Assignment 2

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1 problem 2

1.1 a.

We claim the provided tree correctly categorize the provided example since every example can be inducted from this decision tree. Like GPA above 3.6 is P and below 3.3 is N, then with publication P,otherwise check University Rank, Only rank 2 will be P,other ranks are N. And recommendation doesn't matter.

1.2 b.

Step I

I($\frac{6}{12}$, $\frac{6}{12}$)=1

GPA: $[3.9, 4.0]$ 3(PPP) , $(3.2, 3.9)$ 5($PPPNN$) , $[3.0, 3.2]$ 4($NNNN$)
University: Rank 1— 5(PPPNN),Rank 2— 3(PPN) , Rank 3— 4(PNNN)
Publication: Yes 5(PPPNN) , No 7(PPPNNNN)
Recommendation: good 8(PPPPPNNN) , normal 4(PNNN)

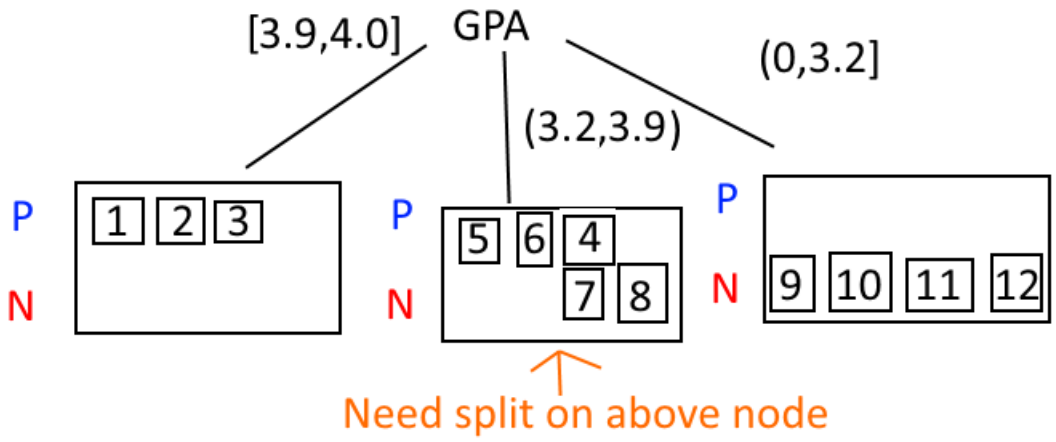
Gain(GPA)=1-[$\frac{3}{12}$ B($\frac{3}{3}$)+$\frac{5}{12}$ B($\frac{3}{5}$)+$\frac{4}{12}$ B($\frac{0}{4}$)]=1-[0.0+0.404562747689+0.0] = 0.595437252311

Gain(University)=1-[$\frac{5}{12}$ B($\frac{3}{5}$)+$\frac{3}{12}$ B($\frac{2}{3}$)+$\frac{4}{12}$ B($\frac{1}{4}$)]= 1-[0.404562747689+0.229573958514+0.270426041486] =0.095437252395

Gain(Publication)=1-[$\frac{5}{12}$ B($\frac{3}{5}$)+$\frac{7}{12}$ B($\frac{3}{7}$)]=1-[0.404562747689+0.574716412687]= 0.020720839624

Gain(Recommendation)=
1-[$\frac{8}{12}$ B($\frac{5}{8}$)+$\frac{4}{12}$ B($\frac{1}{4}$)]=1-[0.636289335283+0.270426041486]= 0.093284623231

So we pick GPA as the best Gain attribute in this level



Step II

I($\frac{2}{5}$, $\frac{3}{5}$)=0.970950594455

University: Rank 1— 2(PN),Rank 2— 1(P) , Rank 3— 2(PN)
Publication: Yes 2(PP) , No 3(PNN)
Recommendation: good 5(PPPNN)

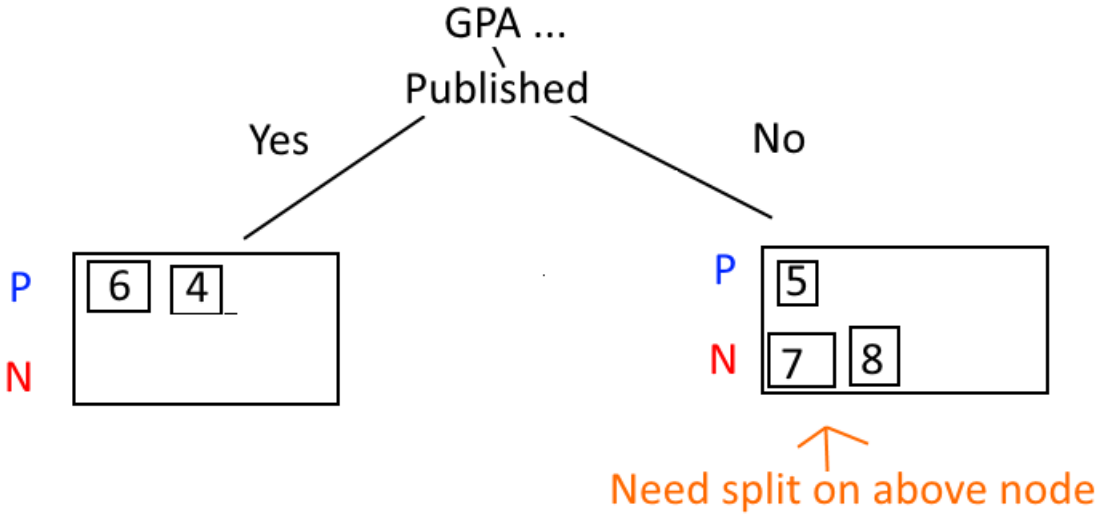
Gain(University)=0.970950594455-[$\frac{2}{5}$ B($\frac{1}{2}$)+$\frac{1}{5}$ B($\frac{1}{1}$)+$\frac{2}{5}$ B($\frac{1}{2}$)]=
0.970950594455-[0.4+0.0+0.4] = 0.170950594455

Gain(Publication)=0.970950594455-[$\frac{3}{5}$ B($\frac{1}{3}$)+$\frac{2}{5}$ B($\frac{2}{2}$)]=0.970950594455-
[0.550977500433+0.0]= 0.419973094022

Gain(Recommendation)=0.970950594455-[$\frac{5}{5}$ B($\frac{3}{5}$)]=0.970950594455-

[0.970950594455+0.0+0.0] = 0

So we pick Publication as the best Gain attribute in this level



Step III

I($\frac{1}{3}$, $\frac{2}{3}$)=0.918295834054

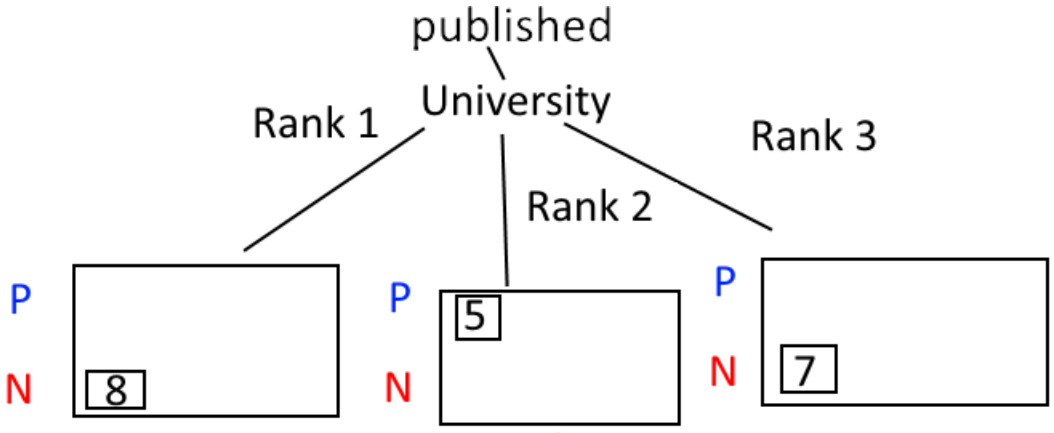
University: Rank 1 — 1(N),Rank 2 — 1(P) , Rank 3 — 1(N)

Recommendation: good 3(PNN)

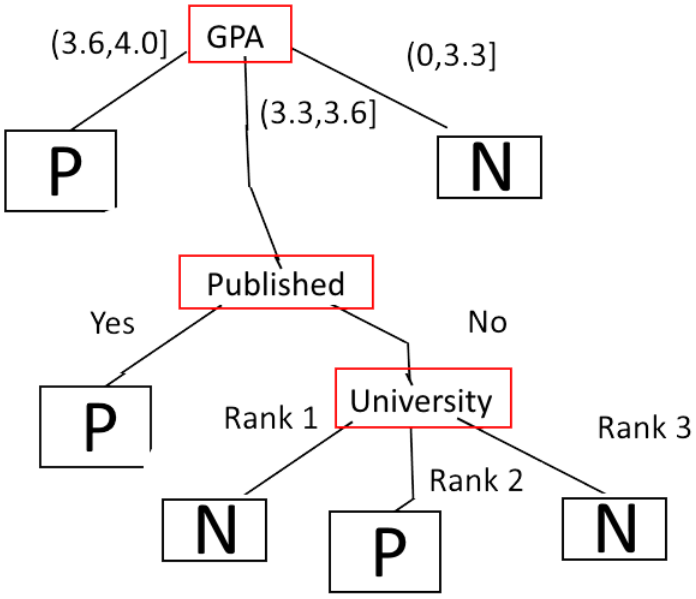
Gain(University)=0.918295834054-[$\frac{1}{3}$ B($\frac{0}{1}$)+$\frac{1}{3}$ B($\frac{1}{1}$)+$\frac{1}{3}$ B($\frac{0}{1}$)]=0.918295834054-[0.0+0.0+0.0]=0.918295834054

Gain(Recommendation)=0.918295834054-[$\frac{3}{3}$ B($\frac{1}{3}$)]=0.918295834054-[0.918295834054]= 0

So we pick University as the best Gain attribute in this level



And the final tree to be returned is



1.3 c.

The decision tree we got from b. is same from the provided one. This is not coincidence, it is believed both tree is generated by applying the decision tree algorithm.

2 problem 3

2.1 a.