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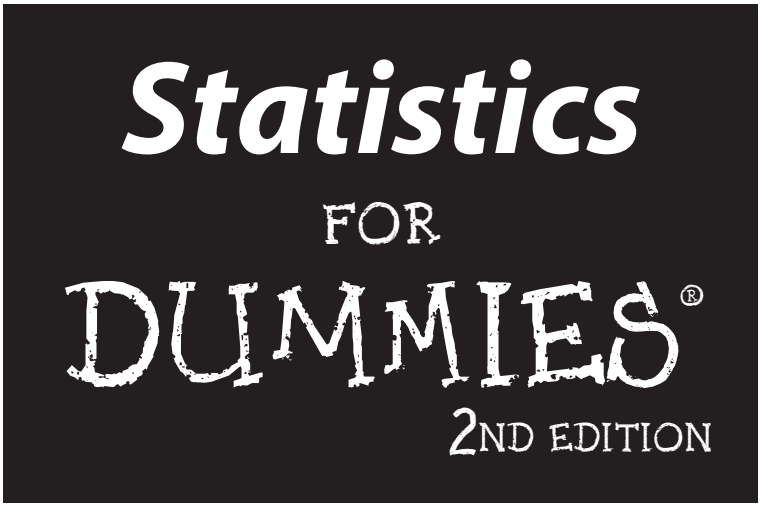

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Dedication

To my husband Eric: My sun rises and sets with you. To my son Clint: I love you up to the moon and back.

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