

Name:	Term #
<b>Homework 12 SOLUTIONS</b>	
(400 points)	

**NOTE:** Chapter 12 of the textbook shows the curves and surfaces. Part A is intended to be done by hand. Part B is an OpenGL application.

## A. (200 pts) Paper and Pencil

(Guidelines: Read the material from the textbook chapter, you can use textbook figures to exemplify your answer, use keywords, summarize your answer, but the answer cannot be longer the 7 lines!)

(There are 27 questions each worth 5 to 10 points)

#### 12.1 REPRESENTATION OF CURVES AND SURFACES

a. Explain.

ANSWER:

#### **12.1.1 Explicit Representation**

a. Write it for curves, lines, circles, and surfaces. ANSWER

#### **12.1.2 Implicit Representation**

a. Write it for curves, lines, circles, and surfaces. ANSWER

#### **12.1.3 Parametric Representation**

a. Write it for curves, lines, circles, and surfaces. ANSWER

#### 12.1.4 Parametric Polynomial Curves Representation

a. Write it for curves.

**ANSWER** 

#### 12.1.5 Parametric Polynomial Surfaces Representation

a. Write it for surfaces.

**ANSWER** 

#### **12.2 DESIGN CRITERIA**

a. Explain.

**ANSWER:** 

#### 12.3 PARAMETRIC CUBIC POLYNOMIAL CURVES

a. Write p(u)..

ANSWER:

#### **12.4 INTERPOLATION**

a. Write interpolation matrix.

ANSWER:

#### **12.4.1 Blending Functions**

a. Write them and draw them. ANSWER

#### **12.4.2 The Cubic Interpolating Patch**

a. Write p(u,v).

**ANSWER** 

#### 12.5 HERMITE CURVES AND SURFACES

a. Explain. ANSWER

#### 12.5.1 The Hermite form

a. Write p(u)" and the Hermite Geometry Matrix. ANSWER

#### **12.5.2 Geometric and Parametric Continuity**

a. Explain. ANSWER

#### 12.6 BEZIER CURVES AND SURFACES

a. Write the Bezier Geometry Matrix and Blending Functions. ANSWER:

#### **12.6.1 BEZIER Surface Patches**

a. Write p(u,v). ANSWER

#### **12.7 CUBIC B-SPLINES**

Explain ANSWER:

#### **12.7.1 The Cubic B-Spline Curve**

What are the B-spline geometry matrix and blending functions. ANSWER:

#### 12.7.2 B-Splines and Basis

Explain ANSWER:

#### **12.7.3 Spline Surfaces**

a. Write p(u,v). ANSWER:

#### **12.8 GENERAL B-SPLINES**

a. Write p(u). ANSWER:

#### **12.8.4 NURBS**

a. Write p(u).

ANSWER:

#### 12.9 RENDERING CURVES AND SURACES

a. Explain.

ANSWER:

#### **12.9.1 Polynomial Evaluation Methods**

a. Explain.

ANSWER:

#### 12.9.2 Recursive Subdivision of Bezier Polynomials

a. Write the values of the resulting points. Take a numerical example you will be tested on this.

ANSWER:

#### 12.9.3 Rendering Other Polynomial Curves by Subdivision

a. Write the conversion matrices for the Interpolation and B-Splines to Bezier.

ANSWER:

#### **12.9.4 Subdivision of Bezier Surfaces**

a. Explain.

ANSWER:

#### 12.11 ALGEBRAIC SURFACES

a. Explain.

ANSWER:

#### **12.11.1 Quadrics**

a. Write q(x,y,z).

ANSWER:

#### 12.11.2 Rendering of Surfaces by Ray Casting

a. Write n and p(a)

ANSWER:

#### 12.11.3 Subdivision Curves and Surfaces

a. Write s0 to s6

ANSWER:

#### 12.11.4 Mesh Subdivision

a. Explain and Write p

ANSWER:

# B. (200 pts) Visual Studio 2008 C++ Project Bezier Surfaces of Revolution

Create Visual Studio 2008 C++, Empty Project, Homework12:

It is often convenient to express the profile using Bezier or B-spline curves. We do this by selecting L+1 control points (Xk, Zk) and using them to create the curve

$$(X(v), Z(v)) = \sum_{k=0}^{L} (X_k, Z_k) N_{k,m}(v)$$

Below is an example of using a profile as a B-spline and it's surface of revolution.



b) the goblet surface of revolution





Given below is the 10 points of a Bezier mystery profile.

1	X	Z
0	1.4	2.25
1	1.3375	2.38125
2	1.4375	2.38125
3	1.5	2.25
4	1.75	1.725
5	2	1.2
6	2	0.75
7	2	0.3
8	1.5	0.075
9	1.5	0

Render the a) and b) as in the figure above for these 10 points.

Build and run this Project: Insert a screenshot of your output.

## **ANSWER:**

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                                      myCurve.h myCurve.c main.c
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Solution 'mohammedhm12' (1 project)
                                                                                          ■ main(int argc, char ** argv)
                                                                                                                                                 v
                                      (Global Scope)
                                                     glBindTexture(GL_TEXTURE_2D, textureNum);
glPixelStorei(GL_UNPACK_SWAP_BYTES,GL_TRUE);
glPixelStorei(GL_UNPACK_ALIGNMENT, 1);
                                           480
   imohammedhm12
                                           481
   🖃 🗁 Header Files
                                           482
         main.h
myCurve.h
                                           483
                                                     glTexParameterf(GL TEXTURE 2D, GL TEXTURE WRAP S, GL REPEAT);
                                                     glTexParameterf (GL_TEXTURE_2D, GL_TEXTURE_WRAP_T, GL_REPEAT);
                                           484
      Resource Files
                                                     glTexParameterf (GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER, GL_LINEAR);
glTexParameterf (GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER, GL_LINEAR);
glTexEnvf(GL_TEXTURE_ENV, GL_TEXTURE_ENV_MODE, GL_MODULATE);
                                           485
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                                           486
         main.c myCurve.c
                                           487
                                           488
                                                     glTexImage2D(GL_TEXTURE_2D,0,3,n,m,0,GL_RGB,GL_UNSIGNED_INT, image);
                                           489
                                                     free(image);
                                           490
                                                     fclose(fd):
                                           491
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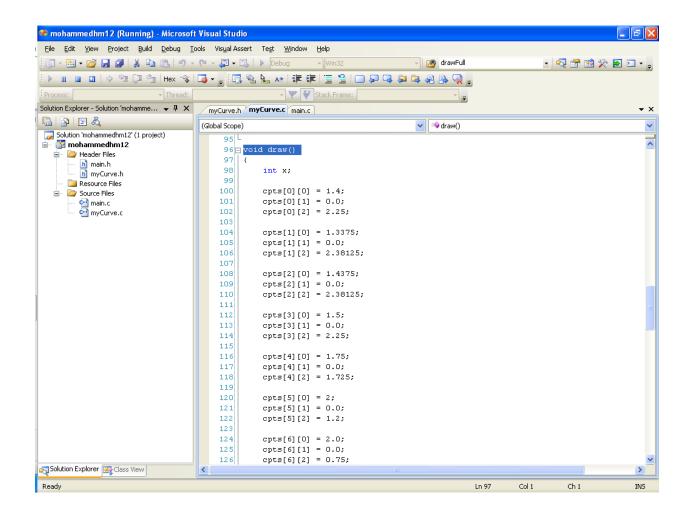
void main(int argc, char **argv)
                                           494 {
                                           495
                                                     glutInit(&argc, argv);
                                                     glutInitDisplayMode(GLUT_DOUBLE | GLUT_RGB | GLUT_DEPTH);
                                           496
                                                     glutInitWindowSize(500, 500);
                                           497
                                           498
                                                     glutInitWindowPosition(0,0);
                                                     glutCreateWindow("Homework 12 - Dr. Mo.");
                                           499
                                           500
                                                     glutReshapeFunc(myReshape);
                                                     glutDisplayFunc(display);
                                           501
                                           502
                                                     init();
                                           503
                                                     //readImage("rose.pnm", 3);
                                           504
                                                     glutKeyboardFunc(processNormalKeys);
                                           505
                                                     glutSpecialFunc(processSpecialKeys);
                                           506
                                                     glEnable(GL_DEPTH_TEST);
                                                     glClearColor (1.0, 1.0, 1.0, 1.0);
glEnable(GL_MAP1_VERTEX_3);
                                           507
                                           508
                                                     glutMainLoop();
                                           509
                                          510 43
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                                                                                           display()
                                                                                                                                                   ٧.
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                                                                         0.0, 1.0, 0.0); /* initial viewer location */
                                                                                                                                                   ^
                                             40
                                             41
   🖃 🗁 Header Files
                                             42 GLdouble rotate[] = {0.0, 0.0, 0.0};
         main.h
myCurve.h
                                                // Display function to dsiplay the Lower House
      Resource Files
                                             45 - void display (void)
   Source Files
         main.c myCurve.c
                                             47
                                                      glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
                                             48
                                                      glLoadIdentity();
                                             49
                                                          gluLookAt(viewer[0],viewer[1],viewer[2],
                                            50
                                                                      viewer[3],viewer[4],viewer[5],
                                            51
                                                                      viewer[6],viewer[7],viewer[8]);
                                            52
                                            53
                                                           glPushMatrix();
                                                               glRotated(1.66875,0.0,1.190625);
glRotated(rotate[0], 1.0, 0.0, 0.0);
glRotated(rotate[1], 0.0, 1.0, 0.0);
glRotated(rotate[1], 0.0, 0.0, 1.0);
glRotated(rotate[2], 0.0, 0.0, 1.0);
glTranslated(-1.66875,0.0,-1.190625);
                                            54
                                            55
                                            56
                                             57
                                             58
                                             59
                                                                            //draw();
                                             60
                                                                             drawFull();
                                             61
                                                           glPopMatrix();
                                                      glFlush();
                                             63
                                                     glutSwapBuffers();
                                             64
                                            65
                                             \, 66 \, // My reshare \, function that has glOrtho (camera settings).
                                             67 woid myReshape(int w, int h)
                                            68 | {
                                             69
                                                     glViewport(0, 0, w, h);
glMatrixMode(GL_PROJECTION);
                                             70
                                             71
                                                      glLoadIdentity();
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Ready
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                                                                                           ✓ arawFull()
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                                                                                                                                                  ^
                                           155 pvoid drawFull()
   🖃 🗁 Header Files
                                           156
         main.h
myCurve.h
                                           157
                                                     double x;
                                           158
      Resource Files
                                           159
                                                      int i;
   Source Files
                                           160
         main.c myCurve.c
                                           161
                                                      glEnable(GL_AUTO_NORMAL);
                                                     glMaterialfv(GL_FRONT, GL_AMBIENT, material[0] );
glMaterialfv(GL_FRONT, GL_DIFFUSE, material[1] );
glMaterialfv(GL_FRONT, GL_SPECULAR, material[2] );
                                           162
                                           163
                                           164
                                           165
                                                     glMaterialf( GL_FRONT, GL_SHININESS, material[3][0]);
                                           166
                                                     glBindTexture(GL_TEXTURE_2D, 3);
                                           167
                                           168
                                           169
                                                      for(x = 0; x < 360; x=x+.1)
                                           170
                                           171
                                                          glPushMatrix();
                                           172
                                                          glTranslated(1.66875,0.0,1.190625);
                                           173
                                           174
                                                               glRotated(x, 0, 0, 1);
                                           175
                                                                   glTranslated(-1.66875,0.0,-1.190625);
                                           176
                                                                    for(i=0; i<10; i++)</pre>
                                           177
                                                                       glTexCoord2f((cpts[i][0]+x/360)*2.0, (cpts[i][1]+x/360)*2.0);
                                           178
                                           179
                                                          glPopMatrix();
                                           180
                                           181 | }
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                                                                                   ✓ =• draw()
                                                                                                                                      ٧
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                                                 cpts[7][0] = 2;
                                                 cpts[7][1] = 0.0;
cpts[7][2] = 0.3;
                                        129
   🖃 🗁 Header Files
                                       130
        main.h
myCurve.h
                                       131
                                                 cpts[8][0] = 1.5;
                                       132
     Resource Files
                                                 cpts[8][1] = 0.0;
cpts[8][2] = 0.075;
                                       133
   Source Files
                                       134
        main.c myCurve.c
                                        135
                                                 cpts[9][0] = 1.5;
cpts[9][1] = 0.0;
cpts[9][2] = 0.0;
                                        136
                                        137
                                        138
                                        139
                                       140
                                                 /*for(x=0; x<10; x++)
                                       141
                                                     glPointSize(5.0);
                                       142
                                                     glBegin(GL_POINTS);
                                       143
                                       144
                                                         glVertex3f(cpts[x][0], cpts[x][1], cpts[x][2]);
                                       145
                                                     glEnd();
                                       146
                                       147
                                                 glFlush();
)*/
                                       148
                                       149
                                        150
                                                 ncpts = 10;
drawCurves();
                                       151
                                        152
                                       153 }
                                       154
                                       155 

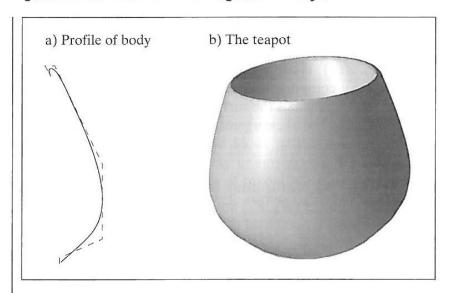
void drawFull()
                                       156 {
                                       157
                                                 double x;
                                       158
                                       159
                                                 int i;
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                                                                   - 🌁 drawFull
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 Process: [6504] mohammedhm12.ex€ ▼ Thread: [7564] Main Thread
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                                                                   ✓ drawCurves()
                             (Global Scope)
                                                                                                            ~
                                 67 /* Draw the indicated curves using the current control points. */
                                 68 - static void drawCurves()
   🚊 - 🗁 Header Files
                                 69 {
       main.h
myCurve.h
                                 70
                                        int i;
                                 71
                                        int step;
     Resource Files
                                        GLfloat newcpts[4][3];
   🖃 🗁 Source Files
                                 73
                                        float m[4][4];
       main.c myCurve.c
                                        /* Set the control point computation matrix and the step size. */
                                 75
                                        computeMatrix( m);
                                 76
                                 77
                                        step = 3:
                                 78
                                        glColor3fv(colors);
                                 79
                                        /* Draw the curves */
                                 80
                                        i = 0
                                 81
                                        while (i + 3 < ncpts)
                                 82
                                            /* Calculate the appropriate control points */
                                 83
                                 84
                                           vmult(m, &cpts[i], newcpts);
                                 85
                                           /* Draw the curve using OpenGL evaluators */
                                 86
                                            glMap1f(GL MAP1 VERTEX 3, 0.0, 1.0, 3, 4, &newcpts[0][0]);
                                           glMapGrid1f(30, 0.0, 1.0);
                                 89
                                            glEvalMesh1(GL_LINE, 0, 30);
                                 90
                                            /* Advance to the next segment */
                                 91
                                            i += step;
                                 92
                                 93
                                        glFlush();
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                                                                                                         → 1 ×
Locals
 Name
                                      Value
                                                                                                        Type ^
                                      0x0012fb14
                                                                                                        float [4][4
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⊕ • [0]
                                                                                                        float [4]
                                      0x0012fb14
Ready
/* Draw the indicated curves using the current control points. */
static void drawCurves()
     int i;
     int step;
     GLfloat newcpts[4][3];
     float m[4][4];
     /* Set the control point computation matrix and the step size. */
     computeMatrix( m);
        step = 3;
     glColor3fv(colors);
     /* Draw the curves */
     i = 0;
     while (i + 3 < ncpts)
           /* Calculate the appropriate control points */
           vmult(m, &cpts[i], newcpts);
           /* Draw the curve using OpenGL evaluators */
           qlMap1f(GL MAP1 VERTEX 3, 0.0, 1.0, 3, 4, &newcpts[0][0]);
           glMapGrid1f(30, 0.0, 1.0);
           glEvalMesh1(GL LINE, 0, 30);
           /* Advance to the next segment */
           i += step;
```

```
}
glFlush();
}
```

# **FIGURE 10.55** Bezier-based profiles for the teapot body.



condition insures that the different Bezier curves blend together with a continuous derivative (recall Section 10.1.2).

The lid of the teapot is also a surface of revolution, and is described in Case Study 10.8.