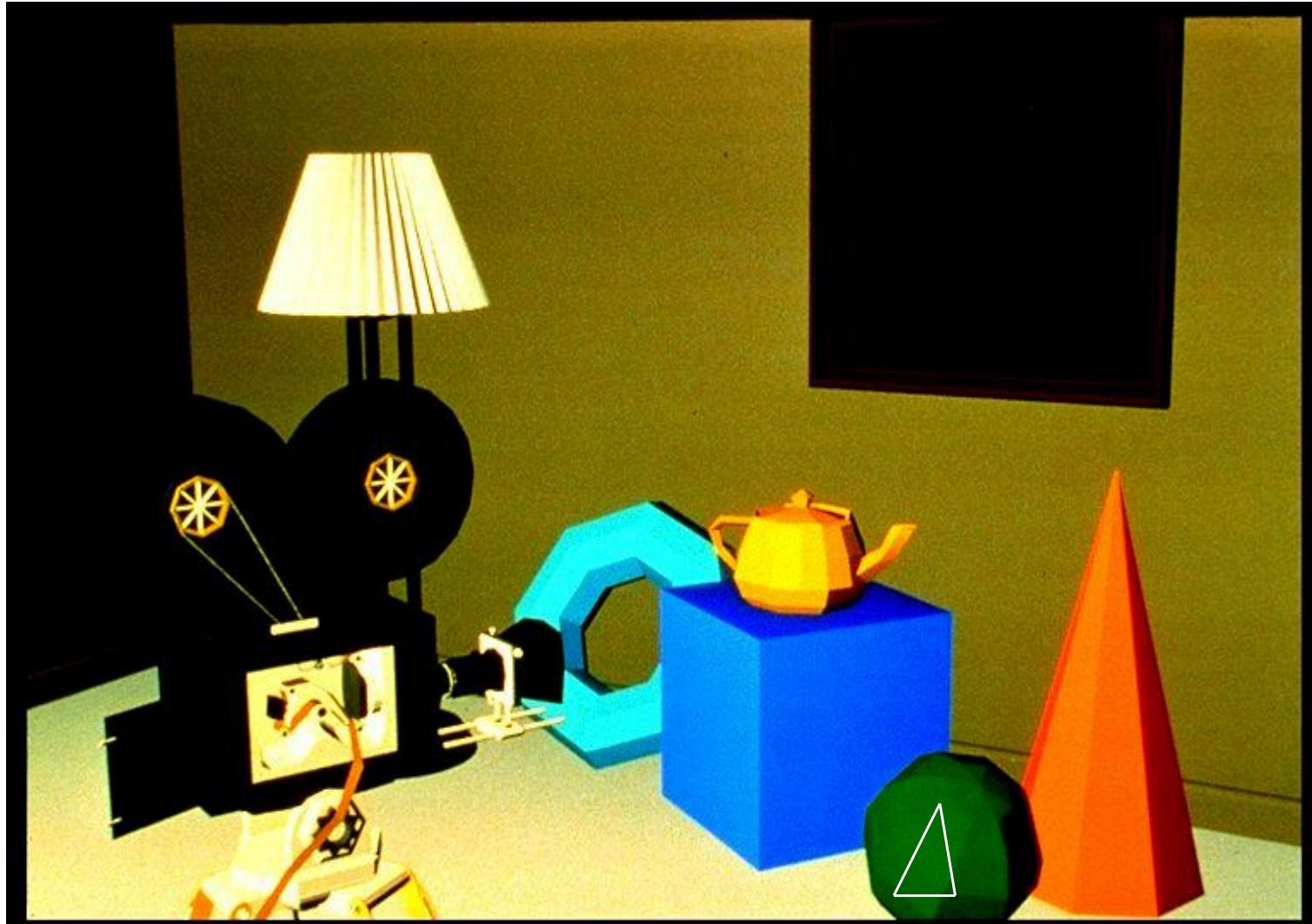
COSC 4370 – Computer Graphics

Lecture 6

Lighting and Shading Chapter 6

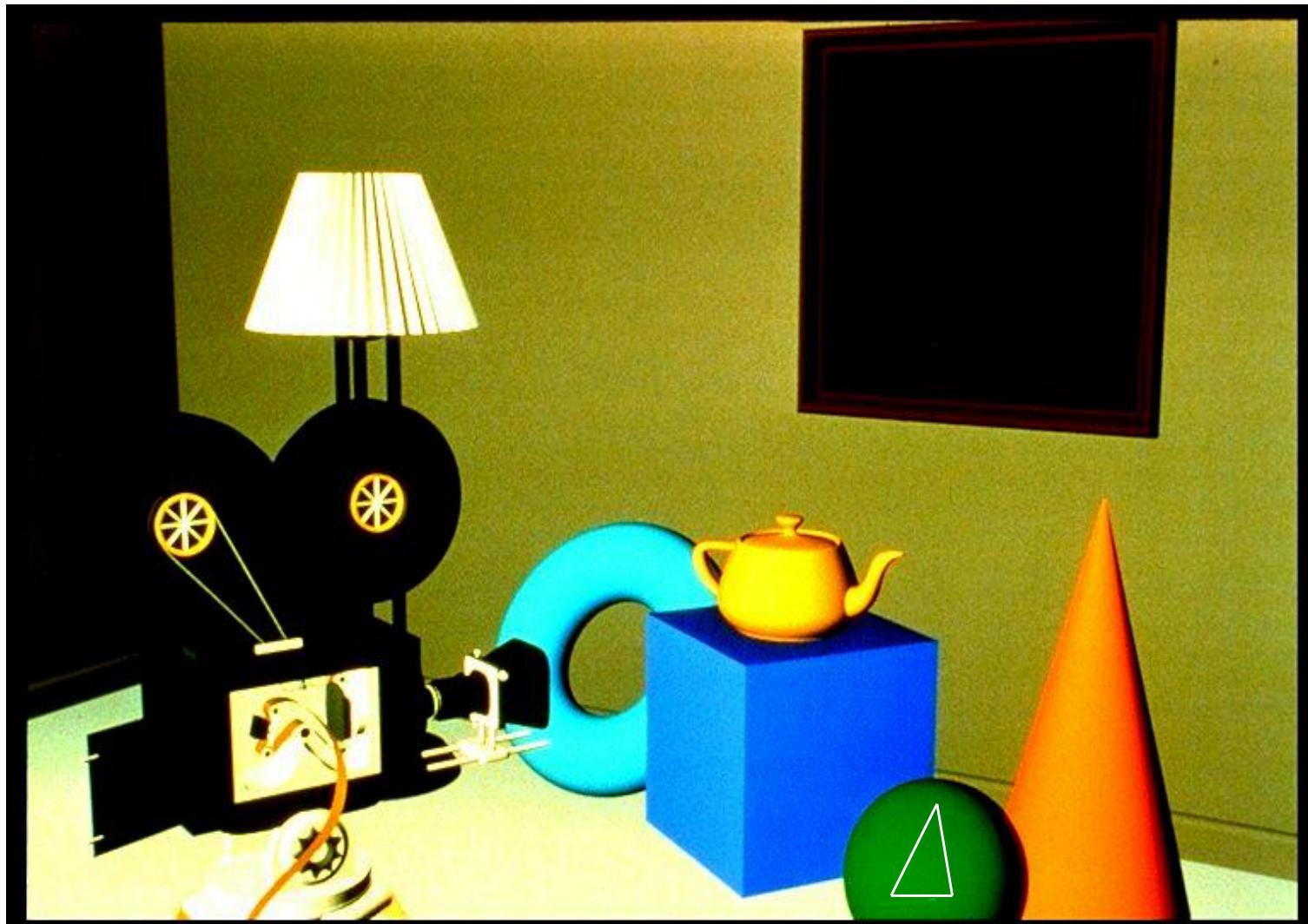


Per-Polygon (Faceted, Flat) Shading



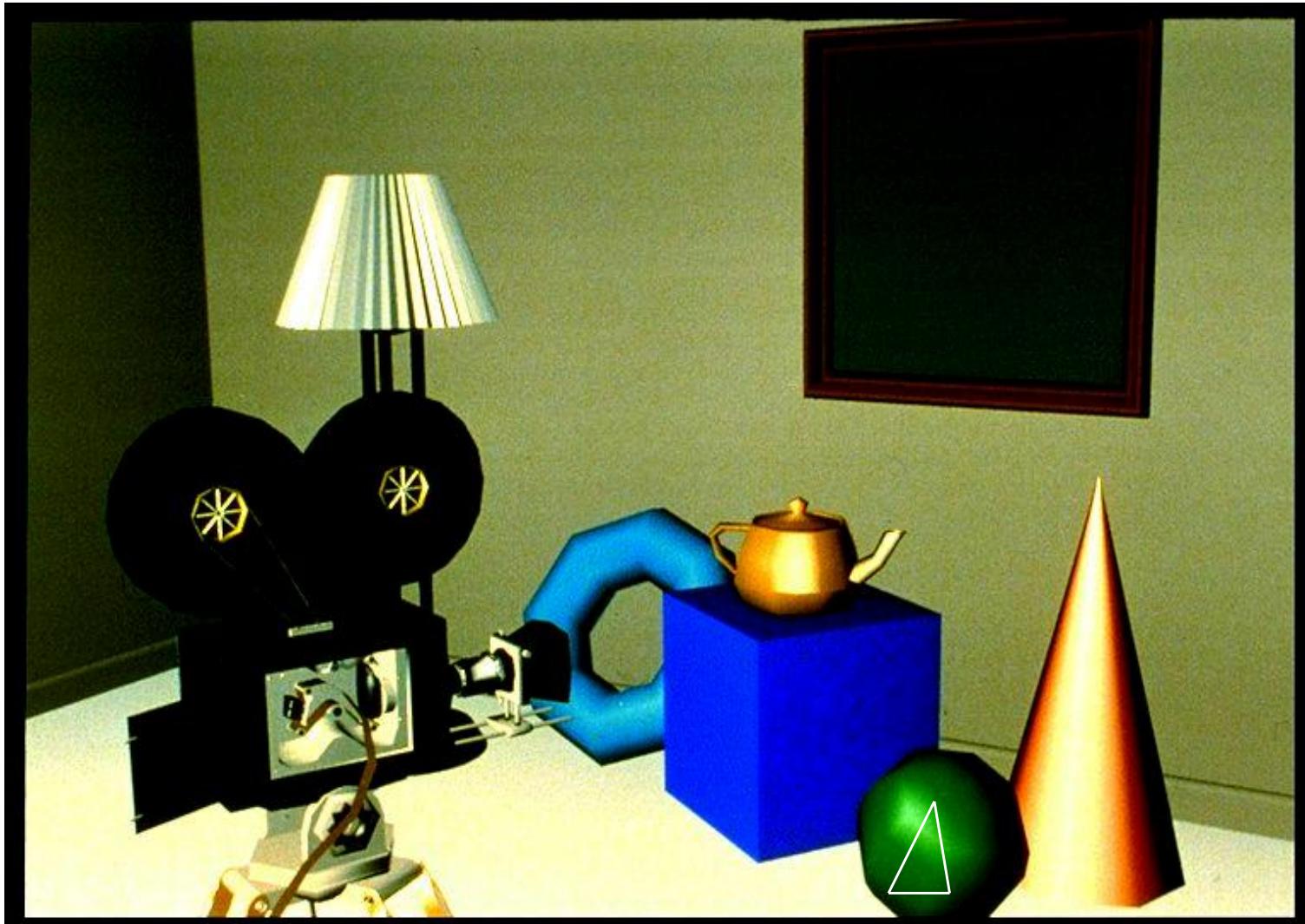
Guess PER POLYGON ? **FLAT / SMOOTH ?**

Gouraud Shading



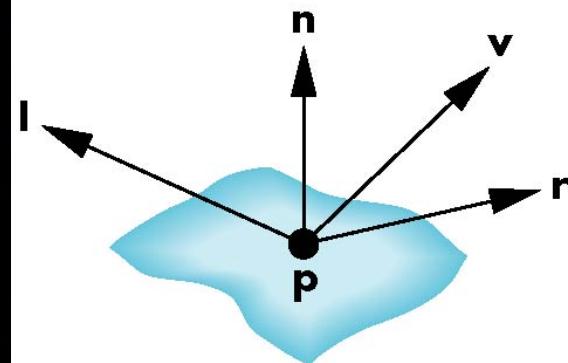
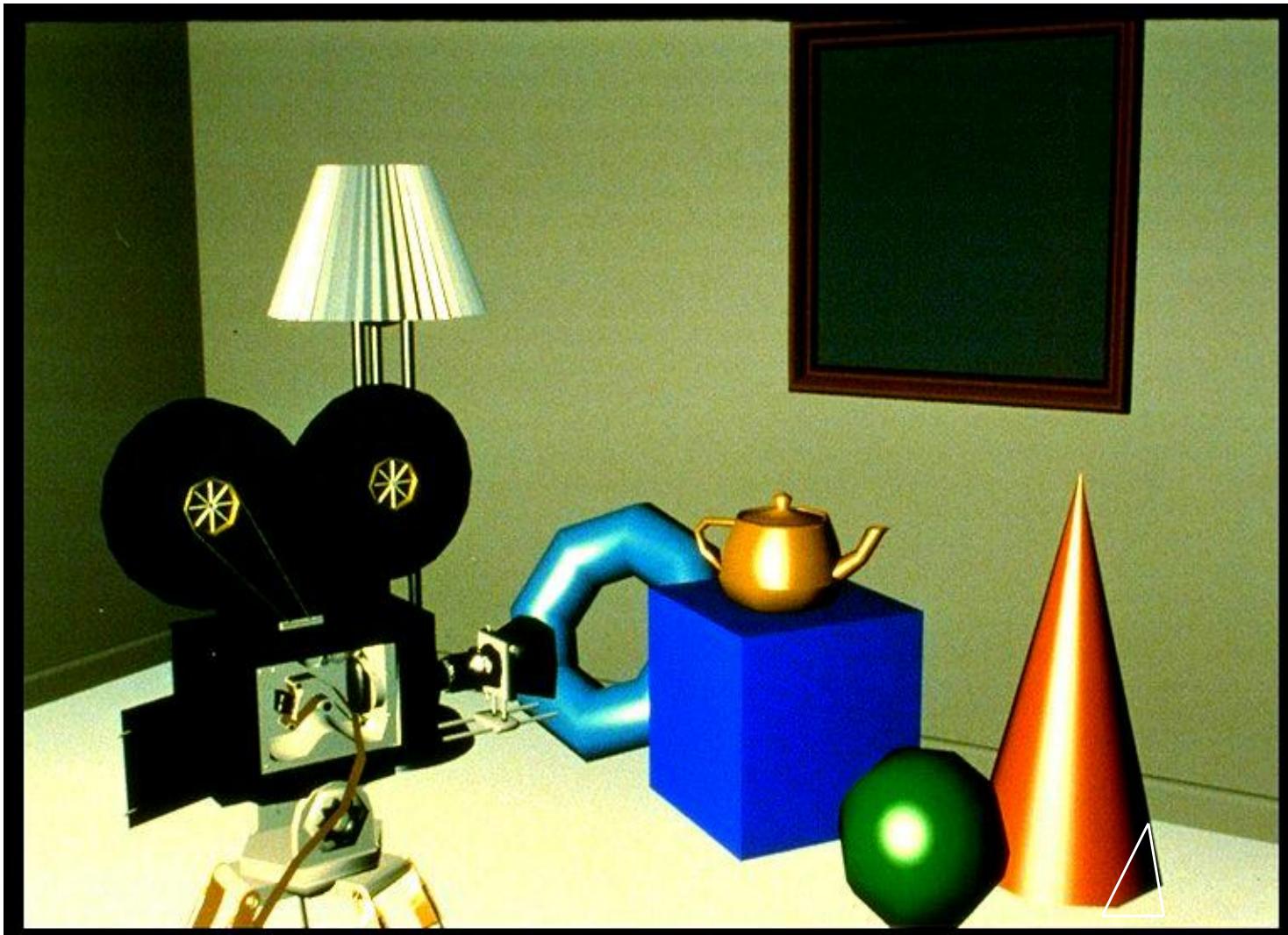
Guess PER POLYGON ? **FLAT / SMOOTH ?**

Specular Reflection



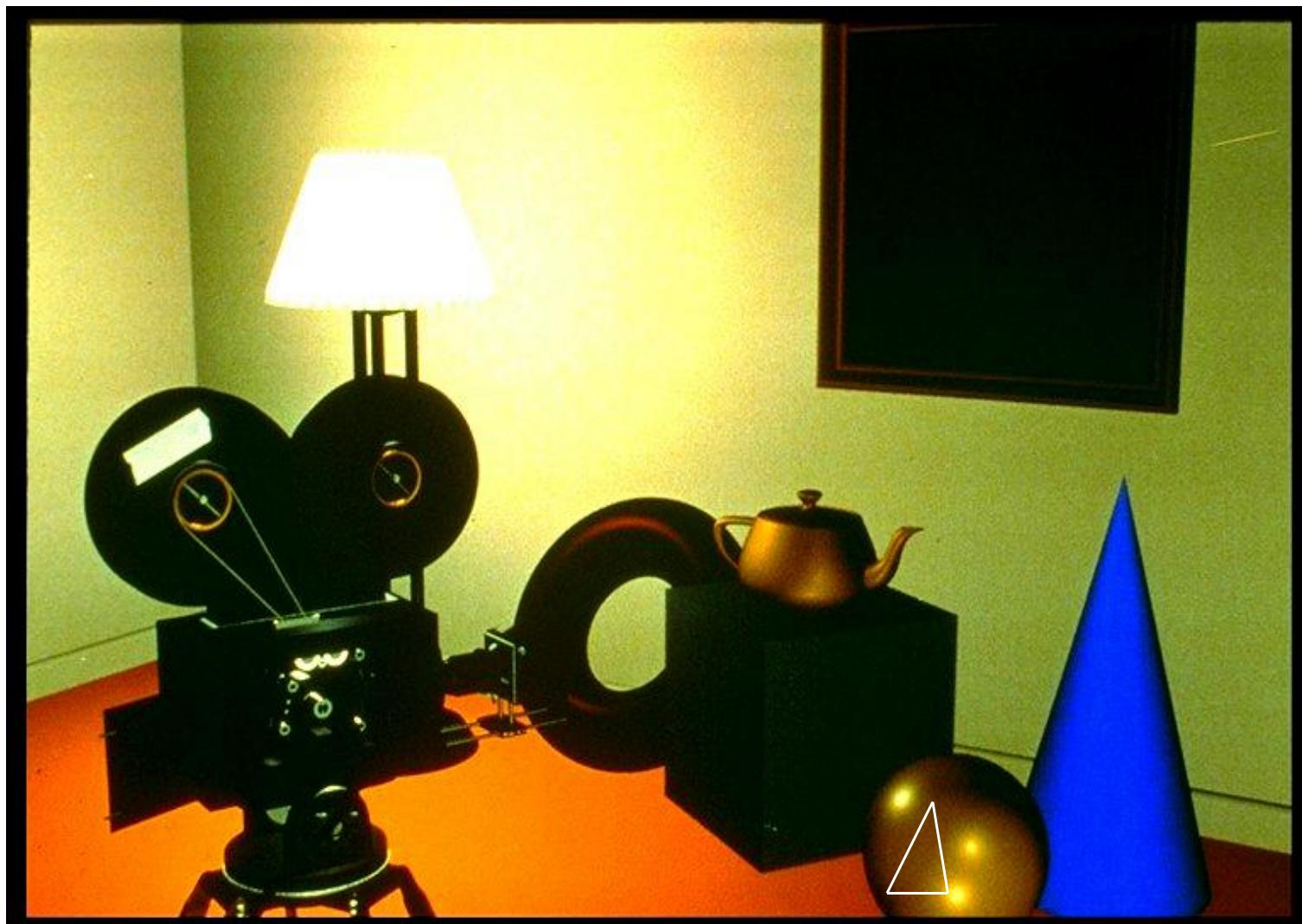
Guess specular reflection ?

Phong Shading



$$I = k_d I_d \ l \bullet n + k_s I_s (v \bullet r)^\alpha + k_a I_a$$

Complex Lighting and Shading



Lighting



PLATE 17: Light sources in a scene. (*Courtesy of Unigine.*)

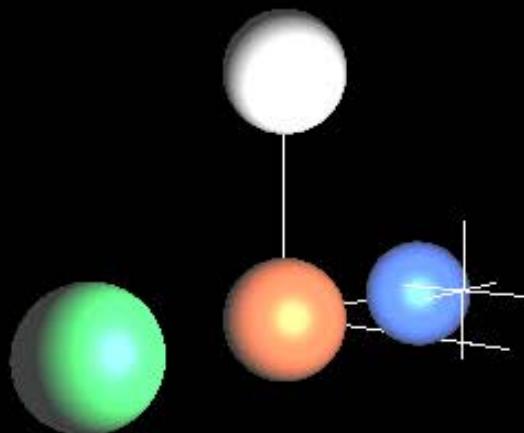
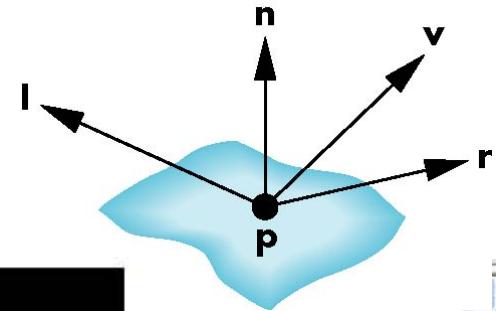
Flat vs Smooth Shading



Guess **FLAT** / **SMOOTH** ?

Lighting Applet

$$I = k_d I_d \mathbf{L} \bullet \mathbf{n} + k_s I_s (\mathbf{V} \bullet \mathbf{R})^\alpha + k_a I_a$$



```
I = k_a * I_a + k_d * I_l * (N . L) + k_s * I_l * (V . R)^n_s
```

Enable ambient

Enable diffuse

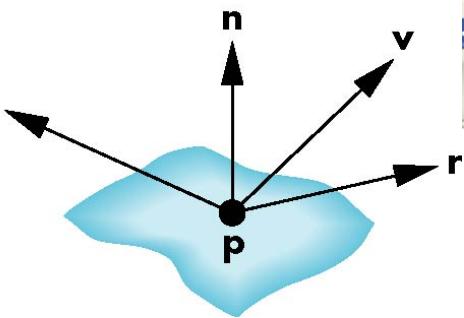
Enable specular

k_a	0.5	k_d	0.7	k_s	0.7
I_a (R,G & B)	0.5	I_l (R,G & B)	2.0	n_s	5

Light attenuation ($1/d^2$)

four_spheres.dat

$$I = k_d I_d \mathbf{l} \bullet \mathbf{n} + k_s I_s (\mathbf{v} \bullet \mathbf{r})^\alpha + k_a I_a$$



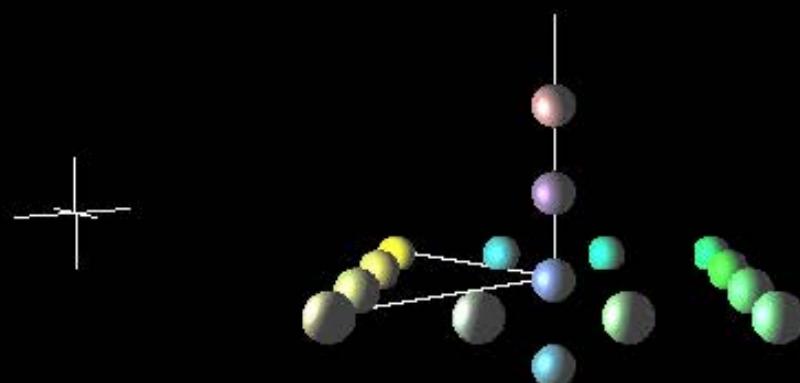
- Specular highlights are done using Phong's shading model.
- The spheres are raytraced individually, going from the furthest to the closest sphere. This means you won't see any shadows.
- If you run this applet on anything less than a 24-bit colour display, the resulting pictures are not going to be that pretty.
- When running this applet under older versions (< 4.x) of Netscape, the function "copy image to window" doesn't work properly: whenever it is redrawn, it shows the current picture. When run using the Appletviewer, it should work fine though.

link [here](#) for a list of all applets.

those of you without the book, an explanation of the lighting model parameters:

k_a	material's ambient coefficient
I_a	ambient light (R, G and B)
k_d	material's diffuse coefficient
I_l	light (at crosshair) intensity (R, G and B)
N	surface normal at point of intersection
L	vector to light from point of intersection
k_s	material's specular coefficient
V	vector to viewer from point of intersection
R	vector L reflected at point of intersection
n_s	material's specular reflection parameter

Lighting Applet



$$I = k_a * I_a + k_d * I_l * (N \cdot L) + k_s * I_l * (V \cdot R)^n_s$$

 Enable ambient Enable diffuse Enable speculark_a

0.5

k_d

0.7

k_s

0.7

I_a (R,G & B)

0.5

I_l (R,G & B)

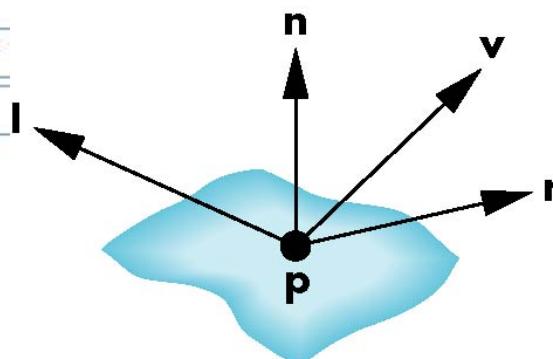
2.0

n_s

5

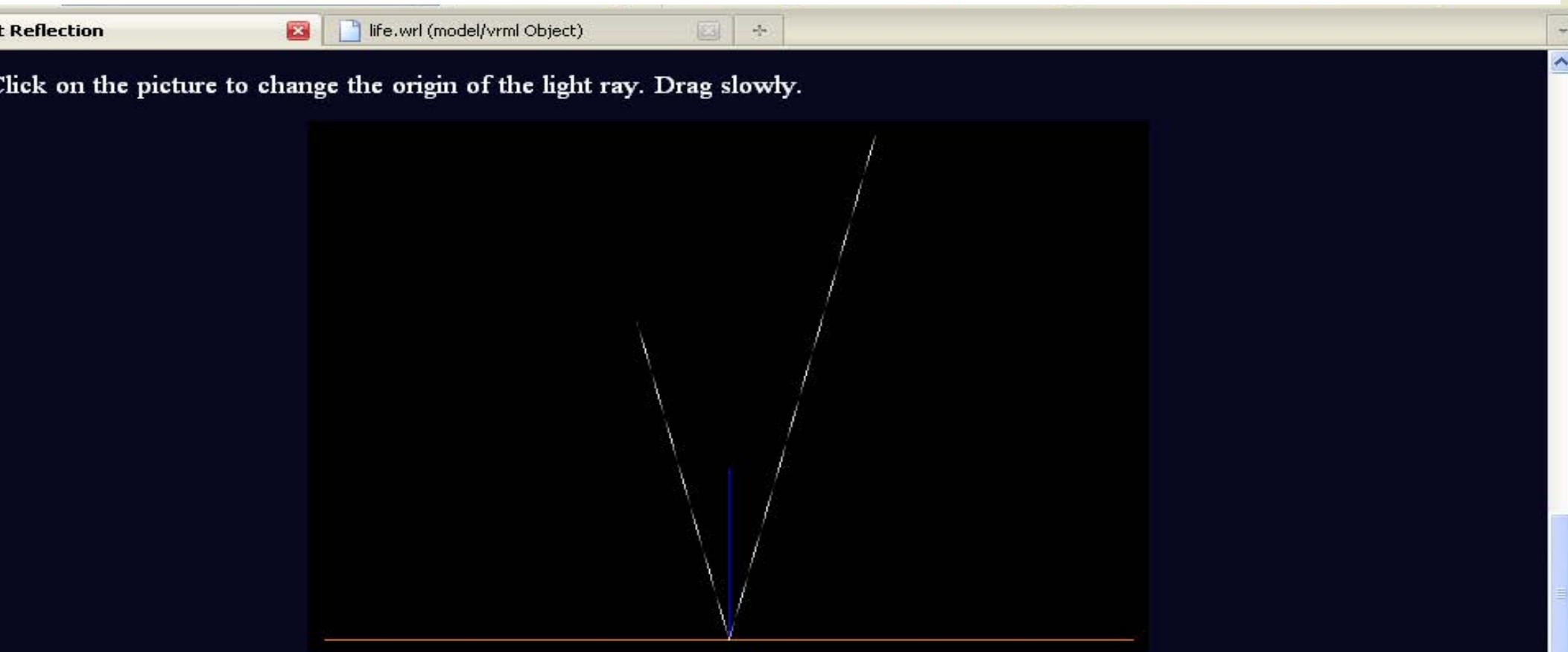
 Light attenuation (1/d^2)

little_spheres.dat



$$I = k_d I_d \mathbf{L} \bullet \mathbf{n} + k_s I_s (\mathbf{V} \bullet \mathbf{r})^\alpha + k_a I_a$$

VRML – Light Reflection



Click on the picture to change the origin of the light ray. Drag slowly.

In the above diagram the reflecting surface is drawn in red, the normal is drawn in blue.

<http://id.mind.net/~zona/mstm/physics/light/rayOptics/reflection/reflection1.html>

Shading I

http://www.3dengines.de/feat_phong.html

Objectives

Learn to shade objects so their images appear three-dimensional

Introduce the types of light-material interactions

Build a simple reflection model---the Phong model - can be used with real time graphics hardware

Objectives

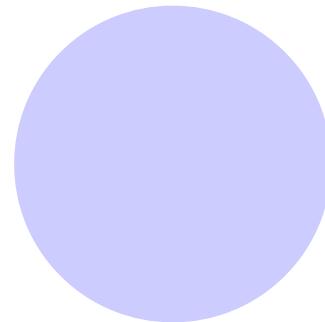
Learn to shade objects so their images appear three-dimensional

Introduce the types of light-material interactions

Build a simple reflection model---the Phong model---that can be used with real time graphics hardware

Why we need shading

- Suppose we build a **model of a sphere** using many polygons and color it with `glColor`. We get something like



- **But we want**



Shading

- Why does the **image** of a **real sphere** look like



- **Light-material interactions** cause each **point P** to have a different **color or shade**

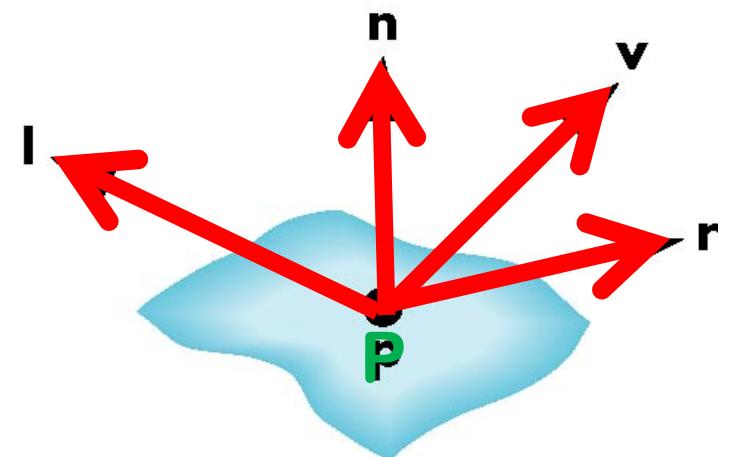
- Need to consider **vectors**

Light source(s) \mathbf{I}

Material properties \mathbf{r}

Location of viewer \mathbf{v}

Surface orientation $\mathbf{P} \rightarrow \mathbf{n}$



Scattering

- Light strikes **A**

Some scattered

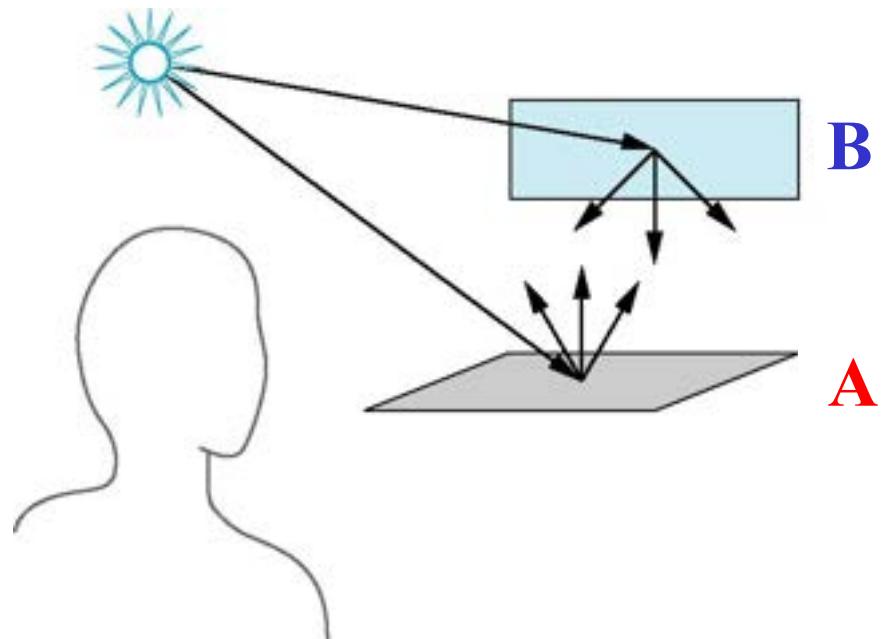
Some absorbed

- Some of scattered light strikes **B**

Some scattered

Some absorbed

- Some of this scattered light strikes **A**
- and so on



Rendering Equation

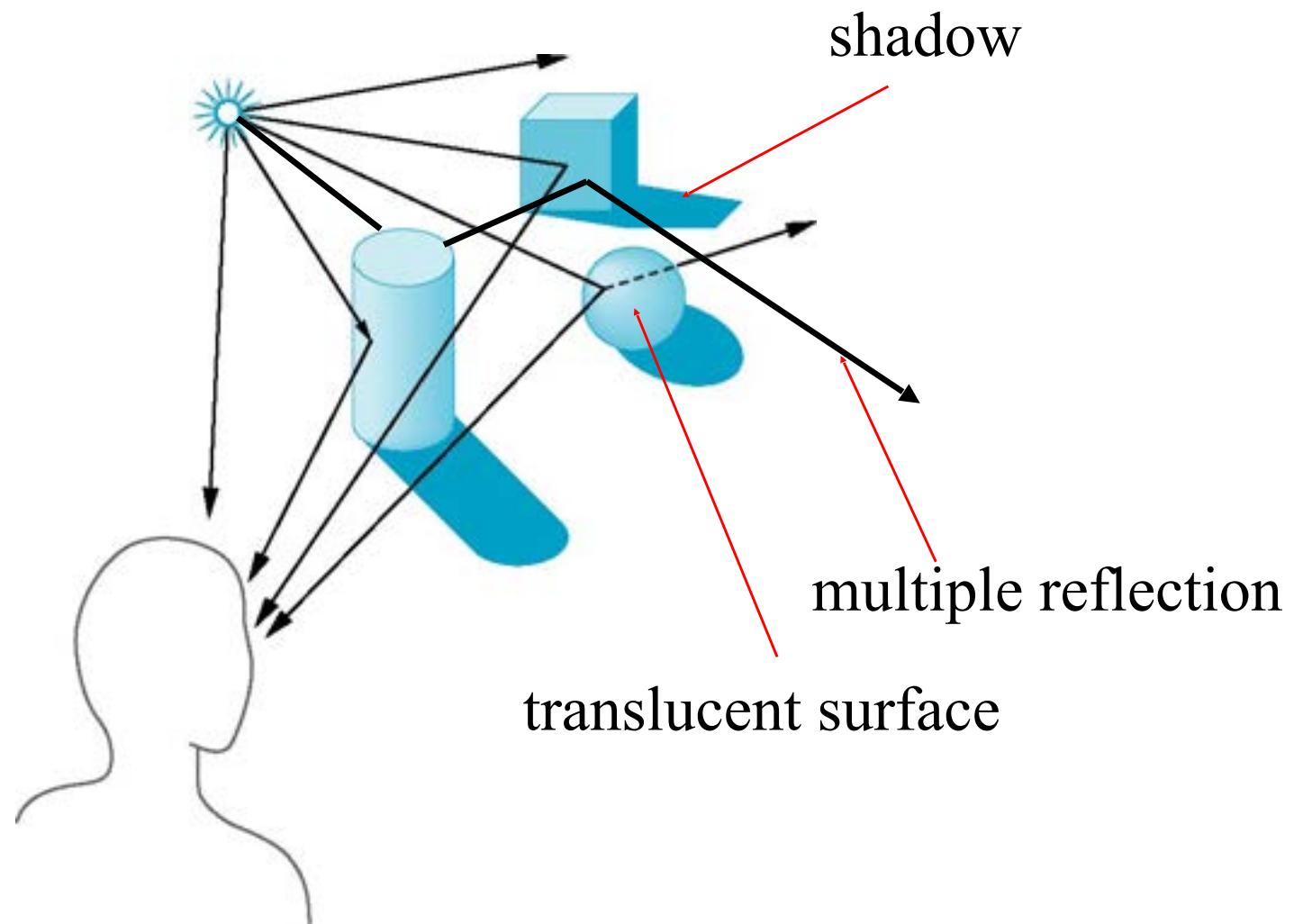
The **infinite** scattering and absorption of light can be described by the ***rendering equation***
(Bidirectional Reflection Distribution Function (BRDF))

Cannot be solved in general

Ray tracing is a special case for perfectly reflecting surfaces

Rendering equation is **global** and includes
Shadows
Multiple scattering from object to object

Global Effects



Local vs Global Rendering

Correct shading requires a global calculation involving all objects and light sources

Incompatible with pipeline model which shades each polygon independently (**local rendering**)

However, in computer graphics, especially real time graphics, we are happy if things “look right”

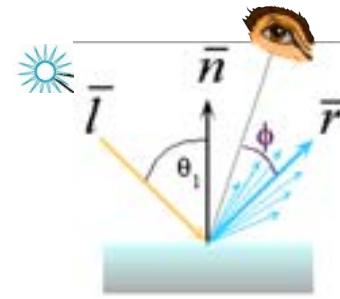
Exist many techniques for **approximating global effects**

Objectives

Learn to shade objects so their images appear three-dimensional

Introduce the **types of** light-material interactions

Build a simple reflection model---the Phong model---that can be used with real time graphics hardware



Light-Material Interaction

Light that strikes an object is partially absorbed and partially scattered (reflected)

The amount reflected determines the color and brightness of the object

A surface appears red under white light because the red component of the light is reflected and the rest is absorbed

The reflected light is scattered (diffuse) in a manner that depends on the smoothness and orientation of the surface (n)

Refraction of Light Applet

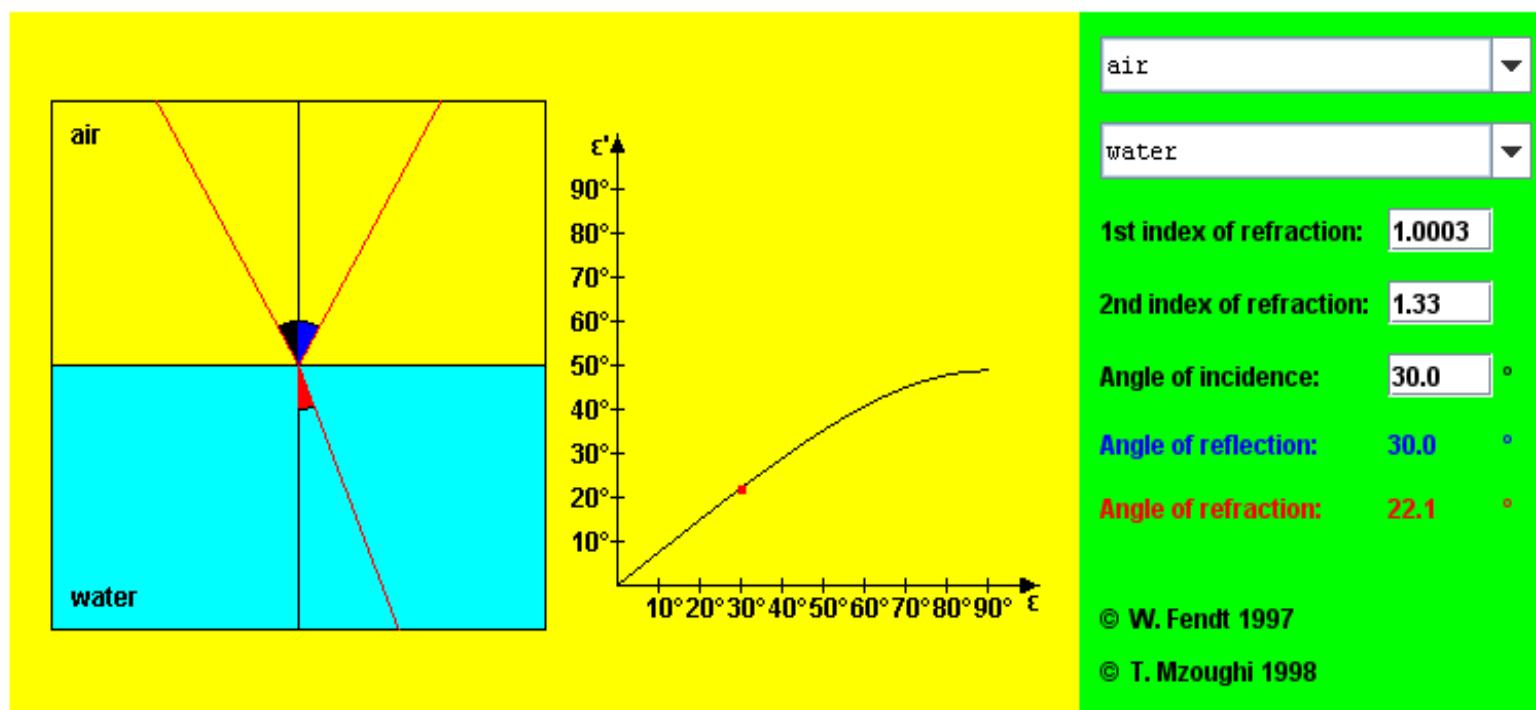
Refraction of Light

A ray of light coming from the top left strikes the boundary surface of two media. (It is possible to choose the substances in both lists.) The medium which has the bigger index of refraction is painted blue, the other yellow. You can vary the incident ray with pressed mouse button. The applet will show the reflected and the refracted ray and calculate the corresponding angles:

Angle of incidence (black)

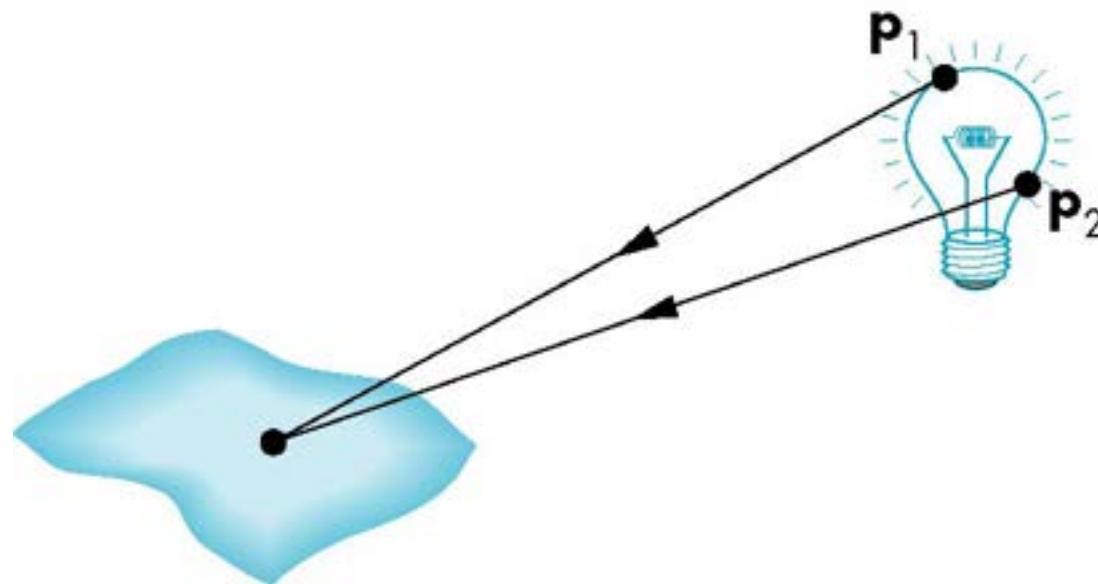
Angle of reflection (blue)

Angle of refraction (red)



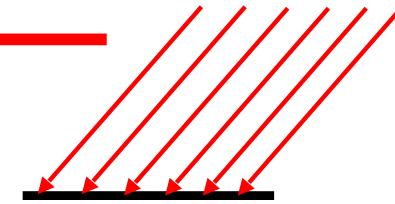
Light Sources

General light sources are difficult to work with because we must integrate light coming from all points on the source

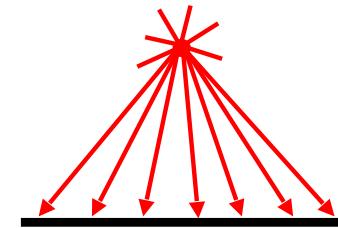


Light Sources

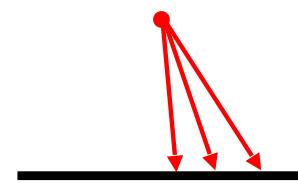
- **directional/parallel** lights
 - **point** at infinity: $(x,y,z,0)^T$



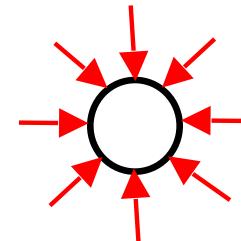
- **point** lights
 - finite **position**: $(x,y,z,1)^T$



- **spotlights**
 - **position**, direction, angle



- **ambient** lights



Simple Light Sources

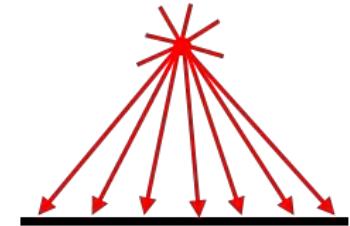
Point source

Model with **position** and **color**

point lights

- finite **position**: $(x,y,z,1)^T$

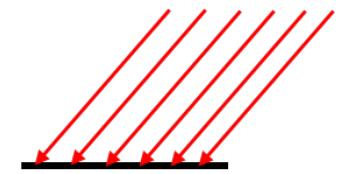
Distant source = **infinite distance away (parallel)**



Spotlight

point at infinity: $(x,y,z,0)^T$

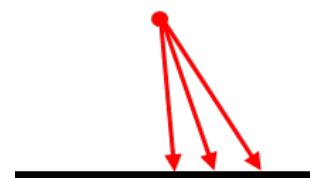
Restrict light from **ideal point source**



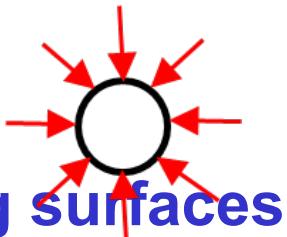
Ambient light

position, direction, angle

Same amount of light everywhere in scene



Can model contribution of many sources and reflecting surfaces



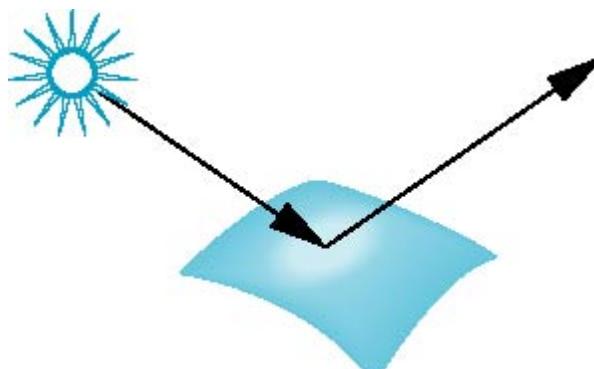
Surface Types

$$I = k_d I_d \mathbf{I} \bullet \mathbf{n} + k_s I_s (\mathbf{v} \bullet \mathbf{r})^\alpha + k_a I_a$$

The **smoother a surface**, the **more reflected light is concentrated in the direction a perfect mirror would reflect the light - specular**

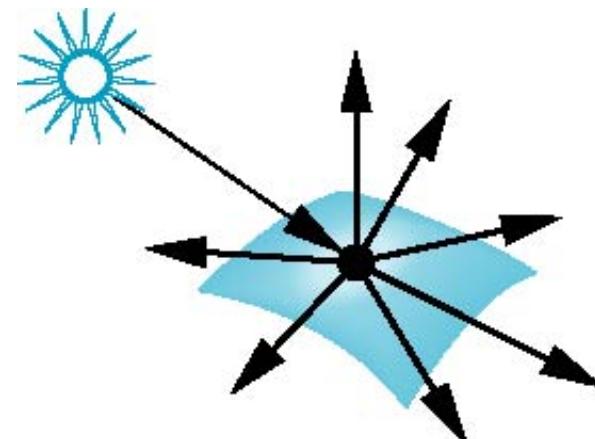
A **very rough surface** scatters light in all directions-**diffuse**

Specular reflections



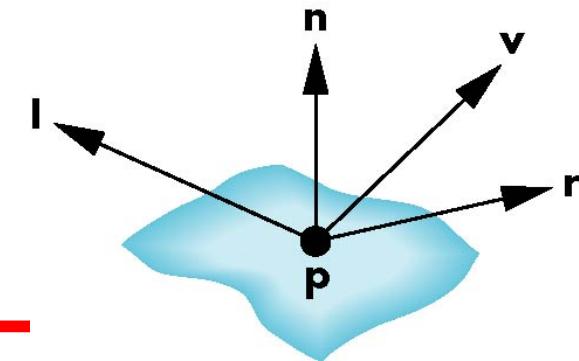
smooth surface

Diffuse reflections



rough surface

Objectives



Learn to shade objects so their images appear three-dimensional

Introduce the **types** of light-material interactions

Build a **simple reflection model--the Phong model**-- that can be used with real time graphics hardware

$$I = k_d I_d \mathbf{I} \bullet \mathbf{n} + k_s I_s (\mathbf{v} \bullet \mathbf{r})^\alpha + k_a I_a$$

Lighting vs. Shading

lighting

simulating the interaction of **light** with **surface**

shading

deciding pixel color

continuum of realism: **when do we do lighting calculation?**

Shading Models

- flat shading

compute **Phong lighting** once for entire polygon

- Gouraud shading

compute **Phong lighting** at the **vertices** and **interpolate** lighting values across polygon

- Phong shading

compute **averaged vertex** normals

interpolate normals across polygon and perform **Phong lighting** across polygon

Phong Model

$$I = k_d I_d \mathbf{l} \bullet \mathbf{n} + k_s I_s (\mathbf{v} \bullet \mathbf{r})^\alpha + k_a I_a$$

- A simple model that can be computed rapidly
- Has three components

Ambient

Diffuse

Specular

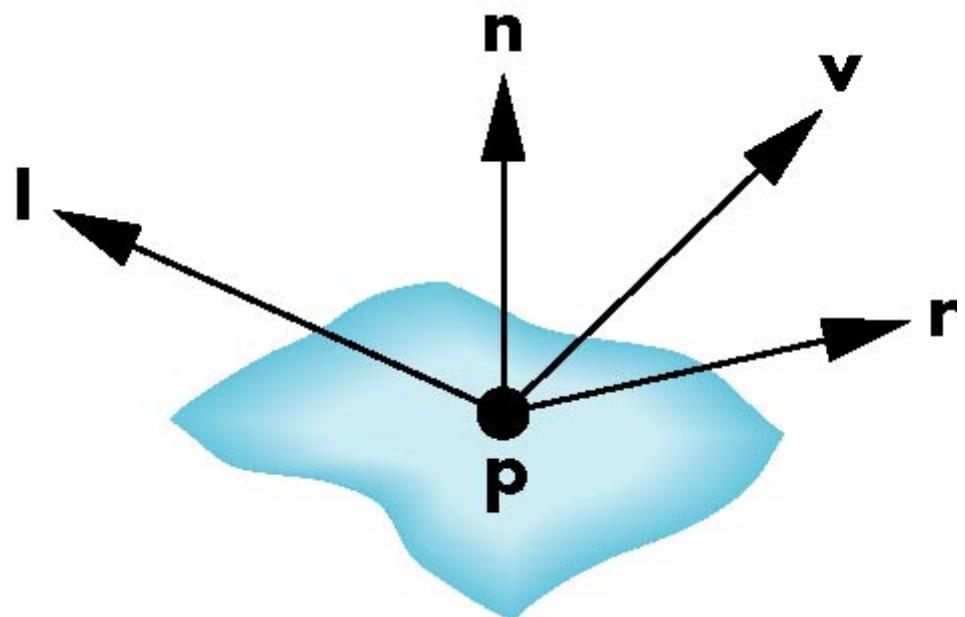
- Uses four vectors

To source \mathbf{l}

To viewer \mathbf{v}

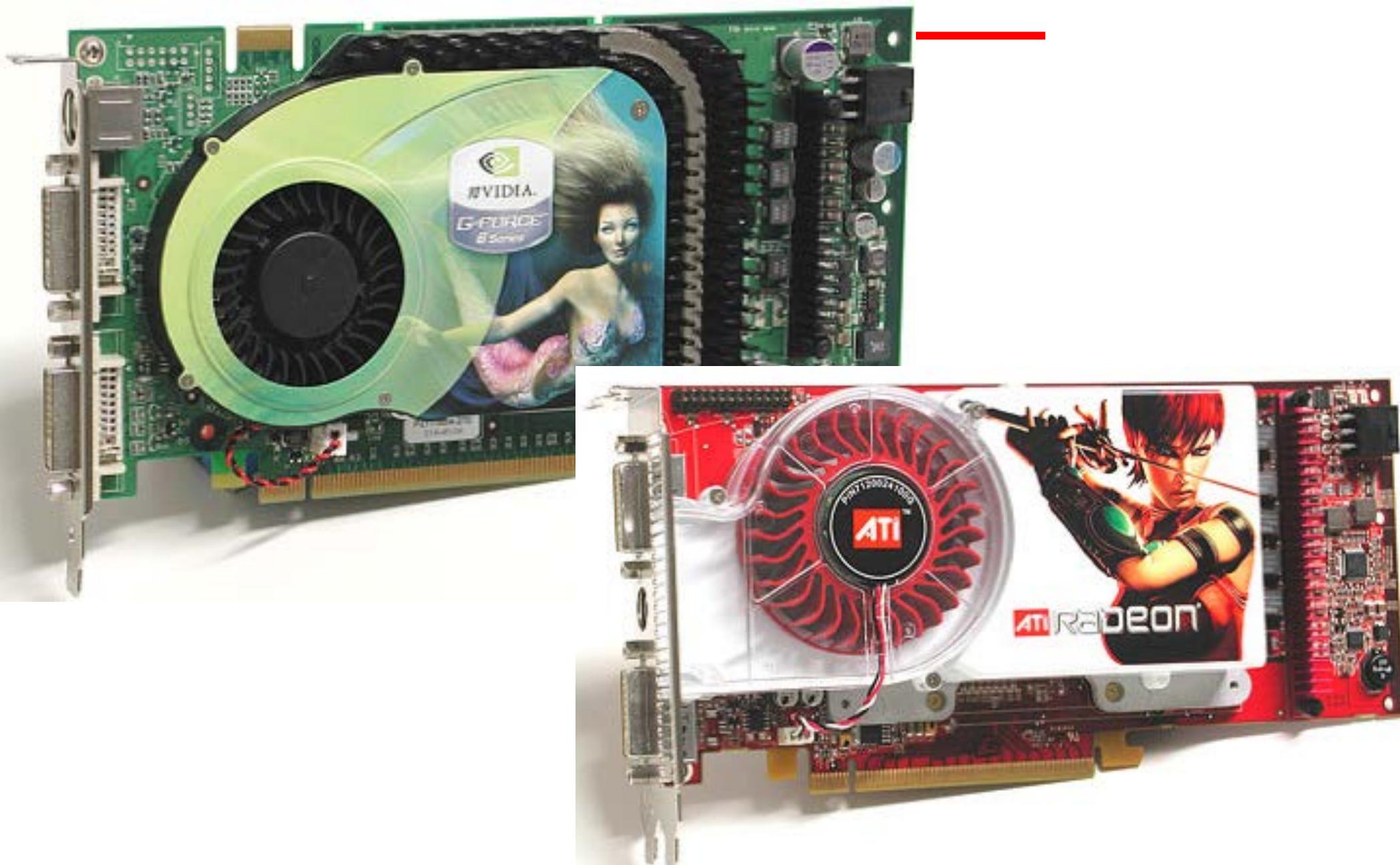
Normal \mathbf{n}

Perfect reflector \mathbf{r}



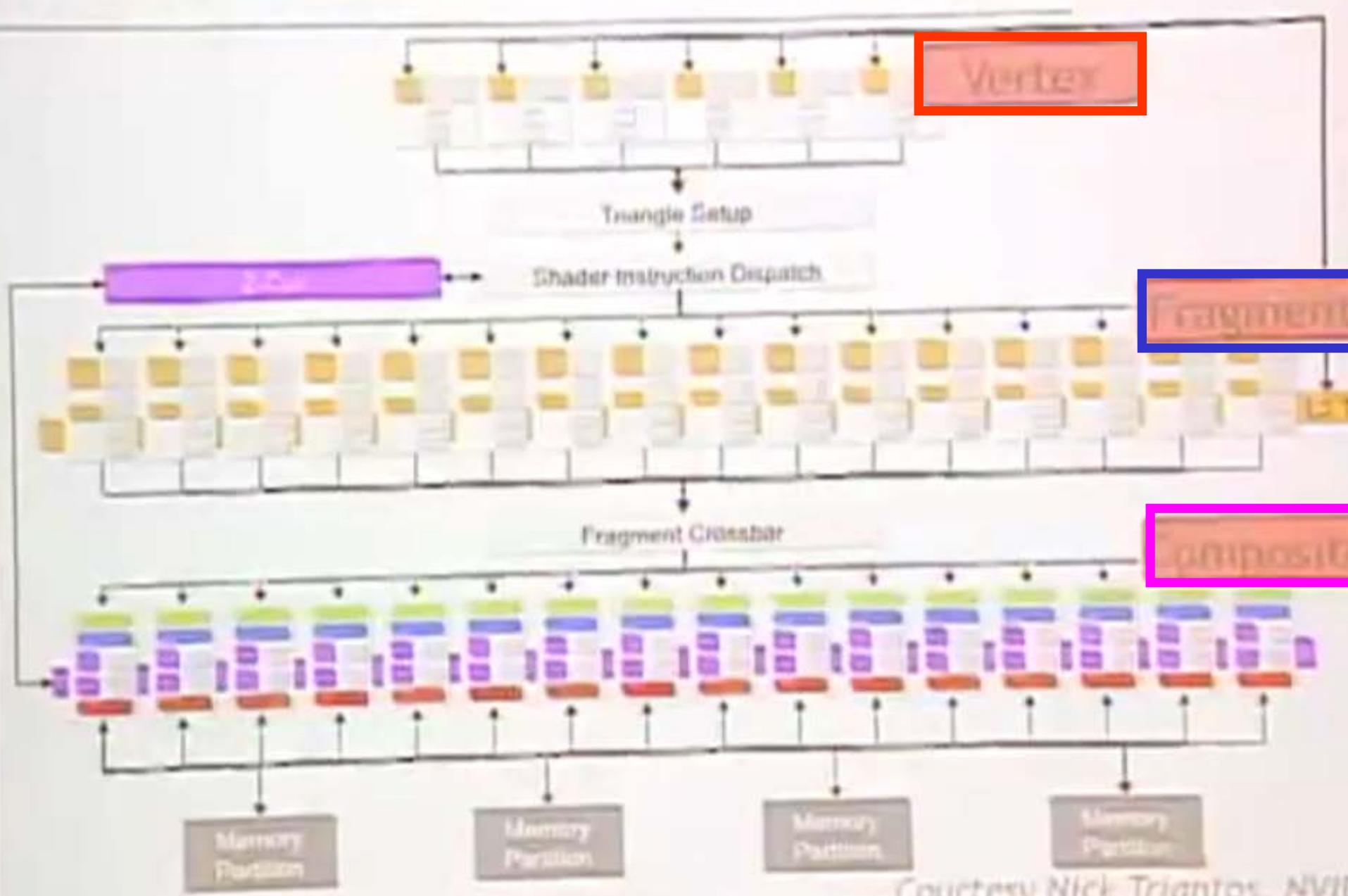
NVIDIA & ATI GPUs

Graphics in REAL-TIME



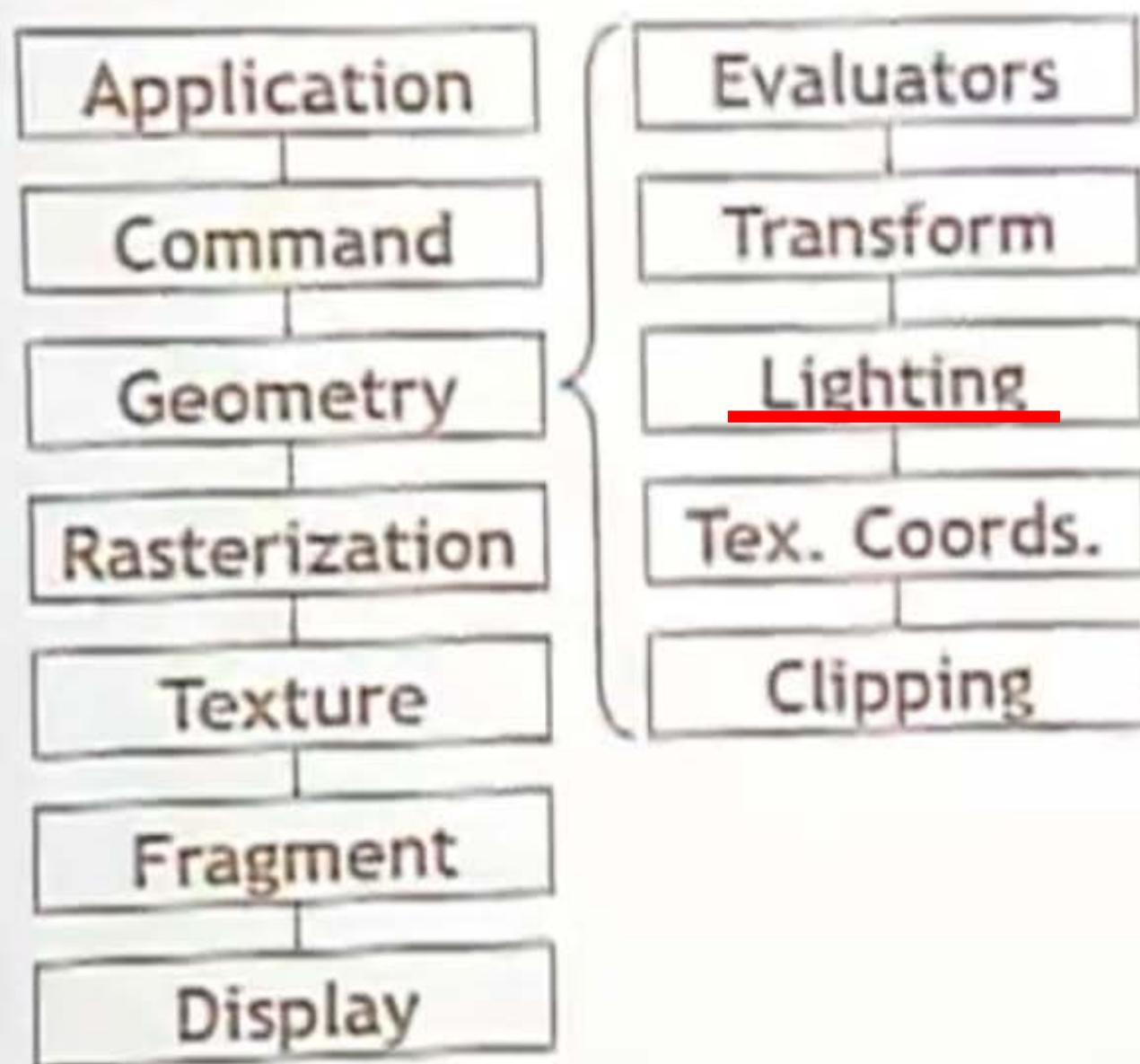
NVIDIA 6800 GPU - PROGRAMMABLE

NVIDIA GeForce 6800 3D Pipeline

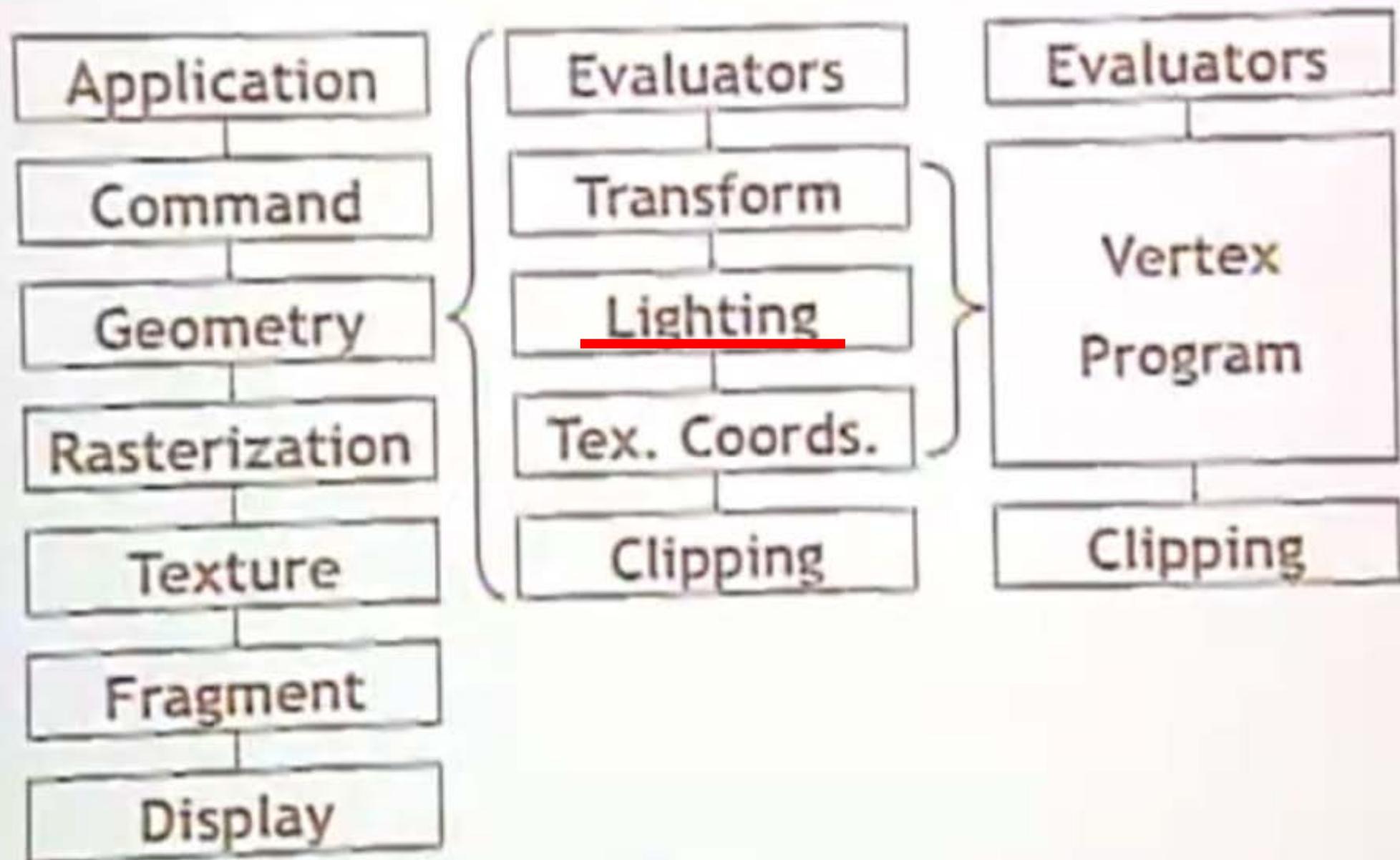


Courtesy Nick Triantos, NVIDIA

Vertex Programs in the Graphics Pipeline



Vertex Programs in the Graphics Pipeline



Hardest Thing To Get Used To

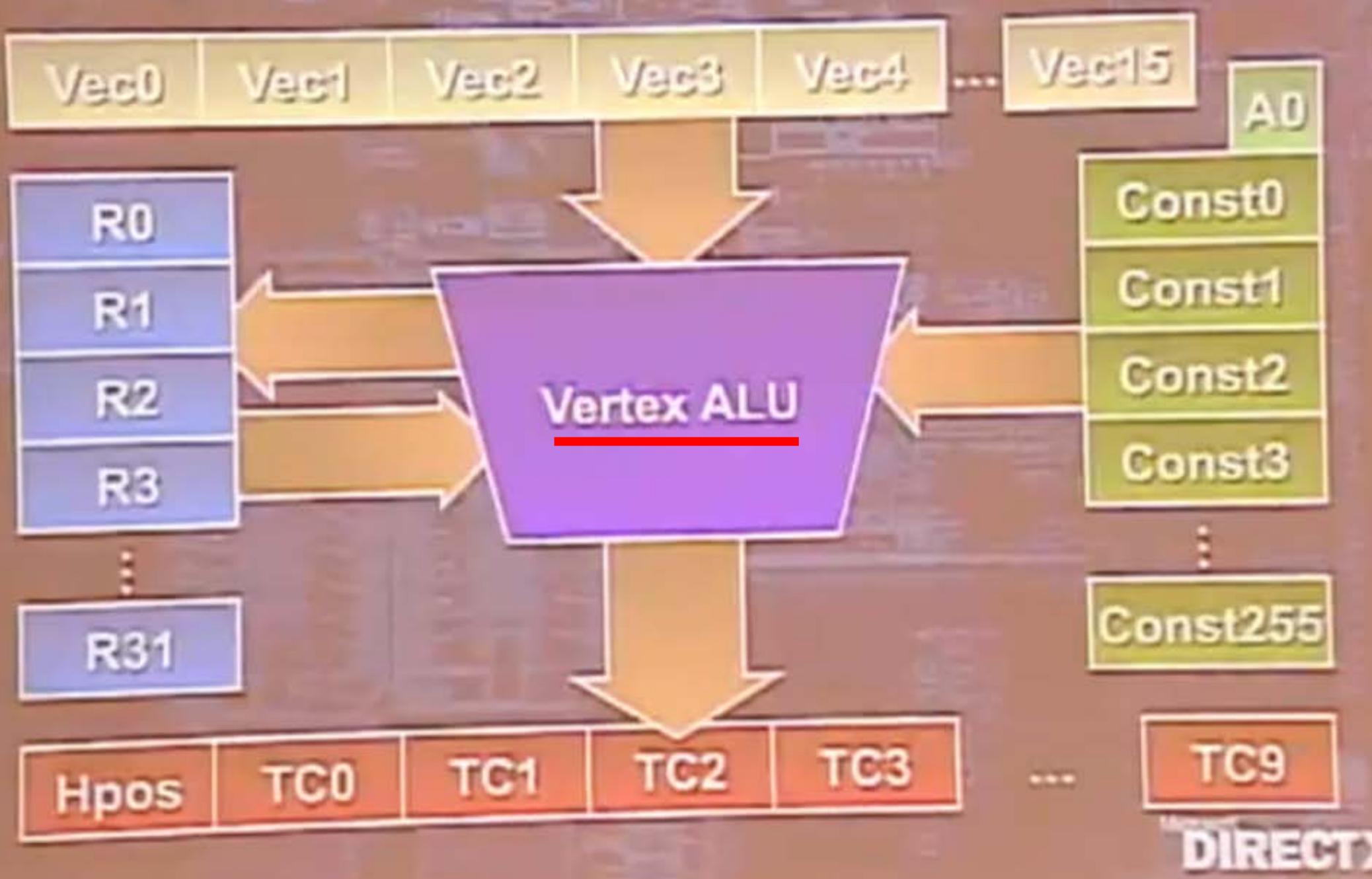
When you write a vertex or fragment program,

You Write One Program.

It Runs On Every Vertex/Fragment.

Programming model is “SPMD” (Single Program, Multiple Data)

Vertex Shader Architecture



Vertex Input Registers (16)

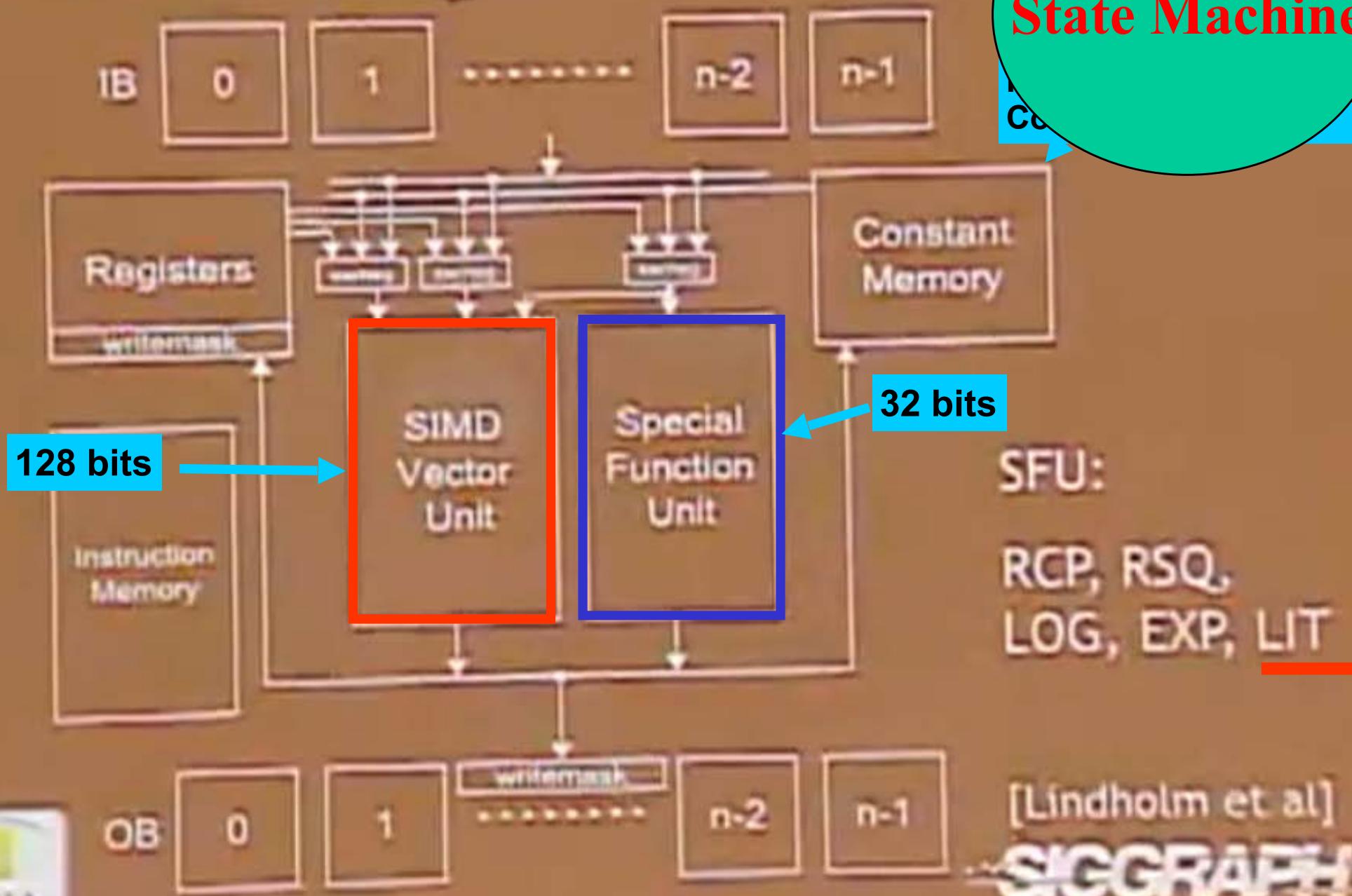
Attribute Register	Conventional per-vertex Parameter	Conventional Command	Conventional Mapping
0	vertex position	glVertex	x,y,z,w
1	vertex weights	glVertexWeightEXT	w,0,0,1
2	normal	glNormal	x,y,z,1
3	Primary color	glColor	r,g,b,a
4	secondary color	glSecondaryColorEXT	
5	r,g,b,fog coordinate	glFogCoordEXT	f,c,0,0,1
6			
7			
8	Texture coord 0	glMultiTexCoord	s,t,r,q
9	Texture coord 1	glMultiTexCoord	s,t,r,q
10	Texture coord 2	glMultiTexCoord	s,t,r,q
11	Texture coord 3	glMultiTexCoord	s,t,r,q
12	Texture coord 4	glMultiTexCoord	s,t,r,q
13	Texture coord 5	glMultiTexCoord	s,t,r,q
14	Texture coord 6	glMultiTexCoord	s,t,r,q
15	Texture coord 7	glMultiTexCoord	s,t,r,q

Vertex Output Registers

(16)

Register Name	Description	Component Interpretation
o[HPOS]	Homogeneous clip space position (x,y,z,w)	
o[COL0]	Primary color (front-facing)	(r,g,b,a)
o[COL1]	Secondary color (front-facing)	(r,g,b,a)
o[BFC0]	Back-facing primary color	(r,g,b,a)
o[BFC1]	Back-facing secondary color	(r,g,b,a)
o[FOGC]	Fog coordinate	(f,*,*,*)
o[PSIZ]	Point size	(p,*,*,*)
o[TEX0]	Texture coordinate set 0	(s,t,r,q)
o[TEX1]	Texture coordinate set 1	(s,t,r,q)
o[TEX2]	Texture coordinate set 2	(s,t,r,q)
o[TEX3]	Texture coordinate set 3	(s,t,r,q)
o[TEX4]	Texture coordinate set 4	(s,t,r,q)
o[TEX5]	Texture coordinate set 5	(s,t,r,q)
o[TEX6]	Texture coordinate set 6	(s,t,r,q)
o[TEX7]	Texture coordinate set 7	(s,t,r,q)

HW Block Diagram



Lindholm
et al

State Machine

SFU:

RCP, RSQ,
LOG, EXP, LIT

[Lindholm et al]

SIGGRAPH
2001

Basic Instructions (VS1.0)

17 instructions - all 4x32 FP

MOV	MIN	DP3
MUL	MAX	DP4
ADD	SLT	DST
MAD	SGE	<u>LIT</u>
RCP	ARL	
RSQ		
EXP		
LOG		

Instruction Set

- NO SUB!
- MOV copy from register to register
- MAD Multiply and Add
- Reciprocal, Reciprocal Square Root (Normals)
- DP3 Dot Product
- DST distance (Pythagorean distance between two vectors)
- MIN, MAX
- ARL addressing instruction
- LIT CISC to the n^{th} power; entire blend lighting model that is part of OPENGL. There are 5 components, specular, diffuse, ambient components and a lot of dot products. The most special purpose instruction that you heard about it.

Program Examples

Vector Cross Product

```

# | i      j      k      | into R2.
# | R0.x  R0.y  R0.z |
## | R1.x R1.y R1.z |
MUL R2, R0.zxyw, R1.yzkw;           // swizzle
MAD R2, R0.yzkw, R1.zxyw, -R2; // swizzle, negation

```

Vector Normalize

Simple Graphics Pipeline

```

# c[0-3] = Mat;
# c[32] = L;
# c[35].x = Md * Ld;
# c[36] = Ms;

DP4 o[HPOS].x, c[0], v[OPOS];      # Transform position.
DP4 o[HPOS].y, c[1], v[OPOS];
DP4 o[HPOS].z, c[2], v[OPOS];
DP4 o[HPOS].w, c[3], v[OPOS];

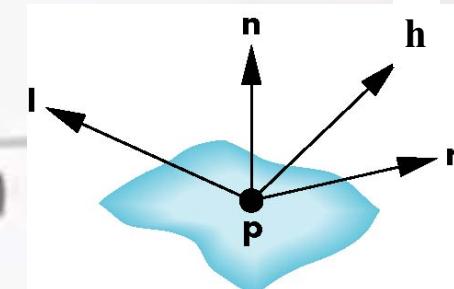
DP3 R0.x, c[4], v[NRML];          # Transform normal.
DP3 R0.y, c[5], v[NRML];
DP3 R0.z, c[6], v[NRML];

DP3 R1.x, c[32], R0;              # R1.x = L DOT N
DP3 R1.y, c[33], R0;              # R1.y = H DOT N
MOV R1.w, c[38].x;                # R1.w = s
LIT R2, R1;                      # Compute lighting
MAD R3, c[35].x, R2.y, c[35].y;  # diffuse + ambient
MAD o[COL0].xyz, c[36], R2.z, R3; # + specular
END

```

Vertex IN Vertex OUT

$$I = k_d I_d \mathbf{L} \bullet \mathbf{n} + k_s I_s (\mathbf{h} \bullet \mathbf{r})^\alpha + k_a I_a$$



Ideal Reflector r

- Normal vector \mathbf{n} is determined by local orientation
- angle of incidence = angle of reflection
- The three vectors must be coplanar

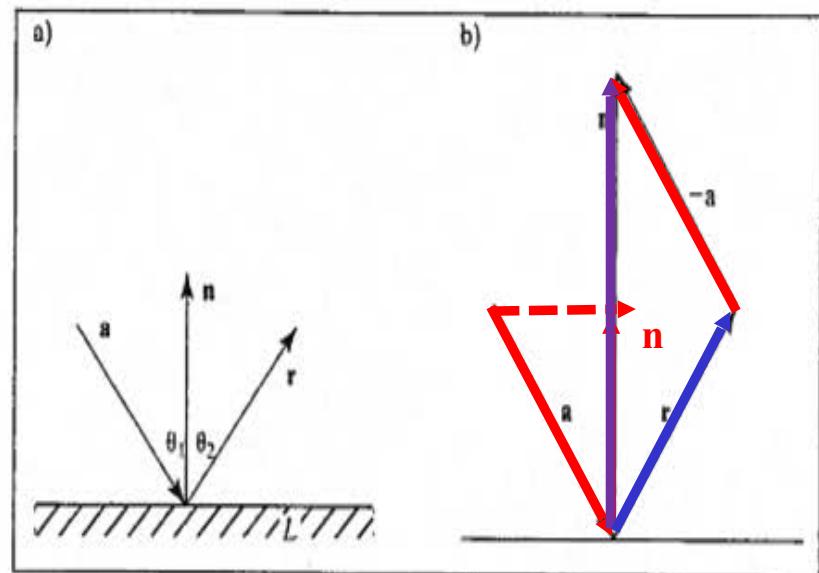


FIGURE 4.13 Reflection of a ray from a surface.

\mathbf{n} is normalized; $|\mathbf{n}| = 1$

$(\mathbf{a} \bullet \hat{\mathbf{n}})$ scalar
 $\hat{\mathbf{n}}$

$(\mathbf{a} \bullet \hat{\mathbf{n}}) \hat{\mathbf{n}}$ vector

Parallelogram rule

$$\mathbf{r} - \mathbf{a} = 2 (\mathbf{-a} \bullet \hat{\mathbf{n}}) \hat{\mathbf{n}}$$

$$\mathbf{r} = \mathbf{a} - 2(\mathbf{a} \bullet \hat{\mathbf{n}}) \hat{\mathbf{n}}$$

Ideal Reflector r

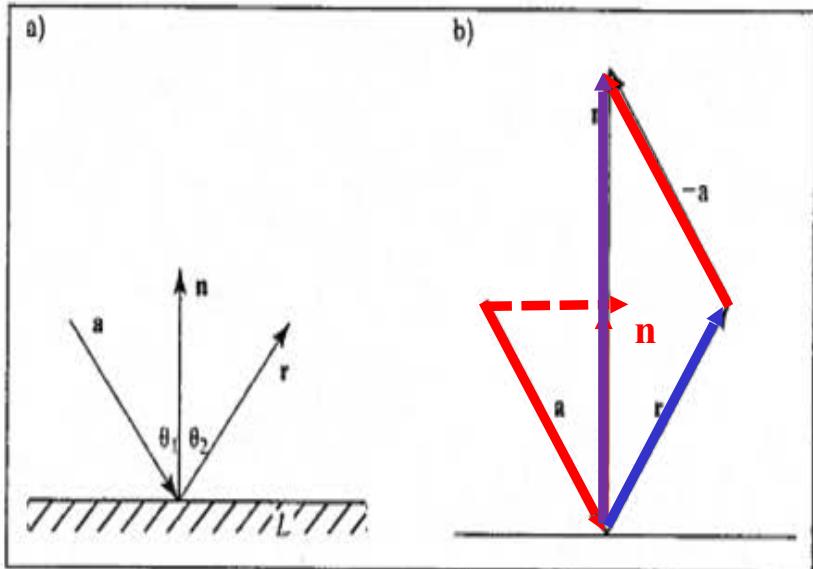


FIGURE 4.13 Reflection of a ray
from a surface.

$$\mathbf{r} = \mathbf{a} - 2(\mathbf{a} \bullet \hat{\mathbf{n}}) \hat{\mathbf{n}}$$

Let $\mathbf{a} = (4, -2)$ and $\mathbf{n} = (0, 3)$. What is \mathbf{r} ?

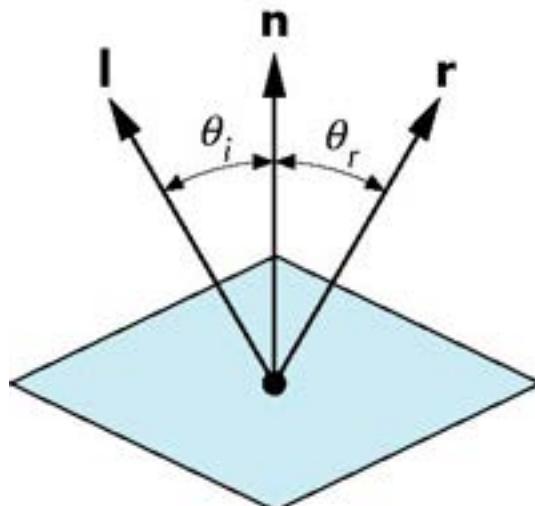
Normalize \mathbf{n} $\hat{\mathbf{n}} = (0, 1)$

$$\mathbf{r} = (4, -2) - 2((4, -2) \bullet (0, 1))(0, 1) = (4, -2) - 2(-2)(0, 1) = (4, -2) - (0, -4) = (4, 2)$$

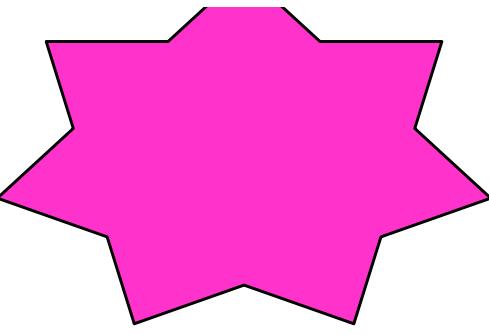
Ideal Reflector r

- Normal vector \mathbf{n} is determined by local orientation
- angle of incidence = angle of reflection
- The three vectors must be coplanar

$$\mathbf{r} = 2 (\mathbf{l} \bullet \mathbf{n}) \mathbf{n} - \mathbf{l}$$



CLASS PARTICIPATION 1!
(Next Slide)



Name: _____

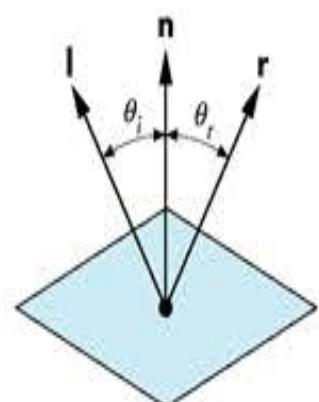
Total score:

Class PARTICIPATION on Lecture 6.doc ANSWER SHEET

(Out of 100 points. Please record your own total score!)

(Attach as score.doc!)

1. (20 points) Draw and Calculate the reflection vector r when $\mathbf{l} = (-1, 1)$ and $\mathbf{n} = (0, 1)$



$$\mathbf{r} = 2(\mathbf{l} \bullet \mathbf{n})\mathbf{n} - \mathbf{l}$$

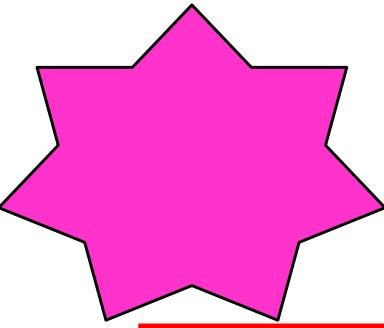
Self Graded - correctly



00:02:00
00:00:00

Start

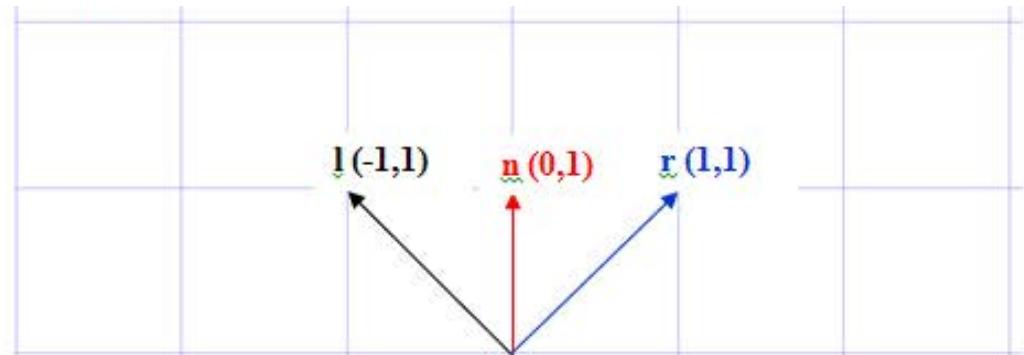
Cancel



Ideal Reflector r

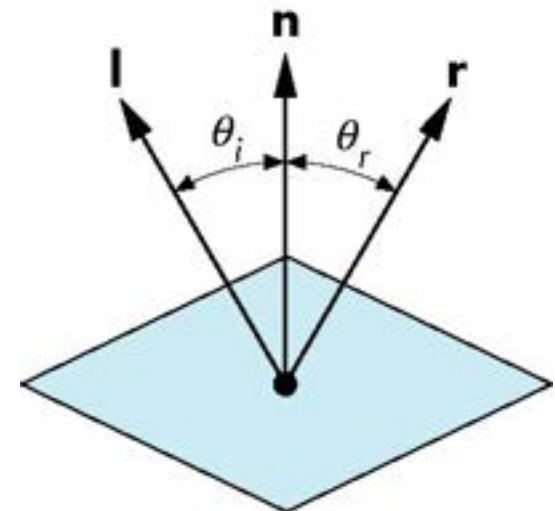
1. **Draw and Calculate** the reflection vector \mathbf{r} when $\mathbf{l} = (-1,1)$ and $\mathbf{n} = (0,1)$

$$\mathbf{r} = 2 (\mathbf{l} \bullet \mathbf{n}) \mathbf{n} - \mathbf{l}$$



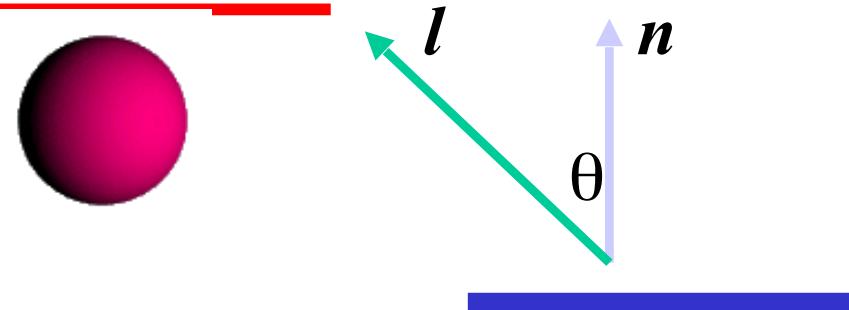
$$\mathbf{r} = 2 [(-1,1) \bullet (0,1)] (0,1) - (-1,1) = 2 \mathbf{l} (0,1) - (-1,1) = (0,2) - (-1,1) = (1, 1)$$

$$\mathbf{r} = (1, 1)$$

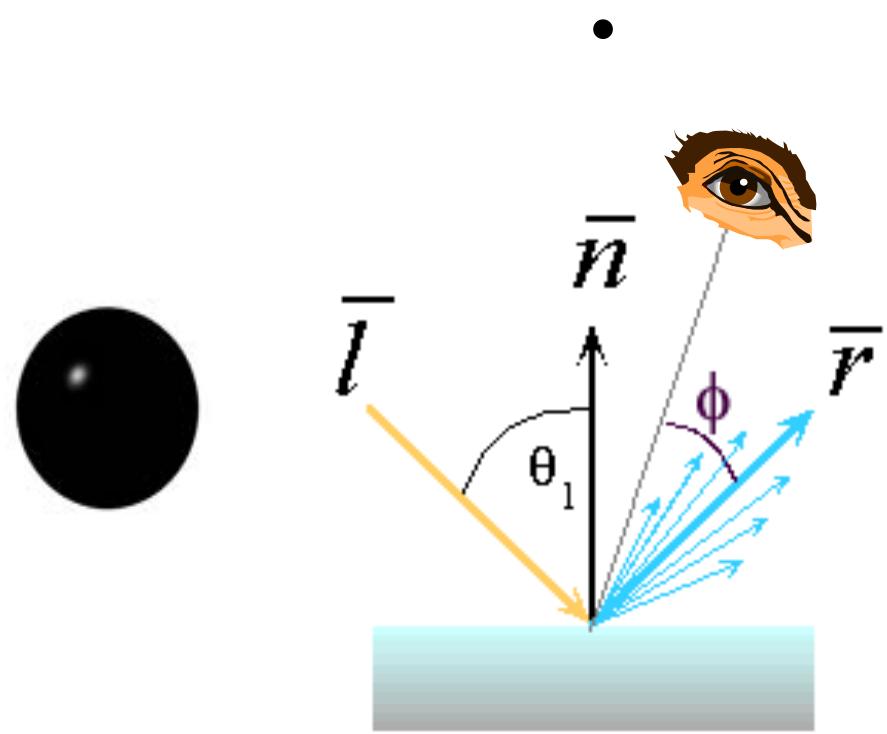


Reflection Equations

$$I_{\text{diffuse}} = k_d I_{\text{light}} (\mathbf{n} \cdot \mathbf{l})$$



$$\mathbf{r} = 2 (\mathbf{l} \bullet \mathbf{n}) \mathbf{n} - \mathbf{l}$$



Reflectance Properties

LAMBERTIAN MODEL

$$\phi(N, S, I') = K_d \cos\theta$$

Diffuse



Lambertian Surface

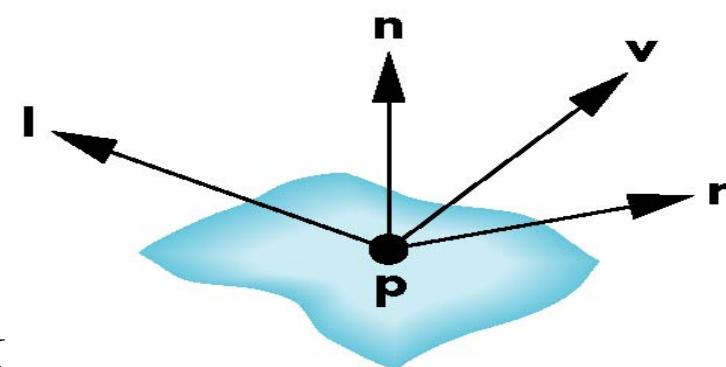
?????

- Perfectly **diffuse reflector**
- **Light scattered equally in all directions**
- Amount of light **reflected** is proportional to the vertical component of incoming light **I**

reflected light $\sim \cos \theta_i$

$\cos \theta_i = \mathbf{l} \bullet \mathbf{n}$ if vectors **normalized**

There are also **three coefficients**, k_r, k_b, k_g ...
of each **color component** is reflected



Ambient

$$I_p = k_a i_a + \sum_{m \in \text{lights}} (k_d (\hat{L}_m \cdot \hat{N}) i_{m,d} + k_s (\hat{R}_m \cdot \hat{V})^\alpha i_{m,s})$$



Diffusion

Specular

Diffuse

LAMBERTIAN MODEL

$$\phi(N, S, V) = K_d \cos \theta$$



Diffuse

Diffuse & Specular

PHONG MODEL

$$I_s = \phi(N, S, V) = \\ K_d \cos \theta + K_s \cos^m \alpha$$



Diffuse 0.3 & Specular 0.7



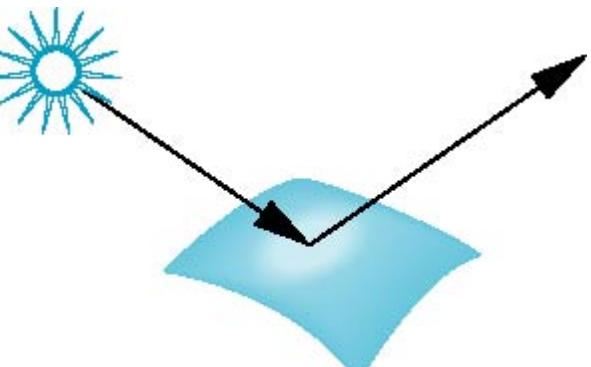
Diffuse 0.7 & Specular 0.3

$K_d=0.3, K_s=0.7, m=2; K_d=0.7, K_s=0.3, m=0.5$

Specular Surfaces

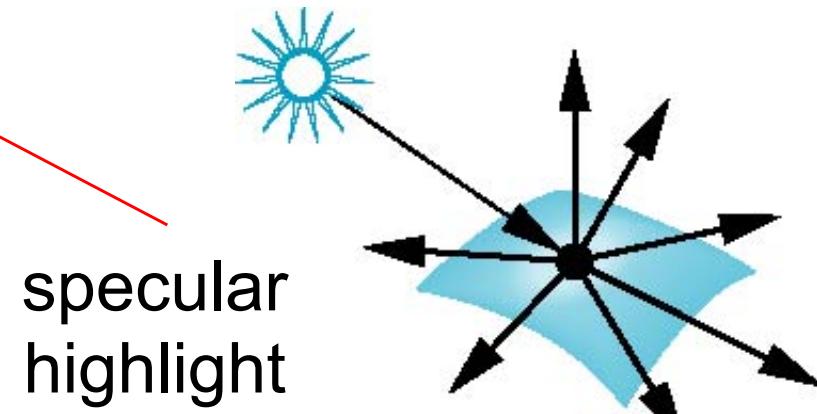
- Most surfaces are **neither ideal Diffusers nor perfectly Specular** (ideal reflectors)
- **Smooth surfaces** show specular highlights due to incoming light being **reflected** in directions concentrated close to the direction of a **perfect reflection**

Specular reflections



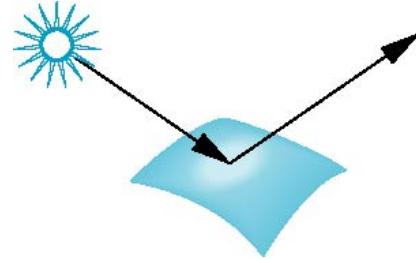
smooth surface

Diffuse reflections



rough surface⁶¹

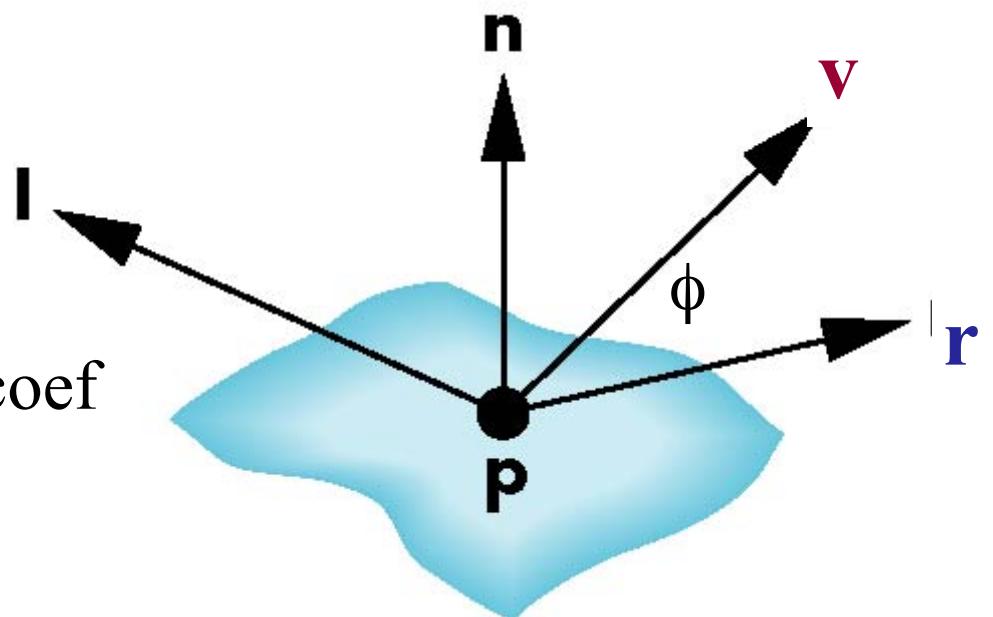
Modeling Specular Reflections



Phong proposed using a **term that dropped off** as the **angle between** the **viewer v** and the ideal reflection **r** increased

$$I_r \sim k_s I \cos^{\alpha} \phi$$

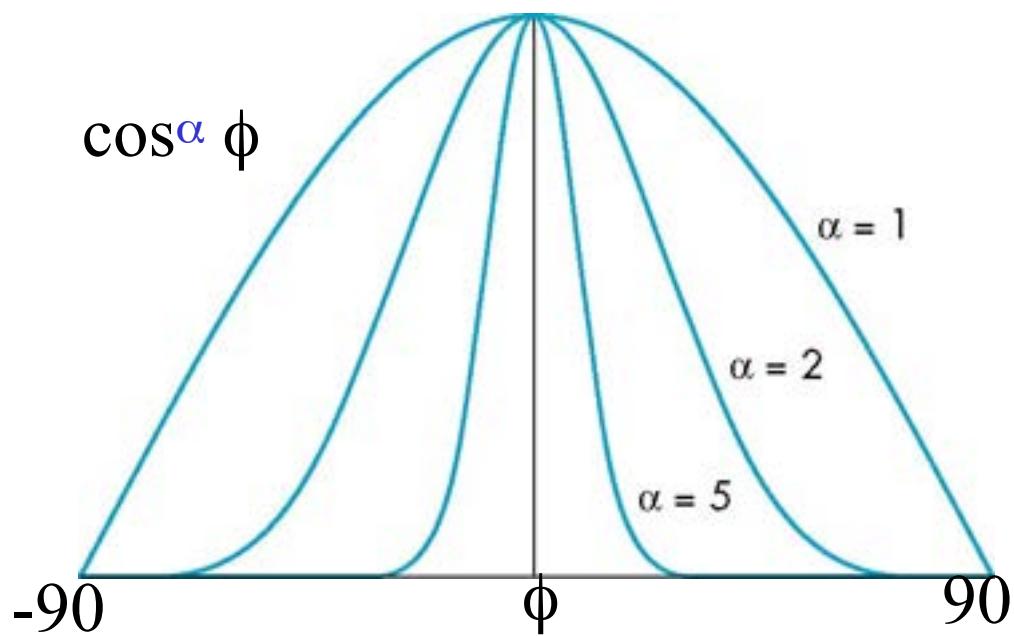
reflected intensity incoming intensity absorption coef
 α shininess coef



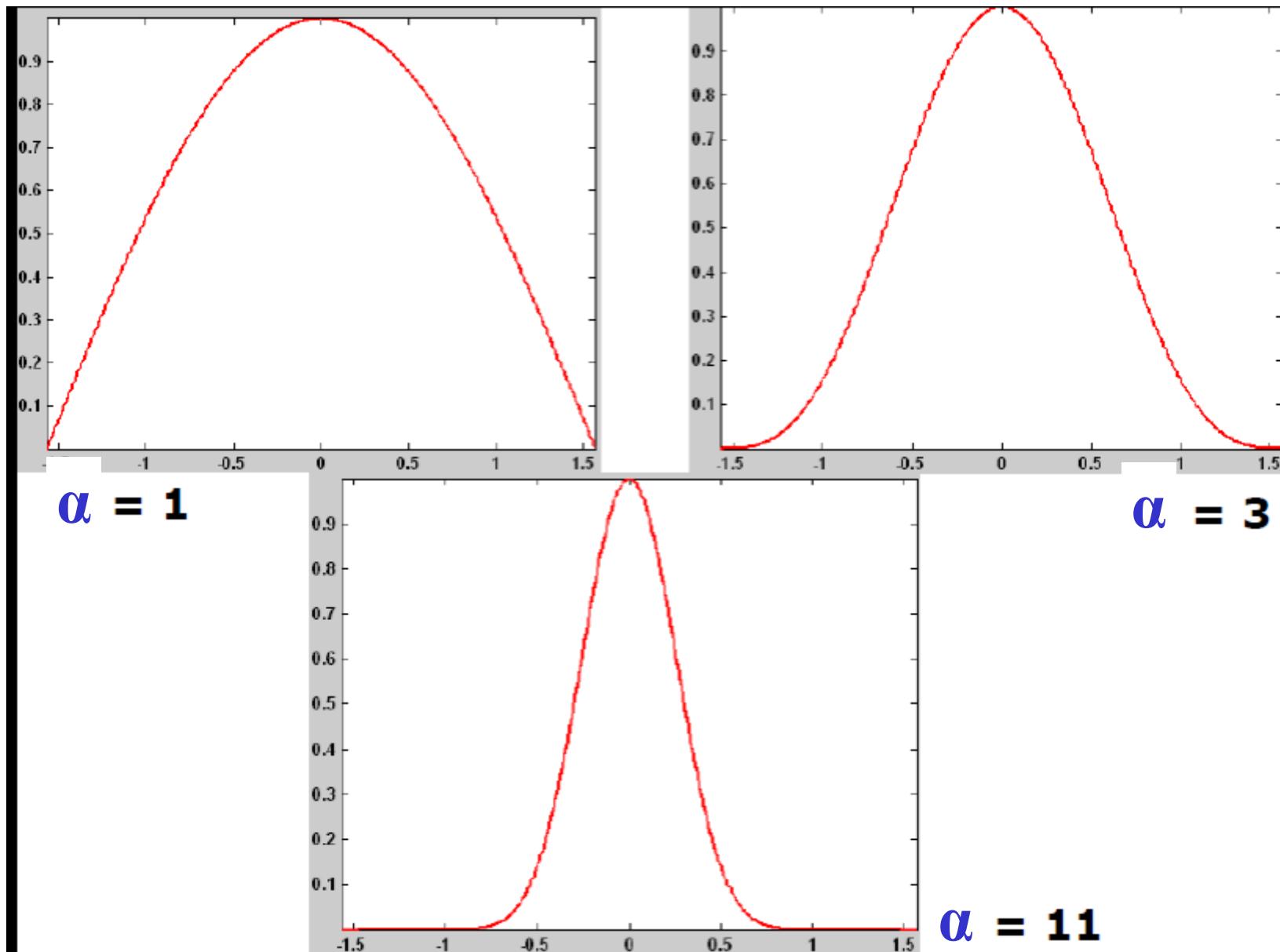
The Shininess Coefficient α

Values of α between 100 and 200 correspond to metals

Values between 5 and 10 give surface that look like plastic



The Shininess Coefficient α



Shading II

shading

deciding **pixel color**

continuum of realism: **when do we do lighting calculation?**

Objectives

- Continue discussion of **shading**
- Introduce **modified Phong model**
- Consider **computation of required vectors**

Ambient Light

- Ambient light is the result of **multiple interactions between (large) light sources** and the **objects** in the environment
- **Amount and color depend** on both the color of the light(s) and the material properties of the **object**

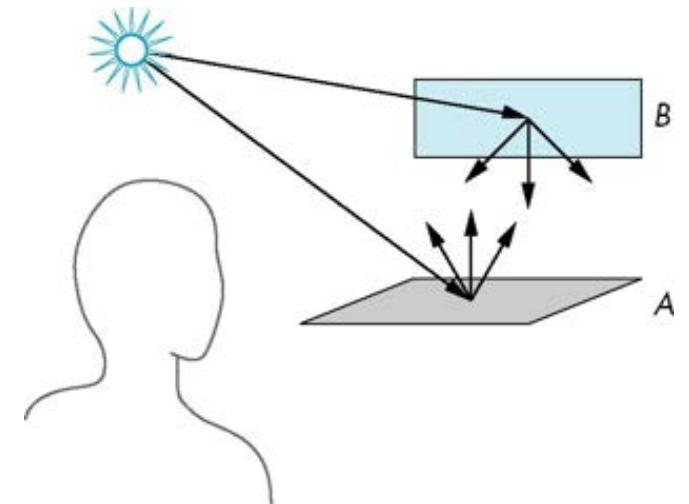
- Add $k_a I_a$ to **diffuse** and **specular** terms

reflection coef

intensity of **ambient** light

Distance Terms

- The light from a **point source** that reaches a **surface** is inversely proportional to **the square of the distance d^2** between them
- We can add a factor of the form $1/(ad + bd + cd^2)$ to the **diffuse** and **specular** terms
- The **constants a, b, c** and linear terms **ad** and **bd** soften the effect of the **point source**



Light Sources

- In the **Phong Model**, we add the results from each **light source**
- **Each light source has separate diffuse, specular, and ambient terms** to allow for maximum flexibility even though this form does not have a physical justification
- Separate **red**, **green** and **blue** components
- Hence, 9 coefficients for **each point source**

$I_{dr}, I_{dg}, I_{db}, I_{sr}, I_{sg}, I_{sb}, I_{ar}, I_{ag}, I_{ab}$

Material Properties

Material properties match light source properties

Nine absorption coefficients

- k_{dr} , k_{dg} , k_{db} , k_{sr} , k_{sg} , k_{sb} , k_{ar} , k_{ag} , k_{ab}

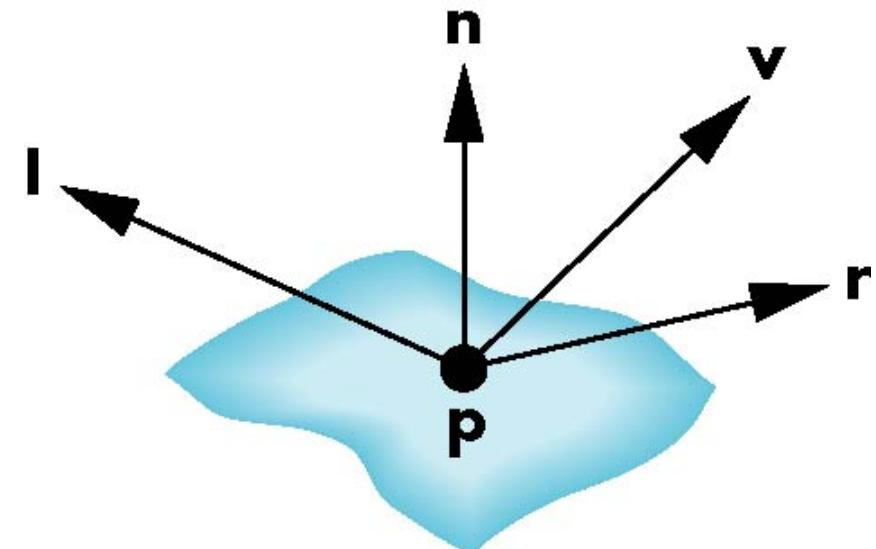
Shininess coefficient α

Adding up the Components

For **each light source** and **each color component**, the **Phong model** can be written (without the distance terms) as

$$I = k_d I_d \mathbf{l} \bullet \mathbf{n} + k_s I_s (\mathbf{v} \bullet \mathbf{r})^\alpha + k_a I_a$$

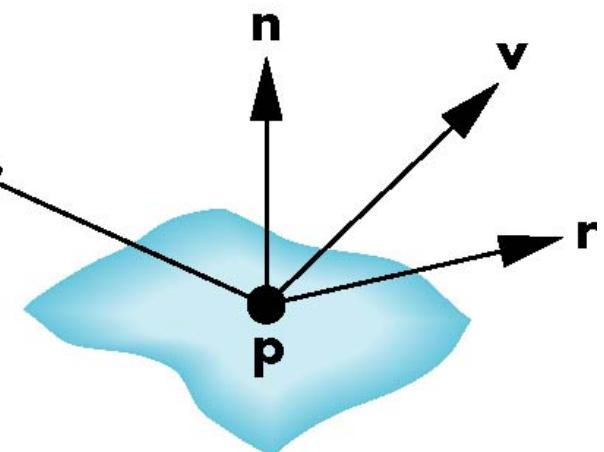
For each color component we add contributions from all sources



Modified Phong Model

The **specular** term in the **Phong mode** is problematic because it requires the calculation of a **new reflection vector r** and **view vector v** for **each vertex**

$$I = k_d I_d \mathbf{l} \bullet \mathbf{n} + \boxed{k_s I_s (\mathbf{v} \bullet \mathbf{r})^\alpha} + k_a I_a$$

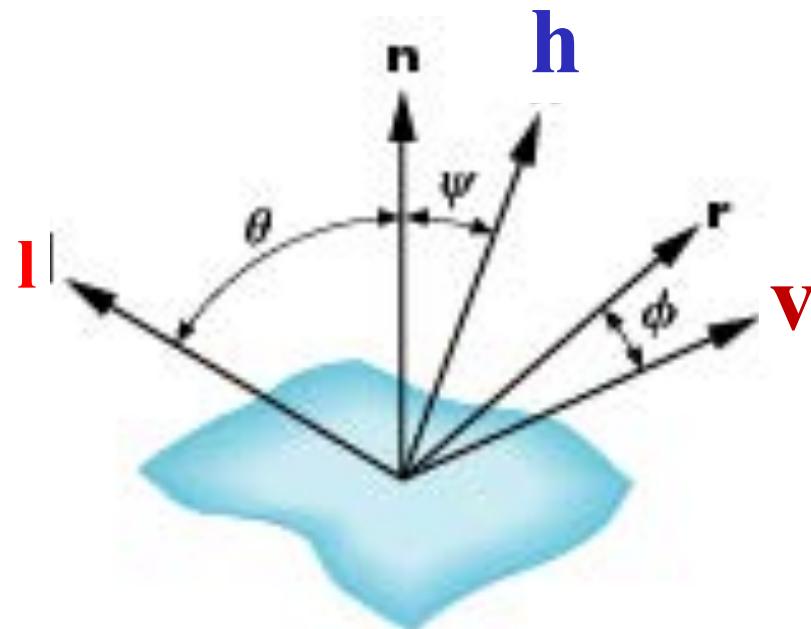


Blinn suggested an approximation using the **halfway vector** that is more efficient

The Halfway Vector h

h is **normalized vector** halfway between \mathbf{l} and \mathbf{v}

$$\mathbf{h} = (\mathbf{l} + \mathbf{v}) / |\mathbf{l} + \mathbf{v}|$$

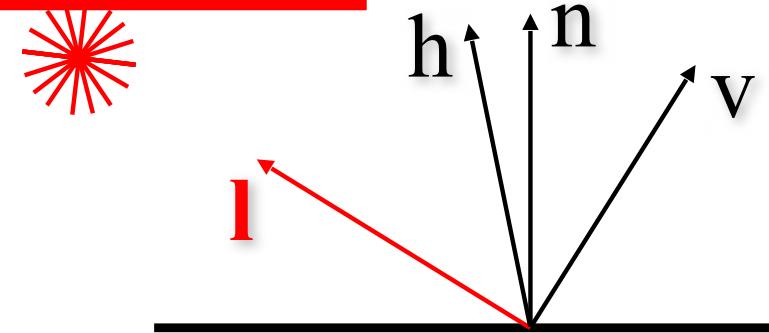


Using the halfway vector h

- Replace $(\mathbf{v} \cdot \mathbf{r})^\alpha$ by $(\mathbf{n} \cdot \mathbf{h})^\beta$
- β is chosen to match shininess
- Note that halfway angle is half of angle between \mathbf{v} and \mathbf{r} if vectors are coplanar
- Resulting model is known as the modified Phong or Blinn lighting model
 - Specified in OpenGL standard

Reflection Equations

Blinn improvement

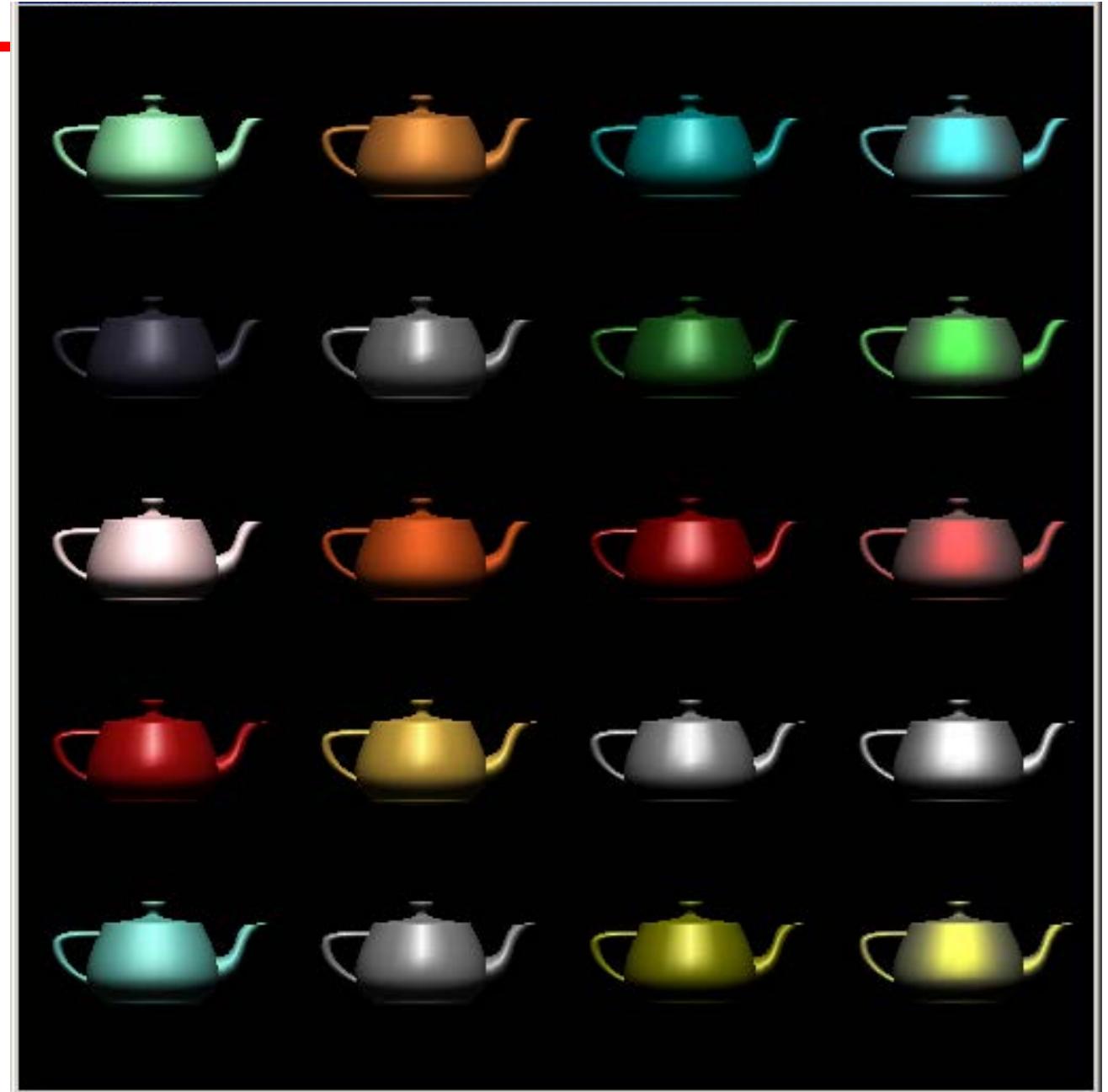


full Phong lighting model

combine ambient, diffuse, specular components

Example

Only differences in
these teapots are
the **parameters**
in the **modified**
Phong model



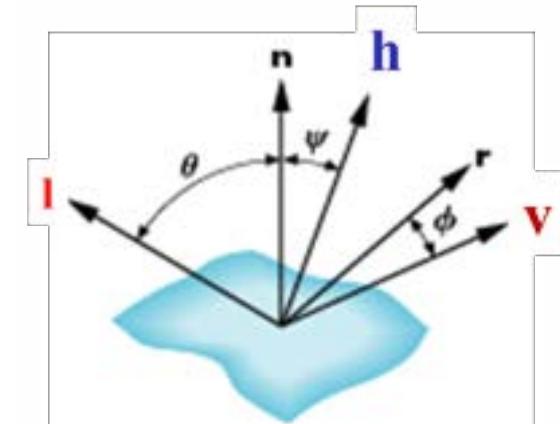
Computation of Vectors

I and **v** are specified by the **application**

Can computer **r** from **I** and **n**

Problem is determining n

For simple surfaces **n** can be determined but how we determine **n** differs depending on **underlying representation of surface**

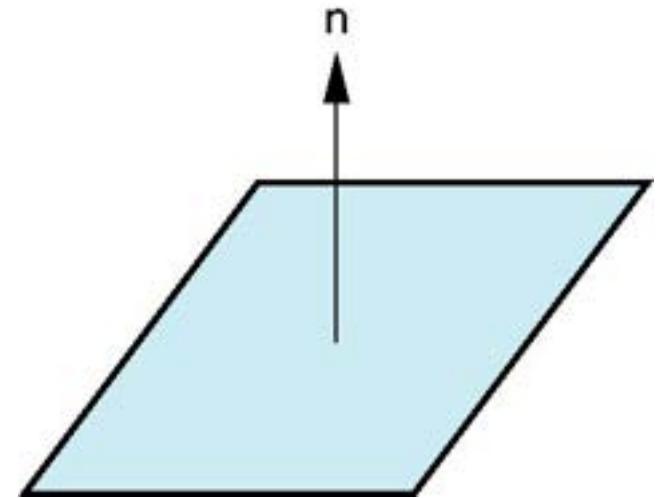


OpenGL leaves determination of normal to application

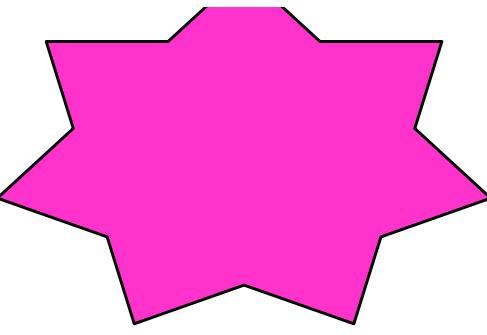
Exception for **GLU quadrics** and **Bezier surfaces** (Chapter 11)

Plane Normals

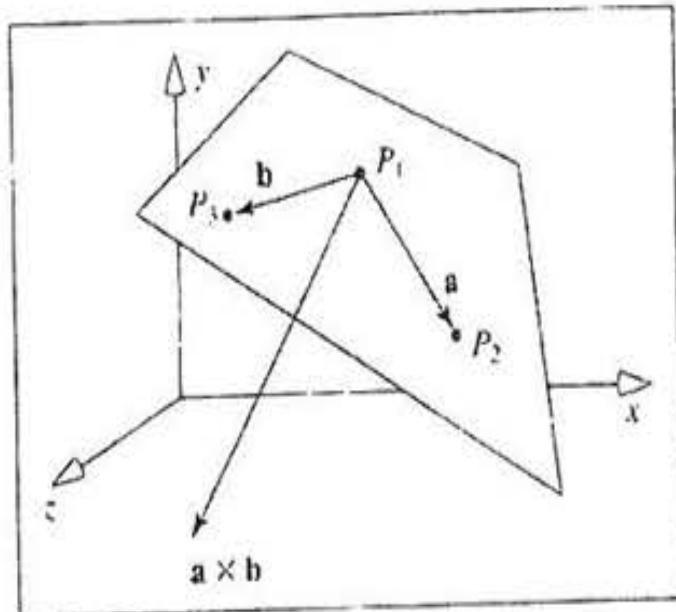
- Equation of plane: $ax + by + cz + d = 0$
- We know that plane is determined by three points p_1, p_2, p_3
- Normal n can be obtained by



CLASS PARTICIPATION 2!
(Next Slide)



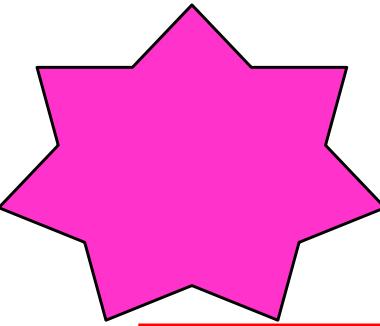
2. (20 points) Write the normal \mathbf{n} to a plane defined by 3 points P_1 , P_2 , P_3 (same as normal \mathbf{n} to a plane defined by two vectors \mathbf{a} and \mathbf{b})



Self Graded - correctly

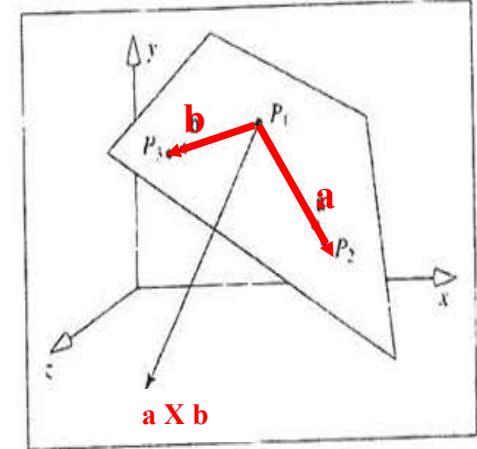
ANSWER:





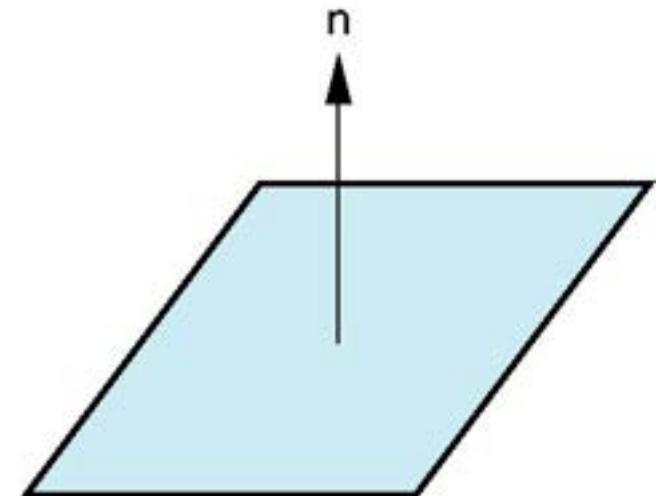
Plane Normals

2. Write the normal \mathbf{n} to a plane defined by 3 points P_1, P_2, P_3 (same as normal \mathbf{n} to a plane defined by two vectors \mathbf{a} and \mathbf{b})



- We know that plane is determined by three points p_1, p_2, p_3 or normal \mathbf{n} and p_1
- Normal \mathbf{n} can be obtained by

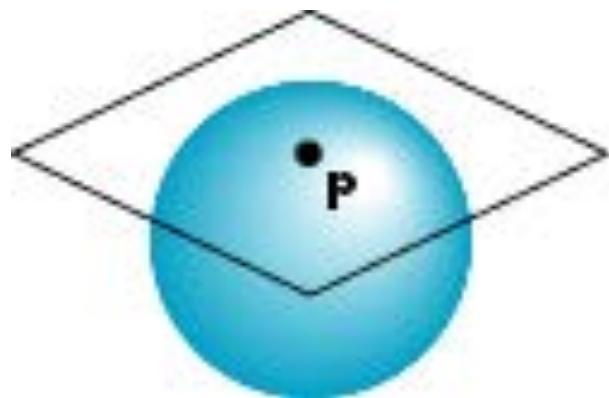
$$\mathbf{n} = (p_2 - p_1) \times (p_3 - p_1)$$



Normal to Sphere

- Implicit function $f(x,y,z)=0$
- Normal given by gradient
- Sphere $f(p)=p \cdot p - 1$

$$\mathbf{n} = [\partial f / \partial x, \partial f / \partial y, \partial f / \partial z]^T = \mathbf{p}$$



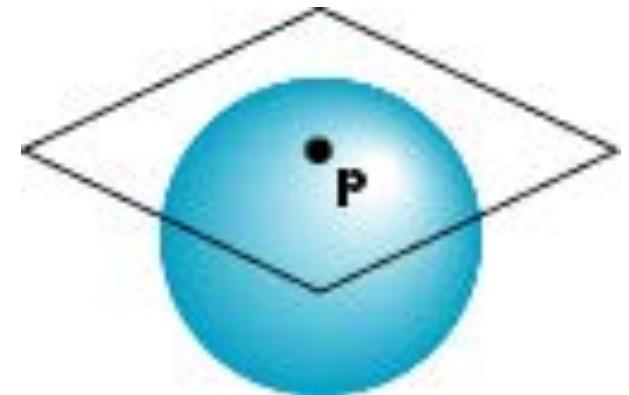
Parametric Form

- For sphere

$$\mathbf{x} = \mathbf{x}(u, v) = \cos u \sin v$$

$$\mathbf{y} = \mathbf{y}(u, v) = \cos u \cos v$$

$$\mathbf{z} = \mathbf{z}(u, v) = \sin u$$



- Tangent plane determined by vectors

$$\frac{\partial \mathbf{p}}{\partial \mathbf{u}} = [\frac{\partial \mathbf{x}}{\partial u}, \frac{\partial \mathbf{y}}{\partial u}, \frac{\partial \mathbf{z}}{\partial u}]^T$$

$$\frac{\partial \mathbf{p}}{\partial \mathbf{v}} = [\frac{\partial \mathbf{x}}{\partial v}, \frac{\partial \mathbf{y}}{\partial v}, \frac{\partial \mathbf{z}}{\partial v}]^T$$

- Normal \mathbf{n} given by **cross product**

$$\mathbf{n} = \frac{\partial \mathbf{p}}{\partial \mathbf{u}} \times \frac{\partial \mathbf{p}}{\partial \mathbf{v}}$$

General Case

We can compute **parametric normals** for other simple cases

- Quadratics

- Parametric polynomial surfaces

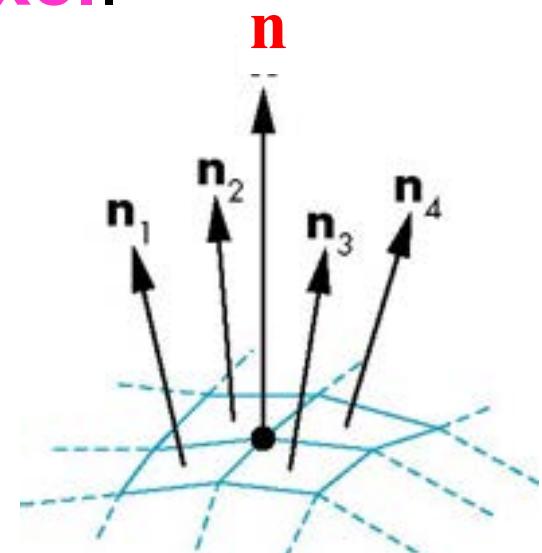
- Bezier surface patches (Chapter 11)

Gouraud Shading

For polygonal models, Gouraud proposed we use the average of the normals of the polygons that share the vertex

The advantage is that it is computationally less expensive, only requiring the evaluation of the intensity equation at the polygon vertices, and then bilinear interpolation of these values for each pixel.

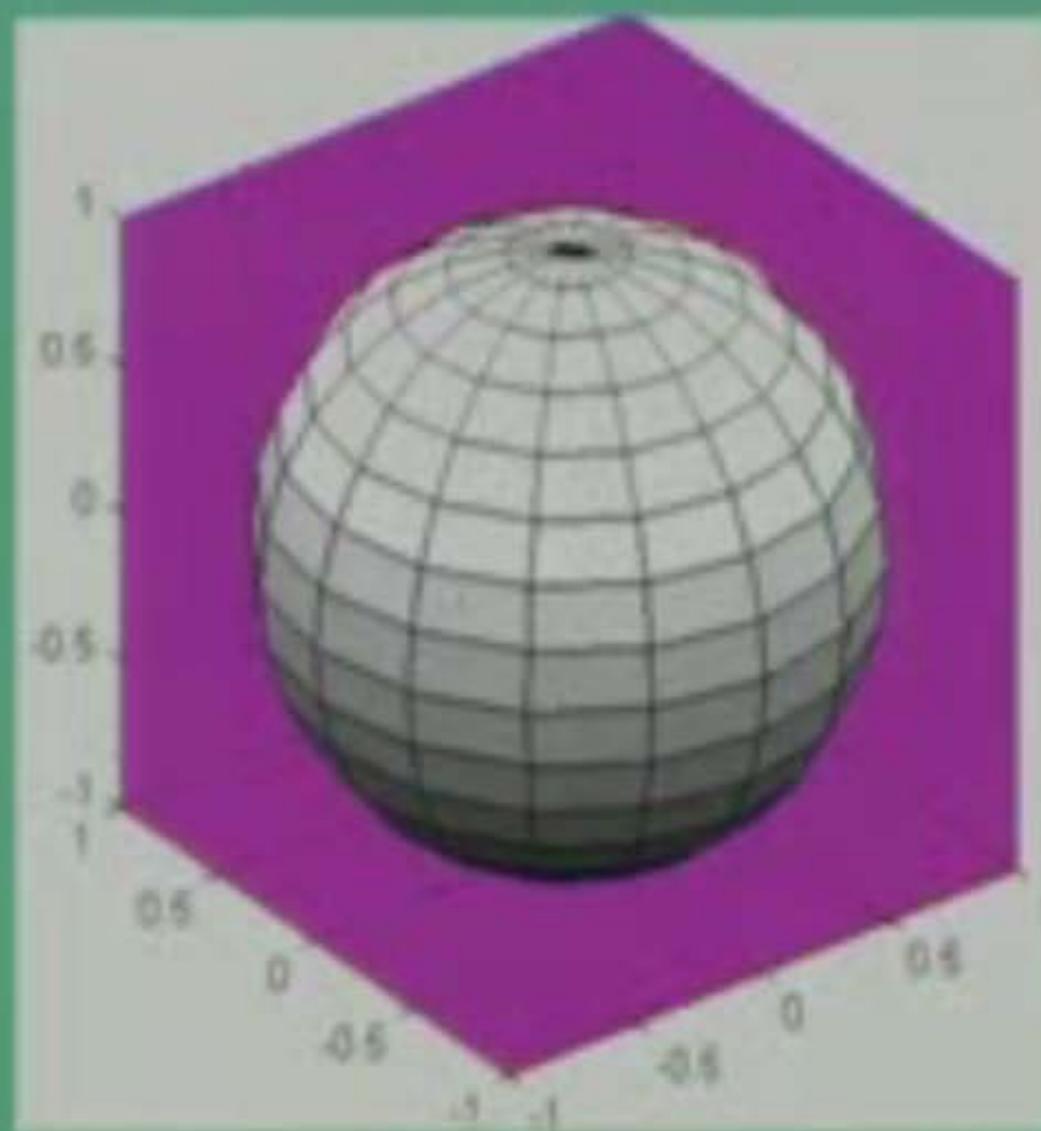
$$\mathbf{n} = (\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4) / |\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4|$$



Shading Model for Polygon

Constant Shading

- Also called *faceted shading*, or *flat shading*.



Illustrating the different shadings of a sphere.



Faceted



Gouraud/
Smooth/
Interpolated

Illustrating the different shadings of a sphere.

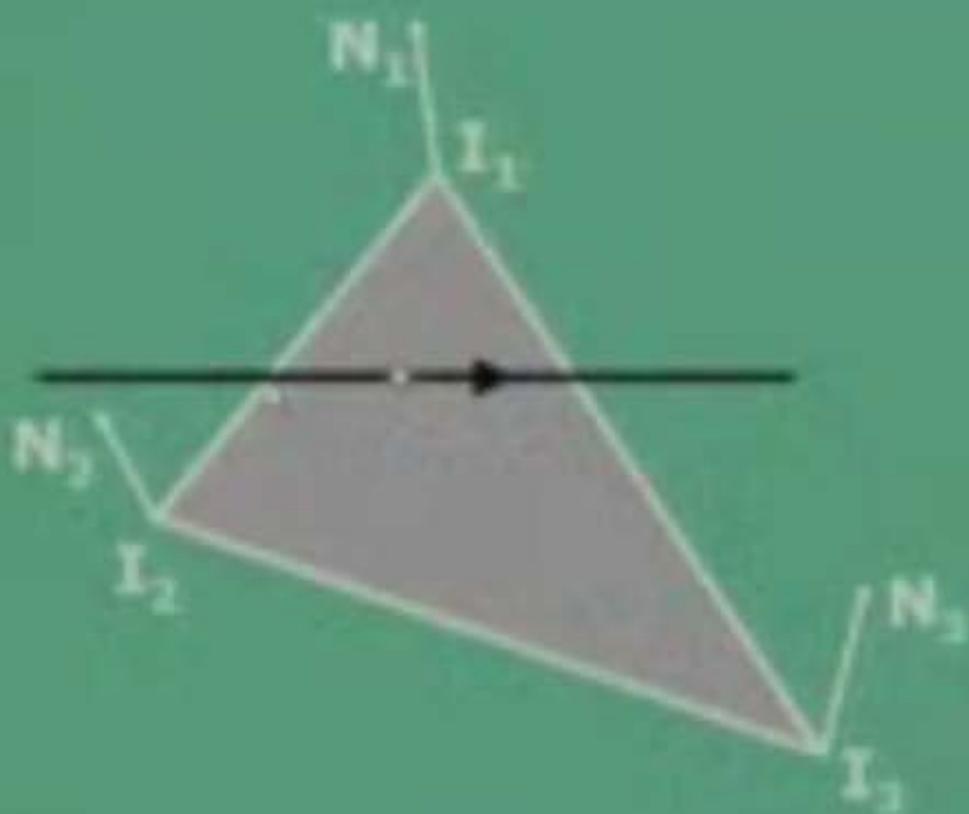


Faceted

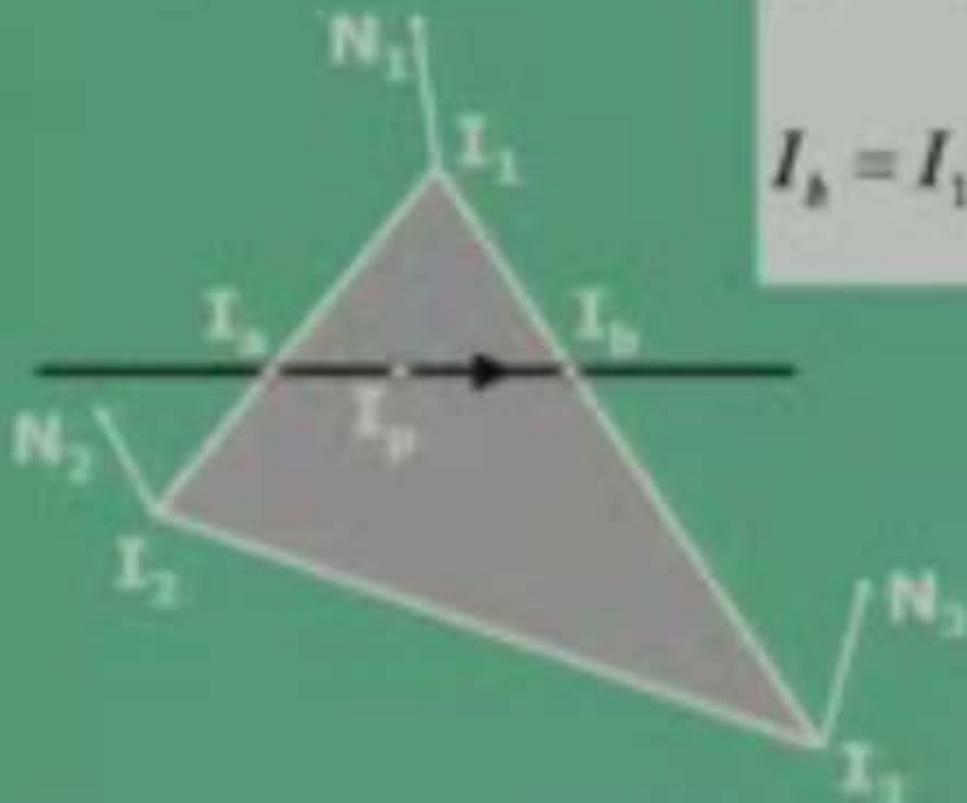


Gouraud/
Smooth/
Interpolated

Illustrating the principle of Gouraud Shading or Color/Intensity Interpolation shading



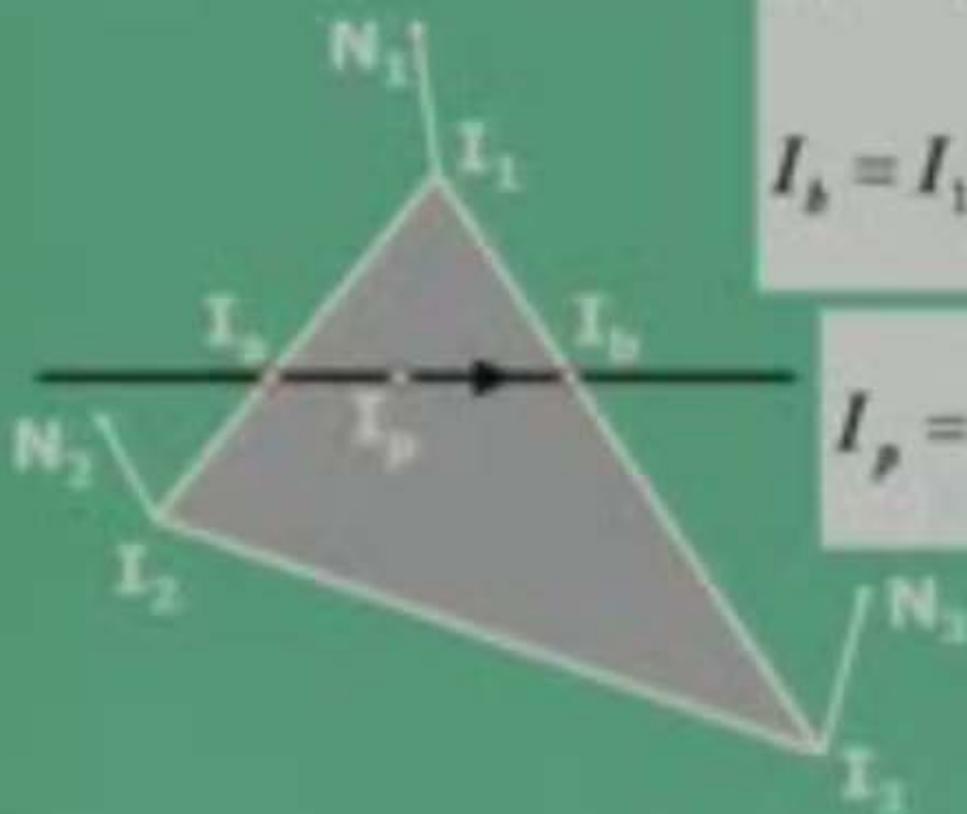
Illustrating the principle of Gouraud Shading or Color / Intensity Interpolation shading



$$I_p = I_1 - (I_1 - I_2) \left(\frac{y_1 - y_p}{y_1 - y_2} \right);$$

$$I_p = I_1 - (I_1 - I_3) \left(\frac{y_1 - y_p}{y_1 - y_3} \right);$$

Illustrating the principle of Gouraud Shading or Color / Intensity Interpolation shading

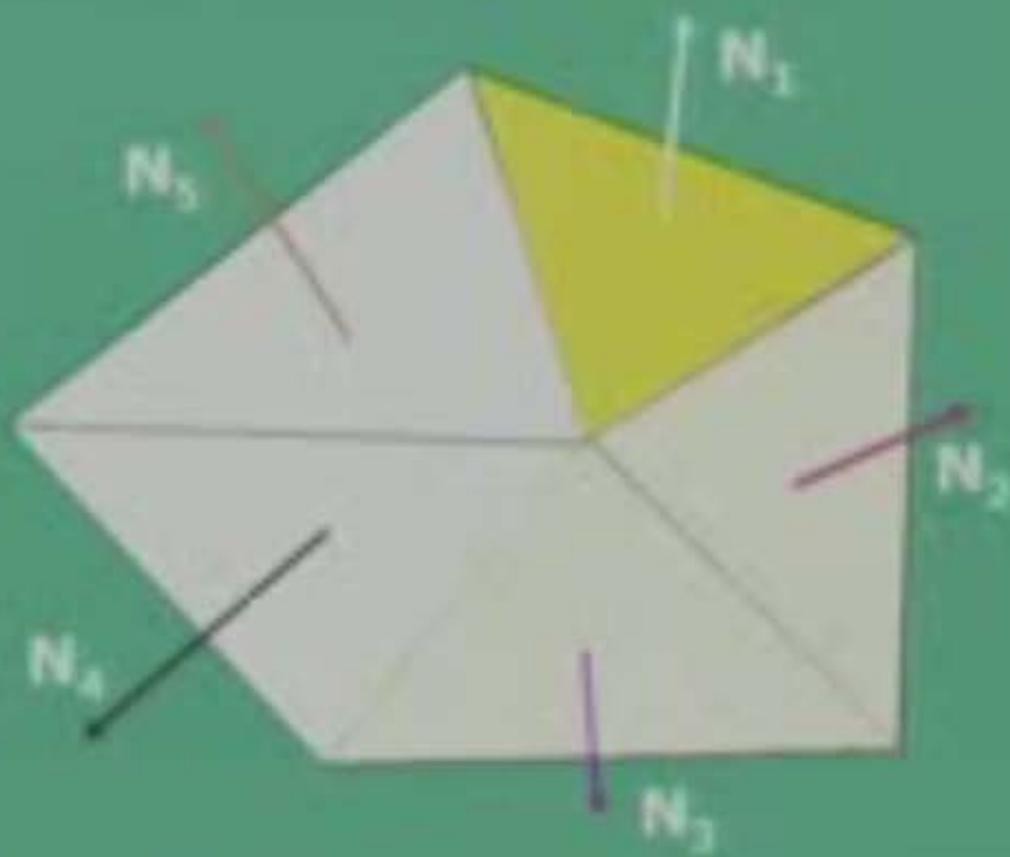


$$I_a = I_1 - (I_1 - I_2) \left(\frac{y_1 - y_e}{y_1 - y_2} \right);$$

$$I_b = I_1 - (I_1 - I_3) \left(\frac{y_1 - y_e}{y_1 - y_3} \right);$$

$$I_p = I_b - (I_b - I_a) \left(\frac{x_b - x_p}{x_b - x_a} \right)$$

Illustrating the principle of
Gouraud Shading or
Color/Intensity Interpolation shading



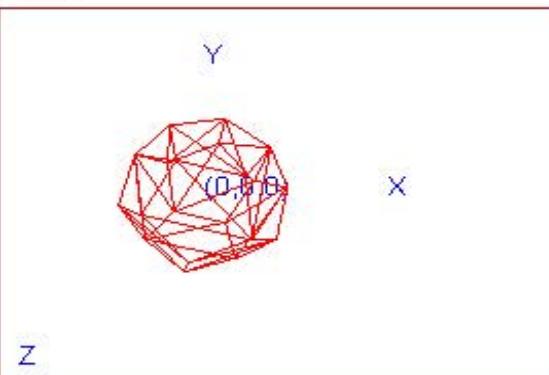


Illustrating the
difference in
shadings in case of
a tea-pot.



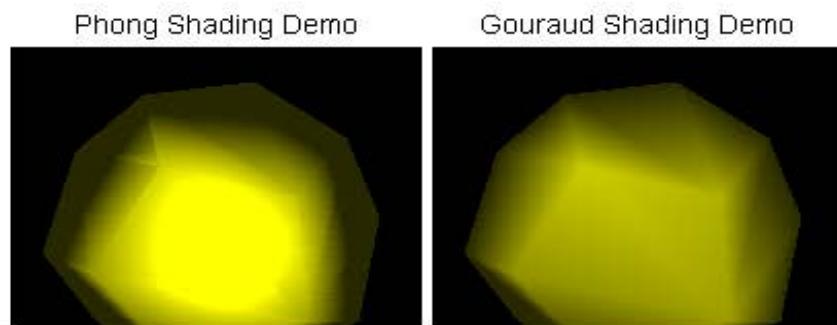
Phong Shading vs Gouraud Shading

Model



rotateY	0.0
rotateZ	0.0
lightX	0.0
lightY	0.0
lightZ	2.0
Ia	200.0
Ip	500.0
Ka	0.2
Kd	0.5
Ks	0.5
Exponent	25.0

Model Phong Gouraud



Shading in OpenGL

Chapter 6 .7

Objectives

- Introduce the **OpenGL** shading functions
- Discuss **Polygonal shading**
 - Flat
 - Smooth
 - Gouraud

Steps in OpenGL shading

1. Enable **shading** and select **model**
2. Specify **normals**
3. Specify **material properties**
4. Specify **lights**

Normals

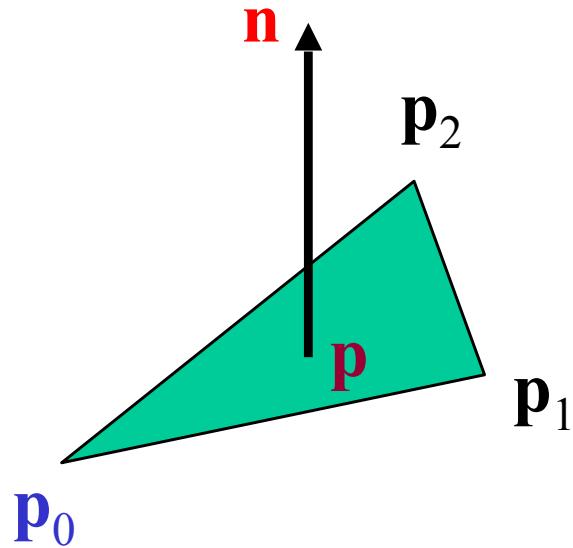
- In OpenGL the **normal vector** is **part of the state**
- Set by `glNormal*`()
`glNormal3f(x, y, z);`
`glNormal3fv(p);`
- Usually we want to **set the normal** to have **unit length** so cosine calculations are correct
Length can be affected by transformations
Note that scaling does not preserve **length**

`glEnable(GL_NORMALIZE)` allows for **auto normalization** at a performance penalty

Normal for Triangle

```
void normal(point p)
{
    /* normalize a vector */
    double sqrt();
    float d =0.0;
    int i;
    for(i=0; i<3; i++) d+=p[i]*p[i];
    d=sqrt(d);
    if(d>0.0) for(i=0; i<3; i++) p[i]/=d;
}
```

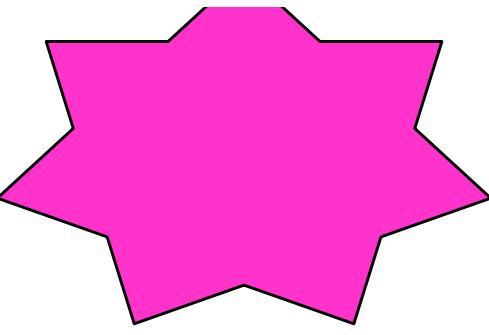
Express \mathbf{n} as a dot product \bullet and cross product \times



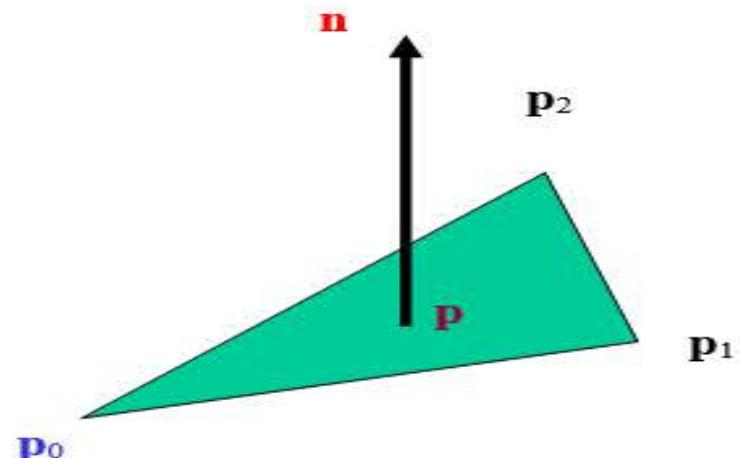
Normalize \mathbf{n}

Note that right-hand rule determines outward face

CLASS PARTICIPATION 3, 4!
(Next Slide)



3. (20 points) Express the normal \mathbf{n} to a triangle both as a dot product \bullet and as cross product \mathbf{X} .



ANSWER:

4. (20 points) Normalize \mathbf{n} to \mathbf{n}

Self Graded - correctly



Normal for Triangle

```
void normal(point p)
{
    /* normalize a vector */
    double sqrt();
    float d =0.0;
    int i;
    for(i=0; i<3; i++) d+=p[i]*p[i];
    d=sqrt(d);
    if(d>0.0) for(i=0; i<3; i++) p[i]/=d;
}
```

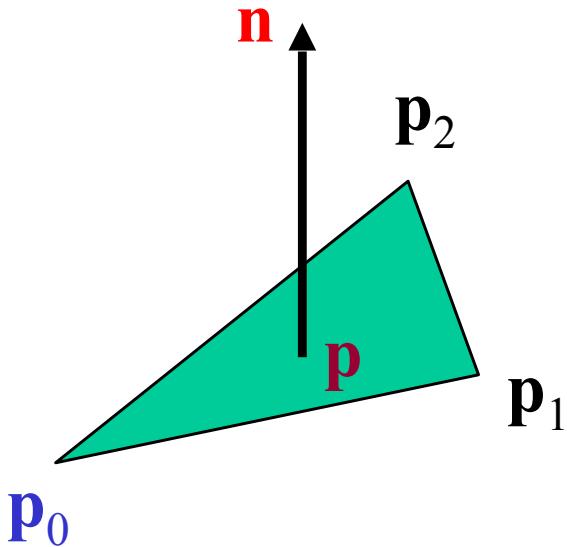
Express \mathbf{n} as a dot product \bullet and cross product \times

plane $\mathbf{n} \bullet (\mathbf{p} - \mathbf{p}_0) = 0$

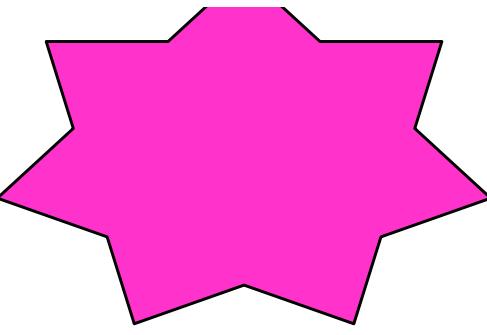
$$\mathbf{n} = (\mathbf{p}_2 - \mathbf{p}_0) \times (\mathbf{p}_1 - \mathbf{p}_0)$$

Normalize \mathbf{n}

$$\text{normalize } \hat{\mathbf{n}} \leftarrow \mathbf{n} / |\mathbf{n}|$$



Note that right-hand rule determines outward face



5. (20 points) Create **Lecture6** Empty Project:

Download **SphereShading.c** from CANVAS.

Class APRTICIPATION on Lecture 6

Publish Edit :

Download and complete this word document.

[Class Participation on Lecture 6.doc](#)

[SphereShading.c](#)

You will be prompted when to Upload completed document to CANVAS as **score.doc** (example 100.doc).

Warning:

TA, at random, will inspect the Uploaded document.

If you score is not honestly entered, you will get a zero.

For the Grader: if the student did not submit, please skip and do not assign a ZERO (MISSING).

Self Graded - correctly

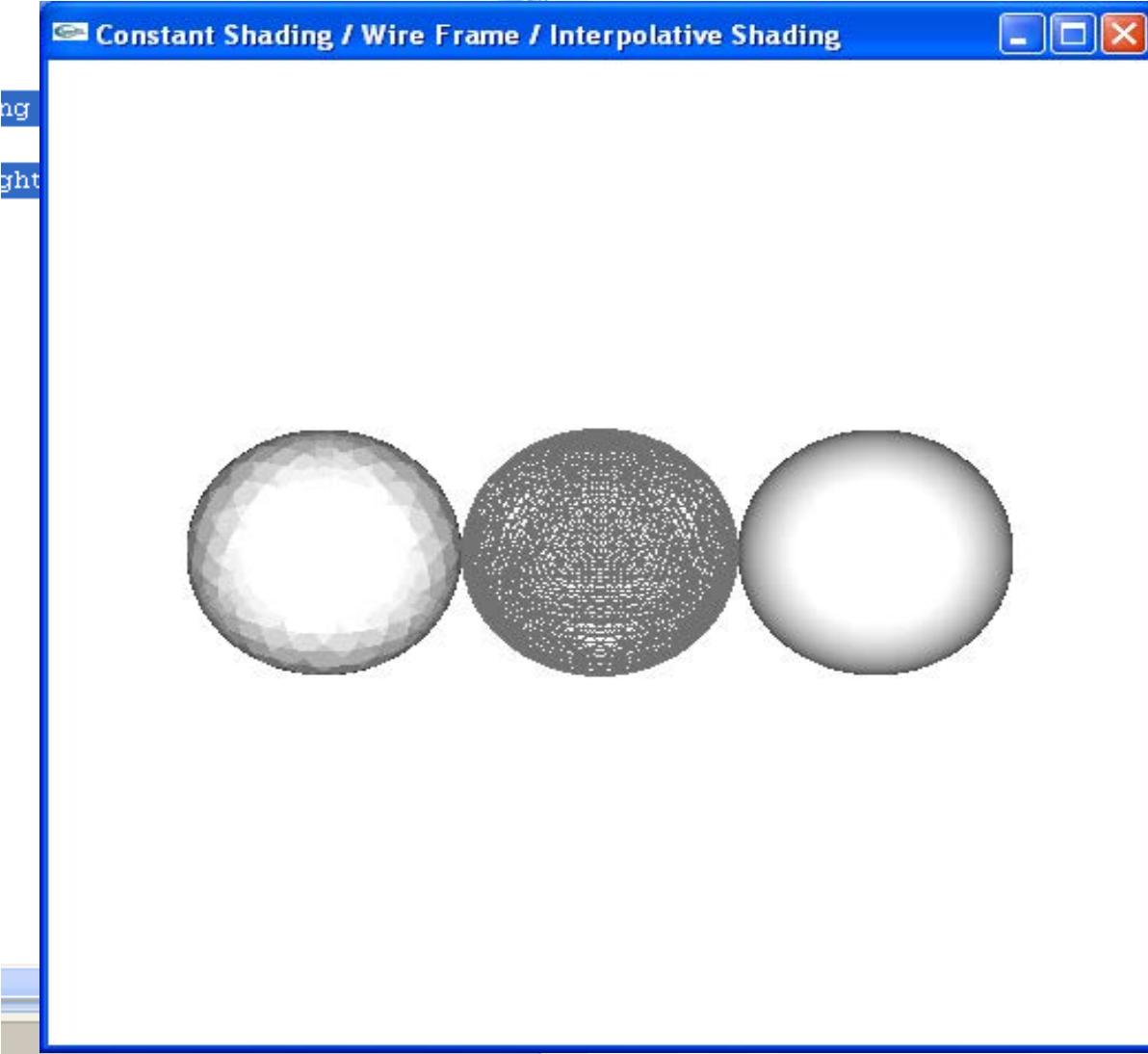


00:02:00
00:00:00

Start

Stop

Comparison Constant Shading/ Wire Frame/ Interpolative Shading



The image shows a Windows application window titled "Constant Shading / Wire Frame / Interpolative Shading". Inside the window, there are three spheres arranged horizontally. The first sphere on the left is rendered in wireframe mode, showing a grid of lines. The middle sphere is rendered in constant shading mode, appearing as a solid dark gray sphere. The third sphere on the right is rendered in interpolative shading mode, showing a gradient from dark gray at the bottom to white at the top. To the left of the application window, a code editor window is visible, displaying C code for a program named "SphereShading.c". The code defines three modes: wire frame, constant shading, and interpolative shading, each involving different OpenGL commands like glClear, glLoadIdentity, glTranslatef, and glDrawElements.

```
* SphereShading.c */
play(void)

displays all three modes, side by side */

clear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
LoadIdentity();

mode 0 = wire frame*/
:=0;
rahedron(n);

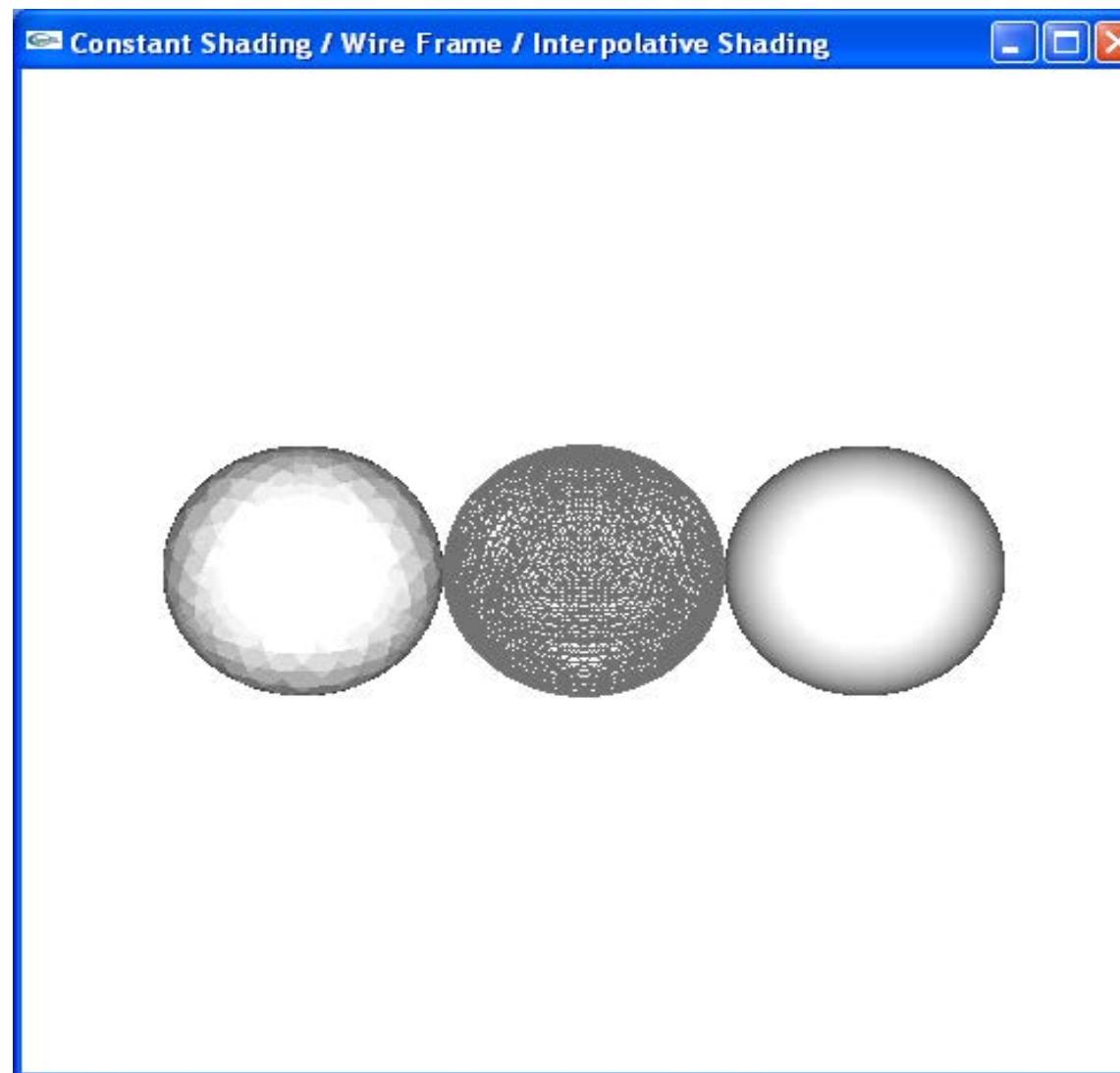
mode 1 = constant shading */
:=1;
translatef(-2.0, 0.0,0.0);
rahedron(n);

mode 2 = interpolative shading */
:=2;
translatef( 4.0, 0.0,0.0);
rahedron(n);

push();
```

Comparison Constant Shading/ Wire Frame/ Interpolative Shading

```
9 void triangle( point a, point b, point c)
0
1 /* display one triangle using a line loop for wire frame, a single
2 normal for constant shading, or three normals for interpolative shading */
3 {
4     if (mode==0)
5         glBegin(GL_LINE_LOOP);
6     else
7         glBegin(GL_POLYGON);
8         if(mode==1) glNormal3fv(a);
9         if(mode==2) glNormal3fv(a);
0         glVertex3fv(a);
1         if(mode==2) glNormal3fv(b);
2         glVertex3fv(b);
3         if(mode==2) glNormal3fv(c);
4         glVertex3fv(c);
5     glEnd();
6 }
```



Enabling Shading

Shading calculations are enabled by

`glEnable(GL_LIGHTING)`

Once lighting is enabled, `glColor()` ignored

Must enable each light source individually

`glEnable(GL_LIGHTi) i=0,1.....`

Can choose light model parameters

`glLightModelfi(parameter, GL_TRUE)`

- `GL_LIGHT_MODEL_LOCAL_VIEWER` do not use simplifying distant viewer assumption in calculation
- `GL_LIGHT_MODEL_TWO_SIDED` shades both sides of polygons independently

Defining a Point Light Source

For **each light source**, we can set an **RGBA** for the **diffuse**, **specular**, and **ambient** components, and for the **position**

```
GL float diffuse0[]    ={1.0, 0.0, 0.0, 1.0};  
GL float specular0[]  ={1.0, 0.0, 0.0, 1.0};  
GL float ambient0[]   ={1.0, 0.0, 0.0, 1.0};  
GLfloat  light0_pos[] = {1.0, 2.0, 3.0, 1.0};  
  
        glEnable(GL_LIGHTING);  
        glEnable(GL_LIGHT0);  
glLightv(GL_LIGHT0, GL_POSITION, light0_pos);  
glLightv(GL_LIGHT0, GL_AMBIENT, ambient0);  
glLightv(GL_LIGHT0, GL_DIFFUSE, diffuse0);  
glLightv(GL_LIGHT0, GL_SPECULAR, specular0);
```

Defining a Point Light Source

The screenshot shows a C++ IDE interface with a project tree on the left and a code editor on the right.

Project Tree:

- Solution 'Lecture 6' (1 project)
 - Lecture 6
 - Header Files
 - Resource Files
 - Source Files
 - SphereShading.c

Code Editor (Global Scope):

```
144 void myinit()
145 {
146     GLfloat mat_specular[]={1.0, 1.0, 1.0, 1.0};
147     GLfloat mat_diffuse[] = {1.0, 1.0, 1.0, 1.0};
148     GLfloat mat_ambient[] = {1.0, 1.0, 1.0, 1.0};
149     GLfloat mat_shininess=(100.0);
150     GLfloat light_ambient[] = {0.0, 0.0, 0.0, 1.0};
151     GLfloat light_diffuse[] = {1.0, 1.0, 1.0, 1.0};
152     GLfloat light_specular[] = {1.0, 1.0, 1.0, 1.0};
153
154     /* set up ambient, diffuse, and specular components for light 0 */
155
156     glLightfv(GL_LIGHT0, GL_AMBIENT, light_ambient);
157     glLightfv(GL_LIGHT0, GL_DIFFUSE, light_diffuse);
158     glLightfv(GL_LIGHT0, GL_SPECULAR, light_specular);
159
160     /* define material properties for front face of all polygons */
161
162     glMaterialfv(GL_FRONT, GL_SPECULAR, mat_specular);
163     glMaterialfv(GL_FRONT, GL_AMBIENT, mat_ambient);
164     glMaterialfv(GL_FRONT, GL_DIFFUSE, mat_diffuse);
165     glMaterialf(GL_FRONT, GL_SHININESS, mat_shininess);
166
167     glShadeModel(GL_SMOOTH);      /*enable smooth shading */
168     glEnable(GL_LIGHTING);        /* enable lighting */
169     glEnable(GL_LIGHT0);          /* enable light 0 */
170     glEnable(GL_DEPTH_TEST);      /* enable z buffer */
171
172     glClearColor (1.0, 1.0, 1.0, 1.0);
173     glColor3f (0.0, 0.0, 0.0);
174 }
175 }
```

The code defines a `myinit()` function. It initializes material properties (specular, ambient, diffuse, shininess) and sets up a point light source (light_ambient, light_diffuse, light_specular). It also enables lighting, specifically enabling light 0. The code is annotated with comments explaining the purpose of each section.

Distance and Direction

- We can add a factor of the form $1/(ad + bd + cd^2)$ to the **diffuse** and **specular** terms

The source colors are specified in **RGBA**

The position is given in **homogeneous coordinates**

If **w =1.0**, we are specifying a finite location

If **w =0.0**, we are specifying a parallel source with the given **direction vector**

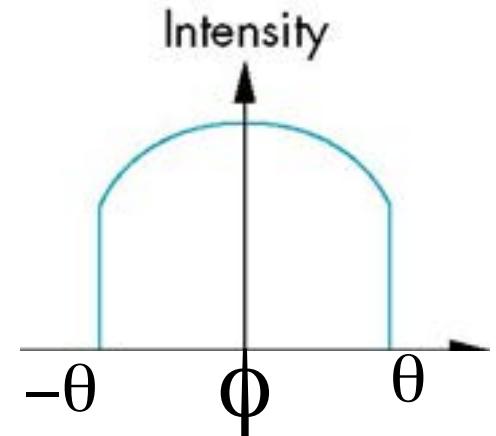
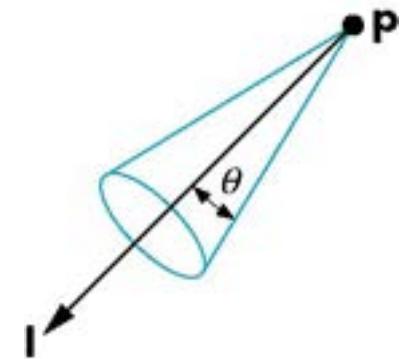
The coefficients in the **distance terms** are by default **a=1.0 (constant terms)**, **b=c=0.0 (linear and quadratic terms)**.

$$a = 0.80;$$

```
glLightf(GL_LIGHT0, GLCONSTANT_ATTENUATION, a);
```

Spotlights

- Use `gLightv` to set
Direction `GL_SPOT_DIRECTION`
- Cutoff `GL_SPOT_CUTOFF`
- Attenuation `GL_SPOT_EXPONENT`
 - Proportional to $\cos^\alpha \phi$



Global Ambient Light

- **Ambient light** depends on color of light sources
 - A **red light** in a white room will cause a red ambient term that disappears when the light is turned off
- **OpenGL** also allows a global ambient term that is often helpful for testing

```
glLightModelfv(GL_LIGHT_MODEL_AMBIENT, global_ambient)
```

Moving Light Sources

- **Light sources** are geometric objects whose **positions** or **directions** are affected by the **model-view** matrix
- Depending on where we place the position (direction) setting function, we can
 - Move the **light source(s)** with the **object(s)**
 - Fix the **object(s)** and move the **light source(s)**
 - Fix the **light source(s)** and move the **object(s)**
 - Move the **light source(s)** and **object(s)** independently

Material Properties

- Material properties are also part of the **OpenGL state** and match the terms in the **modified Phong model**
- Set by **glMaterialv()**

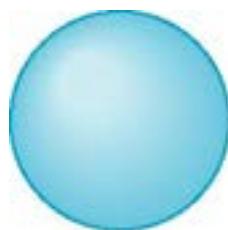
```
GLfloat ambient[] = {0.2, 0.2, 0.2, 1.0};  
GLfloat diffuse[] = {1.0, 0.8, 0.0, 1.0};  
GLfloat specular[] = {1.0, 1.0, 1.0, 1.0};  
        GLfloat shine = 100.0  
  
glMaterialf(GL_FRONT, GL_AMBIENT, ambient);  
glMaterialf(GL_FRONT, GL_DIFFUSE, diffuse);  
glMaterialf(GL_FRONT, GL_SPECULAR, specular);  
glMaterialf(GL_FRONT, GL_SHININESS, shine);
```

Front and Back Faces

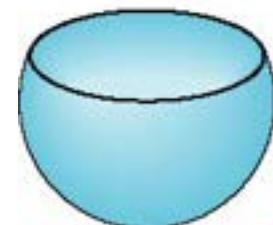
The default is shade **only front faces** which works correctly for convex objects

If we set two sided lighting, **OpenGL** will shade both sides of a surface

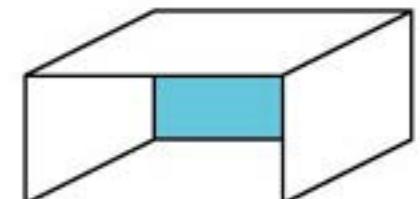
Each side can have its own properties which are set by using **GL_FRONT**, **GL_BACK**, or **GL_FRONT_AND_BACK** in **glMaterialf**



back faces not visible



back faces visible



Defining Material Properties

The screenshot shows a C++ code editor with a red box highlighting the material definition section. The code defines ambient, diffuse, and specular colors for both materials and lights, and sets up lighting and material properties.

```
GLfloat ambient[] = {0.2, 0.2, 0.2, 1.0};
GLfloat diffuse[] = {1.0, 0.8, 0.0, 1.0};
GLfloat specular[] = {1.0, 1.0, 1.0, 1.0};
GLfloat shine = 100.0

void myinit()
{
    GLfloat mat_specular[]={1.0, 1.0, 1.0, 1.0};
    GLfloat mat_diffuse[] = {1.0, 1.0, 1.0, 1.0};
    GLfloat mat_ambient[] = {1.0, 1.0, 1.0, 1.0};
    GLfloat mat_shininess={100.0};

    GLfloat light_ambient[] = {0.0, 0.0, 0.0, 1.0};
    GLfloat light_diffuse[] = {1.0, 1.0, 1.0, 1.0};
    GLfloat light_specular[] = {1.0, 1.0, 1.0, 1.0};

    /* set up ambient, diffuse, and specular components for light 0 */
    glLightfv(GL_LIGHT0, GL_AMBIENT, light_ambient);
    glLightfv(GL_LIGHT0, GL_DIFFUSE, light_diffuse);
    glLightfv(GL_LIGHT0, GL_SPECULAR, light_specular);

    /* define material properties for front face of all polygons */
    glMaterialfv(GL_FRONT, GL_SPECULAR, mat_specular);
    glMaterialfv(GL_FRONT, GL_AMBIENT, mat_ambient);
    glMaterialfv(GL_FRONT, GL_DIFFUSE, mat_diffuse);
    glMaterialf(GL_FRONT, GL_SHININESS, mat_shininess);

    glShadeModel(GL_SMOOTH);      /*enable smooth shading */
    glEnable(GL_LIGHTING);        /* enable lighting */
    glEnable(GL_LIGHT0);          /* enable light 0 */
    glEnable(GL_DEPTH_TEST);      /* enable z buffer */

    glClearColor(1.0, 1.0, 1.0, 1.0);
    glColor3f(0.0, 0.0, 0.0);
}
```

Emissive Term

- We can simulate a **light source** in **OpenGL** by giving a material an emissive component
- **This component is unaffected by any sources or transformations**

```
GLfloat emission[] = (0.0, 0.3, 0.3, 1.0);  
glMaterialf(GL_FRONT, GL_EMISSION, emission);
```

Transparency

- Material properties are specified as RGBA values
- The **A value** can be used to make the surface translucent
- **The default is that all surfaces are opaque** regardless of A
- Later we will **enable blending** and use this feature

Efficiency

- Because material properties are part of the state, if we change materials for many surfaces, we can affect performance
- We can make the code cleaner by defining a material structure and setting all materials during initialization

```
typedef struct materialStruct {  
    GLfloat ambient[4];  
    GLfloat diffuse[4];  
    GLfloat specular[4];  
    GLfloat shininess;  
} MaterialStruct;
```

- We can then select a material by a pointer

Polygonal Shading

- **Shading calculations** are done for **each vertex**
Vertex colors become **vertex shades**
- By default, **vertex** shades are **interpolated across the polygon**
`glShadeModel(GL_SMOOTH);`
- If we use `glShadeModel(GL_FLAT);` the **color at the first vertex will determine the shade of the whole polygon**

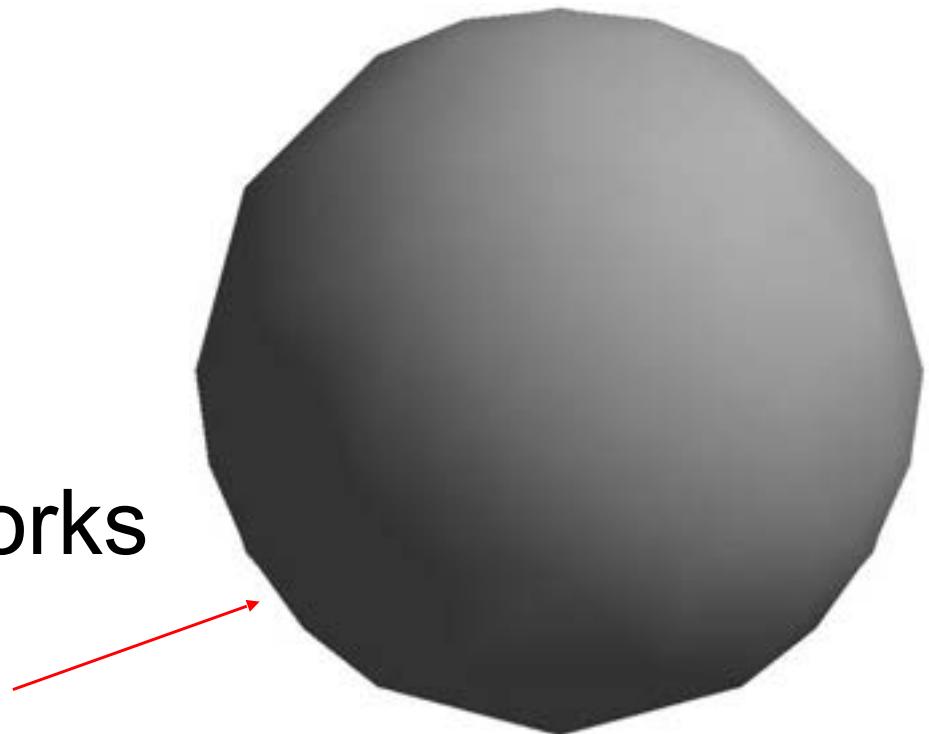
Polygon Normals

- Polygons have a **single normal**
Shades at the vertices as computed by the Phong model can be almost same
Identical for a distant viewer (default) or if there is no **specular** component
- Consider model of sphere
- Want **different normals at each vertex** even though this concept is not quite correct mathematically



Smooth Shading

- We can set a new normal at each vertex
- Easy for sphere model
 - If centered at origin $\mathbf{n} = \mathbf{p}$
- Now smooth shading works
- Note silhouette edge

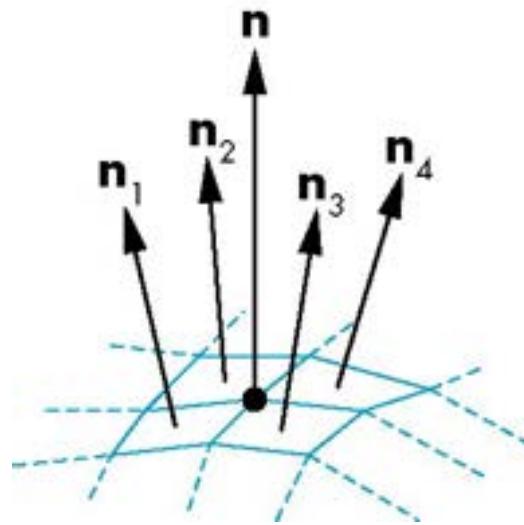


Mesh Shading

The previous example is not general because we
knew the normal at each vertex analytically

For polygonal models, **Gouraud proposed** we use
the average of the normals around a mesh vertex

$$\mathbf{n} = (\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4) / |\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4|$$



Gouraud and Phong Shading

- **Gouraud Shading**

Find average normal at each vertex (vertex normals)

Apply modified Phong model at each vertex

Interpolate vertex shades across each polygon

- **Phong shading**

Find vertex normals

Interpolate vertex normals across edges

Interpolate edge normals across polygon

Apply modified Phong model at each fragment

Comparison

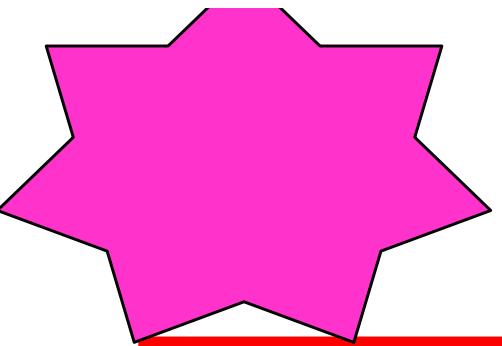
If the polygon mesh approximates surfaces with a high curvatures, **Phong shading may look smooth** while **Gouraud shading may show edges**

Phong shading requires much more work than Gouraud shading

Until recently not available in real time systems

Now can be done using **fragment shaders** (see Chapter 9)

Both need data structures to represent meshes so we can obtain vertex normals



You will be prompted when to **Upload** completed document to CANVAS as **score.doc** (example 100.doc).

Warning:

TA, at random, will inspect the **Uploaded document**.

If your score is not honestly entered you will get a zero.

Please rename document to **score.doc** (example **100.doc**)

Warning: if your score is not honestly honest you will get a zero.

Total score:

Class PARTICIPATION on Lecture 6.doc **ANSWER SHEET**
(Out of 100 points. Please record your own total score!)
(Attach as score.doc!)



VH, it closes at 7:00 PM

NEXT.

10.04.2023 (W 5:30 to 7)

(13)

Homework 6

Lecture 7

10.09.2023 (M 5:30 to 7)

(14)

PROJECT 2

10.11.2023 (W 5:30 to 7)

(15)

EXAM 2 REVIEW

10.16.2023 (M 5:30 to 7)

(16)

EXAM 2

0.04.2023 (W 5:30 to 7)
(13)

Homework 6

Lecture 7

HOMEWORK - 15%

15% of Total + :

Homework 6

Assignments Module | Not available until Oct 2 at 7:00pm | Due Oct 4 at 5:30pm | 400 pts



VH, publish

At 6:45 PM.

End Class 12

**VH, Download Attendance Report
Rename it:
10.2.2023 Attendance Report FINAL**

VH, upload Lecture 6 to CANVAS.