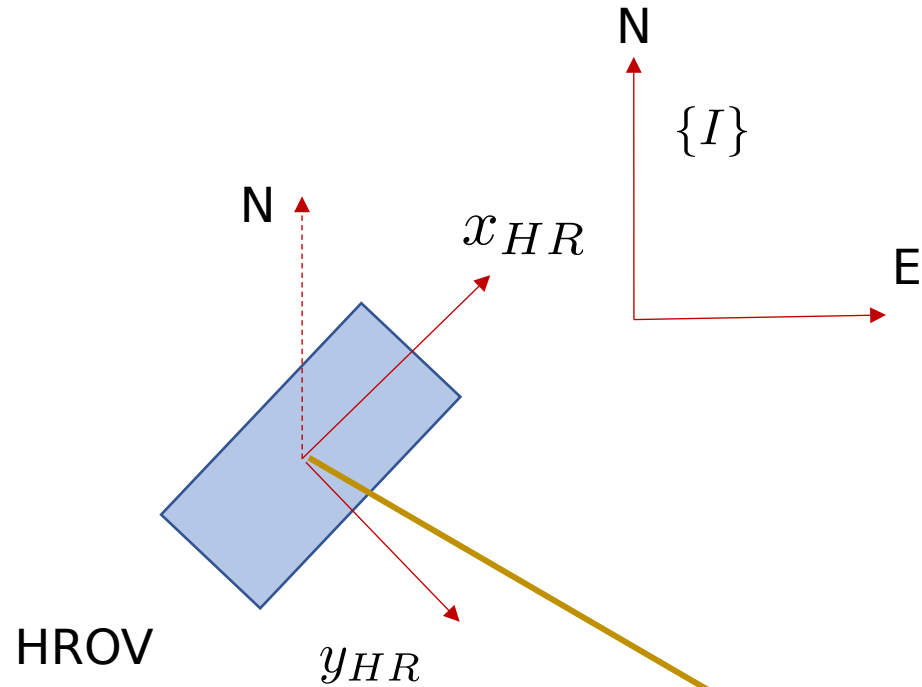


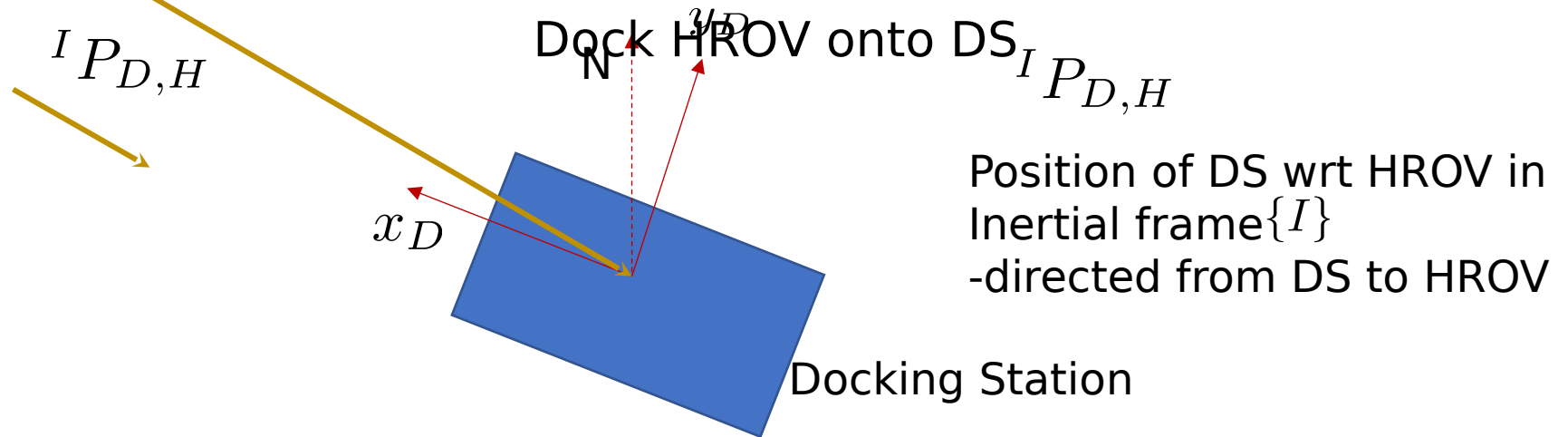
Docking of HROV
(Hybrid ROV/AUV)
April 3, 2024



Set up

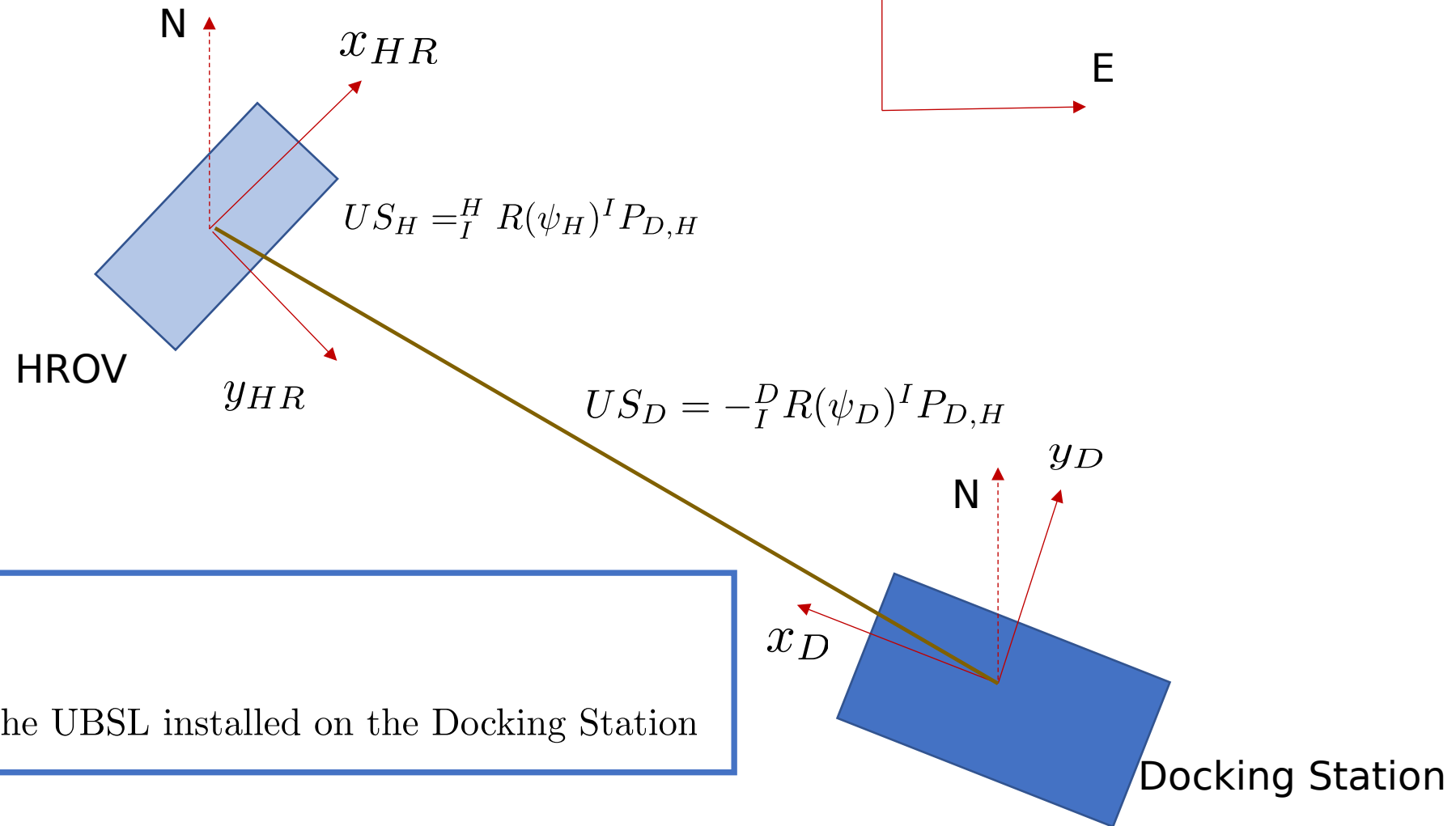
- HROV equipped with USBL that measures the position of the Docking Station (DS) with respect to it
- DS equipped with USBL that measures the position of the HROV with respect to it
- HROV equipped with Doppler log and AHRS

Goal



$$US_H = {}^H_I R(\psi_H)^I P_{D,H}$$

US_H measurement provided by the UBSL installed on the HROV



$$US_D = -{}^D_I R(\psi_D)^I P_{D,H}$$

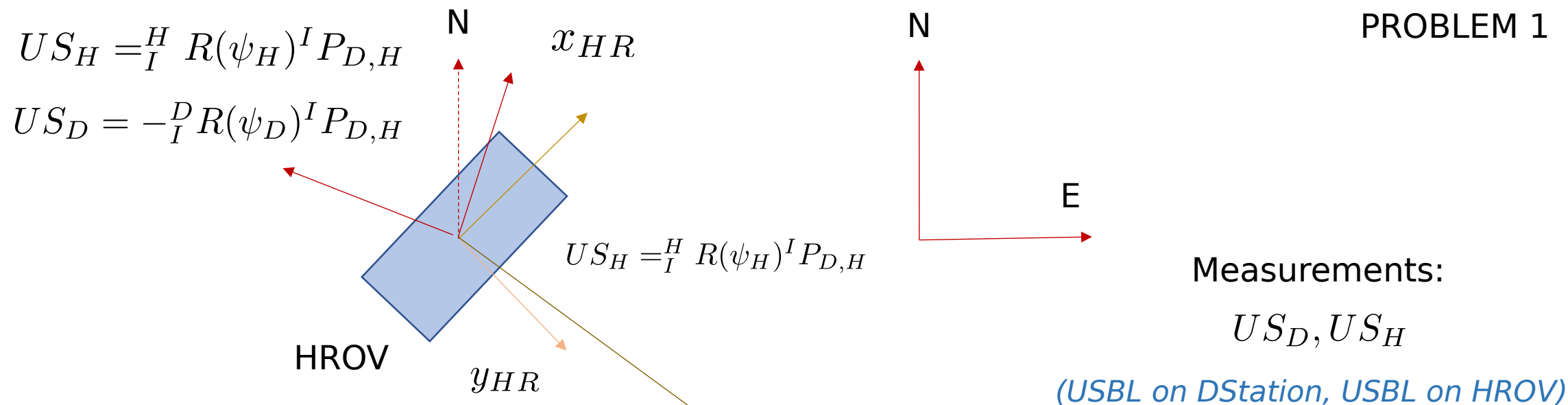
US_D measurement provided by the UBSL installed on the Docking Station

Problem 1

Find the orientation of the Docking Station with respect to the HROV, as captured by the rotation matrix

$${}^H_D R(\cdot)$$

PROBLEM 1



$${}^I P_{D,H} = -{}^I_D R(\psi_D) US_D$$

$${}^I P_{D,H} = {}^I_H R(\psi_H) US_H$$

$${}^I_H R(\psi_H) US_H = -{}^I_D R(\psi_D) US_D$$

$$US_H = -{}^H_I R(\psi_H) {}^I_D R(\psi_D) US_D = -R_D^H(\psi_H, \psi_D) US_D$$

$$US_H = -{}^H_D R(.) US_D$$

${}^H_D R(.)$ Rotation matrix from DS to HROV

Docking Station

PROBLEM 1

$$US_H = -\frac{H}{D}R(.)US_D$$

$$\frac{H}{D}R(.) = \frac{1}{r^2} [r_1 r_2; -r_2 r_1]$$

Clearly, $\|US_H\| = \|US_D\| = r$ (range measured by USBLS)

Now compute explicitly the rotation matrix $\frac{H}{D}R(.)$
that takes $-US_D$ to US_H

Let

$$r_1 = -\langle US_D, US_H \rangle \quad r_2 = [0 \ 0 \ 1][US_D \times US_H]$$

Then

$$\frac{H}{D}R(.) = \frac{1}{r^2} \begin{bmatrix} r_1 & -r_2 \\ r_2 & r_1 \end{bmatrix}$$

$$\rightarrow \theta_{D \rightarrow H} = \text{atan}(r_2, r_1)$$