CP 313 Autonomous Navigation

Homework Assignment #2

1. Consider two views of the high voltage department building provided at the following link:

Due: November 5, 2019

https://github.com/rbccps-iisc/cp313/tree/master/hw_2

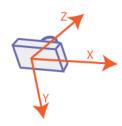
These images were taken by a GoPro camera whose intrinsics are given below.

$$\begin{bmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 2.00957e + 03 & 0 & 2.0e + 03 \\ 0 & 1.99901e + 03 & 1.5e + 03 \\ 0 & 0 & 1 \end{bmatrix}$$

The distortion parameters are given by:

$$[k_1,k_2,p_1,p_2,k_3] = [-1.6246e - 02, -5.0516e - 02, 2.6182e - 04, 4.5523e - 03, 6.347e - 02].$$

Estimate the fundamental matrix associated with the two views, and use this to compute the motion of the camera between the two views. The camera coordinate system is shown in the figure below.



For a rough solution, you may omit the distortion.

2. Consider two views of the Entrepreneurship Centre Building following link: https://github.com/rbccps-iisc/cp313/tree/master/hw_2

The second position of the camera was obtained by traslating by the amount $[0.24, 0, -1.8]^T$ and rotating it about the y-axis by -19° . Based on the above, compute the height and width of the monitor in the image. Use the same convention for the camera coordinate system as in Problem 1. Also, assume the same camera intrinsics.

3. Given the translation \mathbf{t} and rotation \mathbf{R} between two poses of a camera, we know that the essential matrix can be written as $\mathbf{E} = [\mathbf{t_x}]\mathbf{R}$.

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- (a) Show that the cross product operation $[t_x]$ can be written as $[t_x] = \mathbf{SZR_{90}S^T}$, where **S** is an orthonormal basis, **Z** is a 3×3 identity matrix with the last diagonal element zeroed out, and $\mathbf{R_{90}}$ is a matrix that represents a 90° rotation about the first basis vector of **S**.
- (b) Based on the result in (a), show how you would extract the translation vector \mathbf{t} and the rotation matrix \mathbf{R} out of \mathbf{E} .
- 4. Let $\{(\mathbf{x_i}, \mathbf{x_i'})\}$ be a set of matched feature points in two images, where $\mathbf{x'} = \mathbf{f}(\mathbf{x}; \mathbf{p})$. Here $\mathbf{f}(.)$ is a planar transformation parametrized by \mathbf{p} .
 - (a) Assume that the motion between the two views is small. Let $\Delta \mathbf{x} = \mathbf{x}' \mathbf{x} = \mathbf{J}(\mathbf{x})\mathbf{p}$, where \mathbf{J} is the Jacobian of the transformation \mathbf{f} . Derive an equation with \mathbf{p} as the variable that can be solved for p.
 - (b) Using the result in (a) find the solution for the case where the transformation represents a simple translation.