Experimental Methods: Lecture 1

Causal Inference and Alternative Designs

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Road Map to Lecture 1

- Potential outcomes and causal inference
- Average Treatment Effects (ATE)
- Alternative designs
 - Within and Between Subject
 - Multiple Arms
 - Conjoint
 - Treatment Adaptive

Why Should We Do Experiments? I

- Lauren E. Young (2019) The Psychology of State Repression: Fear and Dissent Decisions in Zimbabwe.
 APSR 113(1):140–155.
- What is the effect of the emotion of fear on citizen dissent in autocracies?
- How would we demonstrate that the effect of fear on dissent is unconfounded by other variables?
 - Characteristics that induce emotions
 - New information about a threat

Why Should We Do Experiments? II

- Lab-in-the-field experiment in Harare, Masvingo and Manicaland provinces in Zimbabwe
- Random assignment to treatment or control: Affective emotional memory task (AEMT)
- Ethical implications

Why Should We Do Experiments? III

- Sample: 647 participants from six communities in Zimbabwe where the NGO Voice for Democracy (VfD) has a network of mobilizer and informants; and affected by state-sponsored violence
 - Treatment 1: Enumerator asks to describe a situation of fear around politics and elections [political fear]
 - Treatment 2: Enumerator asks to describe a situation of general fears other than politics or elections [general fear]
 - Control: Enumerator asks to describe a situation that makes them relaxed
- Outcome: Propensity to dissent: hypothetical (via index) and behavioral (via selection of political wristband)

Why Should We Do Experiments? IV

Young (2019)

TABLE 3. The Fear Treatments Reduce Dissent

	Hypothetical		Behavioral	
	General	Political	General	Political
	fear	fear	fear	fear
	(1)	(2)	(3)	(4)
ATE ¹	-0.545	-0.773	-0.104	-0.189
SE ²	(0.077)	(0.080)	(0.050)	(0.053)
RI p- value ³	<0.001	<0.001	0.035	<0.001
<i>N</i>	484	486	329	326
Sample	A	.II	Wristl	band ⁴

¹The first row presents the estimated average treatment effects (ATEs) of the general and political fear treatments on the hypothetical measure of propensity to dissent in columns 1 and 2, and the behavioral measure in columns 3 and 4. ATEs are calculated based on assignment to treatment and weighted by inverse propensity scores by block.

²Robust standard errors (SEs) from linear regression analysis.

³The *p*-value is based on a two-tailed test using randomization inference.

⁴The estimate of the treatment effect on the wristband measure comes from the subset of the sample respondents who were offered a choice between two real wristbands. Results are similar for the full sample.

Why Should We Do Experiments? V

• Young (2019)

FIGURE 2. The Fear Treatments Cause Substantively Large Increases in the Proportion of Respondents Who Are Very Likely or Sure to Dissent During an Election Period Wear Opposition Shirt Attend Opposition Meeting Joke about President 60% 40% 20% Proportion %0 Refuse ZANU Meeting Reveal Opposition to Leader Testify in Trial 40% 20% TG TP TG TG Treatment

Defining Treatment

- The variable d_i indicates whether the *i*th subject is treated
- In the typical case of binary treatments, $d_i = 1$ means the ith subject receives the treatment
- d_i = 0 means the *i*th subject does not receive the treatment
- It is assumed that d_i is observed for every subject

Potential Outcomes

- Y_i : the potential outcome for subject i
- $Y_i(d_i)$: the outcome for subject i, written as a function of the treatment i received; it is generally the case that we observe only one of the potential outcomes for each i
- For the binary-valued treatment, there are two "potential outcomes":
 - $Y_i(1)$, the potential outcome for i conditional on i being treated
 - Y_i(0), the potential outcome for i conditional on i not being treated

Potential Outcome Schedule

- "Hypothetical"
- Comprehensive list of potential outcomes for all subjects
- Rows of this schedule are indexed by i, and the columns are indexed by d
- Potential outcomes for the fifth subject may be found in adjacent columns of the fifth row

Treatments as random variables

- Note on notation: We distinguish between d_i , the treatment that a given subject actually receives, and D_i , the treatment that could be administered hypothetically.
- D_i is a random variable (the ith subject might be treated in one hypothetical study and not in another).
- $Y_i(0)|D_i=1$: untreated potential outcome for subjects that would receive the treatment under a hypothetical random assignment.
- We use D_i when talking about the statistical properties of treatments.

Chattopadhyay & Duflo 2004

- Randomized policy experiment in India
- 1990s, one-third of village council heads reserved for women
- women.csv contains subset of data from West Bengal
- Gram Panchayat (GP) = level of government
- Analysis?
 - Was randomization implemented properly?
 - Conjecture: more drinking facilities under women
 - Conjecture: no effect on irrigation

Potential Outcomes Local Budget

	Budget share if village head is male	Budget share if village head is female	Treatment Effect
Village 1	10	15	5
Village 2	15	15	0
Village 3	20	30	10
Village 4	20	15	-5
Village 5	10	20	10
Village 6	15	15	0
Village 7	15	30	15
Average	15	20	5

Potential Outcome Subgroup

- Sometimes useful to refer to potential outcomes for a subset of the subjects
- Expressions of the form $Y_i(d)|X = x$ denote potential outcomes when the condition X = x holds
- For example, $Y_i(0)|d_i=1$ refers to the untreated potential outcome for a subject who actually receives the treatment

Conditional potential outcomes

- $Y_i(0)|d_i=1$: untreated potential outcome for subjects that receive treatment
- $Y_i(0)|d_i=0$: untreated potential outcome for subjects that do not receive treatment
- $Y_i(1)|d_i=1$: treated potential outcome for subjects that receive treatment
- $Y_i(1)|d_i=0$: treated potential outcome for subjects that do not receive treatment

Individual Level Causal Effect

 For subject i, the effect of the treatment is conventionally defined as the difference between outcomes across the two potential outcomes:

$$\delta_i = Y_i(1) - Y_i(0)$$

Alternatively:

$$Y_i = Y_i(0) + (Y_i(1) - Y_i(0))D_i$$

- Often referred to as the Rubin causal model; perhaps more appropriately, the Neyman-Holland-Rubin causal model
- The Fundamental Problem of Causal Inference only one of the two potential outcomes is realized, so that δ_i is typically non-operational

Realized Potential Outcomes

- Use lower-case letters for realization of the potential quantities (again, typically only one of the two potential outcomes is realized)
 - 1. $y_i(1)$, the outcome observed for i conditional on $d_i = 1$ (i is treated)
 - 2. $y_i(0)$, the outcome observed for i conditional on $d_i = 0$ (i is not treated)

The Fundamental Problem of Causal Inference

Table 1: Table 2.1, p35 Morgan and Winship, *Counterfactuals* and *Causal Inference*

Group	$Y_i(1)$	$Y_i(0)$
Treatment $(D_i = 1)$	Observable	Counterfactual
Treatment $(D_i = 0)$	Counterfactual	Observable

Observed Outcomes

- The connection between the observed outcome and the underlying potential outcome is given by the equation $Y_i = d_i Y_i(1) + (1 d_i) Y_i(0)$
- This equation indicates that the $Y_i(1)$ are observed for subjects who are treated, and the $Y_i(0)$ are observed for subjects who are not treated
- For any given subject, we observe either $Y_i(1)$ or $Y_i(0)$, not both

Observed Outcomes Local Budget

	Budget share if village head is male	Budget share if village head is female
Village 1	?	15
Village 2	15	?
Village 3	20	?
Village 4	20	?
Village 5	10	?
Village 6	15	?
Village 7	?	30

Average Treatment Effect

Average Treatment Effect:

$$E(\delta) = E[Y(1)] - E[Y(0)] = E[Y(1) - Y(0)]$$

- where the expectation is over a population, and so no subscript i
- This is operational, in that we can compute sample estimates of E[Y(1)] and E[Y(0)]: e.g., the sample averages:

$$\hat{y}(1) = \frac{1}{n_1} \sum_{i:d_i=1} y_i(1) \text{ and } \frac{1}{n_0} \sum_{i:d_i=0} y_i(0)$$

• where n_1 and n_0 are the number of subjects in groups d(1) and d(0) respectively

Randomization Generates Unbiased Estimates of Average Treatment Effect

• Rubin (1974) calls this:

$$\hat{\delta} = \hat{y}(1) - \hat{y}(0)$$
$$= \hat{y}_d$$

- ullet Under certain circumstances, this is an unbiased estimate of the population average treatment effect δ
- Why? How?
- Nice, informal treatment in "Two Formal Benefits of Randomization"

Properties of Random Assignment

- Under equal probability random assignment, the conditional ATE among the treated is the same as the conditional ATE among the control group, which is therefore the same as the ATE
- The expected $Y_i(0)$ in the treatment group is the same as the expected $Y_i(0)$ in the control group
- When random assignment is not used (i.e., observational research), the unbiasedness of the difference-in-means estimator becomes a matter of conjecture

Potential Outcomes: Core Assumptions

- We assume that each subject has two potential outcomes $Y_i(1)$ if treated and $Y_i(0)$ if not treated
- Each potential outcome depends solely on whether the subject itself receives the treatment
- Potential outcomes respond only to the treatment and not to some other feature of the experiment - such as assignment or measurement

The Beauty of Randomization: Independence

 Treatment status is statistically independent of potential outcomes and background attributes X

$$Y_i(0), Y_i(1), X \perp \!\!\! \perp D_i$$

 If a subject is randomly assigned to treatment, knowing wheether a subject is treated provides no information about the subject's potential outcomes, or background attributes.

Exclusion restriction

- Let $Y_i(z, d)$ be the potential outcome when $z_i = z$ and $d_i = d$ for $z \in (0, 1)$ and for $d \in (0, 1)$
- For example, if $z_i = 1$ and $d_i = 1$, the subject is assigned to the treatment group and receives the treatment
- Or z_i = 1 and d_i = 0 subject is assigned treatment but does not receive treatment
- The exclusion restriction is that $Y_i(1, d) = Y_i(0, d)$ subjects only respond to input from d_i
- The excludability assumption cannot be verified empirically because we never observe both and for the same subject

Classic Drug Experiment Example

- Treatment group receives a new drug
- Control group receives nothing
- Experiment confounds this treatment with receipt of a pill
- If patients respond to the pill rather than the pill's ingredients, excludability is violated
- Jeopardizes unbiasedness of the difference-in-means estimator

Non-interference

- Permits us to ignore the potential outcomes that would arise if subject i were affected by the treatment of other subjects
- Formally, we reduce the schedule of potential outcomes Y_i(d), where d describes all of the treatments administered to all subjects, to a much simpler schedule Y_i(d), where d refers to the treatment administered to subject i.
- Implies that so long as a subject's treatment status remains constant, that subject's outcome is unaffected by the particular way in which treatments happened to be assigned to other subjects

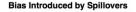
Non-interference violated

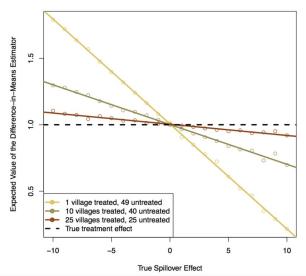
- Police patrols displace crime from treated to untreated areas
- Non-interference violated if your estimand is following:
 - Average potential outcome when a block is treated minus average potential outcome when no blocks are treated
- If police patrols displace crime from treated to untreated areas, observed outcomes in control will not be potential outcomes when no treatment administered anywhere
- Estimated ATE will tend to exaggerate the true ATE

Core assumptions violated?

- Public Health: Providing an infectious disease vaccine to some individuals may decrease the probability that nearby individuals become ill
- Politics: Election monitoring at some polling stations may displace fraud to neighboring polling stations
- Economics: Lowering the cost of production for one firm may change the market price faced by other firms
- Marketing: Advertisements displayed to one person may increase product recognition among her work colleagues

Spillover





Estimating Spillover Effects

- $Y_{00} \equiv Y(Z_i = 0, Z_j = 0)$: Pure Control
- $Y_{10} \equiv Y(Z_i = 1, Z_j = 0)$: Directly treated, no spillover
- $Y_{01} \equiv Y(Z_i = 0, Z_j = 1)$: Untreated, with spillover
- $Y_{10} \equiv Y(Z_i = 1, Z_j = 1)$: Directly treated, with spillover
- We assume...
 - treatment assignments of non-neighboring units do not alter a unit's potential outcomes
 - model spillovers as a binary event: either some neighboring unit is treated, or not

Spillover

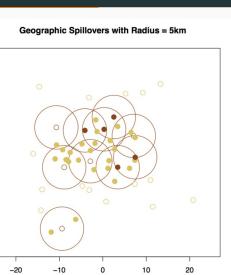
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10

0 -

-10

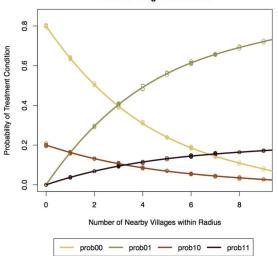
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Control, No Spill
 Treated, No Spill
 Treated, Spill

Spillover





https://egap.org/resource/

10-things-to-know-about-spillovers/

```
# Define two helper functions
complete ra <- function(N,m){
  assign <- ifelse(1:N %in% sample(1:N,m),1,0)
  return(assign)
get condition <- function(assign, adimat){
  exposure <- adimat %*% assign
  condition <- rep("00", length(assign))
  condition[assign==1 & exposure==0] <- "10"
  condition[assign==0 & exposure>0] <- "01"
  condition[assign==1 & exposure>0] <- "11"
  return(condition)
N <- 50 # total units
m <- 20 # Number to be treated
# Generate adjacency matrix
set.seed(343)
coords <- matrix(rnorm(N*2)*10, ncol = 2)
distmat <- as.matrix(dist(coords))
true adjmat <- 1 * (distmat<=5) # true radius = 5
diag(true adimat) <-0
# Run simulation 10000 times
Z mat <- replicate(10000, complete ra(N = N, m = m))</pre>
cond mat <- apply(Z mat, 2, get condition, adjmat=true adjmat)
# Calculate assignment probabilities
prob00 <- rowMeans(cond mat=="00")
prob01 <- rowMeans(cond mat=="01")
prob10 <- rowMeans(cond mat=="10")
prob11 <- rowMeans(cond mat=="11")
```

Estimation

Difference-in-means is an unbiased estimator of ATE

$$E\left[\frac{\sum_{1}^{m} Y_{i}}{m} - \frac{\sum_{m+1}^{N} Y_{i}}{N-m}\right] = E\left[\frac{\sum_{1}^{m} Y_{i}}{m}\right] - E\left[\frac{\sum_{m+1}^{N} Y_{i}}{N-m}\right]$$
$$= E[Y_{i}(1)] - E[Y_{i}(0)]$$
$$= E[\tau_{i}] = ATE$$

Estimation

Difference-in-means estimator implemented via OLS

$$Y_{i} = Y_{i}(0)(1 - d_{i}) + Y_{i}(1)d_{i}$$

$$= Y_{i}(0) + Y_{i}(1) - Y_{i}(0))d_{i}$$

$$= \mu_{Y(0)} + [\mu_{Y(1)} - \mu_{Y(0)}]d_{i} + Y_{i}(0) - \mu_{Y(0)}$$

$$+ [(Y_{i}(1) - \mu_{Y(1)}) - (Y_{i}(0) - \mu_{Y(0)})]d_{i}$$

$$= \alpha + \beta d_{i} + \epsilon_{i},$$

 $\alpha = \mu_{Y(0)}$ (average of untreated potential outcomes for all N), $Y_i(0) =$ untreated potential outcome $\beta = \mu_{Y(1)} - \mu_{Y(0)}$

and ϵ_i comprises idiosyncratic variation in untreated responses plus idiosyncratic variation in treatment effects.

Chattopadhyay & Duflo 2004

- Randomized policy experiment in India
- 1990s, one-third of village council heads reserved for women
- women.csv contains subset of data from West Bengal
- Gram Panchayat (GP) = level of government
- Analysis?
 - Was randomization implemented properly?
 - Conjecture: more drinking facilities under women
 - Conjecture: no effect on irrigation

Name	Description
GP	An identifier for the Gram Panchayat (GP)
village	identifier for each village
reserved	binary variable indicating whether the GP was reserved for women leaders or not
female	binary variable indicating whether the GP had a female leader or not
irrigation	variable measuring the number of new or repaired irrigation facilities in the village since the reserve policy started
water	drinking-water facilities in the village since the reserve policy started

Table 4.6: The Variable Names and Descriptions of the Women as Policy Makers Data.

```
women <- read.csv("women.csv")

##proportion of female politicians in
    reserved GP vs. unreserved GP
mean(women$female[women$reserved] == 1)
[1] 1
mean(women$female[women$reserved == 0])
[1] 0.07476636</pre>
```

```
## drinking-water facilities
mean(women$water[women$reserved == 1]) -
    mean(women$ water[women$ reserved == 0])
## [1] 9.25223
## irrigation facilities
mean(women4irrigation[women\$reserved == 1]) -
    mean(women$irrigation[women$reserved == 0])
\#\# [1] -0.3693319
```

What is a treatment, after all?

Within-subject designs

- Subject i receives multiple treatments at multiple time points t
- Behavioral games; answering questions

Now potential outcomes can be written as $Y_{t-1,t,t+1}$ as a function of whether treatment is administered in the preceding, current, or next time period

ATE is now $E[Y_{010} - Y_{000}]$. Given no anticipation $(Y_{001} = Y_{000})$ and no persistence $(Y_{100} = Y_{000})$, the within-subject design identifies ATE

Within-subject designs

- Costs
 - Demand effects
 - Confounders from multiple treatments (assumptions stated above)
 - Complexity and validity: willingness to pay in Charness et al 2012
- Benefits
 - Internal validity unrelated to assignment mechanism
 - Statistical power
 - Proximity to theory
- Example: Bellemare and Shearer 2009

Between-subject designs

- Formal setup as all of part 1 of today's lecture
- Each individual exposed to 1 treatment
- ATE as difference in means of different groups of individuals
- Costs
 - Natural anchor with respect to (economic) decision-making?
 - Statistical power
- Example: Gneezy and List (2006)
- Overall: confounders > power

Within vs Between: Bellemare et al. 2016

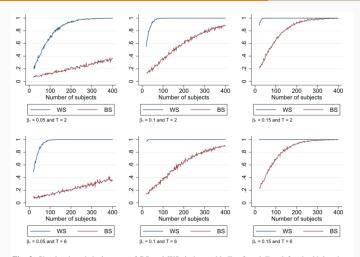


Fig. 2 Simulated statistical power of BS and WS designs with T=2 and T=6 for the high-noise scenario. Simulations based on values $\sigma_{\mu}^2=0.09$ and $\sigma_{\epsilon}^2=0.02$. Results for the BS design are computed by allocating the same number of subjects to control and treatment conditions for all periods. Results for the WS design are computed by assigning all subjects to the same number of control and treatment periods

- Q. Why would you want to collect the same information twice, pre-treatment and post-treatment? Do you gain anything?
- A. Yes, precision!
- Instead of having a single outcome measure Y_i , redefine as *change* from pre-test to post-test
- We compare 2 quantities:
 - $(Y_i X_i)$ for $d_i = 1$
 - $(Y_i X_i)$ for $d_i = 0$
 - difference-in-differences estimator

Is this estimator unbiased?

$$E(\widehat{ATE}) = E[Y_i - X_i | D_i = 1] - E[Y_i - X_i | D_i = 0]$$

$$= E[Y_i | D_i = 1] - E[X_i | D_i = 1] - E[Y_i | D_i = 0] - E[X_i | D_i = 0]$$

$$= E[Y_i(1)] - E[Y_i(0)]$$

In general, difference-in-means and difference-in-differences generate unbiased estimates – but what if we also care about sampling variability of this estimator?

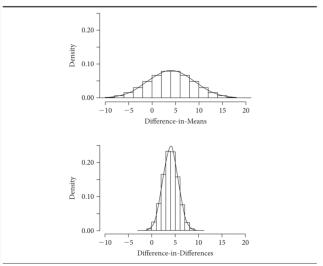
In general,
$$SE(\widehat{ATE}') < SE(\widehat{ATE})$$
 if either holds

$$Cov(Y_i(0), X_i) + Cov(Y_i(1), X_i) > Var(X_i)$$

$$\frac{\textit{Cov}(\textit{Y}_i(0), \textit{X}_i)}{\textit{Var}(\textit{X}_i)} + \frac{\textit{Cov}(\textit{Y}_i(1), \textit{X}_i)}{\textit{Var}(\textit{X}_i)} > 1.$$

That is, when a covariate X_i strongly predicts potential outcomes

Sampling distribution of two estimators: difference-in-means and difference-in-differences



- Define a factorial experiment as an experiment involving factors 1 and 2, with factor 1 conditions being A and B, and factor 2 conditions being C and D and E
- Then, allocate subjects at random to every possible combination of experimental conditions
- {*AC*, *AD*, *AE*, *BC*, *BD*, *BE*}

From Rosen 2010

	Colin		Jose	
	Good grammar	Bad grammar	Good grammar	bad grammar
% Received reply	52 (100)	29 (100)	37 (100)	34 (100)
(**)	()	()	(===)	()

This design requires us to be especially careful with defining the causal estimand – what quantity are we interested in in this application?

Quiz: Why would these two models estimate the same quantities from the Rosen 2010 experiment?

 $\{CG, JG, CB, JB\}$ are indicator variables for each of the 4 treatment groups

 $J_i = 1$ if Jose Ramirez; $G_i = 1$ if good grammar

$$Y_i = b_1 CG + b_2 JG + b_3 CB + b_4 JB + u_i$$

 $Y_i = a + bJ_i + cG_i + d(J_iG_i) + u_i$

What quantity in the table do each of the coefficients represent?

- A special case: conjoint experiments
- What components of the manipulation produce the observed effect?
- We can answer this with a 2x2 design as shown above, but sometimes things are multidimensional
- Subjects chose between *J* profiles, *K* times
 - Each profile has a set of L discretely valued attributes
 - D is total number of levels for attribute I

Hainmueller et al 2014

Please read the descriptions of the potential immigrants carefully. Then, please indicate which of the two immigrants you would personally prefer to see admitted to the United States.

	Immigrant 1	Immigrant 2
Prior Trips to the U.S.	Entered the U.S. once before on a tourist visa	Entered the U.S. once before on a tourist visa
Reason for Application	Reunite with family members already in U.S.	Reunite with family members already in U.S.
Country of Origin	Mexico	Iraq
Language Skills	During admission interview, this applicant spoke fluent English	During admission interview, this applicant spoke fluent English
Profession	Child care provider	Teacher
Job Experience	One to two years of job training and experience	Three to five years of job training and experience
Employment Plans	Does not have a contract with a U.S. employer but has done job interviews	Will look for work after arriving in the U.S.
Education Level	Equivalent to completing two years of college in the U.S.	Equivalent to completing a college degree in the U.S.
Gender	Female	Male

	Immigrant 1	Immigrant 2
If you had to choose between them, which of these two immigrants should be given priority to come to the United States to live?	0	0

AMCE for Attribute Levels in Conjoint

$$\begin{aligned} \operatorname{rating}_{ijk} = & \beta_0 + \beta_1 [\operatorname{age}_{ijk} = 75] + \beta_2 [\operatorname{age}_{ijk} = 68] + \\ & \beta_3 [\operatorname{age}_{ijk} = 60] + \beta_4 [\operatorname{age}_{ijk} = 52] + \\ & \beta_5 [\operatorname{age}_{ijk} = 45] + \epsilon \end{aligned}$$

- The reference category is 36 years old
- β s are estimators for AMCE for ages 68, 75, etc. compared to 36

Types of Sequential Randomised Experiments

- Non-adaptive assignment probabilities fixed
- Treatment-adapative change based on number of subjects in treatment
- Covariate-adaptive change based on covariate profiles of new and previous subjects
- Responsive-adaptive change as function of previous units' outcomes

- ATE is not always quantity of interest
- Particularly online firms such as Google, Tiktok, FB, etc.
 - Randomly assign sampled users to different arms and dynamically re-orient sample based on which is more successful/more informative
 - Identify which of many will get the most clicks
- But also of interest to political scientists: Ballot initiatives and malfeasance information
- How do adaptive multi-arm trials work?

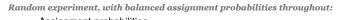
Regret

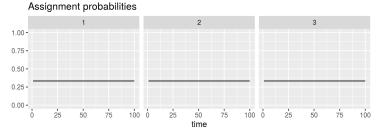
 the difference between the average outcomes we would have observed under optimal assignment and the average outcomes we actually observe under a given assignment algorithm

Example

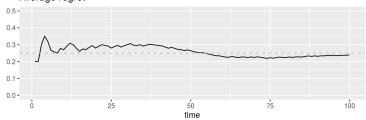
- if the best prototype gives us a 90% click-through rate on average
- a different prototype gives us a 40% rate on average
- the regret from assigning the sub-optimal arm is 0.5

Regret: True arms 1 (.8) 2 (.6) 3 (.3)



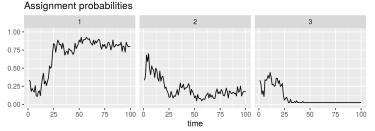


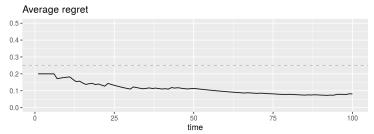
Average regret



Regret: True arms 1 (.8) 2 (.6) 3 (.3)

 $Adaptive\ experiment, updating\ treatment\ assignment\ probabilities\ based\ on\ observed\ outcomes:$





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Molly Offer-Westort et al 2020

	Minimum Wage	Right to Work
Question Text	Imagine that the following ballot measure were up for a vote in your state. [ballot measure text]. If this measure were on the ballot in your state, would you vote in favor or against? [I would vote in favor of this measure, I would vote against this measure]	Imagine that the following ballot measure were up for a vote in your state. [ballot measure text]. If this measure were on the ballot in your state, would you vote in favor or against? [I would vote in favor of this measure, I would vote against this measure]
Proposal 1	The measure would: increase the minimum wage [from (currently) fo (current + 1) per hour, adjusted annually for inflation, and provide that no move than \$13.02 per hour in tip income may be used to offset the minimum wage of employees who regularly receive tips.	The measure would jamend the State Constitution to prohibit, as a condition of employment, forced membership in a labor employment, forced membership in a labor fees, in full or pro-rata ("fair-shear"), to a minon fees, in full or pro-rata ("fair-shear"), to a minon the second of the second seco
Proposal 2	The measure would: raise the minimum wage [from current] to (current +1) per hour effective September 30th, 2021. Bach September 30th thereafter, minimum wage shall increase by \$1.00 per hour until the minimum wage reaches (current + 5) per hour on September 20th, 2026. From that potent to being adjusted annually for inflation starting September 30th, 2027.	The measure [reads / would amend the State Constitution to read]: The right of persons to work may not be denied or abridged on account of membership or nonmembership in any labor union or labor erganization, and all contracts in negation or abrogation of such rights are hereby declared to be invalid, void, and unenforceable.
Proposal 3	The measure reads: Shall the minimum wage for adults over the age of 18 be raised [from {current}] to {current + 1} per hour by January 1, 20197	The measure would [amend the State Constitution to]: bas any new employment contract that requires employee to resign from or belong to a union, pay union dues, or make other payment to a union. Required contributions to charity or other third party instead of payments to charity or other third party instead of payments to the party of the party of the party of the party of the payroll deduction to unions. Violations of the section is a misdemensure.
Proposal 4	The measure would: raise the minimum wage [from {current}] to {current + 1} per hour worked if the employer provides health benefits, or {current + 2} per hour worked if the employer does not provide health benefits.	The measure [reads / would amend the State Constitution to readji: No person shall be deprived of life, liberty or property without due process of law. The right of persons to work shall not be denied or abridged on account of membership or nonmembership in any labor union, or labor organization.
Proposal 5	The measure would: raise the State minimum wage rate [from {current}] to at least {current + 1} per hour, and require annual increases in that rate if there are annual increases in the cost of living.	

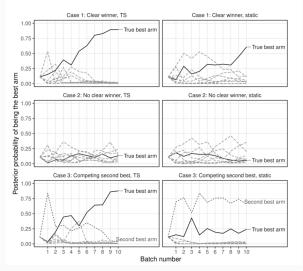
- When researchers are initially agnostic about the relative performance of the K arms, priors are distributed uniformly over parameter space, i.e. Beta(1, 1)
- In each t, treatment is randomly assigned according to probability of arms being best (= highest success rate)

$$P\bigg[\Theta_{k} = \max_{k} \{\Theta_{1}, ..., \Theta_{K}\} | (X_{1}^{n_{1,t}}, ..., X_{K}^{n_{K,t}})\bigg]$$

for K arms, vector of responses under treatment arm k observed up until and including $t X_k^{\{n_{k,t}\}}$ and Θ_k distributions of success rates

- Simulations to illustrate design and estimation
- Sample 100 observations for each of 10 periods, updating posterior probability of being best after each period, and assign treatment probabilities in the subsequent period accordingly
- In the first case, one arm has a true 0.20 probability of success, and the remaining 8 arms have a 0.10 probability of success

Figure 1: Simulated Posterior Probabilities Over Time, Thompson Sampling and Static Designs



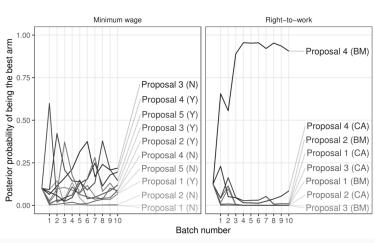


Figure 3: Study One, Overtime Posterior Probabilities

Adaptive experimentation tutorial

- Molly Offer-Westort, Vitor Hadad, Susan Athey
- https://mollyow.shinyapps.io/adaptive/