

In a given integer array A, we must move every element of A to either list B or list C. (B and C initially start empty.)

Return true if and only if after such a move, it is possible that the average value of B is equal to the average value of C, and B and C are both non-empty.

Note:

- $1 \leq \text{len}(A) \leq 30$
- $0 \leq A[i] \leq 10\,000$

First let's do some notations:

A: the initial array

sum(X): the sum of the elements in array X

len(X): the number of elements in array X

B and C: the arrays in which we splitted A

We have:

$$\text{sum}(A) = \text{sum}(B) + \text{sum}(C) \text{ and } \text{len}(A) = \text{len}(B) + \text{len}(C)$$

We also know that the averages of B and C are equal:

$$\text{sum}(B) / \text{len}(B) = \text{sum}(C) / \text{len}(C) \quad (\text{replace the RHS from formulas above})$$

$$\text{sum}(B) / \text{len}(B) = (\text{sum}(A) - \text{sum}(B)) / (\text{len}(A) - \text{len}(B)) \quad (\text{multiply over diagonals})$$

$$\text{sum}(B) * (\text{len}(A) - \text{len}(B)) = (\text{sum}(A) - \text{sum}(B)) * \text{len}(B)$$

$$\text{sum}(B) * \text{len}(A) - \text{sum}(B) * \text{len}(B) = \text{sum}(A) * \text{len}(B) - \text{sum}(B) * \text{len}(B)$$

$$\text{sum}(B) * \text{len}(A) = \text{sum}(A) * \text{len}(B)$$

$$\text{sum}(B) = \text{sum}(A) * \text{len}(B) / \text{len}(A) \quad (\text{property of a partition with respect to our initial array A})$$


Our problem is reduced to finding one partition B in which the sum of the elements is equal to $\text{sum}(A) * \text{len}(B) / \text{len}(A)$

As a first step, we can check only for one partition, and the possible lengths for that partition are in range $[1, n / 2]$, because after exceeding $n / 2$ we have the other partition in range $[1, n / 2]$

As a second step, we need a data structure to store all the possible sums of a subarray up to a certain point.

We can use a list of sets, in which $l[i]$ represents all the possible sums of i elements. In the end, we need to check if the sum $\text{sum}(A) * \text{len}(B) / \text{len}(A)$ is in a valid group i .

Ex: [1, 2, 3, 4]

0							
1	2	3	4				
3	4	5	6	7			