INF4820: Algorithms for Artificial Intelligence and Natural Language Processing

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Common Lisp Fundamentals

Language Technology Group (LTG)

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- ightarrow Toolkit of ('clever') methods for representation and problem solving.





Why Common Lisp?



Eric S. Raymond (2001), How to Become a Hacker.

Lisp is worth learning for the profound enlightenment experience you will have when you finally get it; that experience will make you a better programmer for the rest of your days, even if you never actually use Lisp itself a lot.

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Lisp is worth learning for the profound enlightenment experience you will have when you finally get it; that experience will make you a better programmer for the rest of your days, even if you never actually use Lisp itself a lot.

- High-level and efficient language with especially strong support for symbolic and functional programming.
- ► Rich language: multitude of built-in data types and operations.
- ► Easy to learn:
 - extremely simple syntax,
 - straightforward semantics.
- ► ANSI-standardized and stable.
- ► Incremental and interactive development.

Lisp



- Conceived in the late 1950s by John McCarthy—one of the founding fathers of AI.
- Originally intended as a mathematical formalism.
- A family of high-level languages.
- Several dialects, e.g. Scheme, Clojure, Emacs Lisp, and Common Lisp.
- Although a multi-paradigm language, functional style prevalent.





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- ? 42
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- ? t
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- ? t
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- ? nil \rightarrow nil



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- \rightarrow t
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- \rightarrow nil
- ? pi
- ightarrow 3.141592653589793d0



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- ? 42
- \rightarrow 42
- ? t
- \rightarrow t
- ? nil
- ightarrow nil
- ? pi
- \rightarrow 3.141592653589793d0
- ? foo
- \rightarrow error; unbound

A Note on Terminology



- ► Lisp manipulates so-called *symbolic expressions*.
- AKA s-expressions or sexps.
- Two fundamental types of sexps;
 - 1. atoms (e.g., nil, t, numbers, strings, symbols)
 - 2. lists containing other sexps.
- ► Sexps are used to represent *both* data and code.



- "Parenthesized prefix notation"
- First element (prefix) = operator (i.e. the procedure or function).
- The rest of the list is the operands (i.e. the arguments or parameters).
- Use nesting (of lists) to build compound expressions.
- Expressions can span multiple lines; indentation for readability.

Examples

? (+ 1 2)





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- ? (+ 1 2)
- \rightarrow 3
- ? (+ 1 2 10 7 5)
- \rightarrow 25



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- ? (/ (+ 10 20) 2)
- \rightarrow 15



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- ? (+ 1 2)
- \rightarrow 3
- ? (+ 1 2 10 7 5)
- $\rightarrow 25$
- ? (/ (+ 10 20) 2)
- \rightarrow 15
- ? (* (+ 42 58) (- (/ 8 2) 2))
- → 200

The Syntax and Semantics of CL



```
? (expt (- 8 4) 2)
```

$$\rightarrow$$
 16

► You now know (almost) all there is to know about (the rules of) CL.

9

The Syntax and Semantics of CL



- ? (expt (- 8 4) 2)
- \rightarrow 16
 - ▶ You now know (almost) all there is to know about (the rules of) CL.
 - ► The first element of a list names a function that is invoked with the values of all remaining elements as its arguments.
 - ► A few exceptions, called special forms, with their own evaluation rules.

Creating our own functions



► The special form defun associates a function definition with a symbol:

General form

 $(defun name (parameter_1 ... parameter_n) body)$

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```
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```

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- ? (average 10 20)
- →15



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- ► A recursive procedure; calls itself, directly or indirectly.

$$n! = \begin{cases} 1 & \text{if } n = 0\\ n \times (n-1)! & \text{if } n > 0 \end{cases}$$



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```
n! = \begin{cases} 1 & \text{if } n = 0 \\ n \times (n-1)! & \text{if } n > 0 \end{cases}
(\text{defun ! (n)} \\ (\text{if (= n 0)} \\ 1 \\ (\text{defun (= n 0)})
```



- ► Classic example: the factorial function.
- ► A recursive procedure; calls itself, directly or indirectly.
- May seem circular, but is well-defined as long as there's a base case terminating the recursion.

```
n! = \begin{cases} 1 & \text{if } n = 0\\ n \times (n-1)! & \text{if } n > 0 \end{cases}
```

```
(defun ! (n)
(if (= n 0)
1
(* n (! (- n 1)))))
```



- ► Classic example: the factorial function.
- ► A recursive procedure; calls itself, directly or indirectly.
- May seem circular, but is well-defined as long as there's a base case terminating the recursion.
- ► For comparison: a non-recursive implementation (in Python).

```
n! = \begin{cases} 1 & \text{if } n = 0\\ n \times (n-1)! & \text{if } n > 0 \end{cases}
```

```
(defun ! (n)
(if (= n 0)
1
(* n (! (- n 1)))))
```

```
def fac(n):
    r = 1
    while (n > 0):
        r = r * n
        n = n - 1
    return r
```

A Special Case of Recursion: Tail Recursion



- ► A more efficient way to define *n*! recursively.
- Use a helper procedure with an accumulator variable to collect the product along the way.

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- The recursive call is in tail position;

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- Most CL compilers do tail call optimization (TCO), so that the recursion is executed as an iterative loop.

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- ▶ Once we reach the base case, the return value is ready.
- ▶ Most CL compilers do *tail call optimization* (TCO), so that the recursion is executed as an iterative loop.
- ► (The next lecture will cover CL's built-in loop construct.)

Tracing the processes



Recursive

```
(defun ! (n)
  (if (= n 0)
        (* n (! (- n 1)))))
? (! 7)
\Rightarrow (* 7 (! 6))
\Rightarrow (* 7 (* 6 (! 5)))
\Rightarrow (* 7 (* 6 (* 5 (! 4))))
\Rightarrow (* 7 (* 6 (* 5 (* 4 (! 3)))))
\Rightarrow (* 7 (* 6 (* 5 (* 4 (* 3 (! 2))))))
\Rightarrow (* 7 (* 6 (* 5 (* 4 (* 3 (* 2 (! 1)))))))
\Rightarrow (* 7 (* 6 (* 5 (* 4 (* 3 (* 2 1))))))
\Rightarrow (* 7 (* 6 (* 5 (* 4 (* 3 2)))))
\Rightarrow (* 7 (* 6 (* 5 (* 4 6))))
\Rightarrow (* 7 (* 6 (* 5 24)))
\Rightarrow (* 7 (* 6 120))
\Rightarrow (* 7 720)
\rightarrow 5040
```

Tail-Recursive

```
(defun! (n)
   (!-aux 1 1 n))
(defun !-aux (r i n)
   (if (> i n)
         (!-aux (* r i)
                  (+ i 1)
                  n)))
? (! 7)
\Rightarrow (!-aux 1 1 7)
\Rightarrow (!-aux 1 2 7)
\Rightarrow (!-aux 2 3 7)
\Rightarrow (!-aux 6 4 7)
\Rightarrow (!-aux 24 5 7)
\Rightarrow (!-aux 120 6 7)
\Rightarrow (!-aux 720 7 7)
\Rightarrow (!-aux 5040 8 7)
\rightarrow 5040
```

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(defun ! (n)
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\Rightarrow (* 7 (* 6 (* 5 (* 4 (! 3)))))
\Rightarrow (* 7 (* 6 (* 5 (* 4 (* 3 (! 2))))))
\Rightarrow (* 7 (* 6 (* 5 (* 4 (* 3 (* 2 (! 1)))))))
\Rightarrow (* 7 (* 6 (* 5 (* 4 (* 3 (* 2 1))))))
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```



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? pi→ 3.141592653589793d0



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- ► The quote operator (or simply ''') suppresses evaluation.

```
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```

? (quote pi)
$$\rightarrow$$
 pi



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? 'foobar → foobar



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? (quote pi) \rightarrow pi
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? 'pi
$$\rightarrow$$
 pi

? foobar
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 error; unbound variable

? 'foobar
$$\rightarrow$$
 foobar

? (* 2 pi)
$$\rightarrow$$
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```

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$$\rightarrow$$
 pi

? foobar
$$\rightarrow$$
 error; unbound variable

? 'foobar
$$\rightarrow$$
 foobar

? (* 2 pi)
$$\rightarrow$$
 6.283185307179586d0

?
$$(* 2 pi) \rightarrow (* 2 pi)$$



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```
? pi→ 3.141592653589793d0
```

- ? (quote pi) \rightarrow pi
- ? 'pi ightarrow pi
- ? foobar \rightarrow error; unbound variable
- ? 'foobar \rightarrow foobar
- ? (* 2 pi) \rightarrow 6.283185307179586d0
- ? $(* 2 pi) \rightarrow (* 2 pi)$
- ? () \rightarrow error; missing procedure



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- ? pi→ 3.141592653589793d0
- ? (quote pi) \rightarrow pi
- ? 'pi \rightarrow pi
- ? foobar \rightarrow error; unbound variable
- ? 'foobar \rightarrow foobar
- ? (* 2 pi) → 6.283185307179586d0
- ? $(* 2 pi) \rightarrow (* 2 pi)$
- ?() \rightarrow error; missing procedure
- **?** '() → ()

Both Code and Data are S-Expressions



- ▶ We've mentioned how sexps are used to represent *both* data and code.
- ► Note the double role of lists:
- ► Lists are function calls:

```
? (* 10 (+ 2 3)) \rightarrow 50
```

? (bar 1 2) \rightarrow error; function bar undefined

Both Code and Data are S-Expressions



- ▶ We've mentioned how sexps are used to represent *both* data and code.
- ► Note the double role of lists:
- ► Lists are function calls:

```
? (* 10 (+ 2 3)) \rightarrow 50
? (bar 1 2) \rightarrow error; function bar undefined
```

► But, lists can also be data:

```
? '(foo bar) \rightarrow (foo bar)
? (list 'foo 'bar) \rightarrow (foo bar)
```



```
? (cons 1 (cons 2 (cons 3 nil))) \rightarrow (1 2 3)
```



```
? (cons 1 (cons 2 (cons 3 nil))) \rightarrow (1 2 3)
? (cons 0 '(1 2 3)) \rightarrow
```



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```



```
? (cons 1 (cons 2 (cons 3 nil))) \rightarrow (1 2 3)
? (cons 0 '(1 2 3)) \rightarrow (0 1 2 3)
? (first '(1 2 3)) \rightarrow 1
```



```
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? (rest '(1 2 3)) \rightarrow (2 3)
```



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? (cons 1 (cons 2 (cons 3 nil))) → (1 2 3)
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? (first (rest '(1 2 3))) →
```



```
? (cons 1 (cons 2 (cons 3 nil))) \rightarrow (1 2 3)

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? (rest '(1 2 3)) \rightarrow (2 3)

? (first (rest '(1 2 3))) \rightarrow 2
```



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? (first (rest '(1 2 3))) → 2
? (rest (rest (rest '(1 2 3)))) →
```



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? (cons 1 (cons 2 (cons 3 nil))) → (1 2 3)
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? (rest '(1 2 3)) → (2 3)
? (first (rest '(1 2 3))) → 2
? (rest (rest (rest '(1 2 3)))) → nil
```



► cons builds up new lists; first and rest destructure them.

```
? (cons 1 (cons 2 (cons 3 nil))) \rightarrow (1 2 3)

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```

```
? (list 1 2 3) \rightarrow (1 2 3)
```



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? (first (rest '(1 2 3))) \rightarrow 2

? (rest (rest (rest '(1 2 3)))) \rightarrow nil
```

```
? (list 1 2 3) \rightarrow (1 2 3)
? (append '(1 2) '(3) '(4 5 6)) \rightarrow (1 2 3 4 5 6)
```



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? (rest (rest (rest '(1 2 3)))) \rightarrow nil
```

```
? (list 1 2 3) \rightarrow (1 2 3)
? (append '(1 2) '(3) '(4 5 6)) \rightarrow (1 2 3 4 5 6)
? (length '(1 2 3)) \rightarrow 3
```



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```
? (list 1 2 3) → (1 2 3)
? (append '(1 2) '(3) '(4 5 6)) → (1 2 3 4 5 6)
? (length '(1 2 3)) → 3
? (reverse '(1 2 3)) → (3 2 1)
```



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```

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? (length '(1 2 3)) → 3
? (reverse '(1 2 3)) → (3 2 1)
? (nth 2 '(1 2 3)) → 3
```



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? (cons 1 (cons 2 (cons 3 nil))) → (1 2 3)
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? (rest (rest (rest '(1 2 3)))) → nil
```

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? (list 1 2 3) → (1 2 3)
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? (reverse '(1 2 3)) → (3 2 1)
? (nth 2 '(1 2 3)) → 3
? (last '(1 2 3)) → (3)
```



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? (cons 1 (cons 2 (cons 3 nil))) \rightarrow (1 2 3)

? (cons 0 '(1 2 3)) \rightarrow (0 1 2 3)

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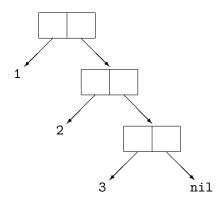
? (rest (rest (rest '(1 2 3)))) \rightarrow nil
```

```
? (list 1 2 3) → (1 2 3)
? (append '(1 2) '(3) '(4 5 6)) → (1 2 3 4 5 6)
? (length '(1 2 3)) → 3
? (reverse '(1 2 3)) → (3 2 1)
? (nth 2 '(1 2 3)) → 3
? (last '(1 2 3)) → (3) Wait, why not 3?
```

Lists are Really Chained 'cons' Cells



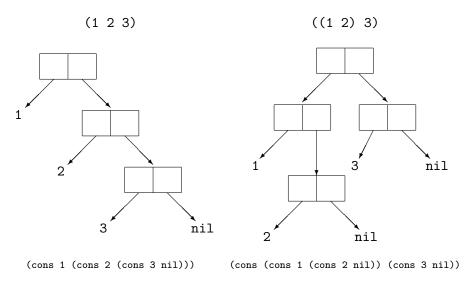




(cons 1 (cons 2 (cons 3 nil)))

Lists are Really Chained 'cons' Cells





Assigning Values: 'Generalized Variables'



► defparameter declares a 'global variable' and assigns a value:

- ? (defparameter *foo* 42) \rightarrow *F00*
- ? *foo* → 42



► defparameter declares a 'global variable' and assigns a value:

- ? (defparameter *foo* 42) \rightarrow *F00*
- ? *foo* \rightarrow 42
- ▶ setf provides a uniform way of assigning values to variables.



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- ... where place can either be a variable named by a symbol or some other storage location:
- ? (setf *foo* (+ *foo* 1))



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... where place can either be a variable named by a symbol or some other storage location:

```
? (setf *foo* (+ *foo* 1))
```

? *foo* \rightarrow 43



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```
? (defparameter *foo* 42) \rightarrow *F00* 
? *foo* \rightarrow 42
```

- ▶ setf provides a uniform way of assigning values to variables.
- ► General form:

```
(setf place value)
```

```
? (setf *foo* (+ *foo* 1))
? *foo* \rightarrow 43
? (setf *foo* '(2 2 3))
```



► defparameter declares a 'global variable' and assigns a value:

```
? (defparameter *foo* 42) \rightarrow *F00* 
? *foo* \rightarrow 42
```

- ▶ setf provides a uniform way of assigning values to variables.
- ► General form:

```
(setf place value)
```

```
? (setf *foo* (+ *foo* 1))
? *foo* → 43
? (setf *foo* '(2 2 3))
? (setf (first *foo*) 1)
```



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```
? (defparameter *foo* 42) \rightarrow *F00*
```

- ▶ setf provides a uniform way of assigning values to variables.
- ► General form:

? $*foo* \rightarrow 42$

```
(setf place value)
```

```
? (setf *foo* (+ *foo* 1))
? *foo* → 43
? (setf *foo* '(2 2 3))
? (setf (first *foo*) 1)
? *foo* → (1 2 3)
```

Some Other Macros for Assignment



Example	Type of x	Effect
(incf x y)	number	(setf x (+ x y))
(incf x)	number	(incf x 1)
(decf x y)	number	(setf x (- x y))
(decf x)	number	(decf x 1)
(push y x)	list	(setf x (cons y x))
(pop x)	list	<pre>(let ((y (first x))) (setf x (rest x)) y)</pre>
(pushnew y x)	list	<pre>(if (member y x) x (push y x))</pre>

Some Other Macros for Assignment



Example	Type of x	Effect
(incf x y)	number	(setf x (+ x y))
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(pop x)	list	<pre>(let ((y (first x))) (setf x (rest x)) y)</pre>
(pushnew y x)	list	<pre>(if (member y x) x (push y x))</pre>

Shall we jointly write our own push and pop?



- ► Sometimes we want to store intermediate results.
- ▶ let and let* create temporary value bindings for symbols.



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```
? (defparameter *foo* 42) → *F00*
? (defparameter *bar* 100) → *BAR*
? (let ((*bar* 7)
         (baz 1))
    (+ baz *bar* *foo*))
\rightarrow 50
? *bar* \to 100
? baz \rightarrow
```



- ► Sometimes we want to store intermediate results.
- ► let and let* create temporary value bindings for symbols.

```
? (defparameter *foo* 42) → *F00*
? (defparameter *bar* 100) → *BAR*
? (let ((*bar* 7)
        (baz 1))
    (+ baz *bar* *foo*))
\rightarrow 50
? *bar* \to 100
? baz → error; unbound variable
```



- ► Sometimes we want to store intermediate results.
- ► let and let* create temporary value bindings for symbols.

- ▶ Bindings valid only in the body of let.
- ▶ Previously existing bindings are *shadowed* within the lexical scope.



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- ► let and let* create temporary value bindings for symbols.

▶ Bindings valid only in the body of let.

? baz → error; unbound variable

- ▶ Previously existing bindings are *shadowed* within the lexical scope.
- ▶ let* is like let but binds sequentially.

Predicates



- ► A *predicate* tests some condition.
- ► Evaluates to a boolean truth value:
 - ▶ nil (the empty list) means false.
 - ► Anything non-nil (including t) means *true*.

▶ Plethora of equality tests: eq, eq1, equal, and equalp.



- eq tests object identity; not applicable for numbers or characters.
- ▶ eql is like eq, but well-defined on numbers and characters.
- equal tests structural equivalence (recursively for lists and strings).
- ► equalp is like equal but insensitive to case and numeric type.



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```
? (eq (list 1 2 3) '(1 2 3)) \rightarrow nil
```



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- equal tests structural equivalence (recursively for lists and strings).
- ► equalp is like equal but insensitive to case and numeric type.

```
? (eq (list 1 2 3) '(1 2 3)) \rightarrow nil
? (equal (list 1 2 3) '(1 2 3)) \rightarrow t
```



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- equal tests structural equivalence (recursively for lists and strings).
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```
? (eq (list 1 2 3) '(1 2 3)) \rightarrow nil
? (equal (list 1 2 3) '(1 2 3)) \rightarrow t
? (eq 42 42) \rightarrow ? [implementation-dependent]
```



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```
? (eq (list 1 2 3) '(1 2 3)) \rightarrow nil
? (equal (list 1 2 3) '(1 2 3)) \rightarrow t
? (eq 42 42) \rightarrow ? [implementation-dependent]
? (eq1 42 42) \rightarrow t
```



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```
? (eq (list 1 2 3) '(1 2 3)) \rightarrow nil
? (equal (list 1 2 3) '(1 2 3)) \rightarrow t
? (eq 42 42) \rightarrow ? [implementation-dependent]
? (eq1 42 42) \rightarrow t
? (eq1 42 42.0) \rightarrow nil
```



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? (eq 42 42) \rightarrow ? [implementation-dependent]
? (eq1 42 42) \rightarrow t
? (eq1 42 42.0) \rightarrow nil
? (equalp 42 42.0) \rightarrow t
```



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```
? (eq (list 1 2 3) '(1 2 3)) \rightarrow nil
? (equal (list 1 2 3) '(1 2 3)) \rightarrow t
? (eq 42 42) \rightarrow ? [implementation-dependent]
? (eq1 42 42) \rightarrow t
? (eq1 42 42.0) \rightarrow nil
? (equalp 42 42.0) \rightarrow t
? (equal "foo" "foo") \rightarrow t
```



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```
? (eq (list 1 2 3) '(1 2 3)) \rightarrow nil

? (equal (list 1 2 3) '(1 2 3)) \rightarrow t

? (eq 42 42) \rightarrow ? [implementation-dependent]

? (eq1 42 42) \rightarrow t

? (eq1 42 42.0) \rightarrow nil

? (equalp 42 42.0) \rightarrow t

? (equal "foo" "foo") \rightarrow t

? (equalp "FOO" "foo") \rightarrow t
```



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- ▶ eql is like eq, but well-defined on numbers and characters.
- equal tests structural equivalence (recursively for lists and strings).
- equalp is like equal but insensitive to case and numeric type.

```
? (eq (list 1 2 3) '(1 2 3)) \rightarrow nil

? (equal (list 1 2 3) '(1 2 3)) \rightarrow t

? (eq 42 42) \rightarrow ? [implementation-dependent]

? (eq1 42 42) \rightarrow t

? (eq1 42 42.0) \rightarrow nil

? (equalp 42 42.0) \rightarrow t

? (equal "foo" "foo") \rightarrow t

? (equalp "F00" "foo") \rightarrow t
```

► Also many type-specialized tests like =, string=, etc.



```
? (defparameter foo 42)
```

```
? (if (numberp foo)
    "number"
    "something else")
```



```
? (defparameter foo 42)
? (if (numberp foo)
         "number"
         "something else")
→ "number"
```



```
? (defparameter foo 42)
 (if (numberp foo)
      "number"
      "something else")
→ "number"
   (cond ((< foo 3) "less")
         ((> foo 3) "more")
         (else "equal"))
```



```
? (defparameter foo 42)
 (if (numberp foo)
      "number"
      "something else")
→ "number"
   (cond ((< foo 3) "less")
         ((> foo 3) "more")
         (else "equal"))
  "more"
```



Examples

```
? (defparameter foo 42)
 (if (numberp foo)
      "number"
      "something else")
→ "number"
   (cond ((< foo 3) "less")
         ((> foo 3) "more")
         (else "equal"))
  "more"
```

General Form

```
(if ⟨predicate⟩
    ⟨then clause⟩
    ⟨else clause⟩)

(cond (⟨predicate₁⟩ ⟨clause₁⟩)
    (⟨predicate₂⟩ ⟨clause₂⟩)
    (⟨predicate₁⟩ ⟨clause₁⟩)
    (t ⟨default clause⟩))
```



- ► Symbols can have values as functions and variables at the same time.
- ▶ #' (sharp-quote) gives us the function object bound to a symbol.

```
? (defun foo (x)
(* x 1000))
```



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- ▶ #' (sharp-quote) gives us the function object bound to a symbol.

```
? (defun foo (x)
(* x 1000))
```

? (defparameter foo 42) \rightarrow 2



- ► Symbols can have values as functions and variables at the same time.
- ▶ #' (sharp-quote) gives us the function object bound to a symbol.

```
? (defun foo (x)
	(* x 1000))
? (defparameter foo 42) \rightarrow 2
? (foo foo) \rightarrow
```



- ► Symbols can have values as functions and variables at the same time.
- ▶ #' (sharp-quote) gives us the function object bound to a symbol.

```
? (defun foo (x)
(* x 1000))
```

? (defparameter foo 42) \rightarrow 2

? (foo foo) \rightarrow 42000



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- ▶ #' (sharp-quote) gives us the function object bound to a symbol.

```
? (defun foo (x)
(* x 1000))
```

? (defparameter foo 42) \rightarrow 2

? (foo foo) \rightarrow 42000

? foo \rightarrow 42



- ► Symbols can have values as functions and variables at the same time.
- ▶ #' (sharp-quote) gives us the function object bound to a symbol.

```
? (defun foo (x) (* x 1000))
? (defparameter foo 42) \rightarrow 2
? (foo foo) \rightarrow 42000
? foo \rightarrow 42
```



- ► Symbols can have values as functions and variables at the same time.
- ▶ #' (sharp-quote) gives us the function object bound to a symbol.

```
? (defun foo (x)
     (* x 1000))
? (defparameter foo 42) \rightarrow 2
? (foo foo) \rightarrow 42000
? foo \rightarrow 42
? #'foo → #<Interpreted Function FOO>
? (funcall #'foo foo) \rightarrow 42000
```



- ► Symbols can have values as functions and variables at the same time.
- ▶ #' (sharp-quote) gives us the function object bound to a symbol.

```
? (defun foo (x)
          (* x 1000))
```

? (defparameter foo 42) \rightarrow 2

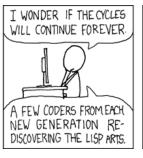
```
? (foo foo) \rightarrow 42000
```

- ? foo $\rightarrow 42$
- ? #'foo \rightarrow #<Interpreted Function FOO>
- ? (funcall #'foo foo) \rightarrow 42000
- #' and funcall (as well as apply) are useful when passing around functions as arguments.

In Conclusion



LISP IS OVER HALF A
CENTURY OLD AND IT
STILL HAS THIS PERFECT,
TIMELESS AIR ABOUT IT.





http://xkcd.com/297/

Next Week



More Common Lisp.

- ► More on argument lists (optional arguments, keywords, defaults).
- ► More data types: Hash-tables, a-lists, arrays, sequences, and structures
- ► More higher-order functions.
- ► Iteration (loop) and mapping.