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Functional Response Models and Consumer Temperature

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Abstract

this is the abstract.

1 Introduction

1.1 Functional Responses and existing models

The functional response describes how predators respond to changes in prey density C. Holling 1959; Solomon 1949. As prey numbers increase, the consumption rate of predators initially increases then levels out, however the specific shape of the period of increase can vary C. Holling 1959. Holling modelled the functional response and suggested three different forms which worked for different types of organisms C. Holling 1959. These are Type I, where the rate of increase in prey consumption with prey density is constant before the plateau, type II where the rate of increase in prey consumption with prey density is decreasing (i.e the curve is hyperbolic and type III, where the rate of increase in prey consumption with prey density increases then decreases C. Holling 1959. The type I model can be described by equation 1, the type II model can be described by equation 3 where x_R is the resource density, c is the number of prey consumed per predator per unit time, a is the discovery or search rate of the consumer and h is the handling time Dawes and Souza 2013; C. S. Holling 1959. The type III model can be described by a generalised version of equation 2, equation 3 where q changes the shape of the curve Dawes and Souza 2013. When $q = 0$, the model is type II and when $q > 0$, the model is type III Dawes and Souza 2013. These equations are often written with Y , the number of prey consumed per predator, instead of c and T , the time, on the right side of the equation, however these equations are equivalent as $c = \frac{Y}{T}$.

$$c = ax_R \quad (1)$$

$$c = \frac{ax_R}{1 + hax_R} \quad (2)$$

$$c = \frac{ax_R^{q+1}}{1 + hax_R^{q+1}} \quad (3)$$

It is important to note that both the search rate and handling times are functions of different aspects of attacking and eating prey Hassel, Lawton, and Beddington 1976. In general, the Holling type II model is very successful, especially considering its simplicity however there are examples where data is better described by a more complex model, such as a type III Holling model Hassel, Lawton, and Beddington 1976. Many other models exist to describe the functional response, often

28 based on variations of the Holling equation accounting for different behavioural aspects Jeschke,
29 Kopp, and Tollrian 2002. Jeschke, Kopp, and Tollrian 2002 attempted to separate handling and
30 digestion time from h . In this example, the model curve tends to be similar to the Holling type
31 II functional response curve, but is more flexible and when both handling time and digestion time
32 are high, the curve is quite different. In addition, if values of a or h change with prey density, then
33 the Holling II model may not fit well (as a and h are constant in this model). In these examples,
34 the type III Holling model can be a good model Hassel, Lawton, and Beddington 1976.

35 1.2 Temperature and Functional Responses

36 1.3 Models

37 Models can be phenomenological or mechanistic. In mechanistic models, all parameters have
38 biological meaning and in phenomenological models they do not, instead a function is used that
39 fits the data or processes Otto and Day 2007; Geritz and Kisdi 2012. Phenomenological models
40 may fit better to data and can be very useful in the absence of mechanistic models. They can
41 be easier to understand, however do not have as much biological meaning as mechanistic models
42 Otto and Day 2007. Geritz and Kisdi 2012 claim that this could stop them being valid for use in
43 biological systems. Mechanistic models can improve our understanding of biology and are useful for
44 making predictions more accurately because when the meanings of parameters of known, biological
45 constraints can be included. They can include as much information about the system as is available
46 Otto and Day 2007; Kendall et al. 1999. Mechanistic models are simplifications of systems and may
47 have strong assumptions but they can still be very useful tools in understanding a biological system.
48 How well a simplified model fits to data can give important insight into what aspects of a system
49 are important in determining the dynamics Geritz and Kisdi 2012. The Holling models described
50 above are mechanistic to some extent however the type III model is more phenomenological due to
51 the non-biological parameter q . Even the Holling type II model may be partially phenomenological
52 because the values of a and h are a function of , multiple biological components Hassel, Lawton,
53 and Beddington 1976.

54 1.4 This work

55 In this paper, 5 models were fitted to experimental functional response data: Holling's type I,
56 Holling's type II, Holling's type III, a polynomial model of degree two (to capture increasing and
57 levelling out of the functional response) and a polynomial model of degree three (to capture a
58 change in the rate of increase of the functional response. Then the best model for each experiment
59 was determined. This was analysed and compared to temperatures. In addition the parameters of

the Holling’s models were compared to the consumer temperature.
It was expected that the Holling type III model would be able to fit better to the data but may have a higher AIC value due the the extra parameter.

2 Methods

2.1 Computing Tools

Bash was used to compile the pdf of the tex file, to calculate and format the word count of the project, using `texcount` and to run the project files. This was used due to the ease off accessing files and files contents compared to other languages as well as its ability to run python and R scripts. Python was used to initially sort the data, add new columns to the dataset and remove datasets with an insufficient number of points and export this updated dataframe as a csv. These tasks are well suited to Python’s abilities. R was used to model to data, plot graphs and analyse the data. This is due to R’s dataframe structures which make it very easy to store and manipulate variables. In addition `ggplot2`’s plotting is very flexible.

2.2 Initial Data Sorting

The data used was from the Biotraits database Dell, Pawar, and Savage 2013, which contains information collated from different studies about how biological traits respond to environmental drivers. The parameters of interest here were the number of prey the predator consumed per unit time and the resource density. Data sorting was carried out in python version 2.7. New columns were added and experiments with less than six experiments were removed. This new dataset was exported to a csv for model fitting. The

2.3 Model Fitting

The data were fitted to five different models, a quadratic model, a cubic model and the three Holling models C. S. Holling 1959 using R 3.6.2 R Core Team 2019. The Holling models were the type I model (equation 1, a linear model where the intercept was the origin), type II model (equation 2) and generalised type III model (equation 3). Models were fitted sequentially for each experiment and plotted. This allowed the fit to be visually inspected as the model fitting process was improved.

2.3.1 Linear models

The Holling type I, quadratic and cubic models models were fitted using `lm` (base R). For the quadratic and cubic models, `poly` was used to compute orthogonal polynomials to avoid correlation

90 of variables.

91 2.3.2 Non-linear Models

92 The Holling type II and type III models were fitted using NLSlm (from the package minpack.lm
93 Elzhov et al. 2016). The coefficients a , h , and q were given a lower bound of zero and the maximum
94 number of iterations was set to 1000. For both type II and type III models, starting values were
95 calculated using starting value functions where a , h and q were estimated, followed by sampling
96 positive values around these initial values and repeatedly running the models and storing the
97 coefficients and AIC values of these models. The coefficients of the model with the lowest AIC
98 were used as the initial values for the main model fitting step. The initial value for h was the
99 maximum value of c . The initial value for a was the initial steep part of the curve which was
100 calculated by repeatedly fitting linear models the dataset then deleting the maximum value of x_R
101 and storing the largest gradient of these models. For the type III model, this initial value of q was
102 set at Once the starting values had been determined, the models were rerun with these initial
103 values and plotted (with the other models).

104 2.4 Data Analysis

105 Data analysis was carried out in R 3.6.2R Core Team 2019. The models were compared using AIC
106 and the most appropriate model was determined for each dataset. AIC was used because other
107 techniques to compare models are not appropriate for non linear models.

108 The confidence intervals for values of q were calculated and (using two times the standard error).
109 When the confidence interval for q overlapped zero, the best AIC was recalculated for the remaining
110 Holling models (because when the confidence interval for q is zero, the type III model is the same
111 as the type III model. A chi-square (χ^2) goodness of fit test was carried out on the best model
112 and the best model type (phenomenological or mechanistic) to determine if the number of models
113 in each category was significantly different.

114 The p-value of each parameter was stored and if the model was not significant, the parameter was
115 removed from analysis of that parameter. Shapiro-Wilk tests were used to test the log consumer
116 temperatures and log parameter values and found that they were not normally distributed. In
117 addition, there were ties in the data so Spearman's rank correlation could not be calculated.
118 Kendall rank order correlation tests were carried out on consumer temperatures and log search
119 rate and consumer temperatures and log handling time for each of the Holling models. Log of the
120 parameters was used because both search rate and the handling time values were mostly very low
121 with a few very large values. The search rate for type III models could not be tested due to a low
122 number of models were search rate was significant.

Chi-square (χ^2) tests were carried out on consumer temperature and best model type and consumer temperature and best Holling model (recalculated). The temperature values were discretised by creating an expectation table with intervals of five degrees and combining these intervals until the expected values were all greater than five.

3 Results

3.1 Number of Fits

Many of the models fit well to the data, for example (Figure1). Most models successfully fit the data. Of the 241 datasets, only 19 Holling type II models and 22 Holling type II models did not converge.

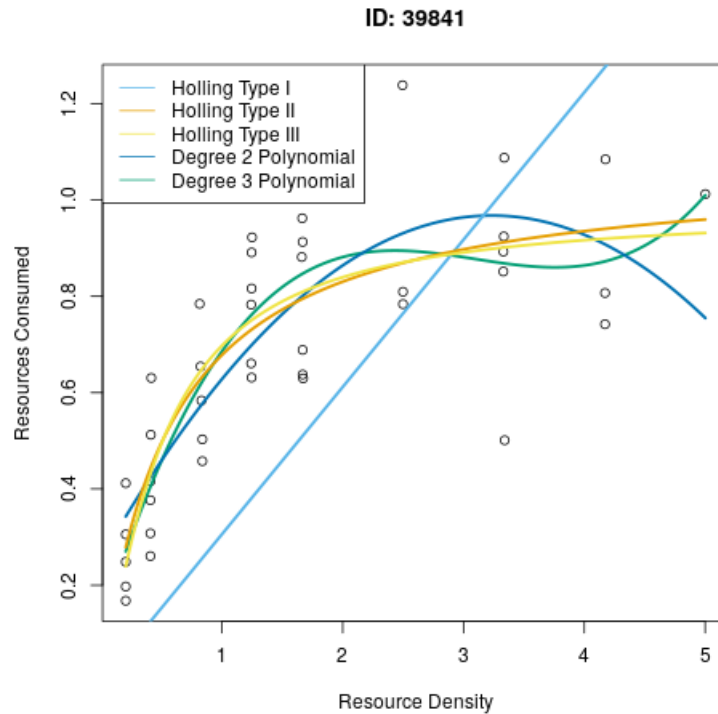


Figure 1: This is a graph for the experiment with ID 39841

3.2 Best Model

The Holling's type II model was most frequently the best model (0.29%) and the polynomial of degree 2 was most frequently the second best model (0.23%) (Figure 2). The mechanistic models were marginally more often the best model (%) than the mechanistic models (Figure 3). The distribution of the best model was not best described by a uniform distribution ($p < 0.01$) but the distribution of the best model type was ($p < 0.05$) (Table1),

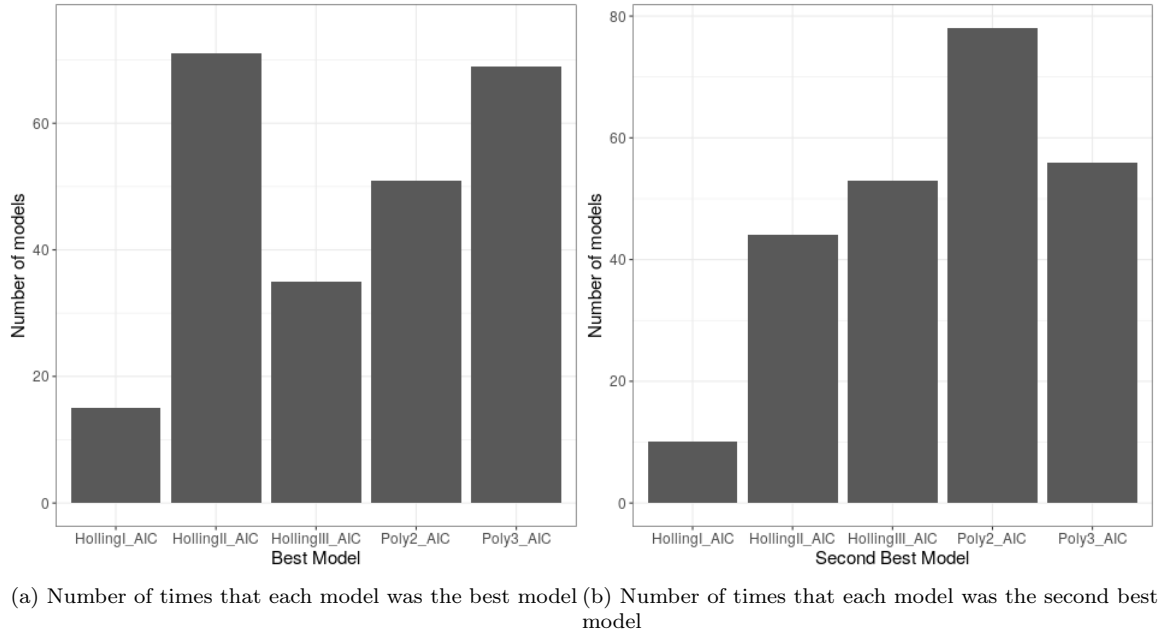


Figure 2: Best and second best model from the lowest and second lowest AIC values. Models are Holling type I, Holling type II, Holling type II, polynomial of degree 2, polynomial of degree 3. $n = 241$

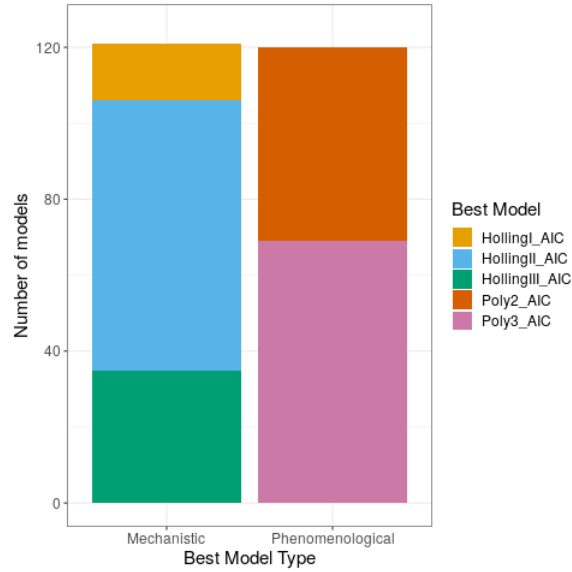


Figure 3: Number of models where the best type was phenomenological or mechanistic. Colour is the model. $n = 241$

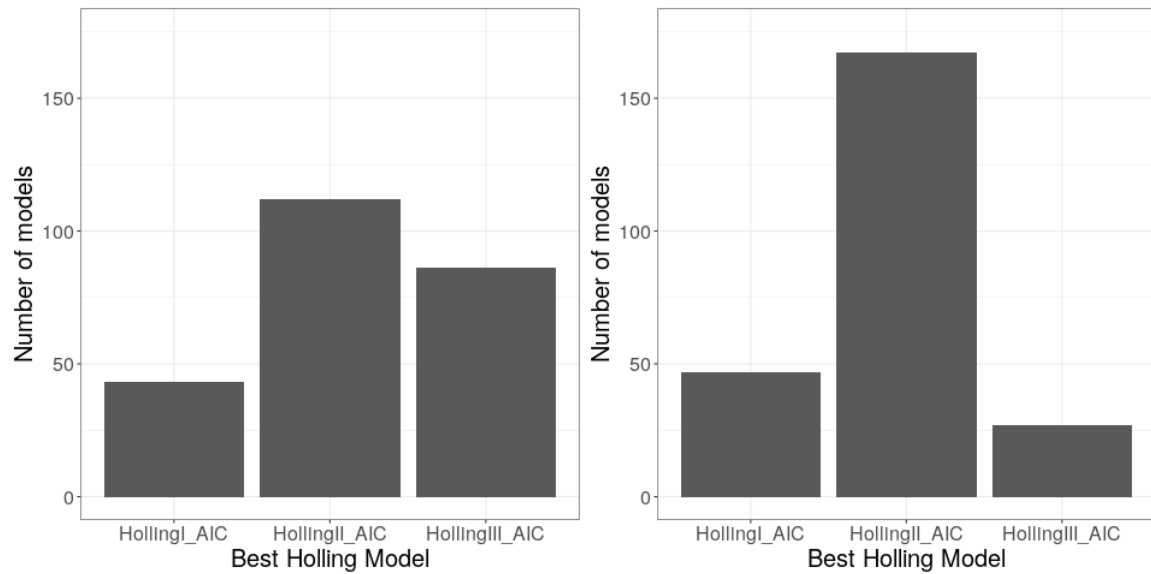
Table 1: Results of chi-squared tests for whether the best model and the best model type (i.e phenomenological or mechanistic) are uniformly distributed

	Chi-squared	p-value
Best Model	46.41	0.00

Best Model Type	0.00	0.95
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3.3 Best Holling Model

Of the three Holling models, the type II model was the best (Figure 4). The best Holling model was recalculated, removing the type III Holling model when the confidence interval for q spanned 0. This affected 59 models. The majority of these were best described by the Holling type II model of the other Holling models, but some were better described by the type I model (Figure 4)

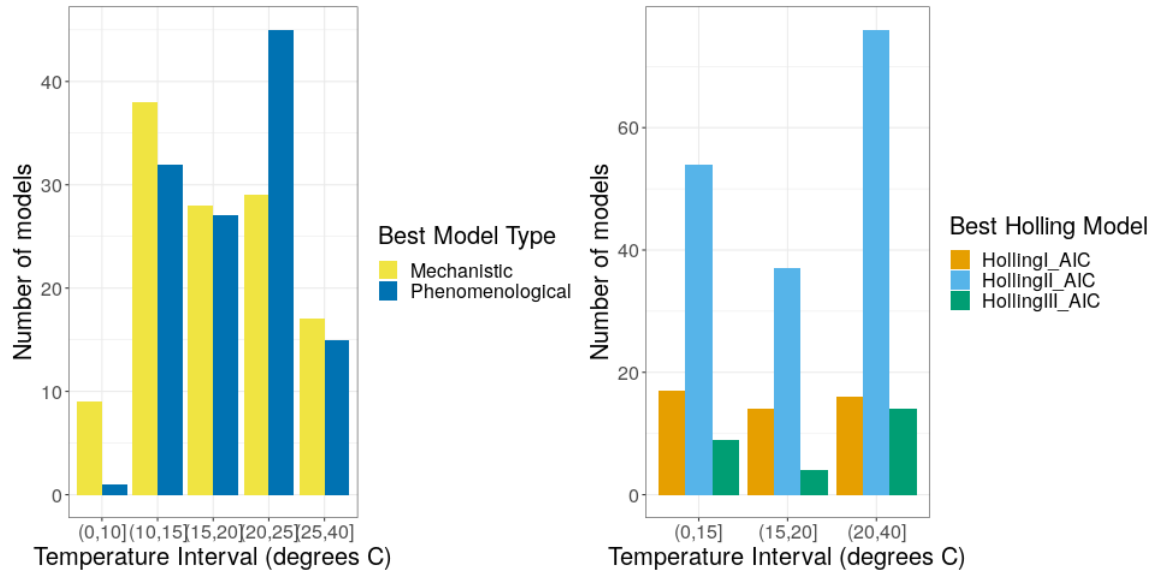


(a) Number of times that each model was the best Holling model
(b) Number of times that each model was the best Holling model, when the best Holling model was recalculated if the confidence intervals of q spanned 0

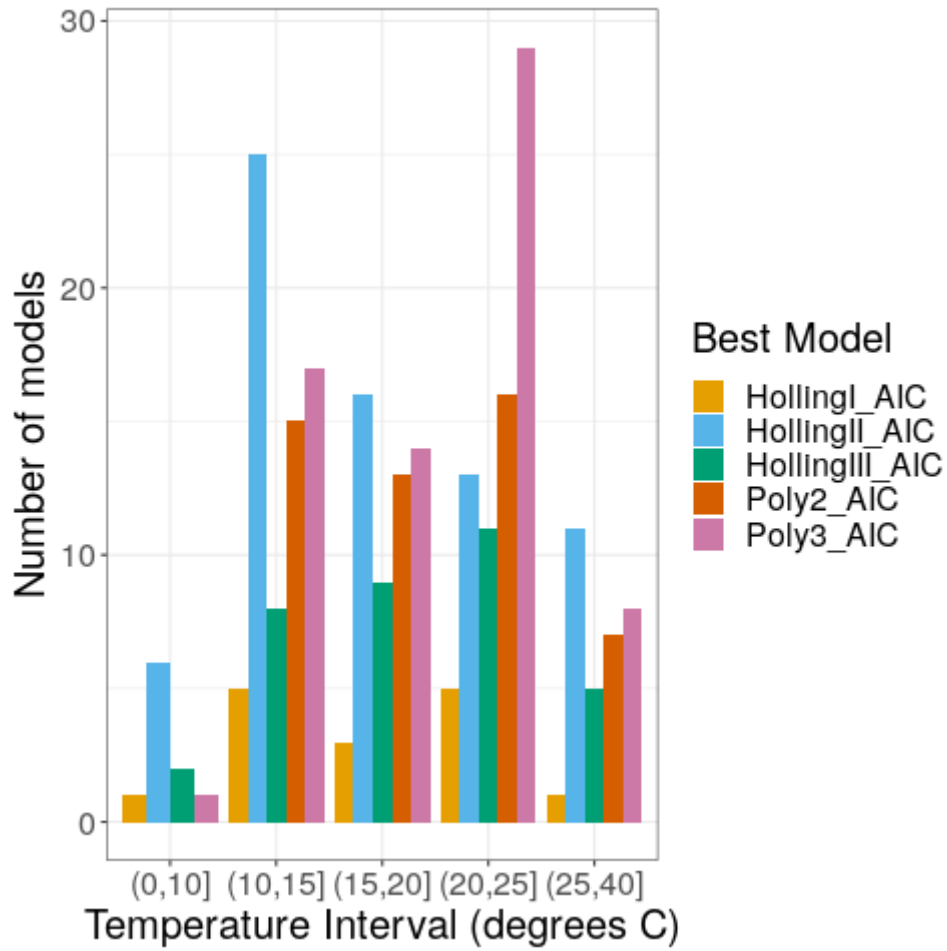
Figure 4: Best model from the lowest AIC values (of the Holling model). Models are Holling type I, Holling type II and Holling type II. $n = 241$

3.4 Temperature and Best Model

The best Holling model did not vary much with the temperature (Figure 5 and the temperature interval was not associated with the best Holling model. ($\chi^2 = 3.48, p = 0.48, df = 4$). At most temperatures (< 20 degrees), more mechanistic models fit the best better. Below 10 degrees this difference was extreme. However at the interval 20 – 25 degrees, more phenomenological models fit the best (Figure 5). The temperature interval was associated with the best model type ($\chi^2 = 10.51, p = 0.03, df = 4$). This difference seemed to be due to the polynomial of degree three being particularly successful in the interval 20 – 25 degrees.



(a) Number of times a mechanistic or a phenomenological model was the best model at each consumer temperature interval. (b) Number of times the recalculated Holling model was the best model at each consumer temperature interval.



(c) Number of times each model was the best model at each consumer temperature interval.

Figure 5: Best model is determined from the lowest AIC values. Colour is the best model type.
 $n = 241$

151 3.5 Temperature and Parameter Values

152 The handling time was and the search rate was The consumer temperatures are associated with
153 the search rate for type I and type II Holling models and handling time for type II and type III
154 Holling models.(Figure 6,Table 2).

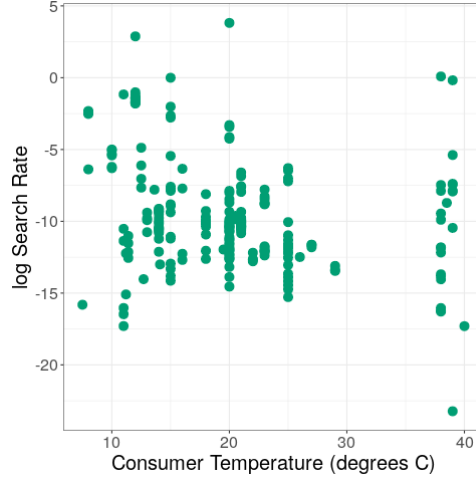
Table 2: Table of results for Kendall rank order correlation tests
for consumer temperature and parameter values.

	z	tau	p-value	n
Search rate type I	-4.58	-0.21	0.00	229.00
Search rate type II	-2.94	-0.18	0.00	137.00
Handling time type II	3.60	0.21	0.00	137.00
Handling time type III	2.39	0.15	0.02	130.00

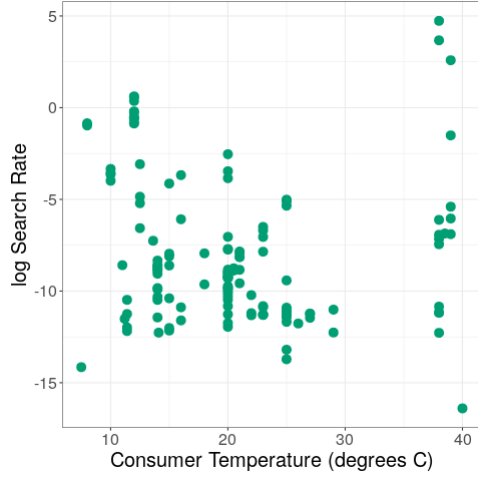
155 The search rate is smaller and less varied at intermediate temperatures, however at very low
156 and very high temperatures, the temperature is very varied and can be very high. There is a
157 weak negative correlation. The handling time shows a weak positive correlation with consumer
158 temperature.

159 4 Discussion

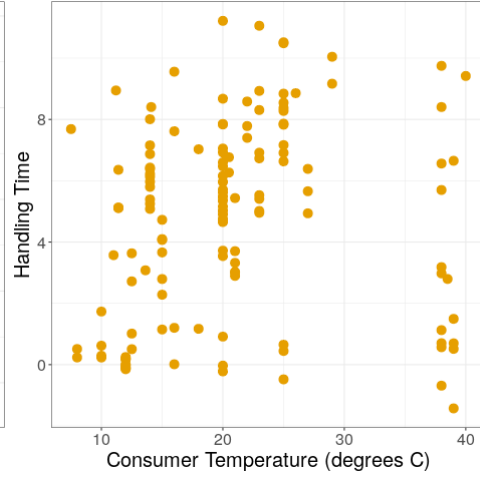
160 5 Conclusion



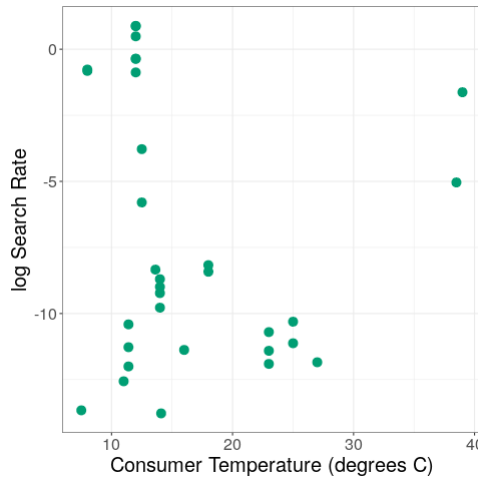
(a) Consumer temperature and log search rate for type I Holling model



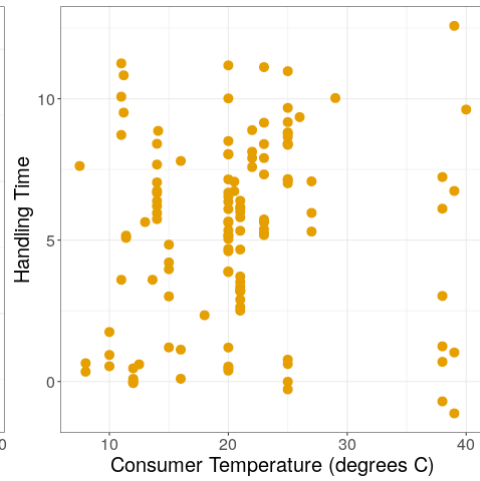
(b) Consumer temperature with log search rate for type II Holling model



(c) Consumer temperature with log handling time for type II Holling model



(d) Resource temperature with log search rate for type III Holling model



(e) Consumer temperature with log handling time for type III Holling model

Figure 6: Logged parameter values and Consumer temperature for Type I, Type II and Type II Holling Models.

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