

$g(\bar{X}) \approx \bar{y}$ PRICE

model feature matrix \bar{X} target

LINEAR TRAIN

REGRESSION

$$g(x_i) \approx y_i$$

A CAR ITS PRICE

$$x_i = (x_{i1}, x_{i2}, \dots, x_{in})$$

$$g(x_{i1}, \dots, x_{in}) \approx y_i$$

$$x_i = [453, 11, 86]$$

$i=10$

$$g(x_i) \approx y_i$$

$$g(x_i) = w_0 + w_1 \cdot x_{i,1} + w_2 \cdot x_{i,2} + \\ + w_3 \cdot x_{i,3}$$

$$g(x_i) = w_0 + w_1 \cdot x_{i,1} + w_2 \cdot x_{i,2} +$$

\uparrow

$w_3 \cdot x_{i,3}$

$$g(x_i) = w_0 + \sum_{j=1}^3 w_j \cdot x_{i,j}$$

w_0

$$7.17 + \boxed{453} \cdot 0.01 + \boxed{11} \cdot \cancel{\boxed{10}} \cdot 0.04 + \boxed{86} \cdot 0.002 =$$
$$\frac{1 \cdot 0.01}{100 \cdot 0.01} = 1$$
$$\frac{1}{10000} = 12.3$$

$$\log(y+1) = p$$

$$y \neq 1 = \exp(p) \quad \Rightarrow \quad y = \exp(p) + 1$$

$$g(x_i) = \underbrace{w_0}_{\sim} + \boxed{\sum_{j=1}^n x_{ij} \cdot w_j} =$$

$$= w_0 \cancel{x_{i0}}_1 + x_i^T w$$

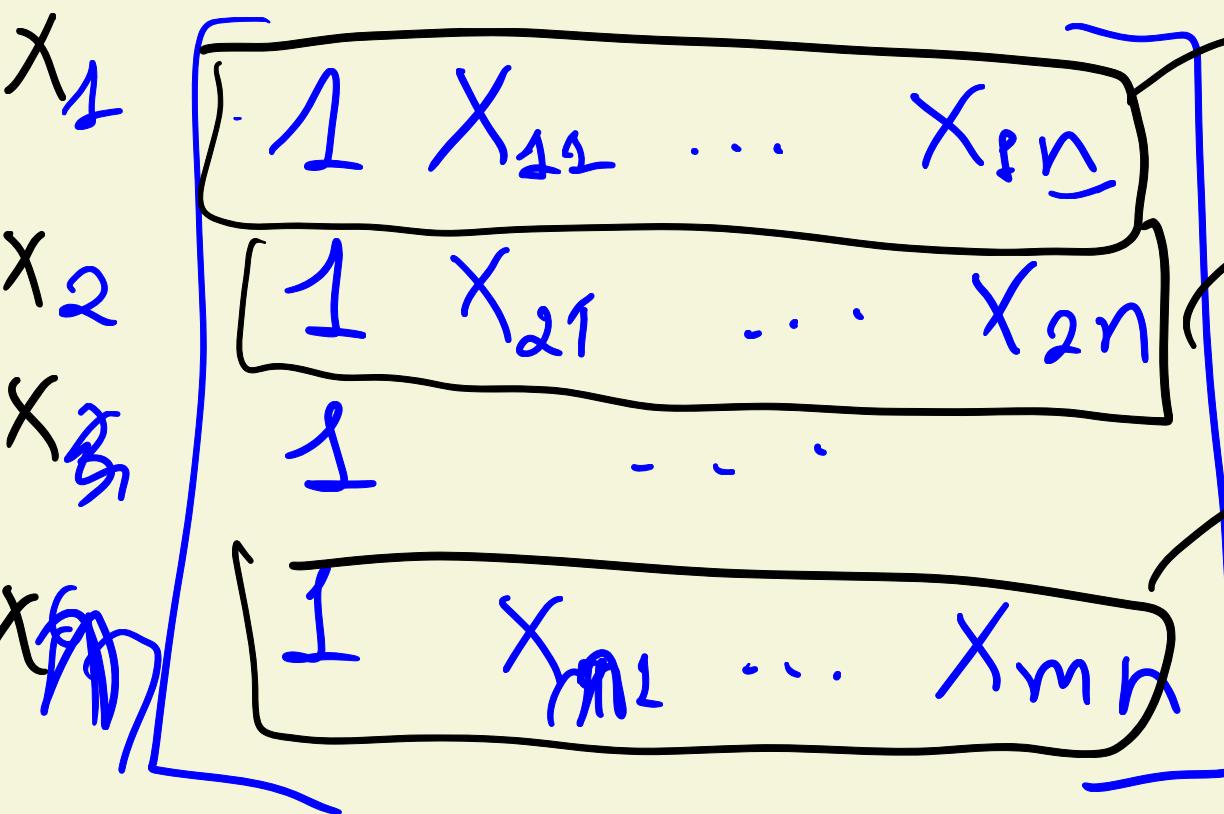
$$W = [w_0 \mid w_1 \ w_2 \ \dots \ w_n]$$

n+1
dim

$$x_i = [1 \ x_{i1} \ x_{i2} \ \dots \ x_{in}]$$

$$\boxed{w^T x_i} = x_i^T w = w_0 + ..$$

~~X~~ $m \times (n+1)$



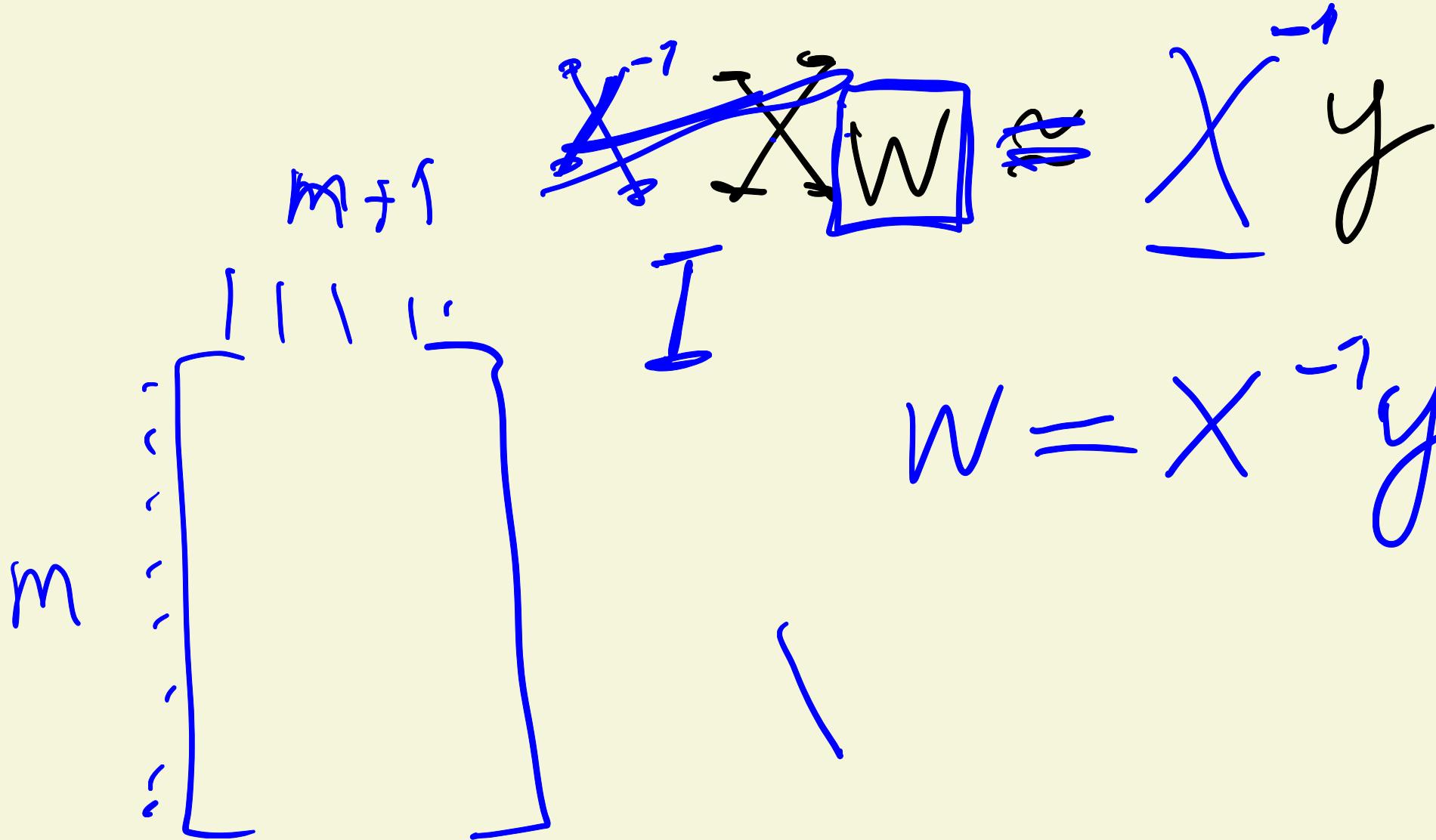
$$w = \begin{bmatrix} w_0 \\ w_1 \\ \vdots \\ w_n \end{bmatrix}$$

$$= \begin{bmatrix} x_1^T \cdot w \\ x_2^T \cdot w \\ \vdots \\ x_m^T \cdot w \end{bmatrix}$$

y_p

PRED

~~X~~ w



$$w = X^{-1}y$$

$$\cancel{\left(\begin{matrix} X^T \\ X \end{matrix} \right)^{-1}} \cancel{X^T} \cancel{I} \cancel{w} = \left(\begin{matrix} X^T \\ X \end{matrix} \right)^{-1} \cancel{X^T} \cancel{y}$$

GRAM
MATRIX
 $(n+1) \times (n+1)$

$$\underline{\underline{w}} = (X^T X)^{-1} X^T y$$

$$†w = w$$

$$g(x_i) = w_0 + \cancel{w_1} x_{i1} + x_{i2} \cdot w_2 =$$

~~w₁~~

missing ENGINE MP

$$= w_0 + x_{i2} \cdot w_2$$

$$RMSE = \sqrt{\frac{1}{m} \sum_{i=1}^m (g(x_i) - y_i)^2}$$

PREDICTION
FOR x_i

ACTUAL
VOLTAGE

$$g(x_i) - y_i$$

PRED

PRICE

y-pred

10	9	11	...	10
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y_train

9	9	10.5	...	11.5
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1	0	0.5	...	-1.5
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1 0

0.25

2.25

SQUARED
ERROR

1 0 0,25 2,25

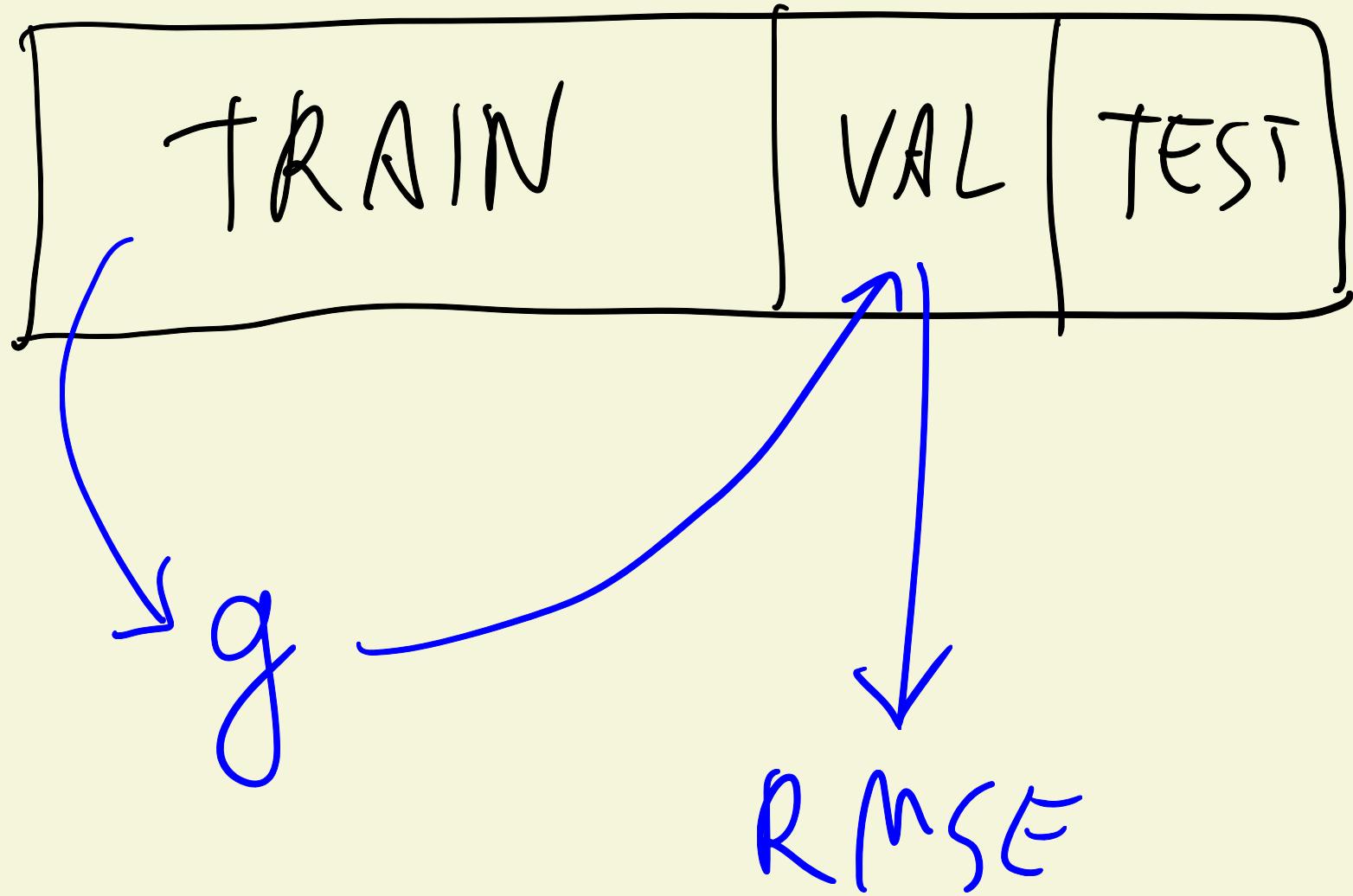
MEAN
SE

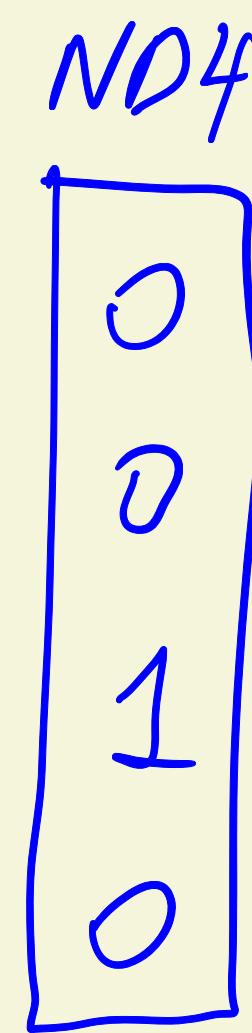
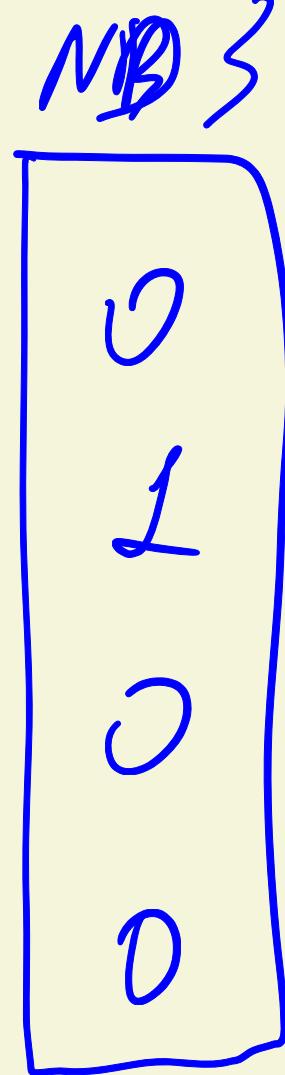
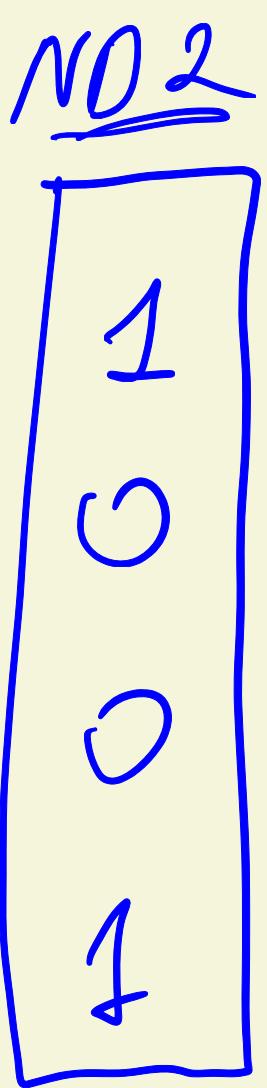
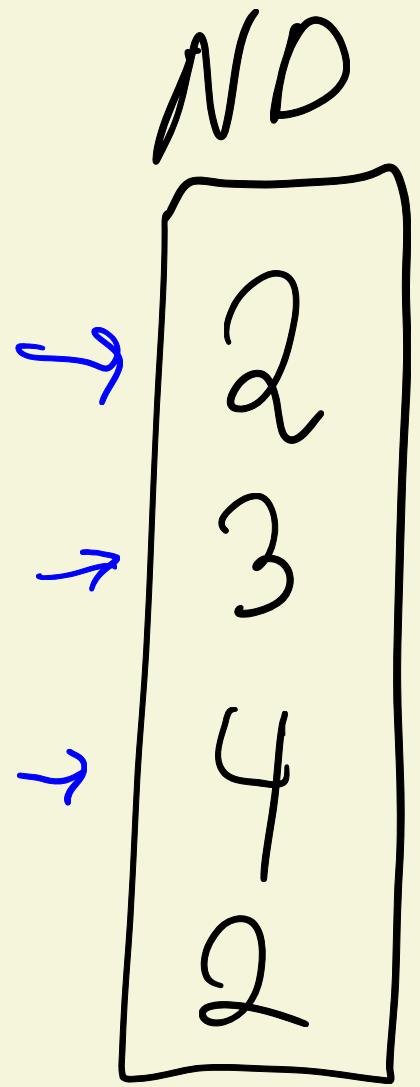


$$\frac{1 + 0 + 0,25 + 2,25}{4} =$$

$$= 0.875$$

$$\sqrt{0.875} = 0.93$$



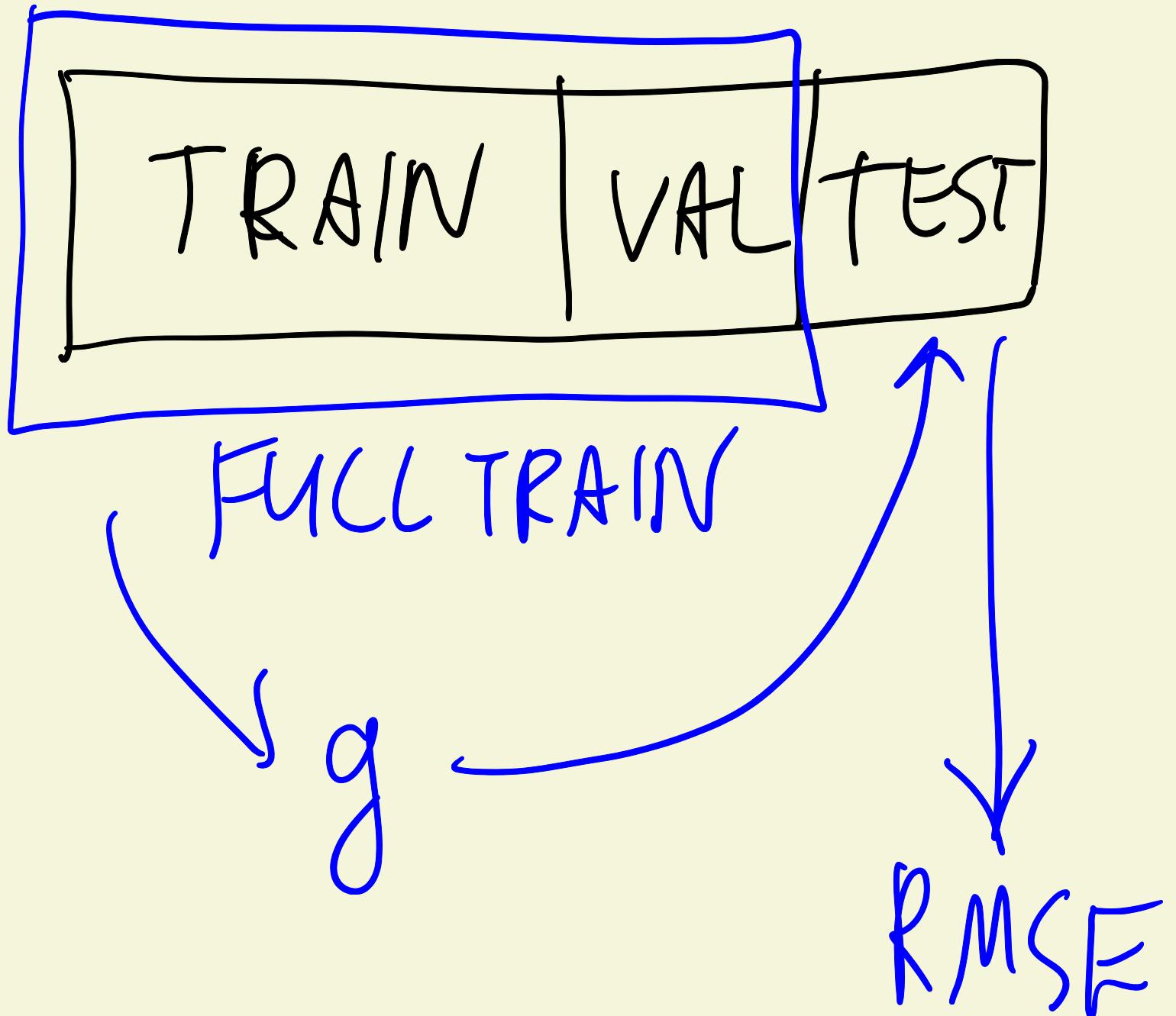


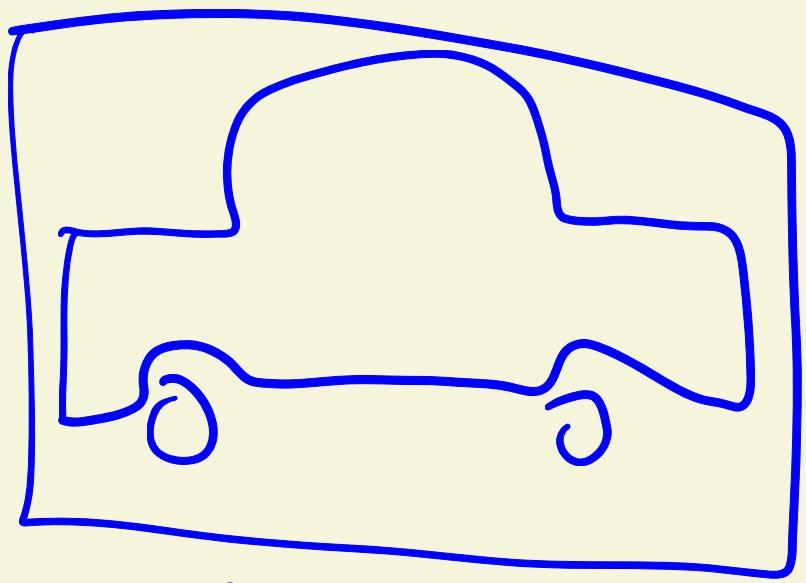
$$w = (X^T X)^{-1} \cdot X^T \cdot y$$

$$X^T X$$

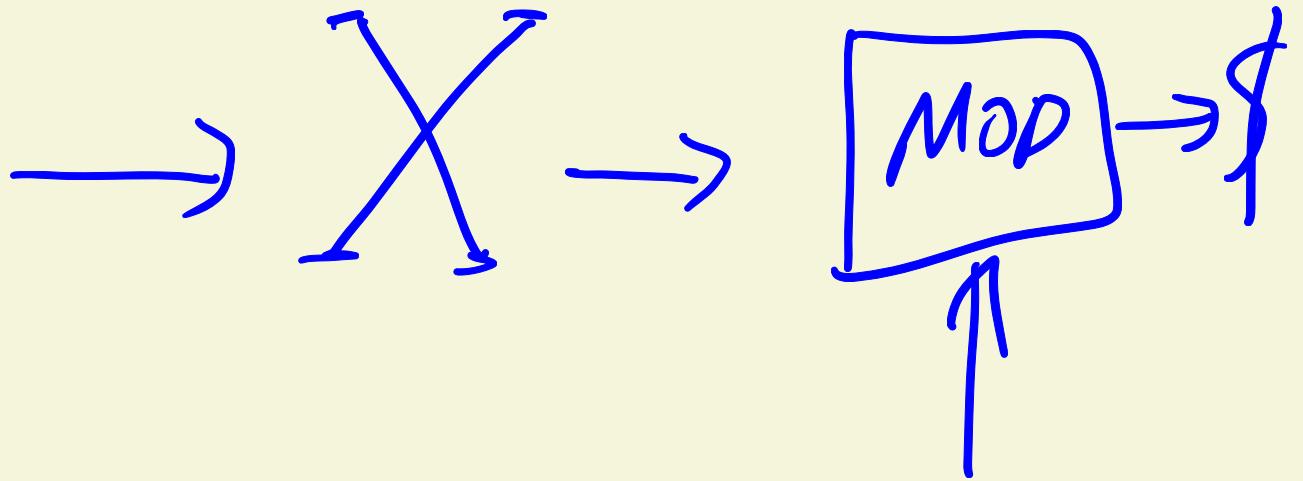
$$X =$$

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	16





{ ... }



FINAL

