

as you are in class 7 you already know some mathematics. so i am going to give some contest related instructions that matches your math syllabus.

GCD / LCM

gcd means greatest common divisor.
lcm means least common multiple.

gcd(x, y) = gcd of x and y
lcm(x, y) = lcm of x and y

in c programming we shall use this 2 functions

```
long long gcd(long long x, long long y)
long long lcm(long long x, long long y)
```

they take 2 parameters and returns gcd or lcm in long long form.

relation between gcd and lcm

$\text{gcd}(x, y) * \text{lcm}(x, y) = x * y$

using this formula we can find the lcm of 2 numbers if their gcd is known.

property of gcd and lcm

$\text{gcd}(a, b, c) = \text{gcd}(\text{gcd}(a, b), c) = \text{gcd}(a, \text{gcd}(b, c))$

$\text{lcm}(a, b, c) = \text{lcm}(\text{lcm}(a, b), c) = \text{lcm}(a, \text{lcm}(b, c))$

*see gcd_lcm.c to learn about them inside codes folder.

minimizing(kata-kati) a fraction

if you have to consider a fraction(vog-nangsho) in C then you can take one variable for numerator(lob) and another for denominator(hor).

say it is 3/12

so you can code like,

```
int a = 3, b = 12;
```

you can also take an array of size 2 and consider the 0th index as numerator and 1st index as denominator.

like,

```
long long f[2];
f[0] = 3; f[1] = 12;
```

to minimize a fraction you have to divide both numerator and denominator by their gcd.

so to minimize first find,
now,
done !

```
long long k = gcd(f[0], f[1]);
f[0] = f[0]/k; f[1] = f[1]/k;
```

prime numbers

prime number is known to you. many difficult problems exist in contest arena related to primes. but i hope if you face any it will be simpler.

the first question anyone can ask about prime is - is this number a prime ? yes or no. if you can answer, then the later part of the problem becomes easy.

so how to decide if a number is prime or not ?

method 1

say, a value n is given we have to test its primality. we can easily start from 2 to $n-1$ and test if n can be divided by any of them. if any of them can divide n we can stop the test there and report n is composite. if none of them can divide n we can report n is prime.

this process is done in `prime_method_1.c` file.

see the code and try to understand the `isPrime(long long n)` function.

method 2

method 1 is very slow and time consuming. say the number $n = 100$. it can be divided by 2 so its not prime.

if $n = 113$, it is odd.

it will never be divisible by any even numbers like, 4, 6, 8 etc. why ? because if it is divisible by any even number, then it is already divisible by 2 !

so we don't need to test with any even value. this method is made clear in `prime_method_2.c` file. look at that. we are jumping with odd numbers.

method 3

from number theory you know that, to know if n is prime or not, it is enough to check its divisibility from 2 to its square root.

e.g. $n = 145$, $\text{sqrt}(n) = \text{sqrt}(145) = 12.0459$

so it is enough to test its divisibility from 2 to 12.

this method is made clear in `prime_method_3.c`.

see there is a slight difference inside the for loop of `isPrime()` function.

this method is faster and easiest for you.

method 4

method 3 is faster but not so fast. there is a method called Sieve of Eratosthenes which is mostly used in contest. the main idea is to generate all the prime from 0 to a higher range at the beginning of the program in an array. then using the array we can directly tell about the primality of a number.

why is this useful ?

when you are using method 3 or previous ones, there for each number you are starting the test from 2 until the number or its square root.

e.g. $n = 100$

you run the test counting from 2 till 99 (method 1 or 2) or till square root of 99.

again if $n == 50$ you do the same from 2 till 49 or $\text{sqrt}(50)$

the counting process goes again and again.

but in sieve of eratosthenes we do the counting only once.

this method is somewhat complex. i will explain in brief how it works.

in school you did it.

first write from 1 to the range of number you want to find primes within. say it is 20.

```
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
```

now cross 1 as it is not prime.

```
x 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
```

now you get 2 at the start. so it is a prime. now cross all that are divisible by 2. it becomes,

```
x 2 3 x 5 x 7 x 9 x 11 x 13 x 15 x 17 x 19 x
```

now you get another prime 3.

now cross all that are divisible by 3 if not crossed already. 9 and 15 are crossed out. it becomes,

```
x 2 3 x 5 x 7 x x x 11 x 13 x x x 17 x 19 x
```

then 5 is another prime found. cross any number divisible by 5. none found. because, 10, 15 and 20 are already crossed. so 7 is prime. none is found as a victim of 7.

likewise, 11, 13, 17 and 19 are found as primes.

the algorithm given is prime_method_4.c works in this way and also uses the square root technique described in method 3.

how to use this method ?

take a global array called P.

then immediately after main run the function named sieve().

done. the method will generate a list of prime from 0 to 1000000

now, the thing happened here is,

```
if n is a prime number then p[n] == 1
if n is not prime then P[n] == 0
```

you can use an if condition to test it. see prime_method_4.c to understand.

in contest try to use this method 4. it must work within the time limit. but i hope method 3 will work for your contest. if method 3 fails and gives TLE you must use method 4 – the sieve().

***i declared the size of P array 1000000 + 10 for safety. its always good to keep some extra space from the maximum limit. it helps us to ignore mistakes.**

Fibonacci series

fibonacci series is

1 1 2 3 5 8 13 21 ...

every element is the sum of previous two element and by default the first two element is 1.

a program named fibo.c is given to print first n numbers of the fibonacci series. it may help.