# **Elastic and Plastic Properties**

- Elastic deformation: non-permanent and reversible deformation
- Young's modulus: stiffness of a material

$$egin{aligned} \circ & \sigma = E arepsilon \ \circ & \sigma = \sigma_{eng} = rac{F}{A_o} \ \circ & arepsilon = arepsilon_{eng} = rac{\Delta L}{L_o} \end{aligned}$$

- $\circ$  Within the same class of materials, higher E means higher melting point
- Modulus of resilience: energy absorbed during elastic deformation area under stress-strain curve

$$\bullet \ \mathrm{MOR} = \frac{\sigma_y^2}{2E}$$

• Poisson's ratio: applicable for isotropic materials

$$\circ \ \nu = -\frac{\varepsilon_x}{\varepsilon_z} = -\frac{\varepsilon_y}{\varepsilon_z}$$

ullet Bond length:  $r_o$  is the interatomic distance that minimizes potential energy

$$E \propto \left(rac{dF}{dr}
ight)_{r_o}$$

- Yield strength:  $\sigma_y$
- Ultimate tensile strength:  $\sigma_{UTS}$
- Fracture (tensile) strength:  $\sigma_f$
- <u>Ductility:</u> amount of deformation before failure (% elongation or % area reduction)
- Toughness: energy absorbed before failure
- Hardness: resistance to localized plastic deformation

# 9. Crystal Strengthening

- 1. Grain size reduction smaller grain size means more area at grain boundaries, which impede dislocation motion
  - $\circ$  Hall-Petch equation:  $\sigma_y = \sigma_o + k_y d^{-1/2}$
- 2. Solid-Solution substitutional and interstitial atoms cause stresses in lattice, which impede dislocation motion
- 3. Work hardening plastic deformation (work hardening) strengthens metals by <u>increasing</u> <u>dislocation density</u> and <u>dislocation-dislocation interaction</u>, which impedes dislocation motion

$$egin{array}{ll} \circ & \sigma_T = K arepsilon_T^n \ \circ & \% CW = rac{A_o - A_d}{A_o} \cdot 100 \end{array}$$

# 10. Recrystallization and Grain Growth

- ullet Homologous temperature:  $T_H=rac{T_{
  m deformation}}{T_{
  m melting\ point}}$  (in Kelvin)
  - $\circ~$  Pure metals:  $T_H < 0.4$  cold work,  $T_H > 0.4$  hot work

- $\circ~$  Alloys:  $T_H < 0.6$  cold work,  $T_H > 0.6$  hot work
- Rolling (work hardening) increases strength but decreases ductility. Grains are elongated
- <u>Annealing:</u> reverse effects of work hardening by releasing energy stored during work hardening,
   which drives recovery and recrystallization
  - Results in smaller grains

#### 1. Recovery

 Restoration of electrical and thermal properties. Dislocations reconfigure to have lower strain energy

#### 2. Recrystallization

- New strain-free equiaxed grains with low dislocation densities are formed
- o Recrystallization temperature: temperature at which recrystallization completes in one hour
- o Recrystallization temperature decreases with increased cold work
- $\circ$  With more cold work, activation energy Q decreases so the rate of recrystallization at a given temperature increases
- Recrystallization occurs more rapidly in pure metals than alloys because solute atoms reduce mobility of grain boundaries

#### 3. Grain growth

- Grains grow to reduce grain boundaries and energy within material
- $\circ$   $d^n d^n_0 = Kt$

#### 11. Fracture

Ductile versus brittle fracture

- fracture toughness  $K_c$ : material's resistance to brittle fracture under presence of crack. Describes stress situation around crack tip
- $K_t$ : stress concentration factor

Griffith equation: calculates critical stress for crack propagation

### 12. Fatigue

Fatigue failure requires tensile stresses

- <u>Shot-Peening:</u> stores residual compressive stresses
- <u>Case-Hardening</u>: carbon or nitrogen rich surface created through atomic diffusion

S-N curve: relates fatigue strength and fatigue life (number of cycles until failure)

### 13. Ductile-Brittle Transition

- Drastic reduction in ductility as temperature is decreased
  - o Ductile failure: due to dislocation movement
  - o Brittle failure: due to cracks
- Higher strain rate increases the DBT temperature
- Higher carbon % of steel increases DBT temperature

Simulates severe conditions. Difference in potential energy is the absorbed energy

## 14. Creep Failure

- Time dependent permanent deformation of materials subjected a constant load at elevated temperatures
- Occurs at above  $0.4T_m$  for metals
- 1. Primary creep: due to work hardening
- 2. <u>Secondary creep:</u> constant creep rate due to balancing of work hardening and recovery. 90% of creep time
- 3. <u>Tertiary creep:</u> acceleration of creep until rupture
- Higher temperature and higher stress increase creep rate
- Creep resistant: high melting temperature, high elastic modulus, and large grain size
- <u>Larson-Miller parameter:</u> relates temperature and time to rupture

### 15. Corrosion

- Corrosion: chemical attack, resulting in oxidation (loss of electrons)
  - Driving force is reduction of energy
- Ingredients
  - Reduction in energy
  - Water or moisture to act as medium for ion conduction and ionic transport
  - Source of oxidant (normally O2, sometimes sulfur)
  - Mass transport of oxidant to the metal
- Stress corrosion: occurs at regions of high stress
- Galvanic corrosion:
  - o More reactive metal (anode) is oxidized it corrodes
  - Less reactive metal (cathode) is reduced it is protected
  - $\circ$  Galvanic series: ranks reactivity of metals and alloys in seawater at  $25^{\circ}\mathrm{C}$
  - EMF series: pure metals
- Corrosion protection
  - Protective oxide impedes oxygen transfer to metal interior. For example, chromium forms an oxide layer
  - Physical barriers uses less chemically active metal layer, which inhibits contact with water and oxygen. For example, nickel, tin, chromium
  - Sacrificial (cathodic) protection uses more chemically active metal layer, which corrodes while main metal stays intact

## 16. Phase Diagrams

- <u>Phase:</u> homogeneous portion of system that has uniform physical and chemical characteristics
  - Equilibrium conditions

Binary Isomorphous Systems: two elements, liquid and solid regions each contain one phase

Liquidus line: boundary between all liquid and liquid/solid two phase region

- Solidus line: boundary between all solid and liquid/solid two phase region
- <u>Phase composition:</u> use tie line intersection with liquidus and solidus to find composition of liquid and solid phases
- Lever rule: gives mass fraction of liquid and  $\alpha$ -solid. Assumes infinite diffusion, so mass is distributed instantaneously
- <u>Non-equilibrium cooling:</u> cored structures, where center of solid particles have higher concentration

# 17. Phase Diagrams II

<u>Binary Eutectic Systems:</u> two elements, and there is a single chemical composition that solidifies at a lower temperature than any of its constituents

- Cooling at eutectic temperature: <u>lamellae</u> (alternating layers) of  $\alpha$  and  $\beta$  form
- If cooling crosses eutectic isotherm, then lamellae will form, in addition to primary regions. There will be primary  $\alpha$ , eutectic  $\alpha$ , and  $\beta$