Lab 4 – Contrasts, Estimation, and Power Analysis

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Today's Topics

- CONTRASTS
- 2 ESTIMATION
- 3 Power

CHAIN SAW DATA

```
sawData <- read.csv("sawData.csv")</pre>
sawData
       y Brand
     24
     50
## 10 61
## 11 57
## 12 45
## 13 48
             С
## 14 41
             С
## 15 54
## 16 29
## 17 40
## 18 22
## 19 34
              D
## 20 30
```

Contrasts

Suppose we want to make 3 a priori comparisons:

- (1) Groups A&D vs B&C
- (2) Groups A vs D
- (3) Groups B vs C

	Comparision	Null hypothesis
1	AD vs BC	$\frac{\mu_A + \mu_D}{2} - \frac{\mu_B + \mu_C}{2} = 0$
2	A vs D	$\mu_A - \mu_D = 0$
3	B vs C	$\mu_B - \mu_C = 0$

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Constructing contrasts in R

Coefficients

```
ADvBC \leftarrow c(1/2, -1/2, -1/2, 1/2)

AvD \leftarrow c(1, 0, 0, -1)

BvC \leftarrow c(0, 1, -1, 0)
```

Are they orthogonal?

```
      sum(ADvBC)
      sum(ADvBC * AvD)

      ## [1] 0
      ## [1] 0

      sum(AvD)
      sum(ADvBC * BvC)

      ## [1] 0
      ## [1] 0

      sum(BvC)
      sum(AvD * BvC)

      ## [1] 0
      ## [1] 0
```

Yes, they are.

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Contrasts

Fit the model with contrasts

Now "split" apart the sum-of-squares

```
summary(aov.out, split = list(Brand =
                   list("ADvBC"=1, "AvD"=2, "BvC"=3)))
                Df Sum Sq Mean Sq F value Pr(>F)
##
## Brand
                 3 1080
                           360.0
                                  3.556 0.03823 *
    Brand: ADvBC 1
                     980
                           980.0 9.679 0.00672 **
    Brand: AvD
               1 10
                          10.0 0.099 0.75738
    Brand: BvC
               1
                      90
                           90.0 0.889 0.35980
## Residuals
                16 1620 101.2
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

WE NEED TO PUT THE CONTRASTS INTO A MATRIX

To use contrasts in R, each set of coefficients must be formatted as a column in a matrix.

We can use cbind for this:

```
contrast.mat <- cbind(ADvBC, AvD, BvC)
contrast.mat

## ADvBC AvD BvC

## [1,] 0.5 1 0

## [2,] -0.5 0 1

## [3,] -0.5 0 -1

## [4,] 0.5 -1 0
```

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DIFFERENCE IN MEANS FOR EACH CONTRAST

Group means

Contrasts

```
(group.means <- tapply(sawData$y, sawData$Brand, mean))

## A B C D

## 33 43 49 31
```

Difference in means for A vs D

```
group.means <- unname(group.means) # Drop names (optional)
group.means[1] - group.means[4]
## [1] 2</pre>
```

Difference in means for B vs C

```
group.means[2] - group.means[3]
## [1] -6
```

Difference in means for AD vs BC

```
mean(group.means[c(1,4)]) - mean(group.means[2:3])
## [1] -14
```

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STANDARD ERRORS FOR EACH CONTRAST

SE for A vs D

SE for B vs C

SE for AD vs BC

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© CONTRASTS

2 ESTIMATION

Today's Topics

3 Power

ESTIMATING CONFIDENCE INTERVALS

In an ANOVA context, confidence intervals can be constructed using the equation:

$$\mathsf{CI} = \mathsf{Point} \ \mathsf{estimate} \pm t_{\alpha/2,a(n-1)} \times \mathsf{SE}$$

As usual, the hard part is computing the SE¹

Confidence intervals from one-way ANOVA

SE's for the effect sizes (α 's)

```
effects.SE <- model.tables(aov.out, type="effects", se=TRUE)

effects.SE

## Tables of effects

## ## Brand

## Brand

## A B C D

## -6 4 10 -8

##

## Standard errors of effects

## ## Brand

## ## Standard errors of effects

## ## Prand

## ## Brand

## ## Standard errors of effects

## ## Brand

## ## 1.5

## replic. 5
```

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¹See page 300 of Dowdy et al. for SE formulas

CONFIDENCE INTERVALS FROM ONE-WAY ANOVA

Extract the α 's and the SEs

```
# str(effects.SE)
alpha.i <- as.numeric(effects.SE$tables$Brand)
SE <- as.numeric(effects.SE$se)</pre>
```

Compute confidence intervals

```
tc <- qt(0.975, 4*(5-1))
lowerCI <- alpha.i - tc * SE
upperCI <- alpha.i + tc * SE</pre>
```

Put results into a data.frame

```
CI <- data.frame(effect.size=alpha.i, SE,</pre>
                 lowerCI, upperCI)
round(CI, 2)
     effect.size SE lowerCI upperCI
## 1
              -6 4.5 -15.54
                                 3.54
## 2
               4 4.5
                       -5.54
                                13.54
## 3
              10 4.5
                         0.46
                                19.54
## 4
              -8 4.5 -17.54
                                 1.54
```

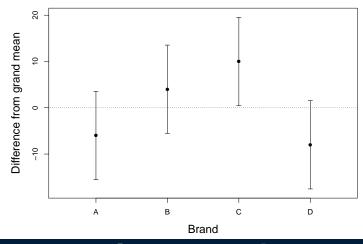
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PLOT EFFECTS AND CIS

```
plot(1:4, CI$effect.size, xlim=c(0.5, 4.5), ylim=c(-18, 20), xaxt="n",
    xlab="Brand", ylab="Difference from grand mean", pch=16, cex.lab=1.5)
axis(1, at=1:4, labels=c("A", "B", "C", "D"))
abline(h=0, lty=3)
arrows(1:4, CI$lowerCI, 1:4, CI$upperCI, code=3, angle=90, length=0.05)
```



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Power analysis for a 2-sample t-test

```
power.t.test(n=NULL, delta=3, sd=2, sig.level=0.05,
             power=0.8)
##
##
        Two-sample t test power calculation
##
                 n = 8.06031
##
##
             delta = 3
                sd = 2
##
         sig.level = 0.05
##
##
             power = 0.8
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
```

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POWER ANALYSIS FOR ONE-WAY ANOVA

```
power.anova.test(groups=4, n=5, between.var=360.0,
                 within.var=101.2, power=NULL)
##
##
        Balanced one-way analysis of variance power calculation
##
##
            groups = 4
##
                 n = 5
##
       between.var = 360
##
        within.var = 101.2
         sig.level = 0.05
##
##
             power = 0.9999359
##
## NOTE: n is number in each group
```

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Assignment

Researchers wish to know if food supplementation affects the growth of nestling Canada warblers. The treatment groups are: (A) No supplementation control, (B) low, (C) medium, (D) high, and (E) very high. The response variable is the weight of a 10 day old nestling.

- (1) The researchers are interested in the following contrasts. Are they ortholognal?
 - ► Groups A,B vs C,D,E
 - Groups A vs B
 - ► Groups C vs D,E
 - ► Groups D vs E
- (2) Using the warblerWeight data, test the null hypothesis of each contrast by constructing an ANOVA table in **R**.
- (3) For each contrast:
 - ► Compute the difference in the means
 - ► The SE of the difference in means
 - ▶ The 95% CI for the difference in means
- (4) Suppose you wanted to replicate the study with a smaller sample size of n=2 per treatment group? What would be your power?

Submit your answers in a self-contained script before the next lab.

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