Lab 3 – Completely Randomized ANOVA (a.k.a. One-way ANOVA)

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Today's Topics

Brief Overview of ANOVA

2 ANOVA IN R

Multiple comparisons

ONE-WAY ANOVA

Scenario

- We have independent samples from a > 2 groups
- We assume a common variance

Questions

- Do the means differ?
- By how much? (What are the effect sizes?)

Null hypothesis

- $H_0: \mu_1 = \mu_2 = \mu_3 = \ldots = \mu_a$
- Or:
- $H_0: \alpha_1 = \alpha_2 = \alpha_3 = \ldots = \alpha_a = 0$

Additive model

$$y_{ij} = \mu + \alpha_j + \varepsilon_{ij}$$

where:

- Residuals: $\varepsilon_{ij} \sim \text{Norm}(0, \sigma^2)$
- Group means: $\mu_i = \mu + \alpha_i$

BRIEF OVERVIEW OF ANOVA

MILITIDI E COMPADISONS

CHAIN SAW DATA

The data as 4 vectors

```
kick.angle.brandA <- c(42,17,24,39,43)
kick.angle.brandB <- c(28,50,44,32,61)
kick.angle.brandC <- c(57,45,48,41,54)
kick.angle.brandD <- c(29,40,22,34,30)
```

Format as a data.frame

```
n <- length(kick.angle.brandA)
a <- 4
sawData <- data.frame(
   Kick.angle=c(kick.angle.brandA, kick.angle.brandB,
        kick.angle.brandC, kick.angle.brandD),
   Brand=rep(c("A","B","C","D"), each=n))</pre>
```

Prier Overview of ANOVA

ANOVA IN R

MULTIPLE COMPARISONS

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Two ANOVA FUNCTIONS: aov AND lm

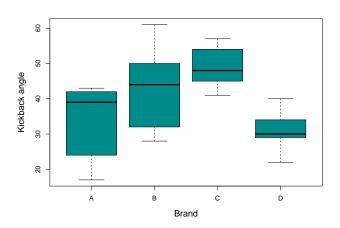
R has 2 common functions for doing ANOVA: aov and lm

We will primarily use aov in this class

Crude characterization

	aov	lm
Emphasis	ANOVA tables	Linear models
Typical use	Designed experiments	Regression analysis
Multiple error strata?	Yes	No

VIZUALIZE THE DATA



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USING aov

Do the analysis

```
aov.out1 <- aov(Kick.angle ~ Brand, data=sawData)</pre>
```

View the ANOVA table

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```
Estimates of effect sizes (\alpha's) and SE
```

model.tables(aov.out1, type="effects", se=TRUE)

```
model.tables(aov.out1, type="means", se=TRUE)

## Tables of means
## Grand mean
##
## 39
##
## Brand
## Brand
## A B C D
## 33 43 49 31
##
## Standard errors for differences of means
## Brand
## 6.364
## replic. 5
```

EF OVERVIEW OF ANOVA ANOVA IN R MULTIPLE

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Multiple comparisons

CREATE ANOVA TABLE BY HAND

Grand mean

```
ybar. <- mean(sawData$Kick.angle)
ybar.
## [1] 39</pre>
```

Find the group means, the hard way

Find the group means, the easier way

```
ybar.i <- tapply(sawData$Kick.angle, sawData$Brand, mean)
ybar.i

## A B C D
## 33 43 49 31</pre>
```

Sums of squares

replic.

```
Sums of squares among
```

Tables of effects

Standard errors of effects

4.5

Brand

##

##

##

##

Brand

A B C D

-6 4 10 -8

Brand

```
SSa <- n*sum((ybar.i - ybar.)^2)
SSa
## [1] 1080</pre>
```

Sums of squares within

```
y.ij <- sawData$Kick.angle
SSw <- sum((y.ij - rep(ybar.i, each=n))^2)
SSw
## [1] 1620</pre>
```

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Means squares and F statistic

Mean squares among

```
df1 <- a-1
MSa <- SSa / df1
MSa
## [1] 360</pre>
```

Mean squares within

```
df2 <- a*(n-1)

MSw <- SSw / df2

MSw

## [1] 101.25
```

F statistic

```
F.stat <- MSa / MSw
F.stat
## [1] 3.555556
```

PRIED OVERVIEW OF ANOVA

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TODAY'S TOPICS

- BRIEF OVERVIEW OF ANOVA
- 2 ANOVA IN R
- 3 Multiple comparisons

CRITICAL VALUES AND p-VALUES

Critical value

```
F.crit <- qf(0.95, df1, df2)
F.crit
## [1] 3.238872
```

p-value

```
p.value <- 1 - pf(F.stat, df1, df2)
p.value
## [1] 0.03823275</pre>
```

Conclusion: Reject the null

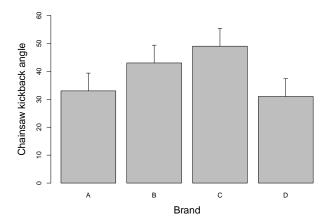
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Group means +1 SE



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TUKEY'S HONESTLY SIGNIFICANT DIFFERENCE TEST

```
TukeyHSD(aov.out1)
     Tukey multiple comparisons of means
##
       95% family-wise confidence level
##
## Fit: aov(formula = Kick.angle ~ Brand, data = sawData)
##
## $Brand
       diff
                   lwr
                              upr
                                      p adj
            -8.207419 28.2074187 0.4213711
         16 -2.207419 34.2074187 0.0955690
## C-A
## D-A
         -2 -20.207419 16.2074187 0.9888365
## C-B
          6 -12.207419 24.2074187 0.7826478
        -12 -30.207419 6.2074187 0.2726522
       -18 -36.207419 0.2074187 0.0532168
```

MULTIPLE COMPARISONS

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MULTIPLE COMPARISONS

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Assignment

A biologist wants to compare the growth of four different tree species she is considering for use in reforestation efforts. All 32 seedlings of the four species are planted at the same time in a large plot. Heights in meters are recorded after several years. The data are in the file treeHt.csv:

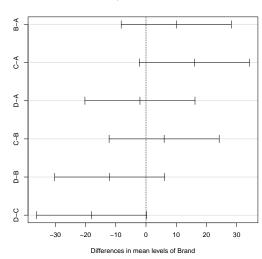
Create an R script to do the following:

- (1) Create an ANOVA table using the aov and summary functions.
- (2) Create an ANOVA table (degrees of freedom, sums-of-squares, mean-squared error, and F-value) without using aov. Compute either the critical value of F or the p-value.
- (3) Add a comment to the script indicating what the null hypothesis is, and whether or not it can be rejected at the $\alpha=0.05$ level.
- (4) Use Tukey's HSD test to determine which pairs of means differ at the $\alpha = 0.05$ level. Add a comment, indicating which pairs are different.
- (5) Create a barplot showing the means and SEs.

PLOT TUKEY'S CONFIDENCE INTERVALS

plot(TukeyHSD(aov.out1))





ANOVA IN R

Multiple comparisons