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7 Functional Responses and Temperature

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## Abstract

this is the abstract.

## 1 Introduction

The functional response describes how predators respond to changes in prey density (**hollingsawfly1959**)(**Solomon19**). As prey numbers increase, the consumption rate of predators initially increases then levels out, however the specific shape of the period of increase can vary (**hollingsawfly1959**). Holling modelled the functional response and suggested three different forms which worked for different types of organisms (**hollingsawfly1959**). These are Type I, where the rate of increase in prey consumption with prey density is constant before the plateau, type II where the rate of increase in prey consumption with prey density is decreasing and type III, where the rate of increase in prey consumption with prey density increases then decreases (**hollingsawfly1959**). The type I model can be described by equation 1, the type II model can be described by equation 3 where  $x_R$  is the resource density,  $c$  is the number of prey consumed per predator per unit time,  $a$  is the discovery or search rate of the consumer and  $h$  is the handling time (**Dawes2013**)(**Holling1959**). The type III model can be described by a generalised version of equation 2, equation 3 where  $q$  changes the shape of the curve(**Dawes2013**). When  $q = 0$ , the model is type II and when  $q > 0$ , the model is type III (**Dawes2013**). These equations are often written with  $Y$ , the number of prey consumed per predator, instead of  $c$  and  $T$ , the time, on the right side of the equation, however these equations are equivalent as  $c = \frac{Y}{T}$ .

$$c = ax_R \tag{1}$$

$$c = \frac{ax_R}{1 + hax_R} \tag{2}$$

$$c = \frac{ax_R^{q+1}}{1 + hax_R^{q+1}} \tag{3}$$

Models can be phenomenological or mechanistic. The Holling models described above are mechanistic however the type III model is more phenomenological due to the non-biological parameter  $q$ .

## 36 2 Methods

### 37 2.1 Computing Tools

### 38 2.2 Initial Data Sorting

39 The data used was from the Biotraits database (**Dell2013**), which contains information collated  
40 from different studies about how biological traits respond to environmental drivers. The param-  
41 eters of interest here were the number of prey the predator consumed per unit time and the resource  
42 density. Data sorting was carried out in python version 2.7. New columns were added and exper-  
43 iments with less than six experiments were removed. This new dataset was exported to a csv for  
44 model fitting. The

### 45 2.3 Model Fitting

46 The data were fitted to five different models, a quadratic model, a cubic model and the three  
47 Holling models (**Holling1959**) using R 3.6.2 (**RCoreTeam2017**). The Holling models were the  
48 type I model (equation 1, a linear model), type II model (equation 2) and generalised type III  
49 model (equation 3). Models were fitted sequentially for each experiment and plotted. This allowed  
50 the fit to be visually inspected as the model fitting process was improved.

#### 51 2.3.1 Linear models

52 The Holling type I, quadratic and cubic models were fitted using `lm` (base R). For the  
53 quadratic and cubic models, `poly` was used to compute orthogonal polynomials to avoid correlation  
54 of variables.

#### 55 2.3.2 Non-linear Models

56 The Holling type II and type III models were fitted using `NLSlm` (from the package `minpack.lm`  
57 (**Elzhov2016**)). The coefficients  $a$ ,  $h$ , and  $q$  were given a lower bound of zero and the maximum  
58 number of iterations was set to 1000. For both type II and type III models, starting values were  
59 calculated using starting value functions where  $a$ ,  $h$  and  $q$  were estimated, followed by sampling  
60 positive values around these initial values and repeatedly running the models and storing the  
61 coefficients and AIC values of these models. The coefficients of the model with the lowest AIC  
62 were used as the initial values for the main model fitting step. The initial value for  $h$  was the  
63 maximum value of  $c$ . The initial value for  $a$  was the initial steep part of the curve which was  
64 calculated by repeatedly fitting linear models the dataset then deleting the maximum value of  $x_R$   
65 and storing the largest gradient of these models. For the type III model, this initial value of  $q$  was

set at Once the starting values had been determined, the models were rerun with these initial values and plotted (with the other models).

## 2.4 Data Analysis

The models were compared using AIC and the most appropriate model was determined for each dataset. AIC was used because other techniques to compare models are not appropriate for non linear models. The confidence intervals for values of  $q$  were calculated and (using two times the standard error). When the confidence interval for  $q$  overlapped zero, the best AIC was recalculated for the remaining four models (because when the confidence interval for  $q$  is zero, the type III model is the same as the type III model).

## 3 Results

### 3.1 Number of Fits

Many of the Hollings model fit well to the data 1.

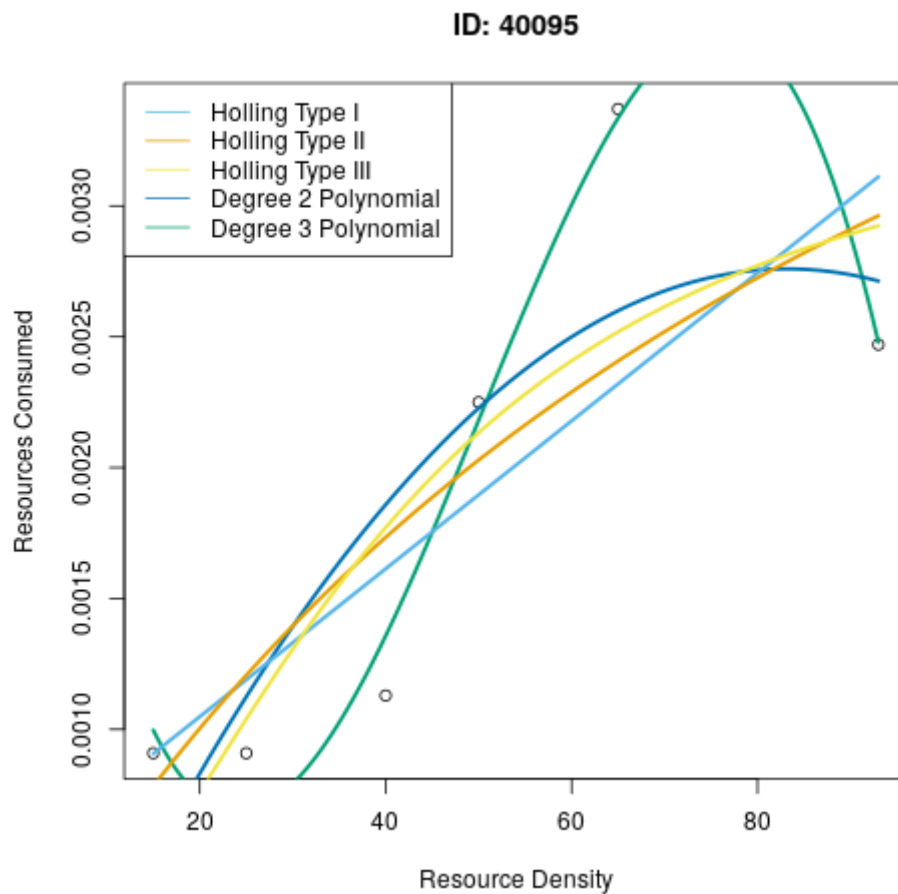
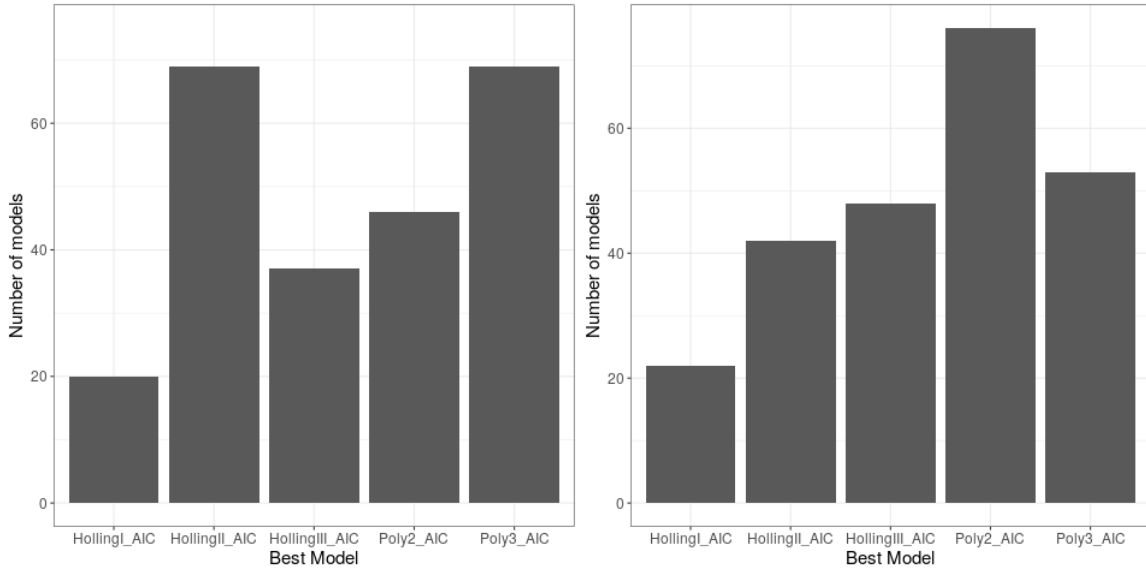


Figure 1: This is a graph for 40095

### 3.2 Best Model

The Holling's type II model was most frequently the best model (29.5%) and the polynomial of degree 2 was most frequently the second best model (31.5%) (Figure 2). The mechanistic models were marginally more often the best model (53.1%) than the mechanistic models (Figure 3 )



(a) Number of times that each model was the best model (b) Number of times that each model was the second best model

Figure 2: Best and second best model from the lowest and second lowest AIC values. Models are Holling type I, Holling type II, Holling type II, polynomial of degree 2, polynomial of degree 3. n=241

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81 The distribution of the best model was not best described by a uniform distribution but the  
82 distribution of the best model type was (Table??),

### 3.3 Temperature and Parameter Values

84 The consumer temperatures are associated with the search rate and handling time (Figure 4, Table  
85 ??) The search rate is smaller and less varied at intermediate temperatures, however at very low  
86 and very high temperatures, the temperature is very varied and can be very high. There is a  
87 weak negative correlation. The handling time shows a weak positive correlation with consumer  
88 temperature.

## 4 Discussion

## 5 Conclusion

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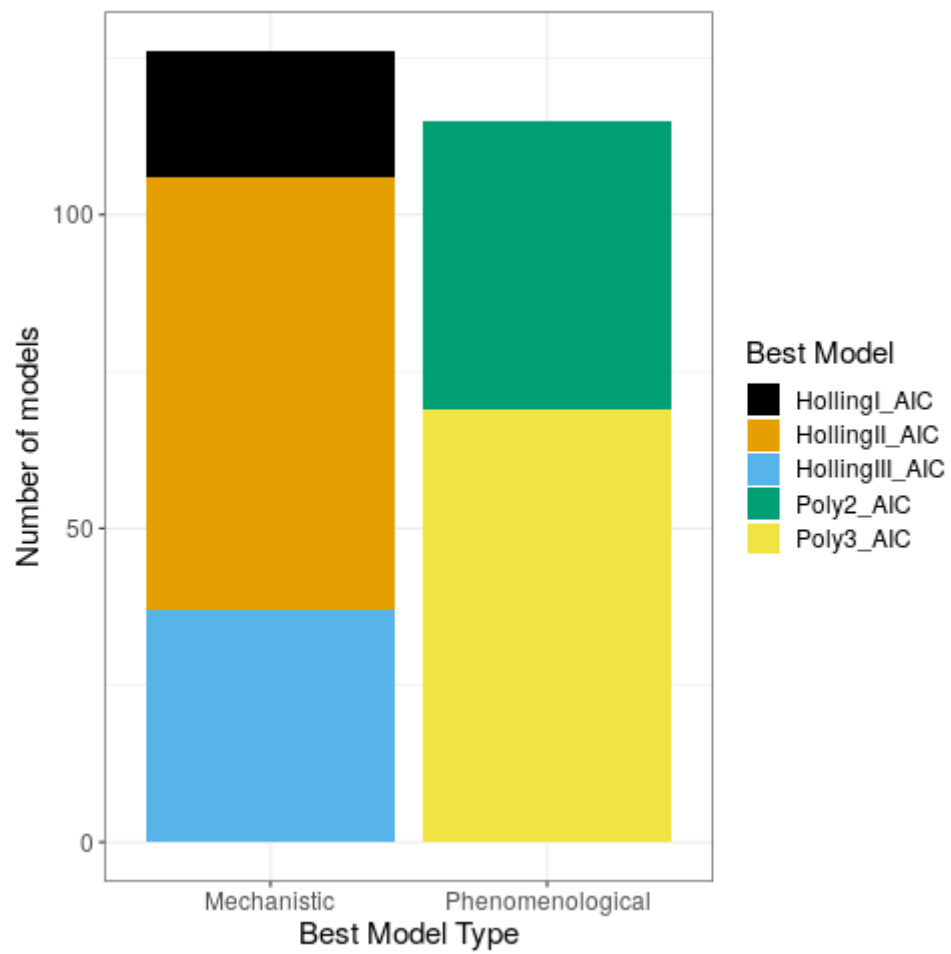
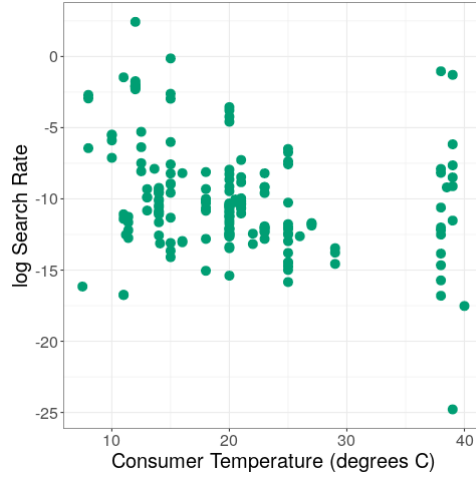
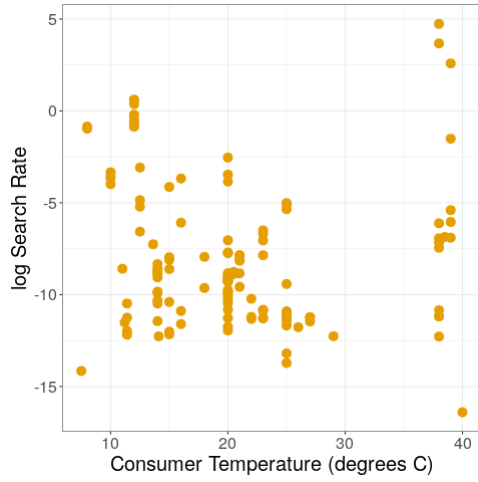


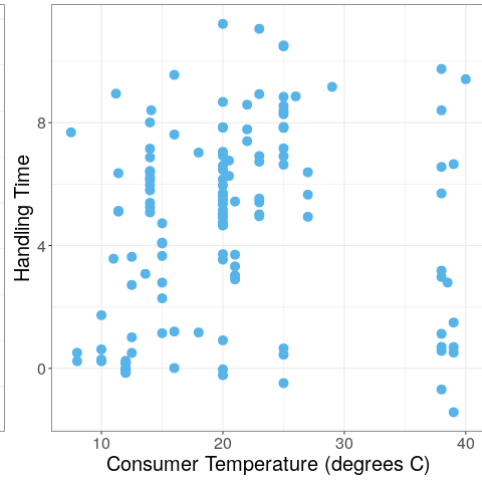
Figure 3: Number of models where the best type was phenomenological or mechanistic. Colour is the model. n=241



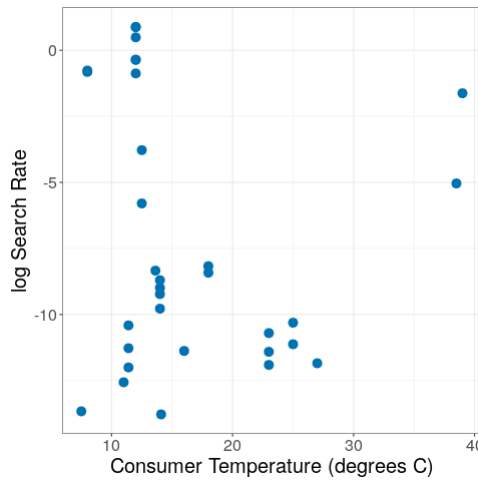
(a) Consumer temperature and log search rate for type I Holling model



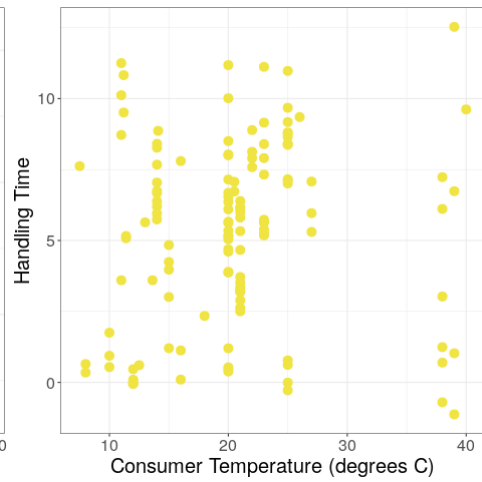
(b) Consumer temperature with log search rate for type II Holling model



(c) Consumer temperature with log handling time for type II Holling model



(d) Resource temperature with log search rate for type III Holling model



(e) Consumer temperature with log handling time for type III Holling model

Figure 4: Logged parameter values and Consumer temperature for Type I, Type II and Type II Holling Models.

- 91 1. A citation command in parentheses: (**hollingsawfly1959**).
- 92 2. A citation command for use in the flow of text: As **Holling1966** said ...
- 93 3. A citation command which automatically switches style depending on location and the option
- 94 setting in the package declaration (see line 12 in the LaTeX source code). In this case, it
- 95 produces a citation in parentheses: (**hollingsawfly1959**).