

Empirical Distributions

```
clear

corg = load('organicmatter_one.txt');

plot(corg,zeros(1,length(corg)), 'o' )

nbin = round(sqrt(length(corg)))

vmin = min(corg) + 0.5*range(corg)/nbin;
vmax = max(corg) - 0.5*range(corg)/nbin;
vwth = range(corg)/nbin;
v = vmin : vwth : vmax;
```

```
v =  
Columns 1 through 4  
    9.7383    10.3814    11.0245    11.6676  
Columns 5 through 8  
   12.3107   12.9537   13.5968   14.2399
```

```

emin = min(corg);
emax = max(corg);
ewth = range(corg)/nbin;
e = emin : ewth : emax;

```

```

e =
Columns 1 through 4
    9.4168    10.0598    10.7029    11.3460
Columns 5 through 8
    11.9891    12.6322    13.2753    13.9184
Column 9
    14.5615

```

```

for i = 1 : nbin
    if i < nbin
        corgb = corg(emin+(i-1)*ewth<=corg & emin+i*ewth>corg);
        n(i) = length(corgb);
    else
        corgb = corg(emin+(i-1)*ewth<=corg & emin+i*ewth>=corg);
        n(i) = length(corgb);
    end
end

```

```

n =
    2     2    10     7    14     9    12     4

```

```
h = histogram(corg);
```

```
h =  
Histogram with properties:  
    Data: [60x1 double]  
   Values: [2 6 13 20 15 4]  
  NumBins: 6  
 BinEdges: [9 10 11 12 13 14 15]  
 BinWidth: 1  
 BinLimits: [9 15]  
Normalization: 'count'  
  
    FaceColor: 'auto'  
    EdgeColor: [0 0 0]
```

```
cdfplot(corg)
```

```
mean(corg)
```

```
median(corg)
```

```
quantile(corg,[.25 .50 .75])
```

```
boxplot(corg)
```

`range(corg)`

`var(corg)`

`std(corg)`

`kurtosis(corg)`

`skewness(corg)`

Try to play the following two commands

randtool

disttool

The t-Test

$$\hat{t} = \frac{|\bar{a} - \bar{b}|}{\sqrt{\frac{n_a + n_b}{n_a n_b} \cdot \frac{(n_a - 1) \cdot s_a^2 + (n_b - 1) \cdot s_b^2}{n_a + n_b - 2}}}$$

The one-sample t-test is used to test the hypothesis that the mean of a Gaussian-distributed population has a value specified in the null hypothesis. The two-sample t-test is employed to test the hypothesis that the means of two Gaussian distributions are identical.

Two-sample test

```
clear

load('organicmatter_two.mat');

histogram(corg1,'FaceColor','b'), hold on
histogram(corg2,'FaceColor','r'), hold off

na = length(corg1); nb = length(corg2);
ma = mean(corg1); mb = mean(corg2);
sa = std(corg1); sb = std(corg2);

tcalc = abs((ma-mb))/sqrt(((na+nb)/(na*nb)) * ...
    (((na-1)*sa^2+(nb-1)*sb^2)/(na+nb-2)))

tcalc =
    0.7279

tcrit = tinv(1-0.05/2,na+nb-2)

tcrit =
    1.9803
```



```
[h,p,ci,stats] = ttest2(corg1,corg2,0.05)
```

```
h =  
    0
```

```
p =  
    0.4681
```

```
ci =  
   -0.3028  
    0.6547
```

```
stats =  
    tstat: 0.7279  
         df: 118  
         sd: 1.3241
```

Test1:

Load 'organicmatter_three.mat' to do two-sample T-test

```
load('organicmatter_three.mat');
```

The F-Test

The two-sample F -test by Snedecor and Cochran (1989) compares the variances s_a^2 and s_b^2 of two distributions, where $s_a^2 > s_b^2$. An example is the comparison of the natural heterogeneity of two samples based on replicated measurements. The sample sizes n_a and n_b should be above 30. Both the sample and population distributions must be Gaussian. The appropriate test statistic with which to compare the variances is then

$$\hat{F} = \frac{s_a^2}{s_b^2}$$

```
clear
```

```
load('organicmatter_four.mat');
```

```
s1 = std(corg1)
```

```
s2 = std(corg2)
```

```
df1 = length(corg1) - 1
```

```
df2 = length(corg2) - 1
```

```
if s1 > s2
```

```
    slarger = s1
```

```
    ssmaller = s2
```

```
else
```

```
    slarger = s2
```

```
    ssmaller = s1
```

```
end
```

```
    slarger =
```

```
        1.2550
```

```
    ssmaller =
```

```
        1.2097
```

```
Fcalc = slarger^2 / ssmaller^2
```

```
Fcrit = finv(1-0.05/2,df1,df2)
```

```
Fcalc =
```

```
    1.0762
```

```
Fcrit =
```

```
    1.6741
```

```
[h,p,ci,stats] = vartest2(corg1,corg2,0.05)
```

```
h =  
    0
```

```
p =  
    0.7787
```

```
ci =  
    0.6429  
    1.8018
```

```
stats =  
    fstat: 1.0762  
        df1: 59  
        df2: 59
```

Test2: Load 'organicmatter_five.mat' to do the two-sample F-test

```
load('organicmatter_five.mat');
```