



Master's Thesis Presentation

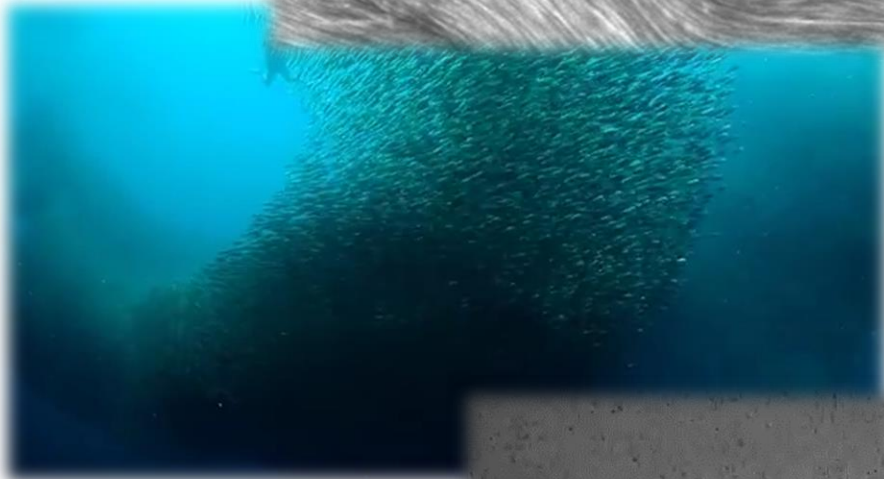
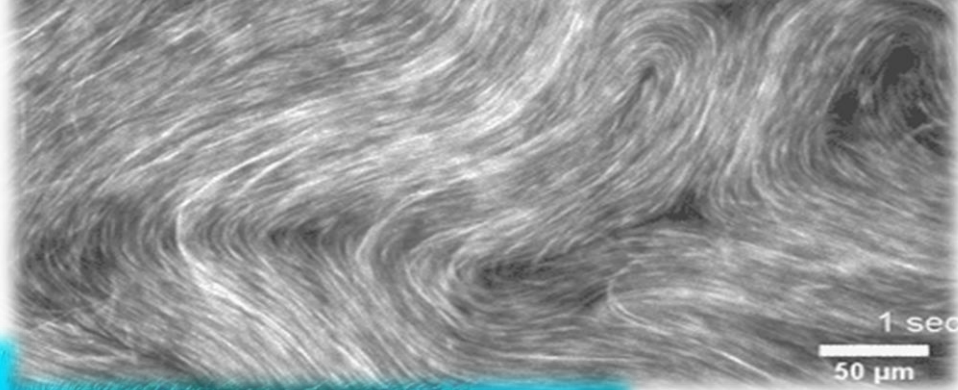
Active Colloids in Shear Flow

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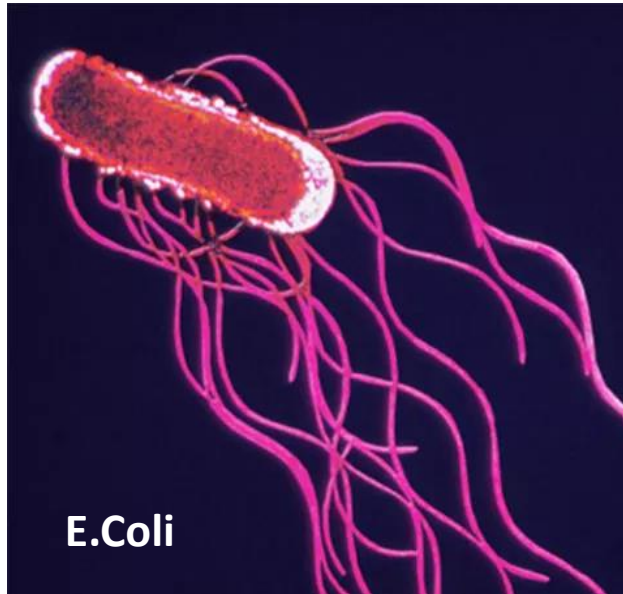
28th June, 2019



What are Active Particles?

- Colloidal particles ($\sim 1 \text{ nm} - 1000 \text{ nm}$) which can self-propel by using energy from surroundings and perform directed motion at short times.
- Classification : Biological and Artificial

Biological Swimmers



Turner et al. J. Bacteriol, 2000



Turner et al. J. Bacteriol, 2000



N. Petkov et al. 2007

Active colloids

Solid Colloids



SiO₂-Pt Janus particles in H₂O₂

CPPG, IITK (2018)




Au-Pt Microrods in H₂O₂

Paxton et al. JACS, (2006)

Active emulsions

Soft Emulsion Droplets



5CB LC droplets in TTAB Solution

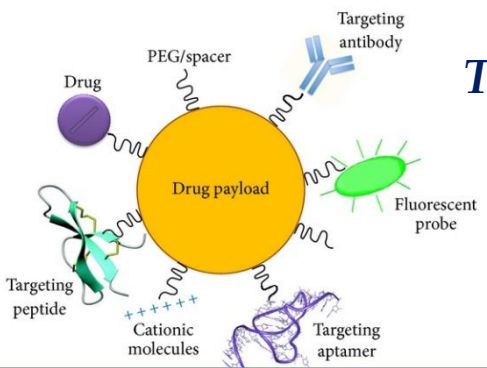
CPPG, IITK (2018)



Oil droplets containing microtubule bundle

Dogic Lab, UCSB

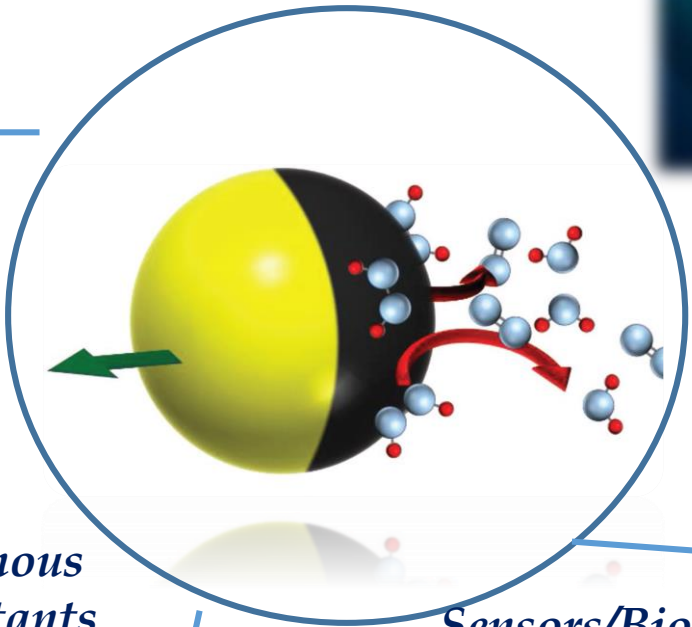
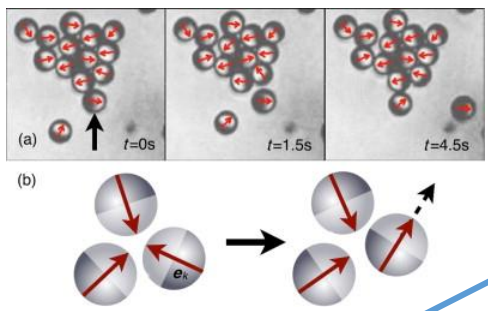
Artificial Active Colloids : Significance



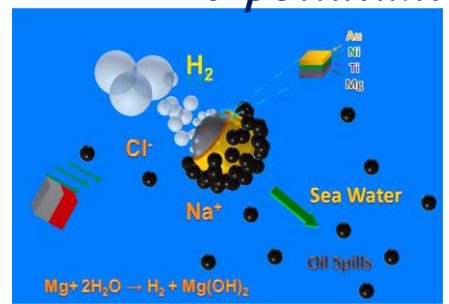
Targeted Drug/Cargo Delivery

Model Systems

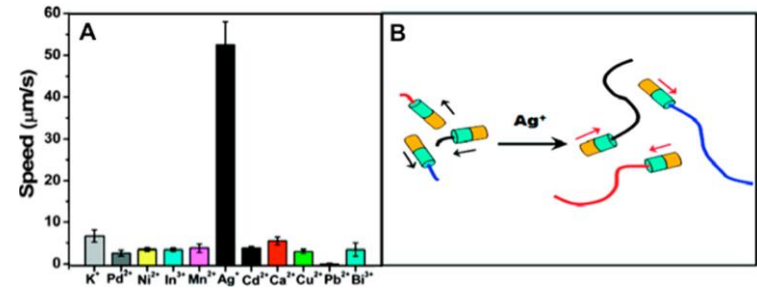
Novel Colloidal Self-assembly



Autonomous De-pollutants



Sensors/Bio-markers



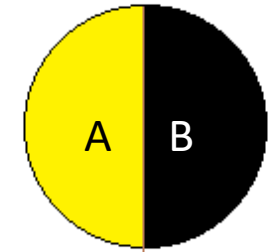
Mechanisms of propulsion

Key requirements:

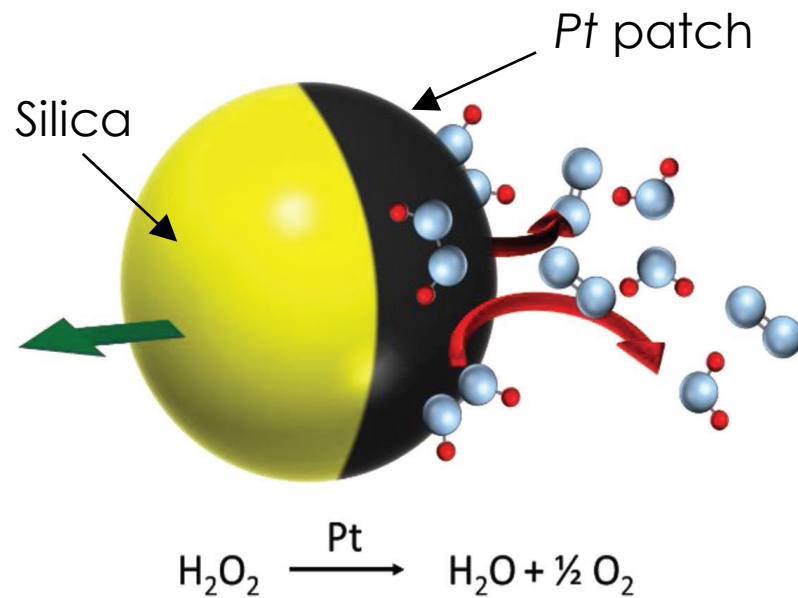
- A local gradient(chemical /physical)
- Asymmetry in particle composition



Janus particle



Self-Diffusiophoresis



Archer et al. Adv. Sc., (2017)

Self-Thermophoresis

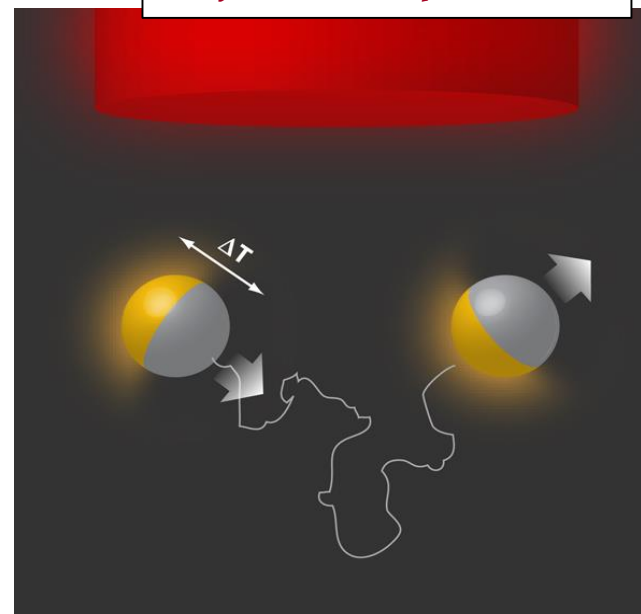
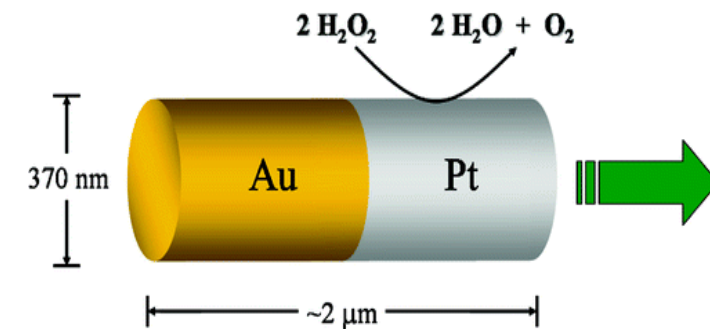


Image from APS Physics

Self-electrophoresis



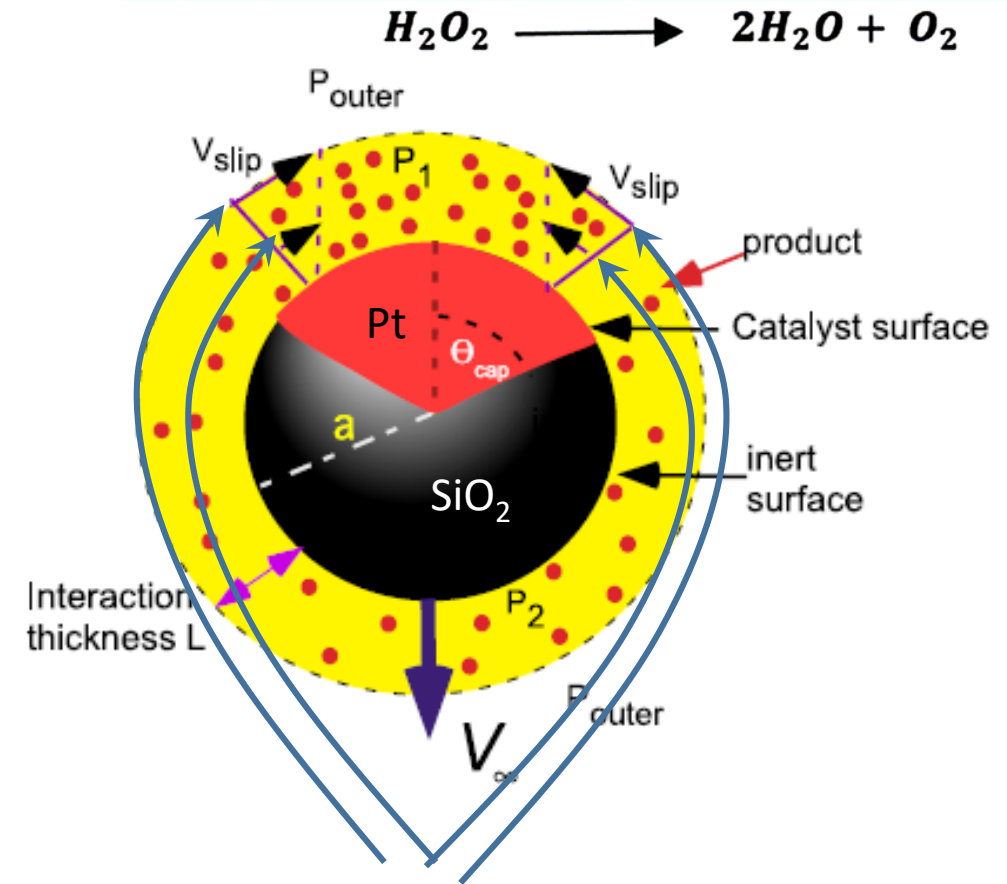
Paxton et al. JACS, (2006)

A bit about self-diffusiophoresis

Self-propelling **Janus particle** (made of silica and Platinum(Pt)) in water + H_2O_2 medium

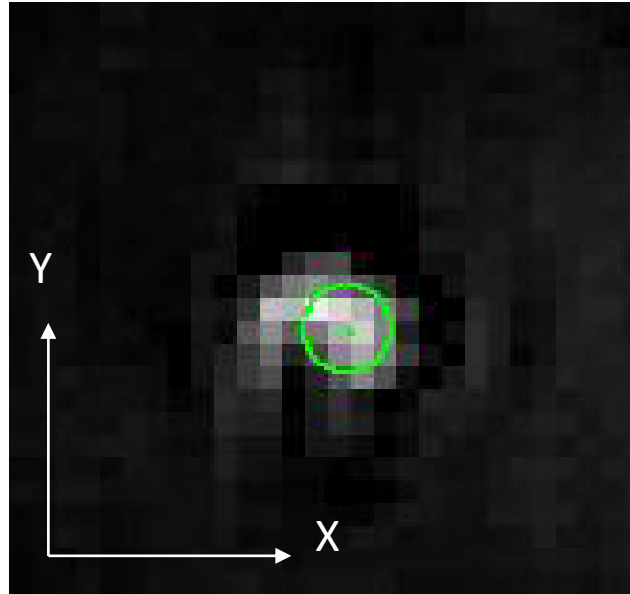
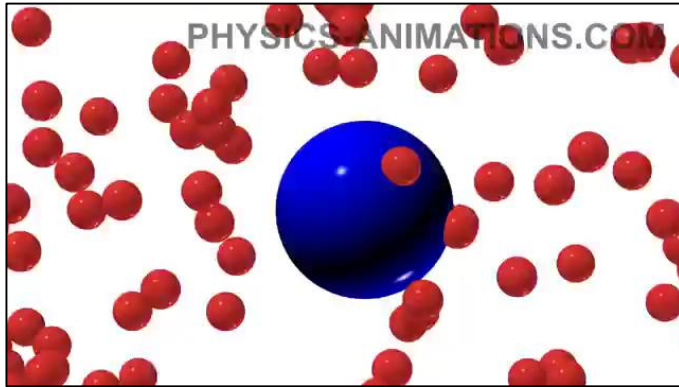


2 wt% H_2O_2 in water



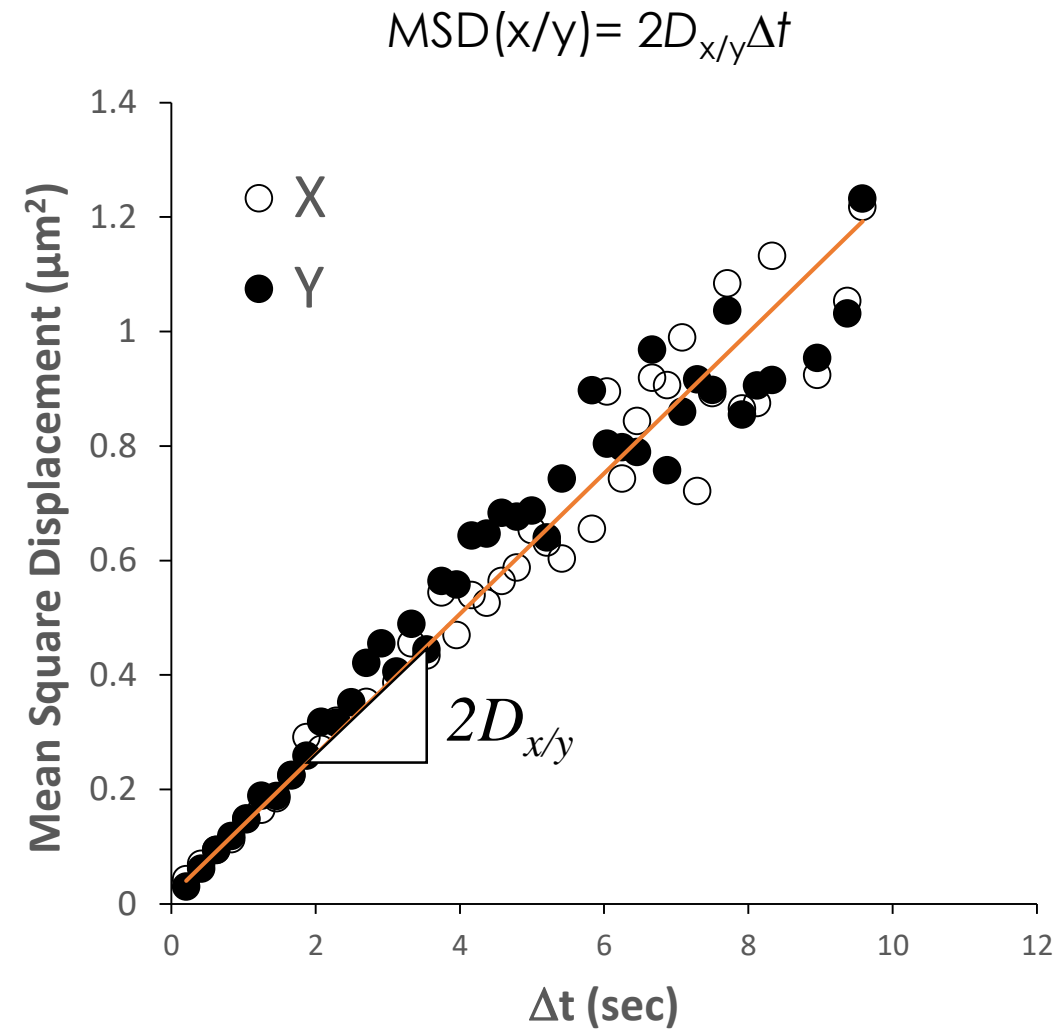
Maldrelli et al. Phy. Of. Fluid.,(2016)

Brownian Motion

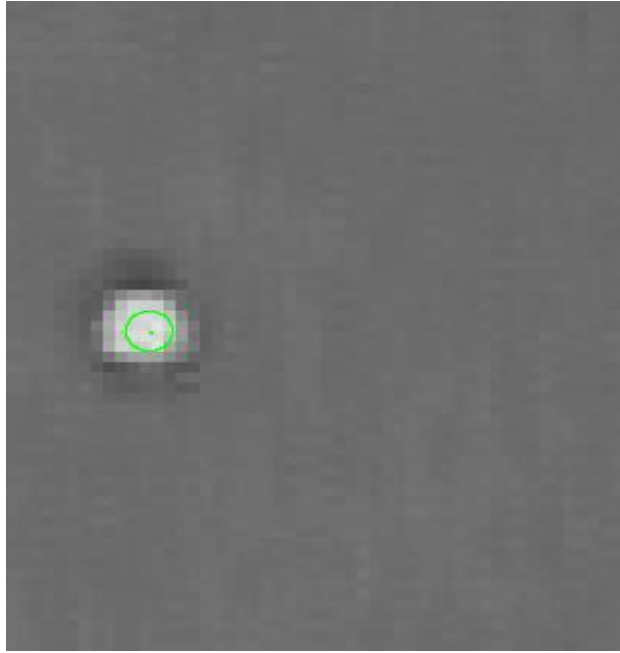


- Colloid undergoes random **Brownian Motion**
- Slope of MSD vs time elapsed gives **Brownian Diffusivity 'D'**.

- Stokes Einstein Relation
$$D = \frac{kT}{6\pi\eta a}$$

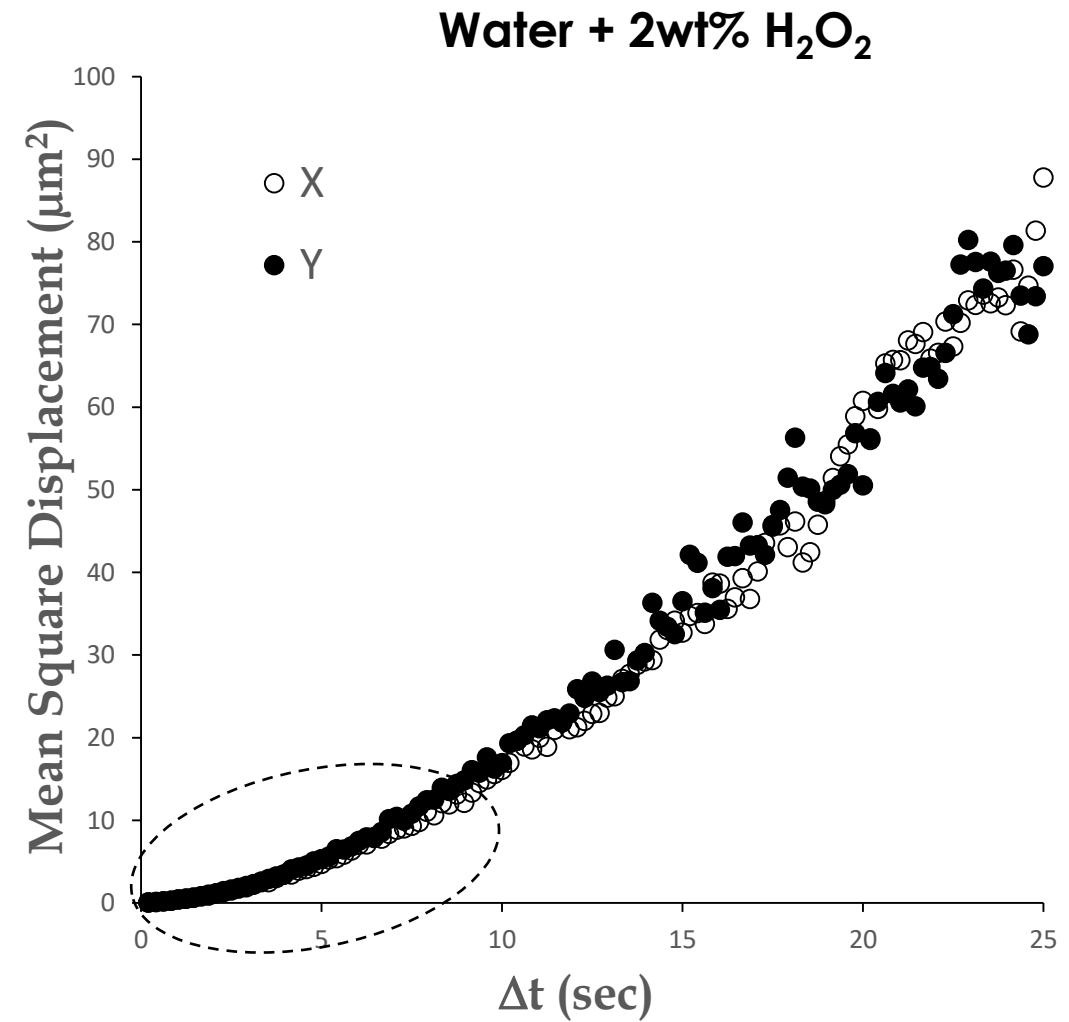


Self-Propelled Motion



○ Rotational Diffusion $\tau_R = \frac{kT}{8\pi\eta R^3}$

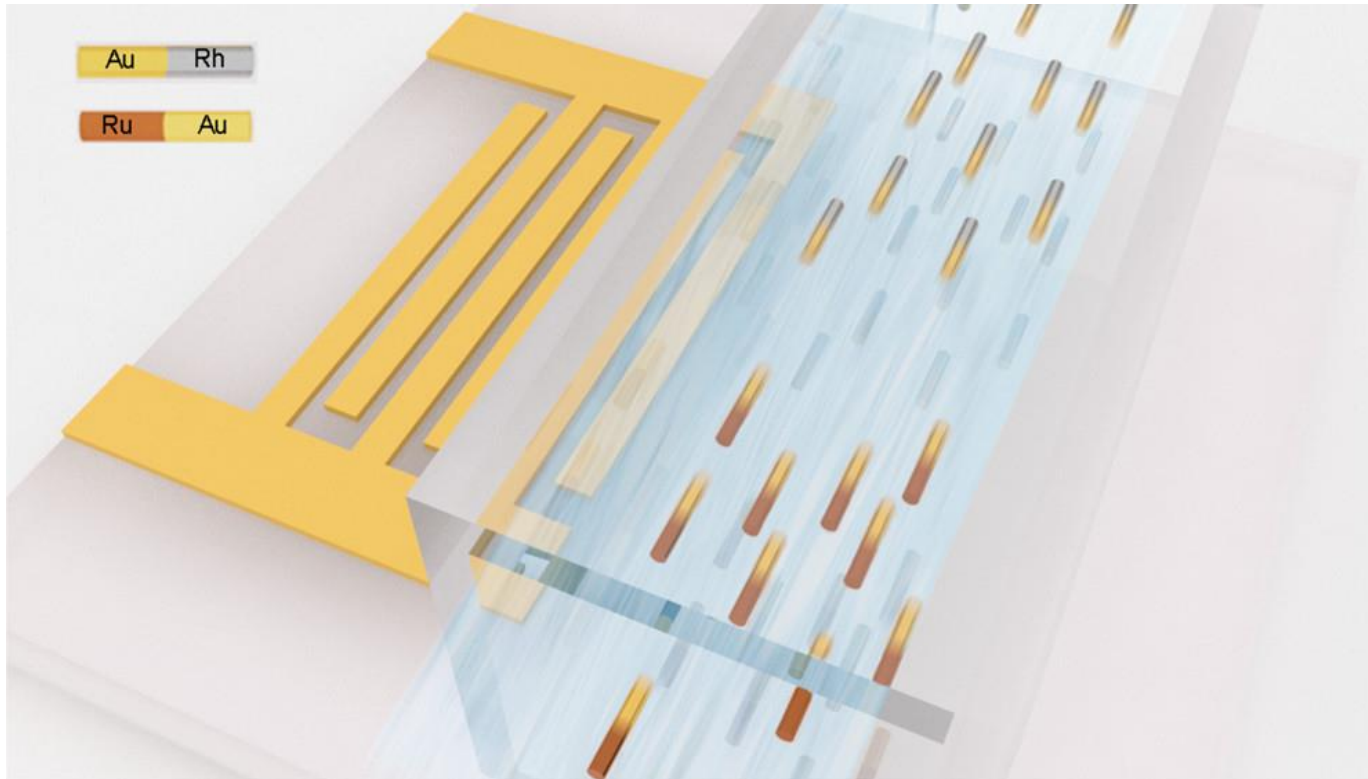
$$MSD = 2D\Delta t + v^2\Delta t^2 \quad \Delta t \ll \tau_R$$



What so far?

Ren et. al (2017)

Au-Rh microrods in H_2O_2 solution, Chemical - Acoustic hybrid propulsion

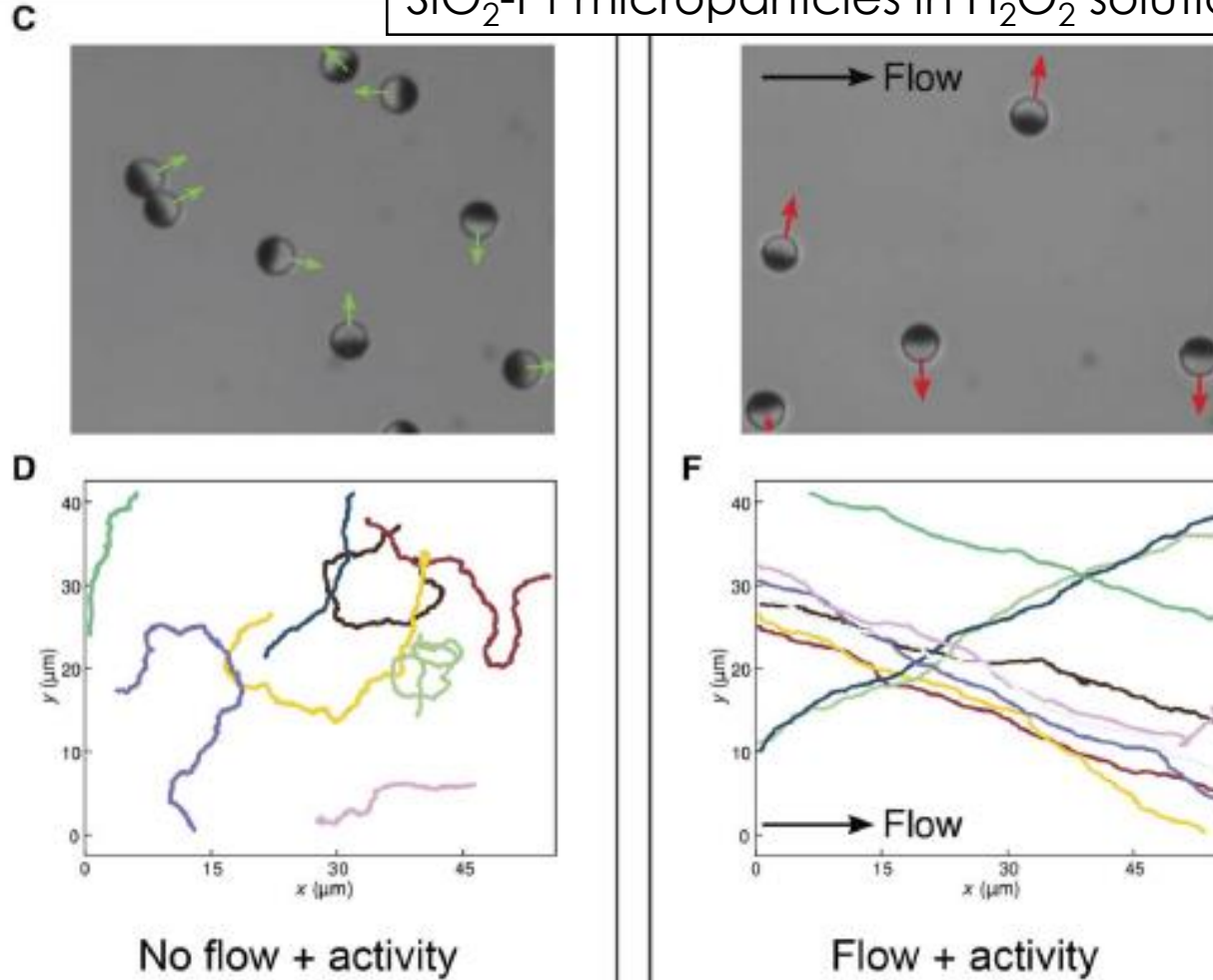


Particles exhibit upstream Rheotaxis

What so far?

Katuri et. al (2018)

SiO₂-Pt microparticles in H₂O₂ solution



Particles exhibit Cross-Stream migration

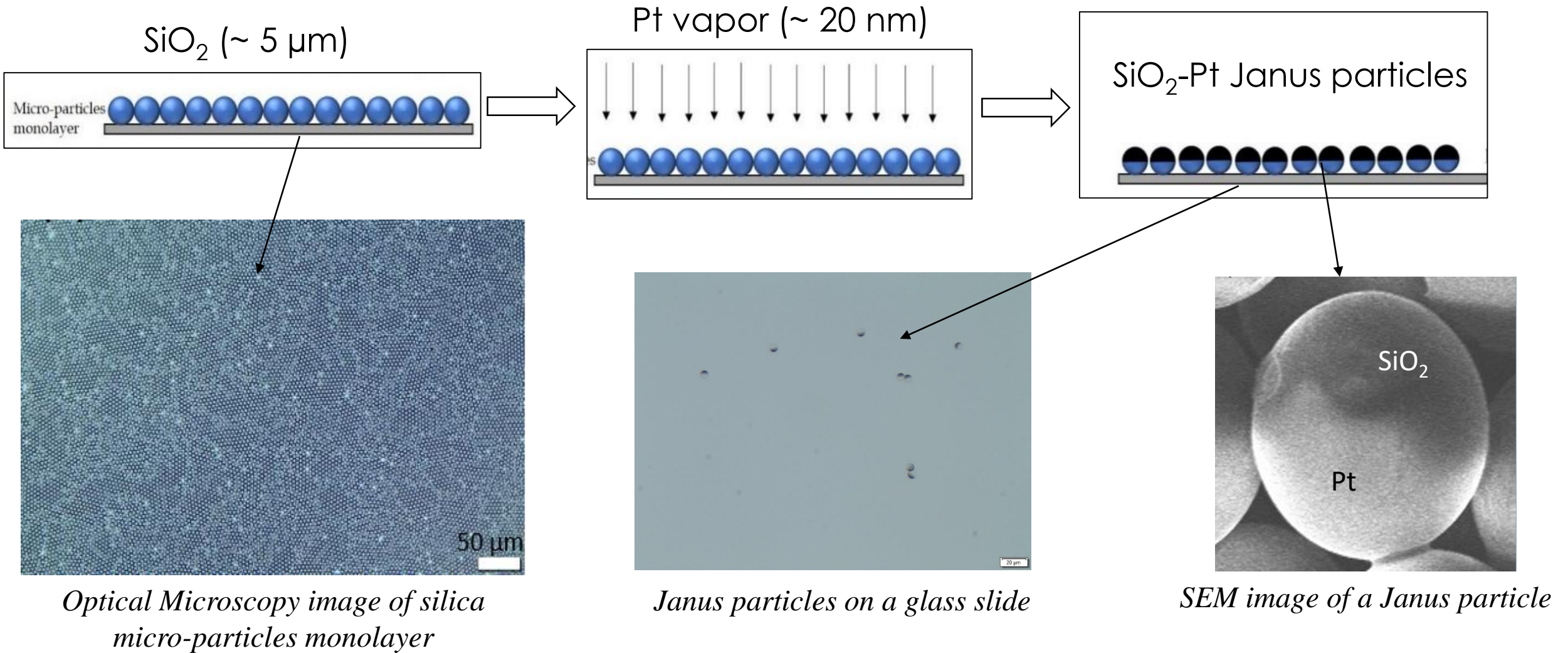
- **When ?**

Conditions in which cross migration will be present

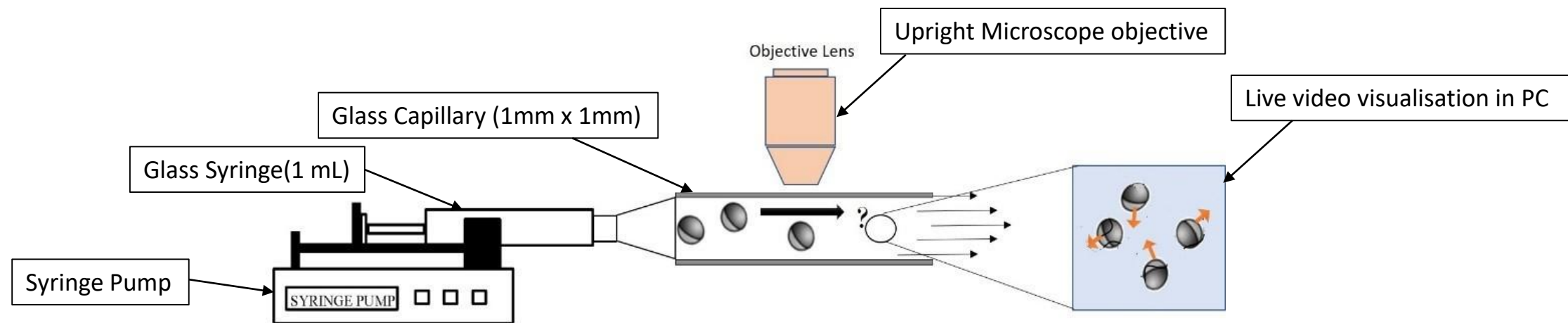
- **How much?**

Variation in extent of cross migration with varying flow

Synthesis of Janus particles



Flow Experiments and Data Analysis



Schematic of the experimental set-up

Control Experiments

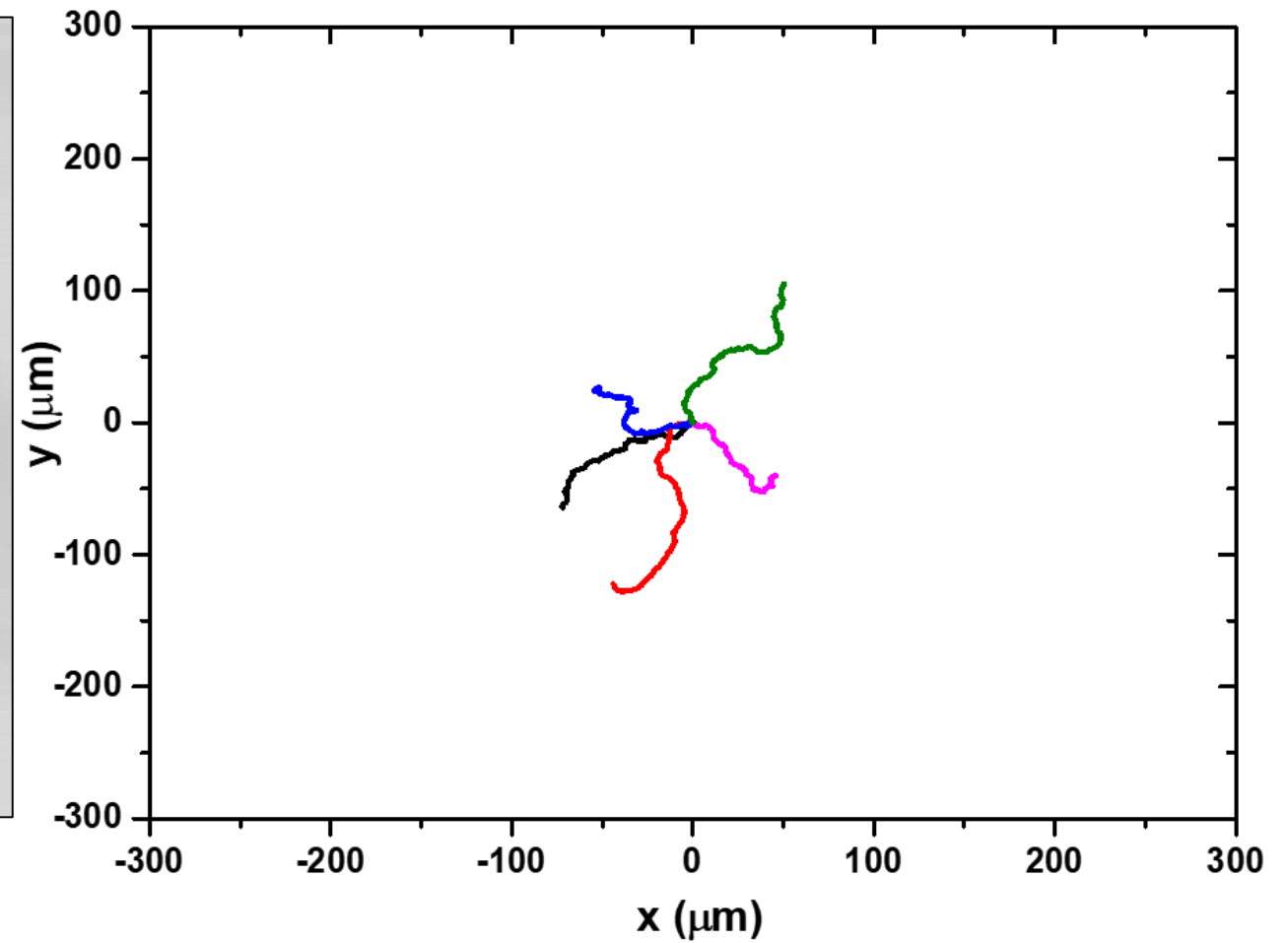
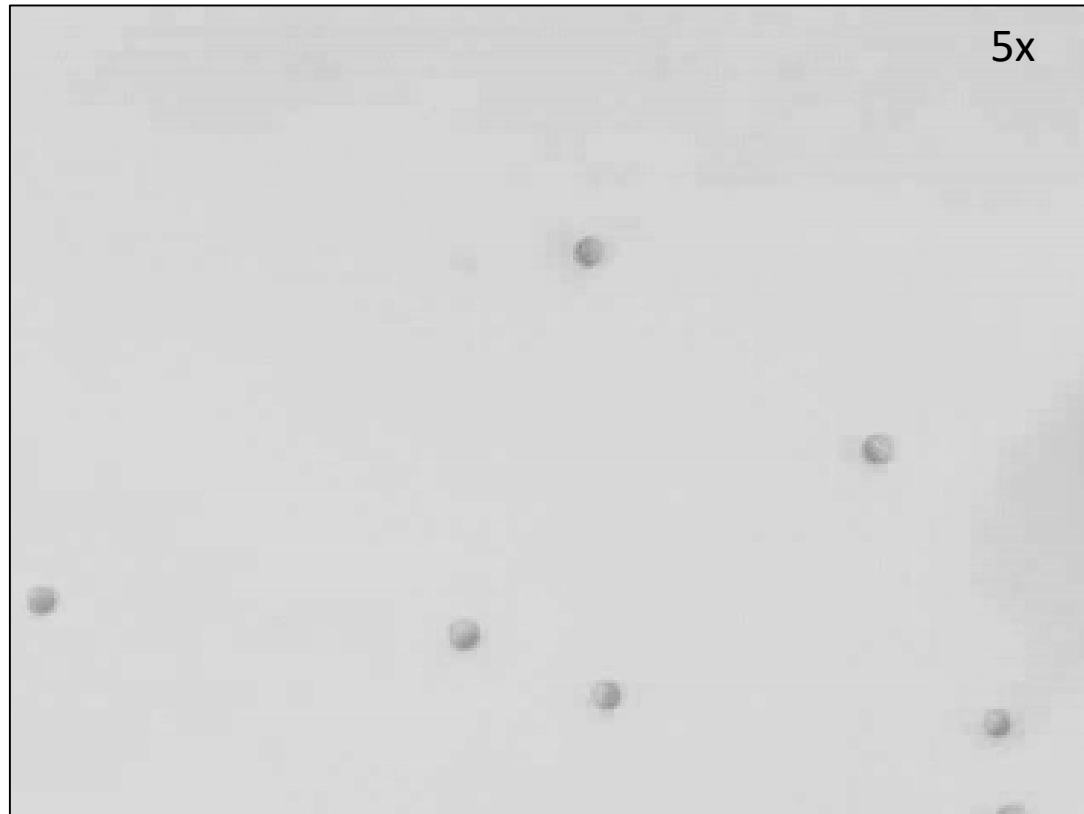
- Active Motion (0.5 wt%, 1 wt%, 2 wt% of H_2O_2)
- Flow without activity (100, 200, 500, 750, 900, 1000 $\mu\text{L/hr}$)

- Single particle tracking using Microscope
- Data analysis using Image J and Matlab

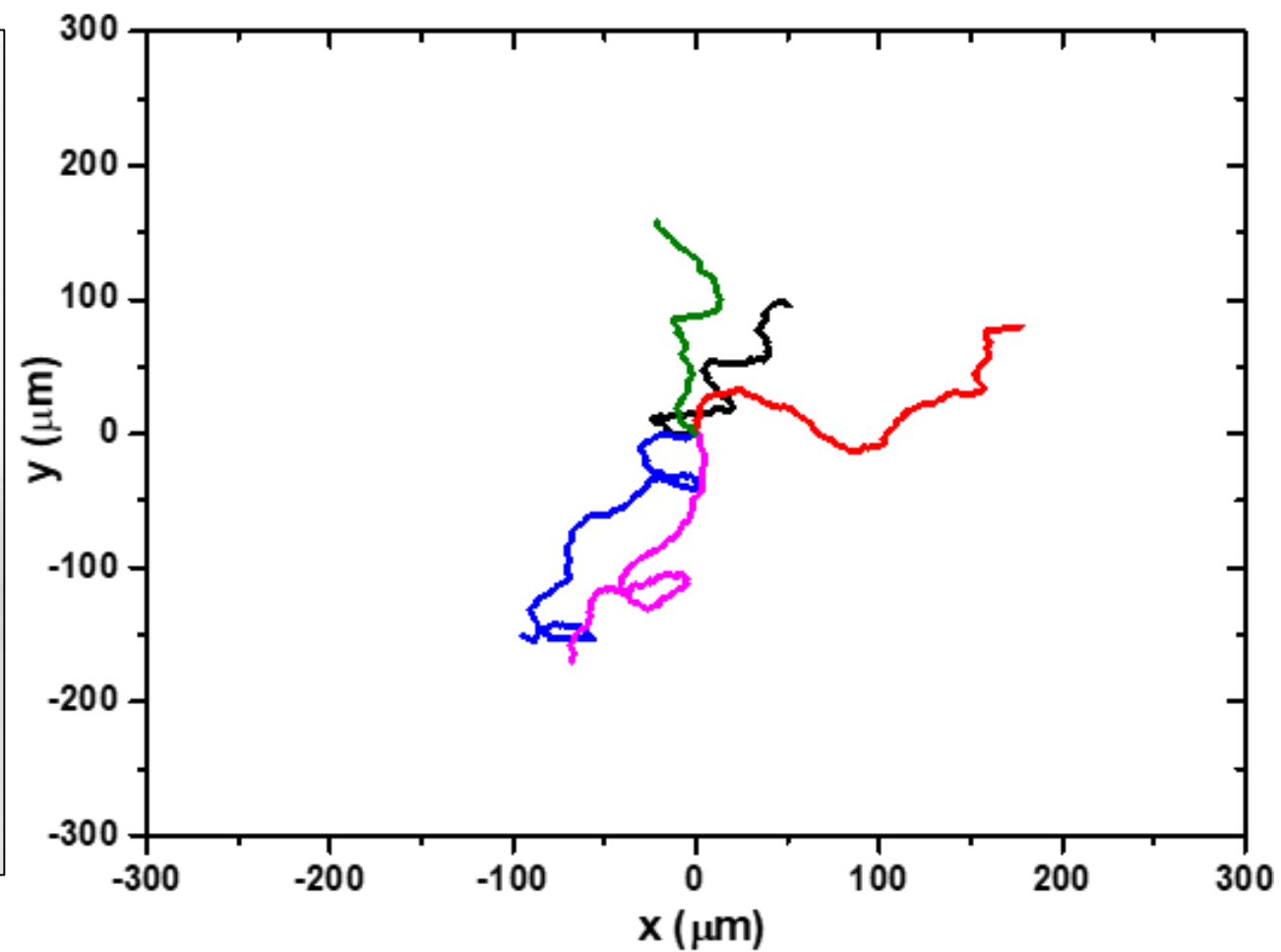
Active motion in shear flow experiment

- Combination of different H_2O_2 concentrations and flow rates.

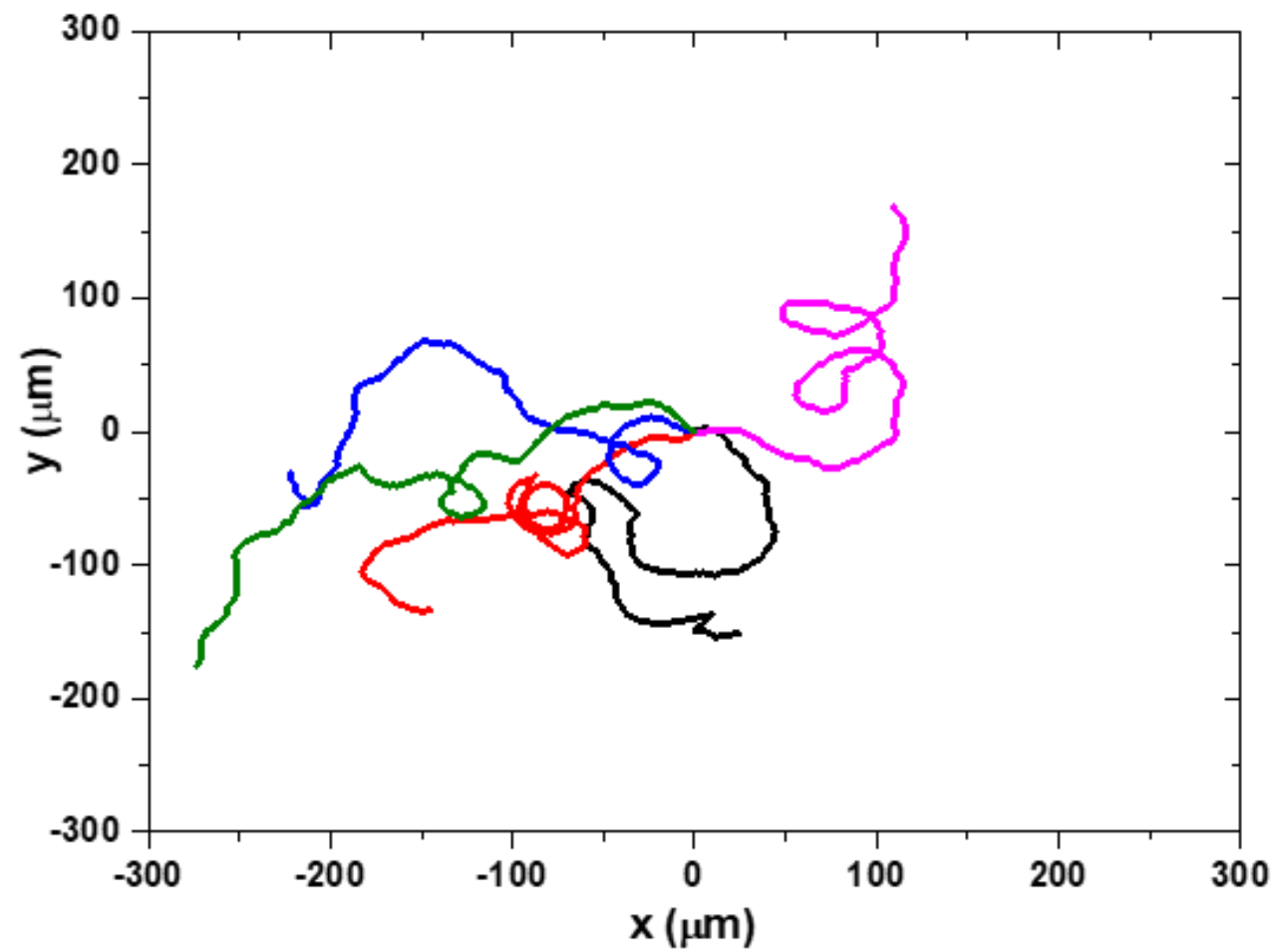
0.5 wt% H_2O_2 in water



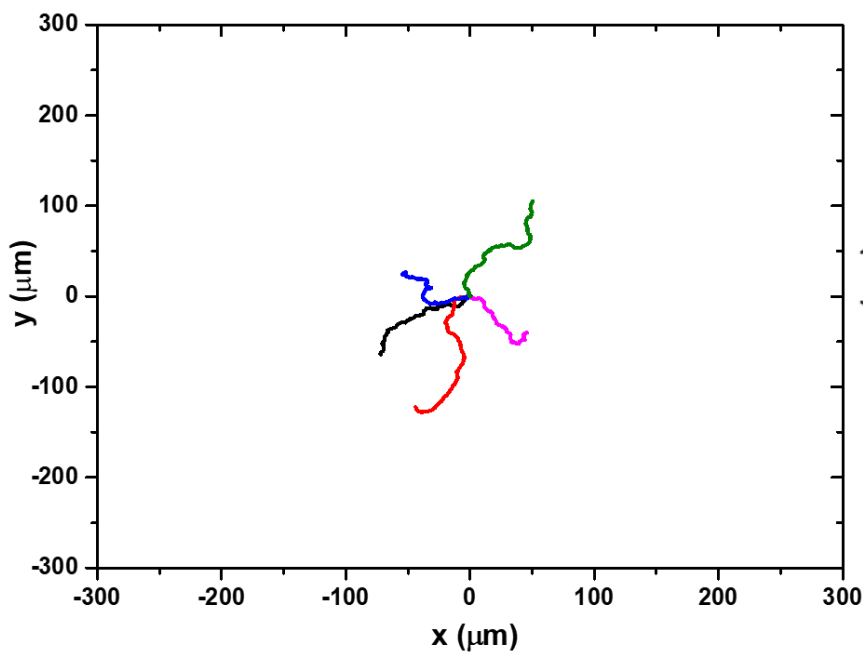
1 wt% H_2O_2 in water



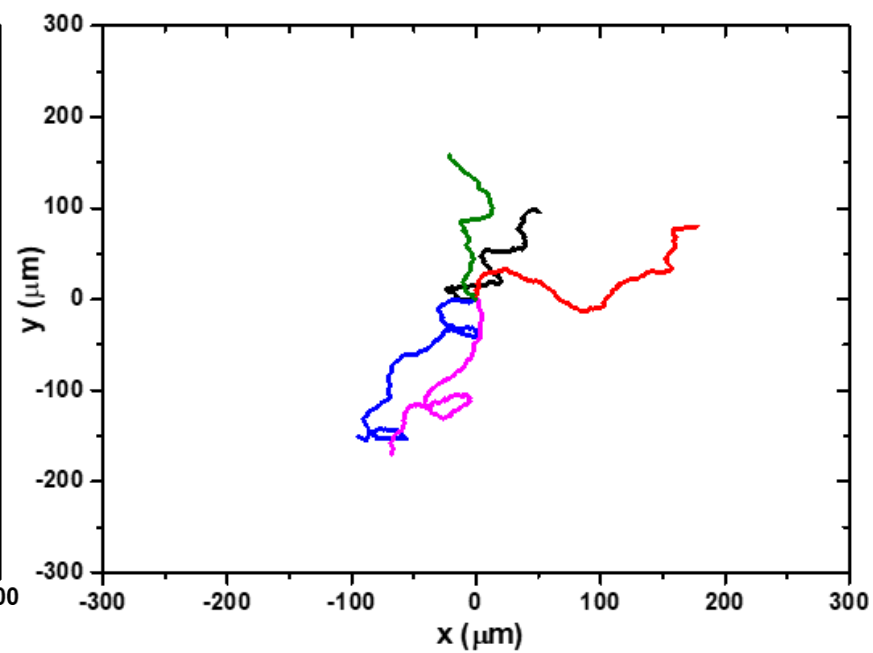
2 wt% H_2O_2 in water



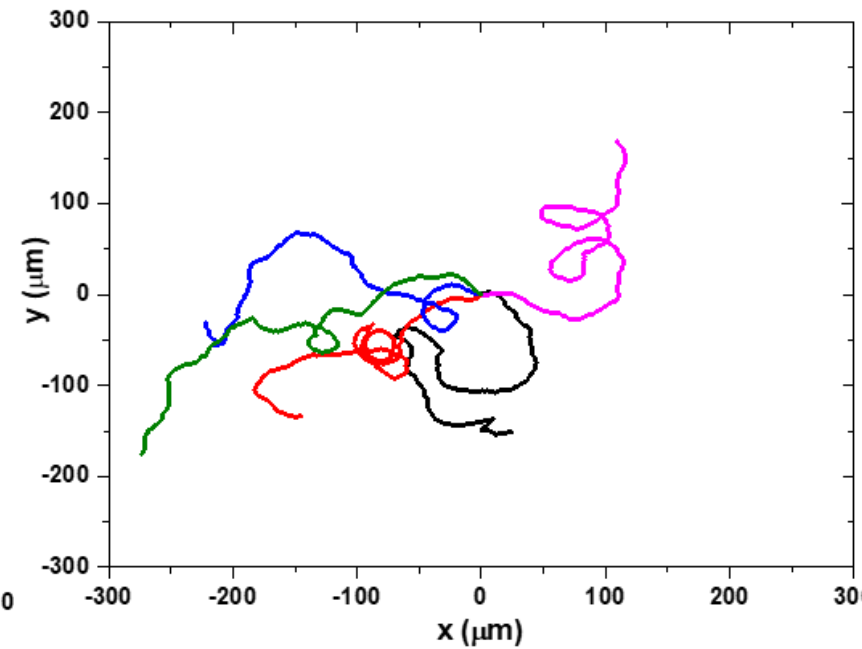
0.5 wt% H_2O_2 in water



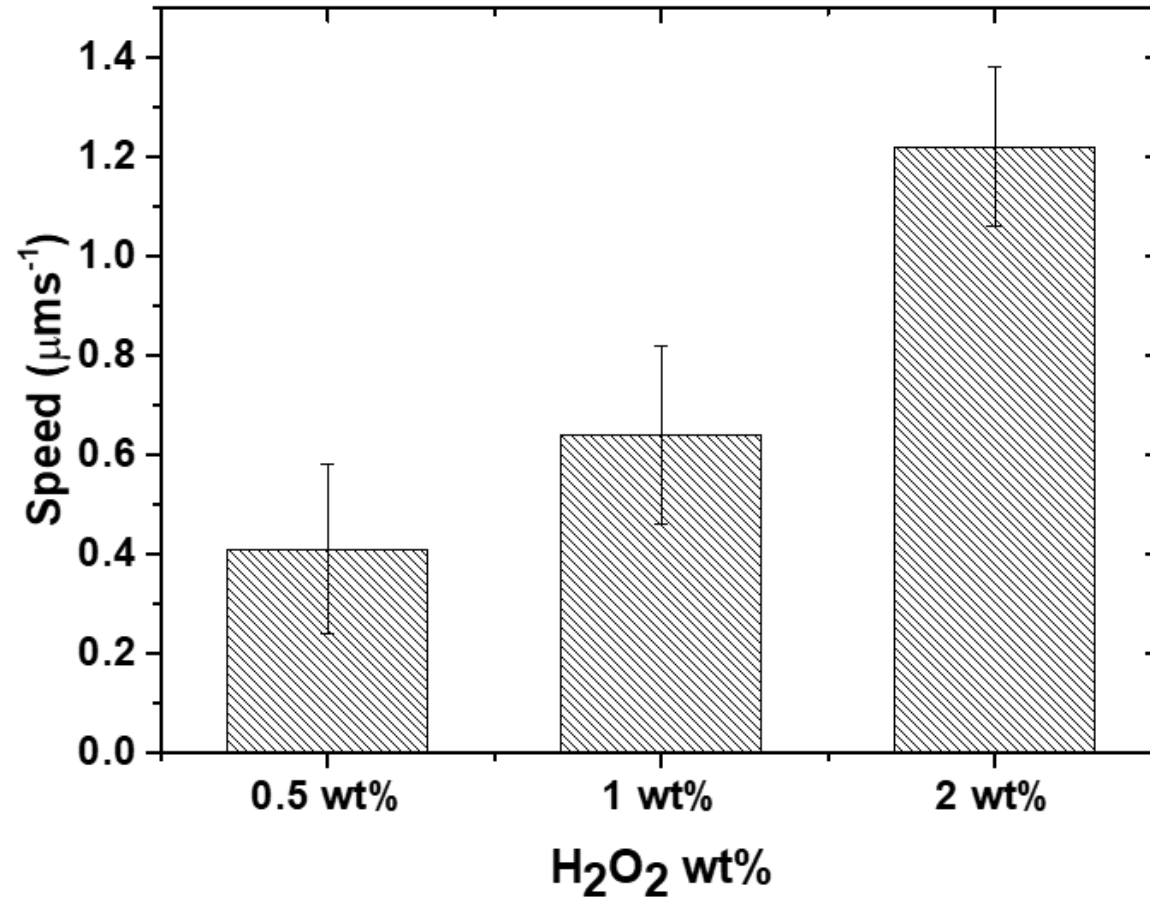
1 wt% H_2O_2 in water



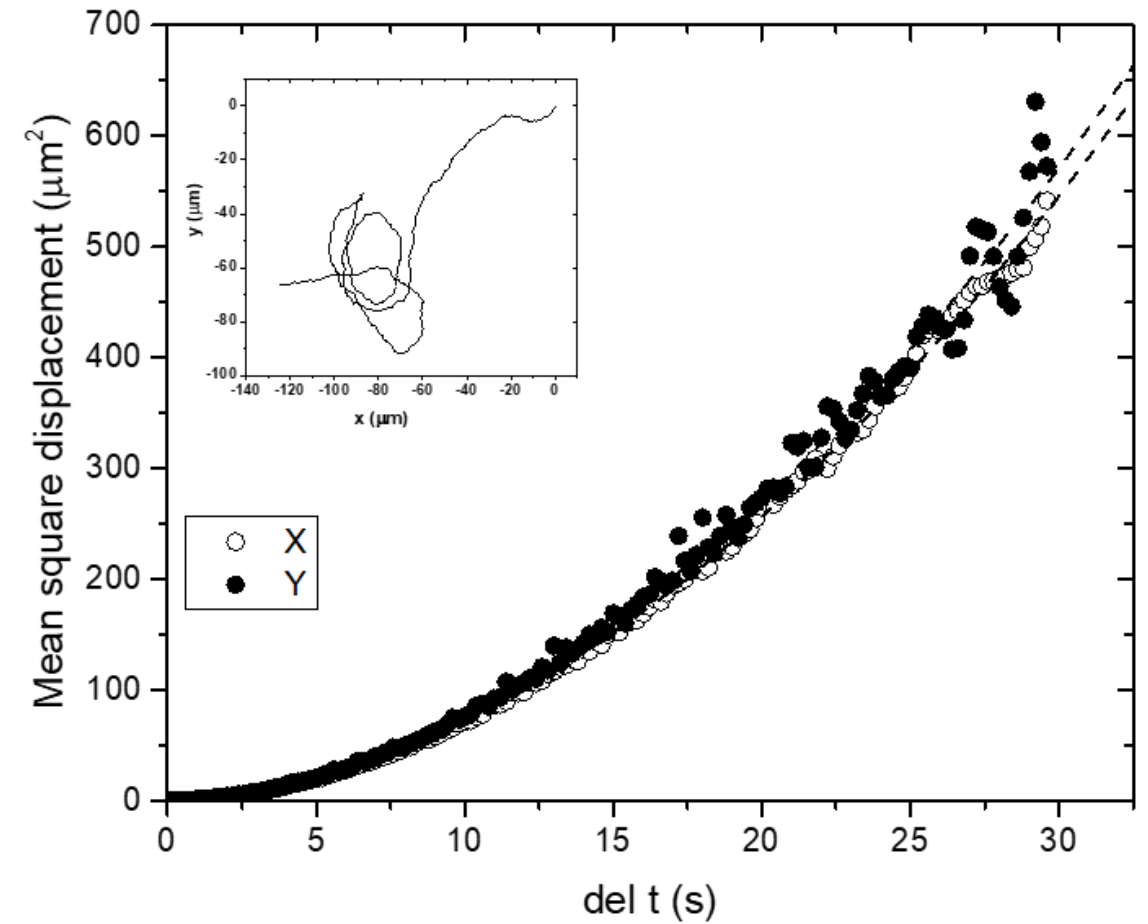
2 wt% H_2O_2 in water



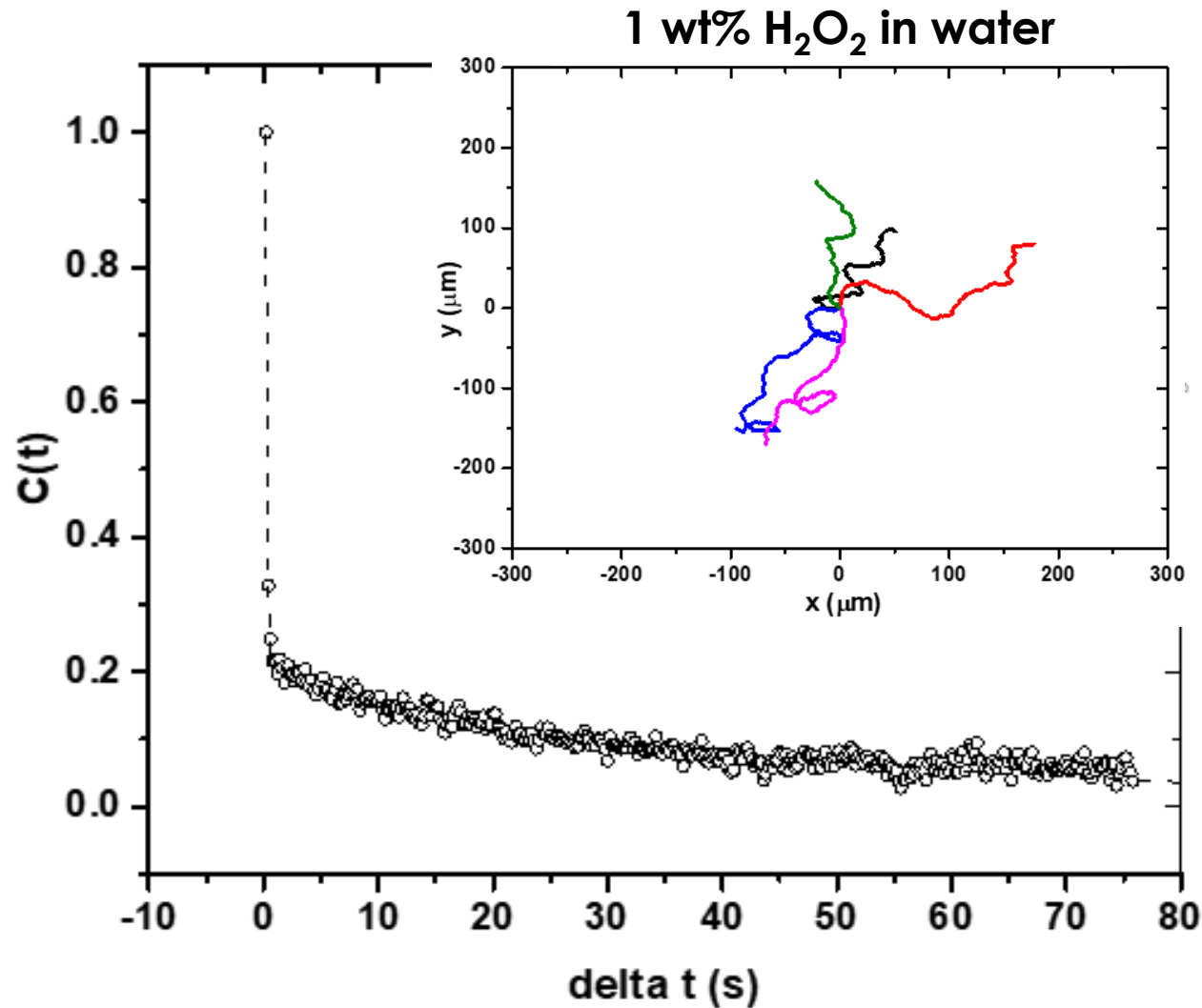
Active motion – Speed Calculation



$$MSD = 2D\Delta t + v^2\Delta t^2 \quad \Delta t \ll \tau_R$$



Active motion - τ_R Calculation



$$C(t) = \left\langle \frac{\vec{v}(t + \Delta t) \cdot \vec{v}(t)}{|\vec{v}(t + \Delta t)| |\vec{v}(t)|} \right\rangle$$

where,

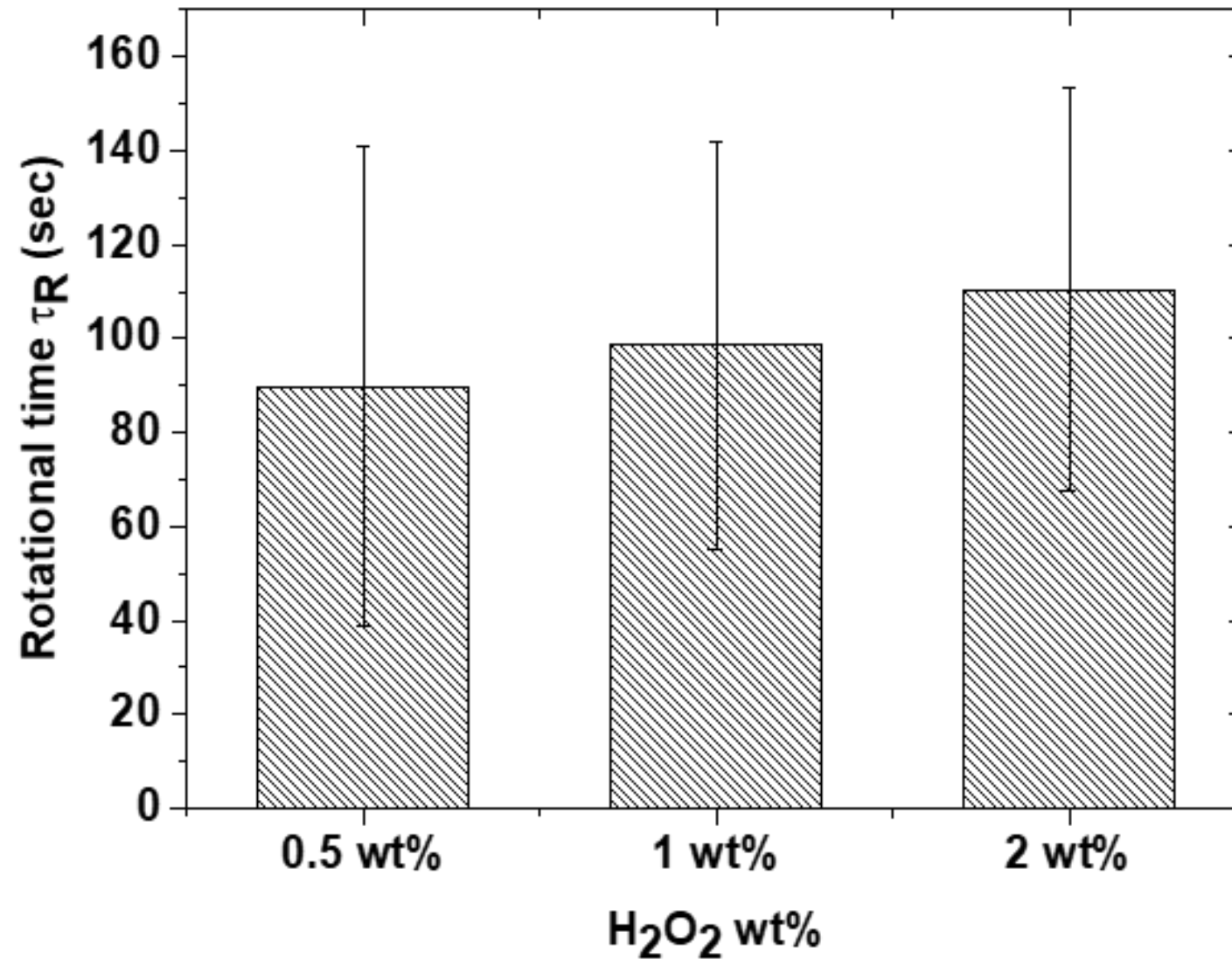
$C(t)$ = autocorrelation function

$v(t)$ = velocity of particle at time 't'

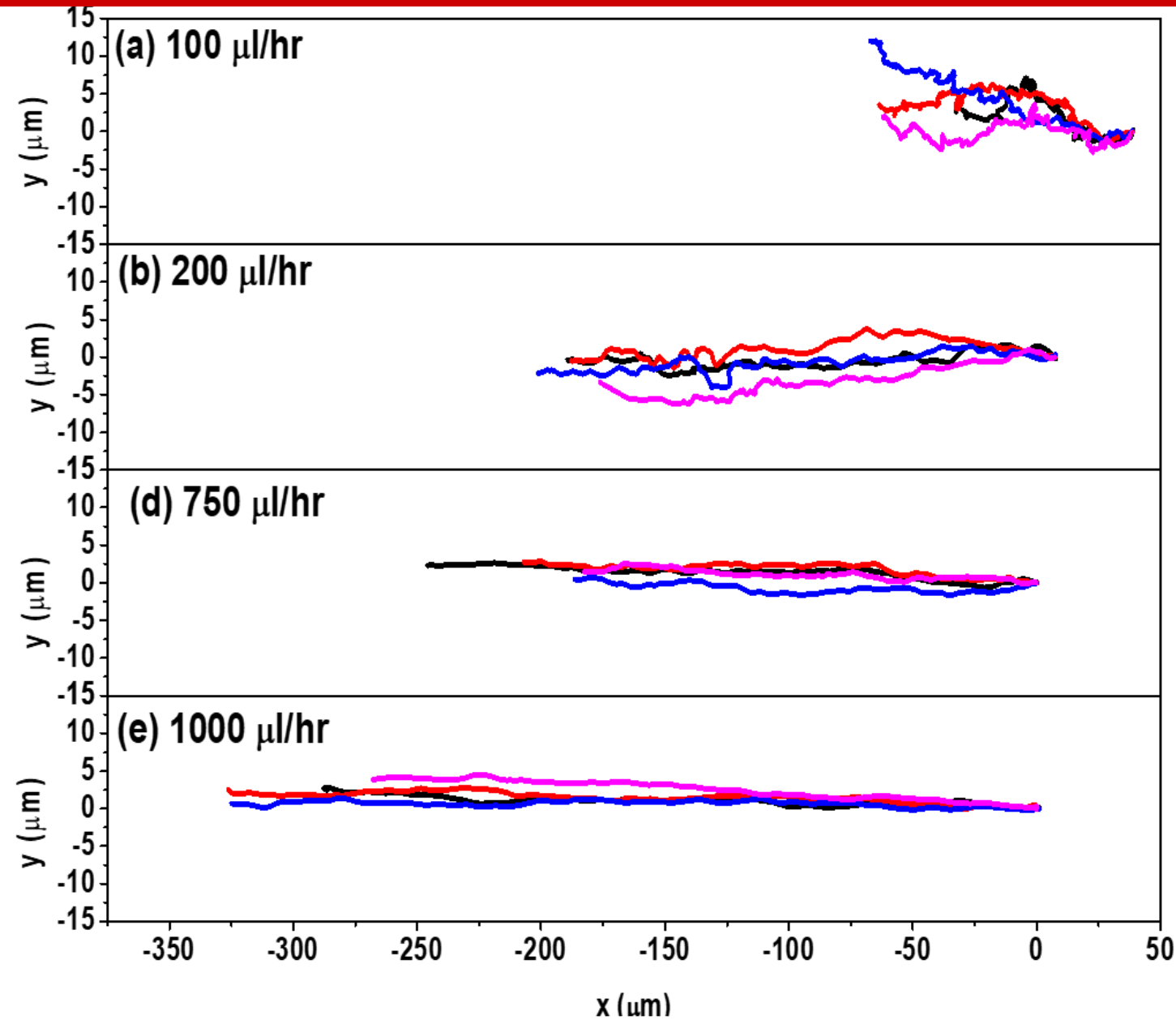
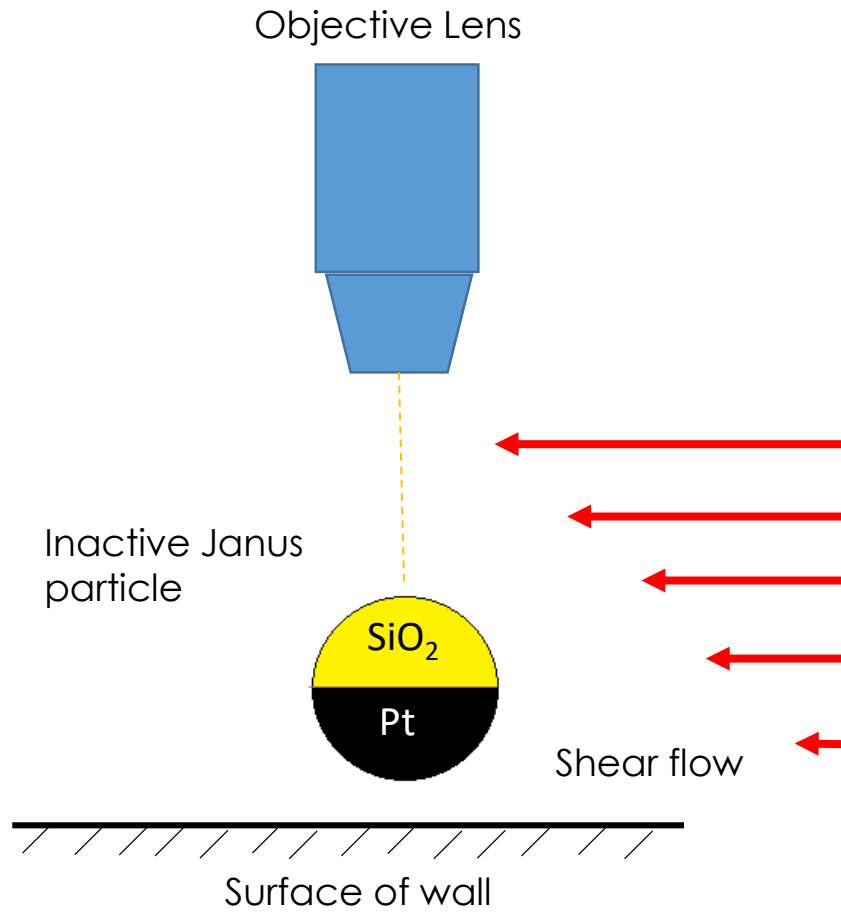
Δt = lag time

$$C(\Delta t) = 4D\delta(\Delta t) + e^{-2\Delta t / \tau_R}$$

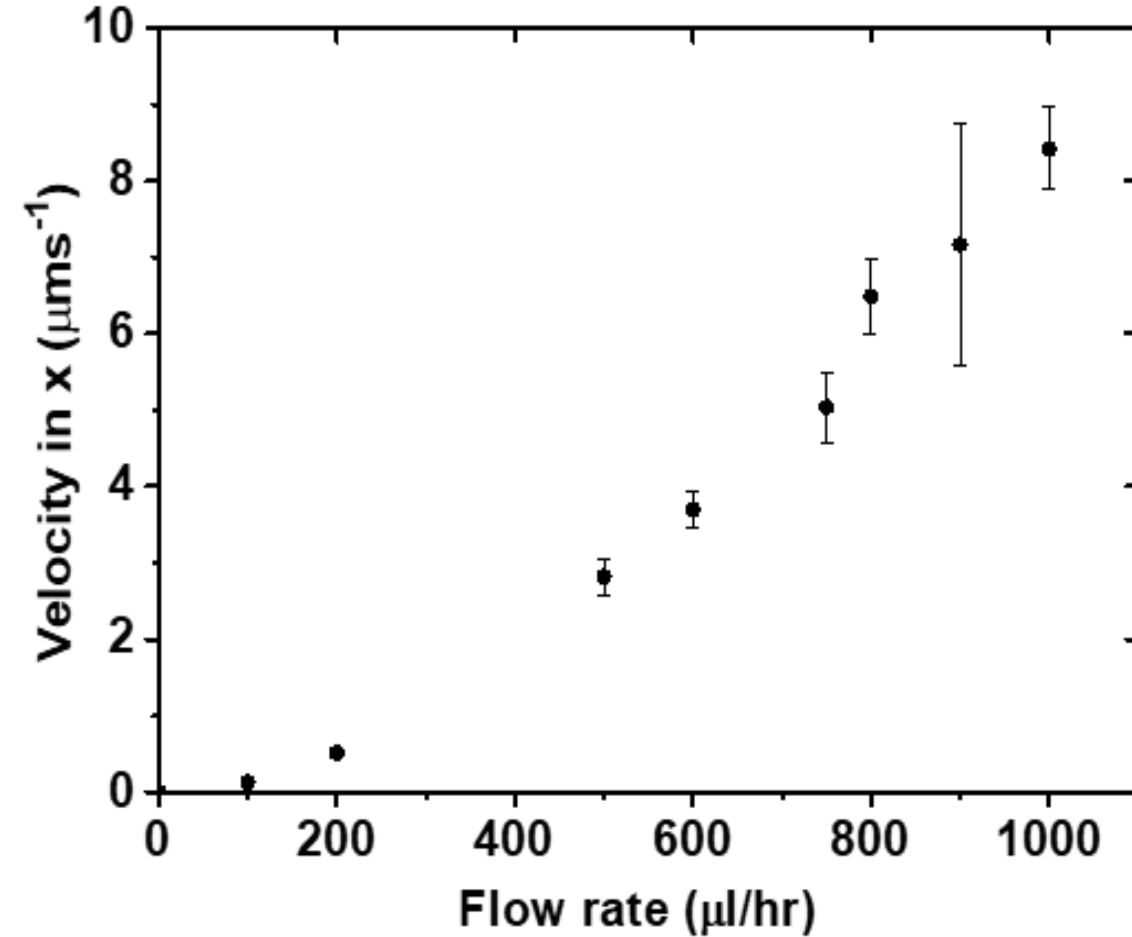
Active motion(Autocorrelation function)



Inactive motion in flow



Inactive motion in flow



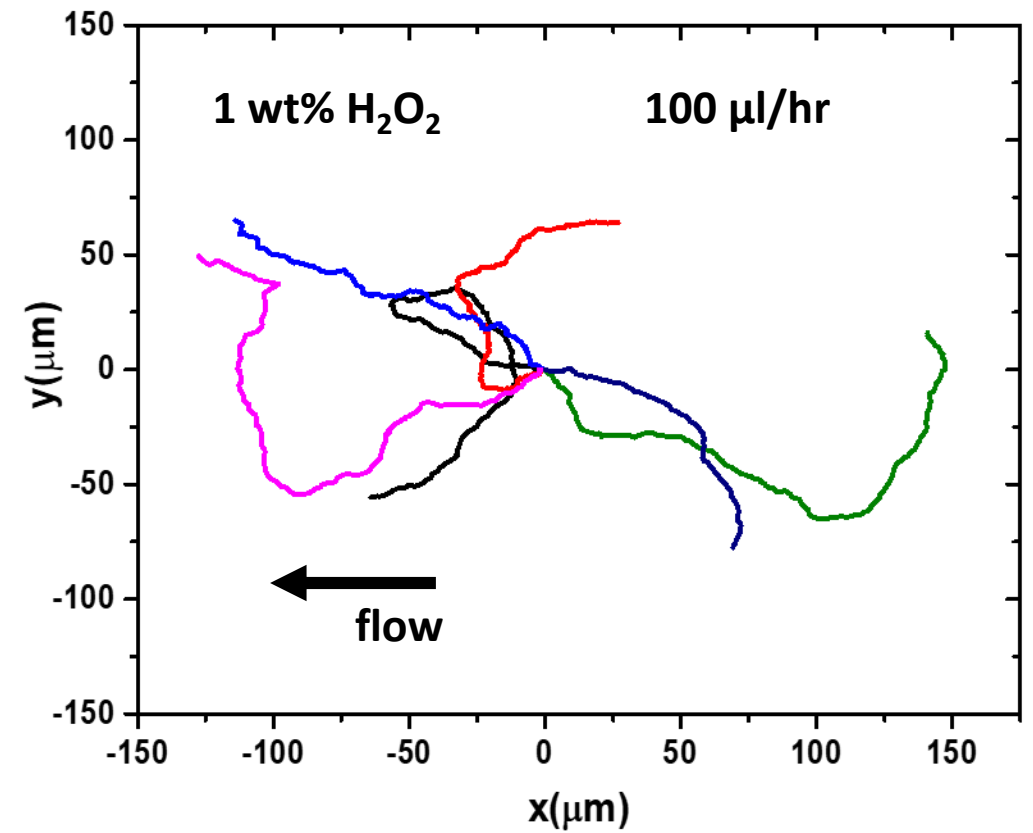
Note:

- Reynold's No. $Re = \frac{\rho v_x a}{\eta} = 4.77 \times 10^{-5}$ (very low $\sim 10^{-5}$)

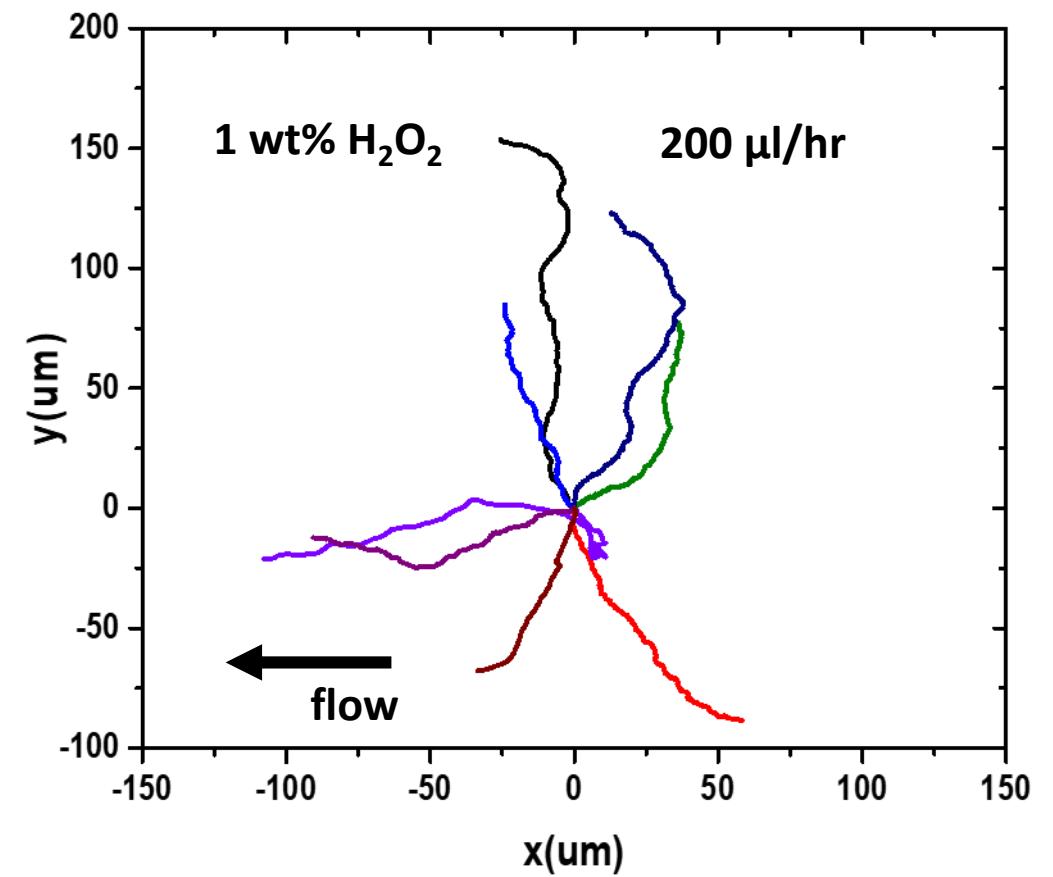
- Effect of flow on reaction is minimal

- $Pe = \frac{v_x a}{D_s} = 0.0053$ (very low $\ll 1$)

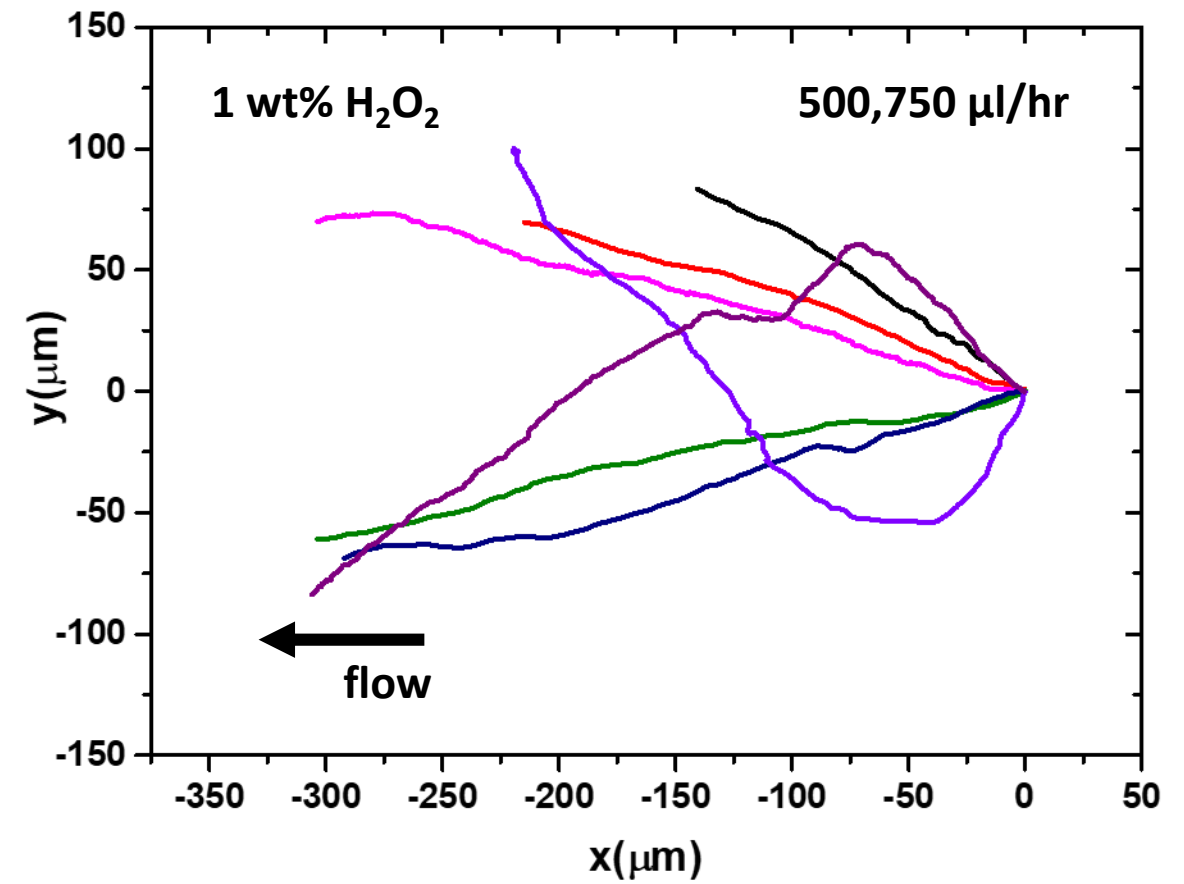
Active motion in flow



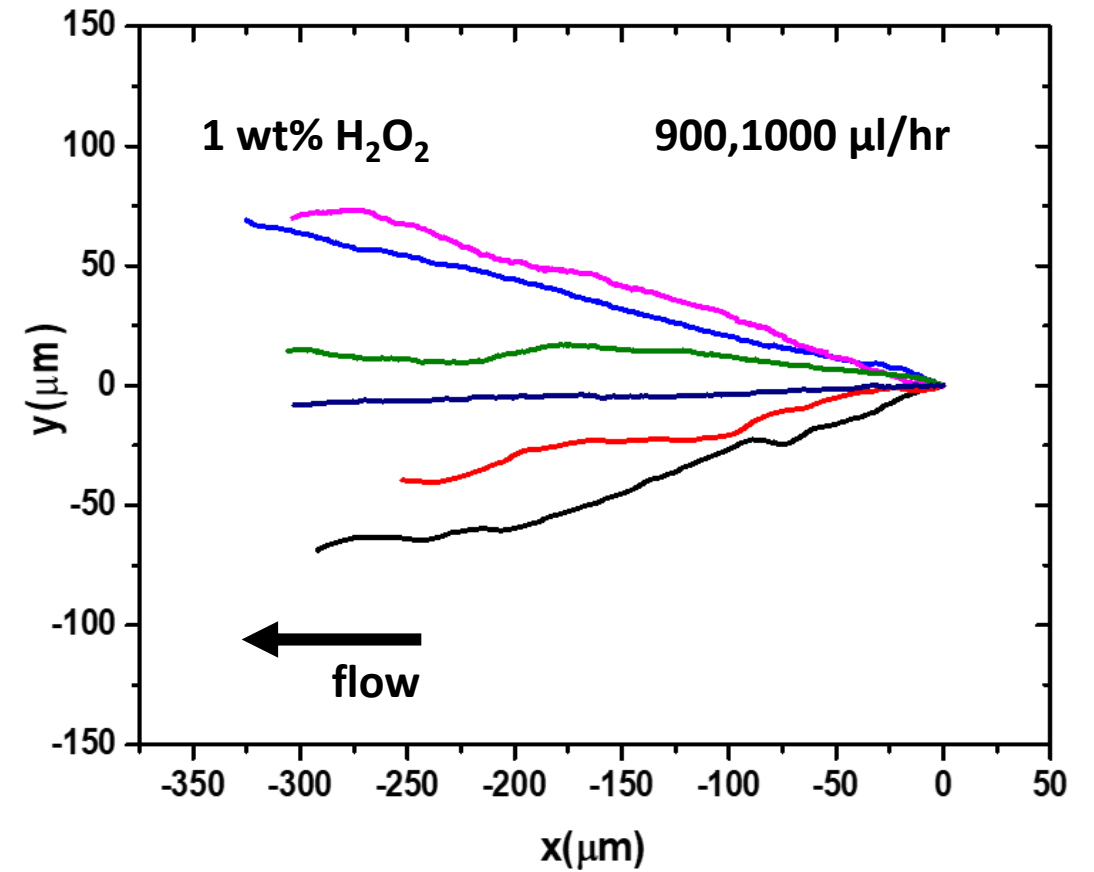
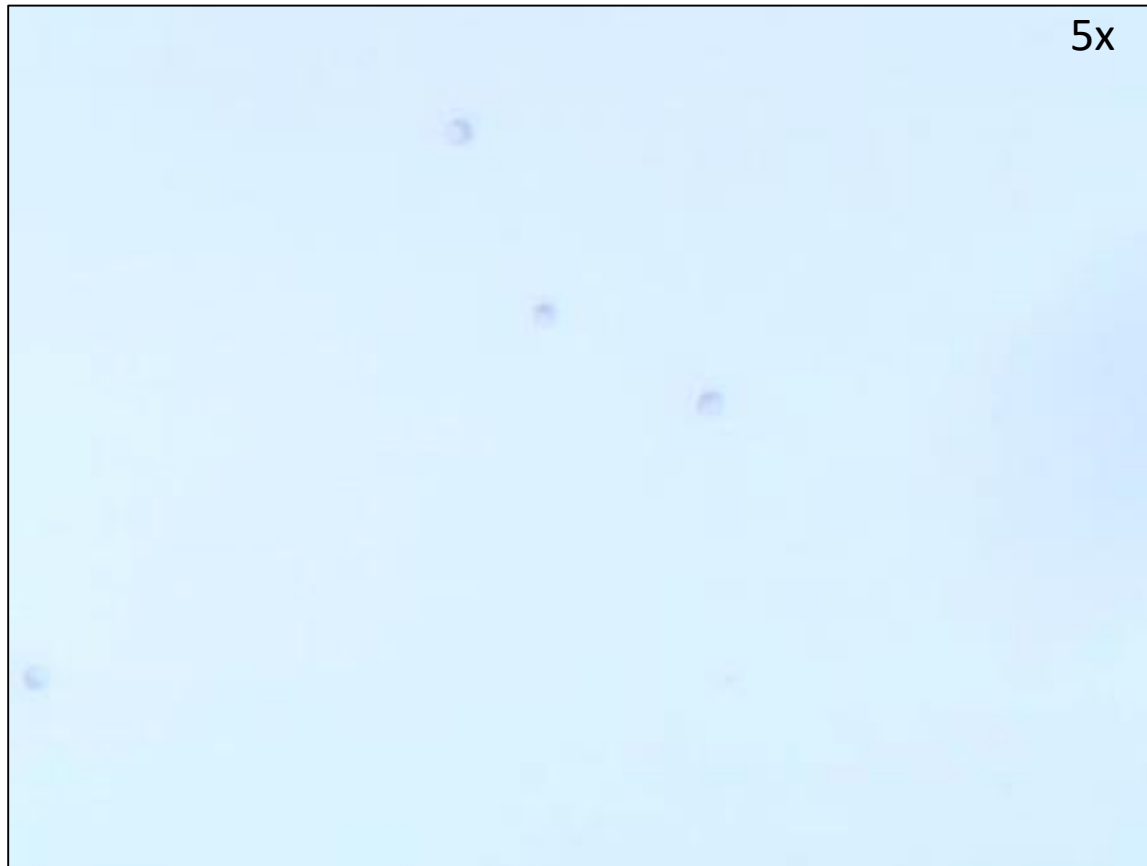
Active motion in flow



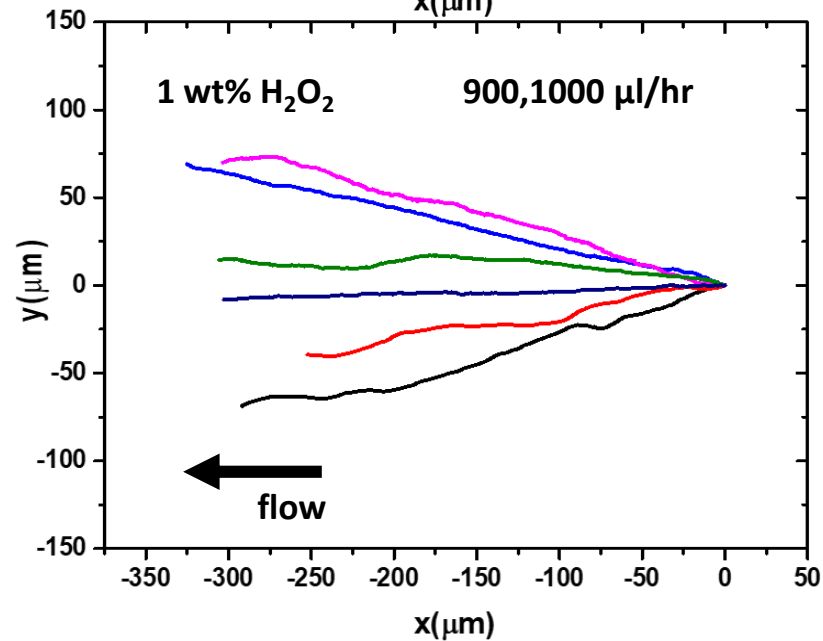
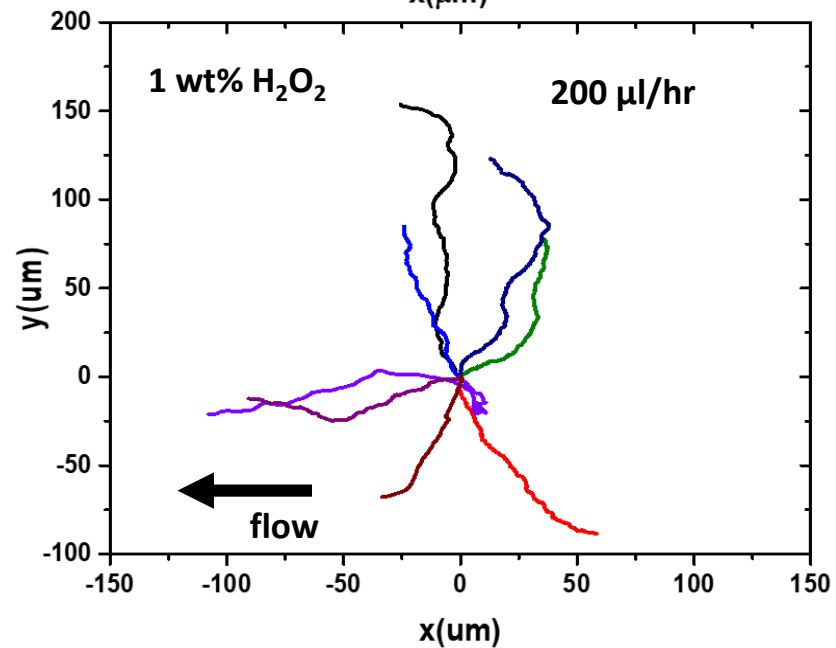
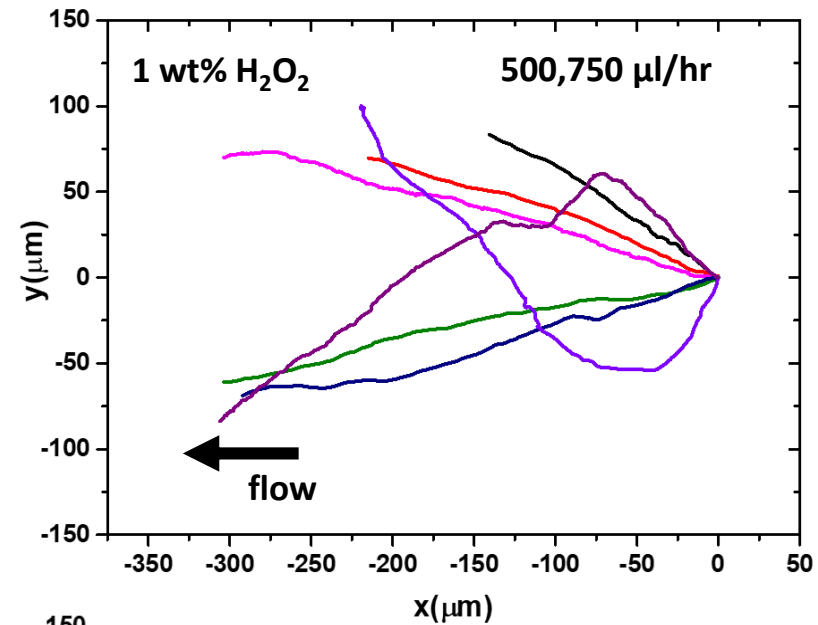
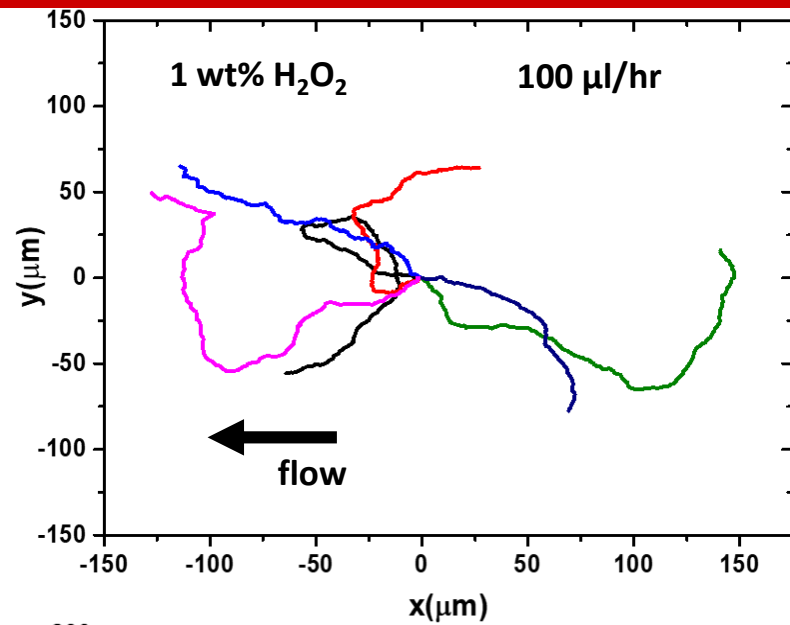
Active motion in flow



Active motion in flow



Active motion in flow

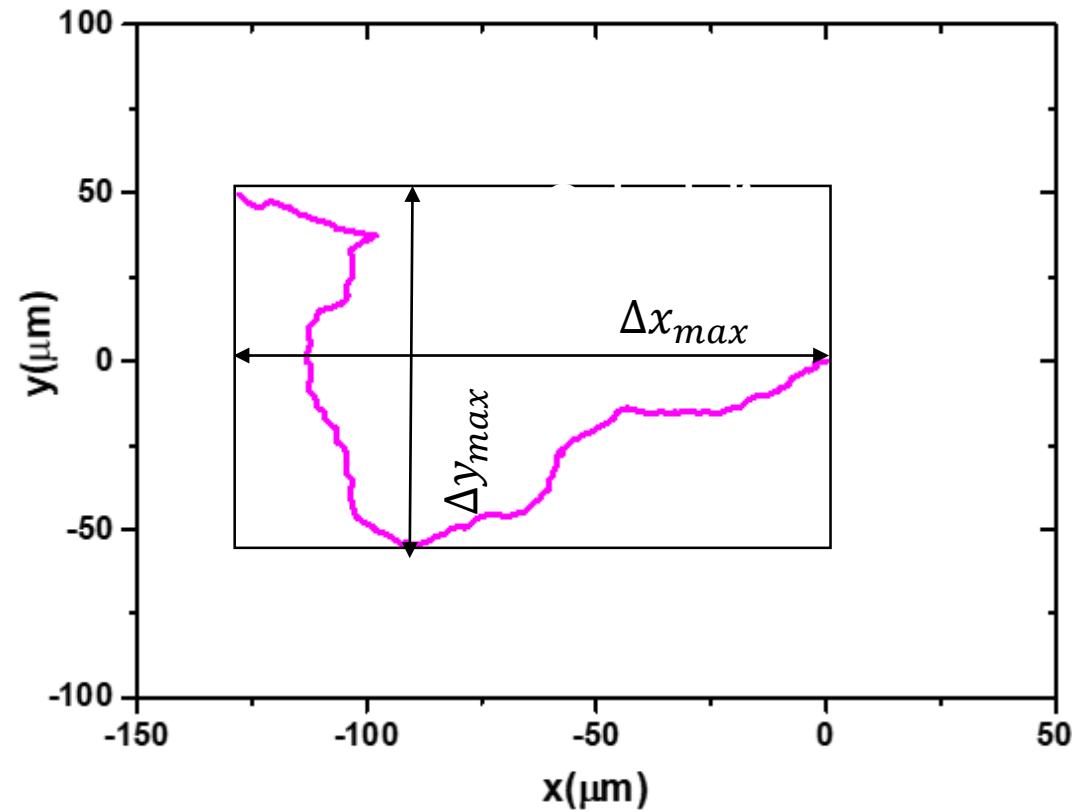


Defining anisotropy (α) in the system

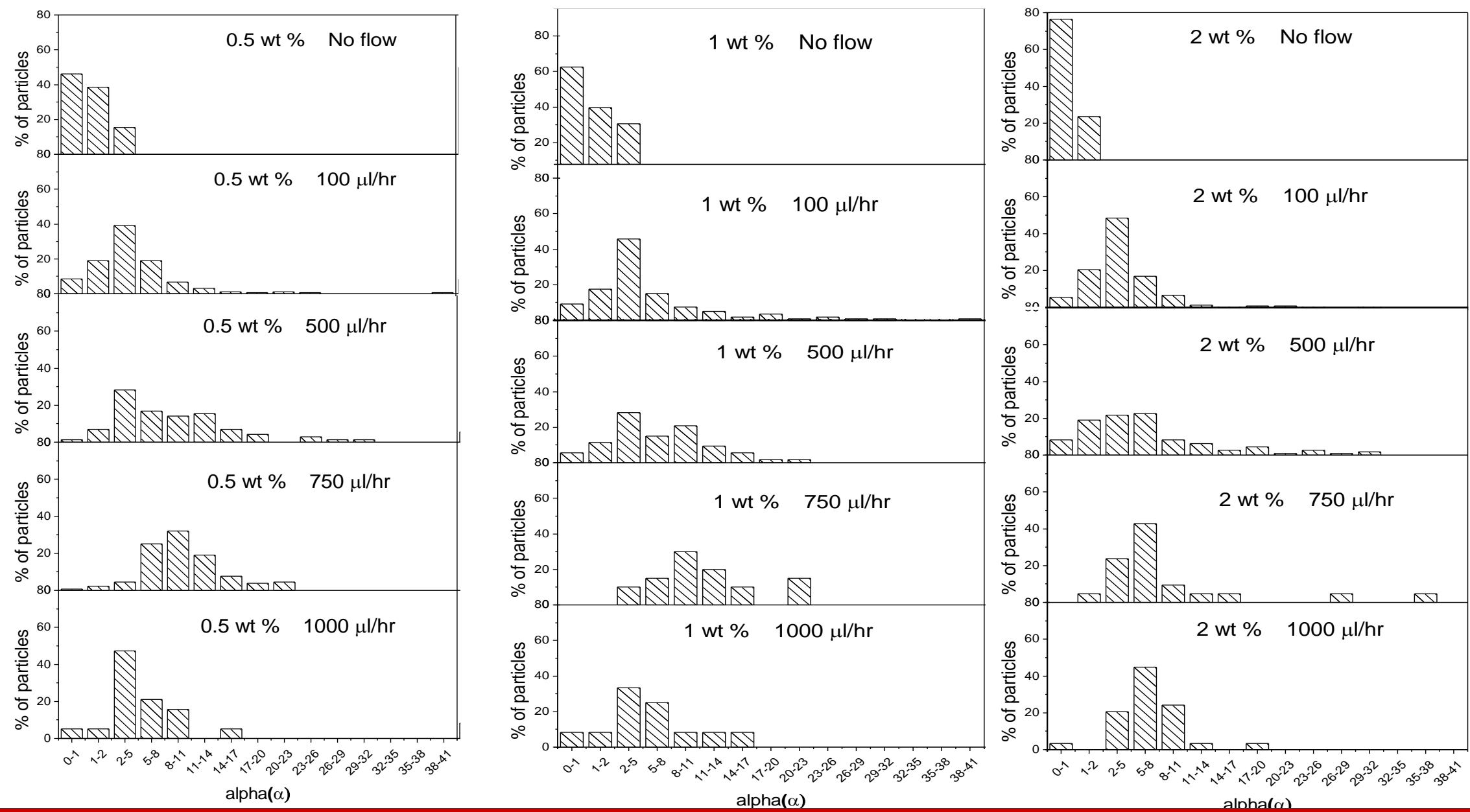
We define anisotropy alpha as

$$\alpha = \frac{\left(\Delta y_{\max} / \Delta x_{\max} \right)_{activity+flow}}{\left(\Delta y_{\max} / \Delta x_{\max} \right)_{flow}}$$

For a given trajectory,



Distribution of α for different systems

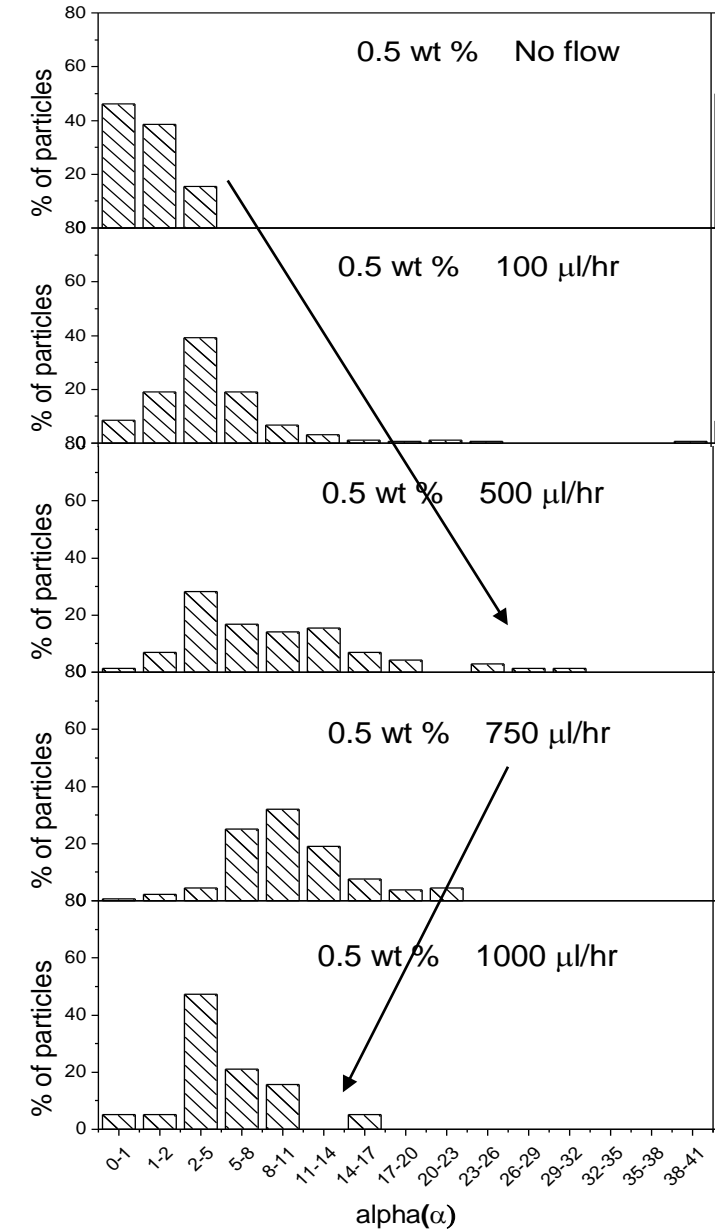


Key observations

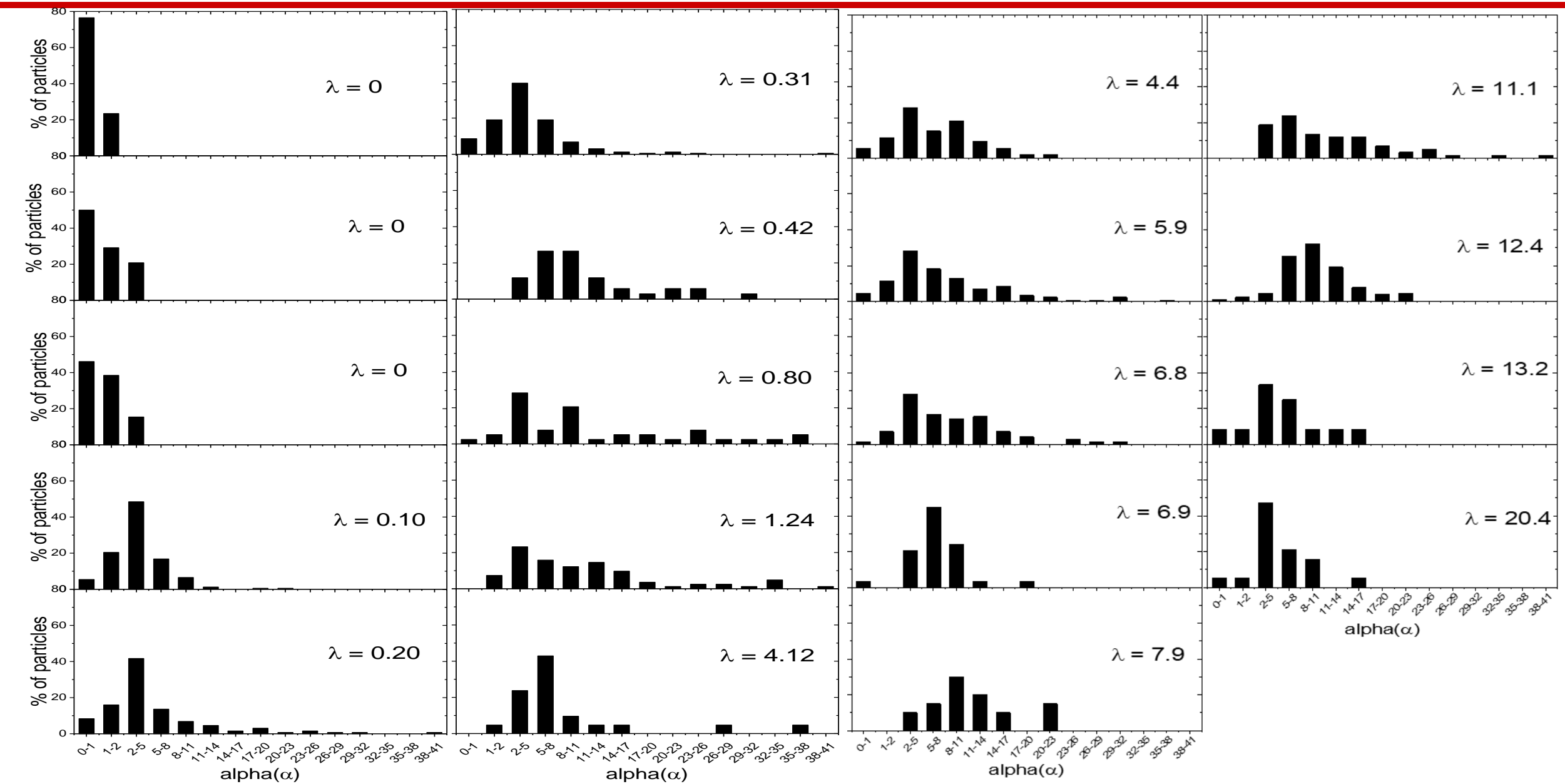
- Low flow $\rightarrow \alpha \sim 1$
- Moderate flow \rightarrow range of α widens towards higher values
- High flow \rightarrow Range of α starts to shrink
- Behaviour universal and dependent on the activity of particle

We define dimensionless parameter

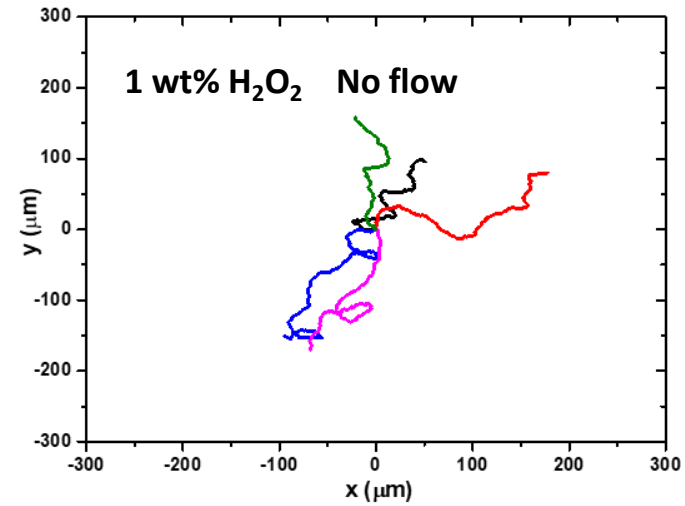
$$\lambda = \frac{v_{x,flow}}{v_{activation}}$$



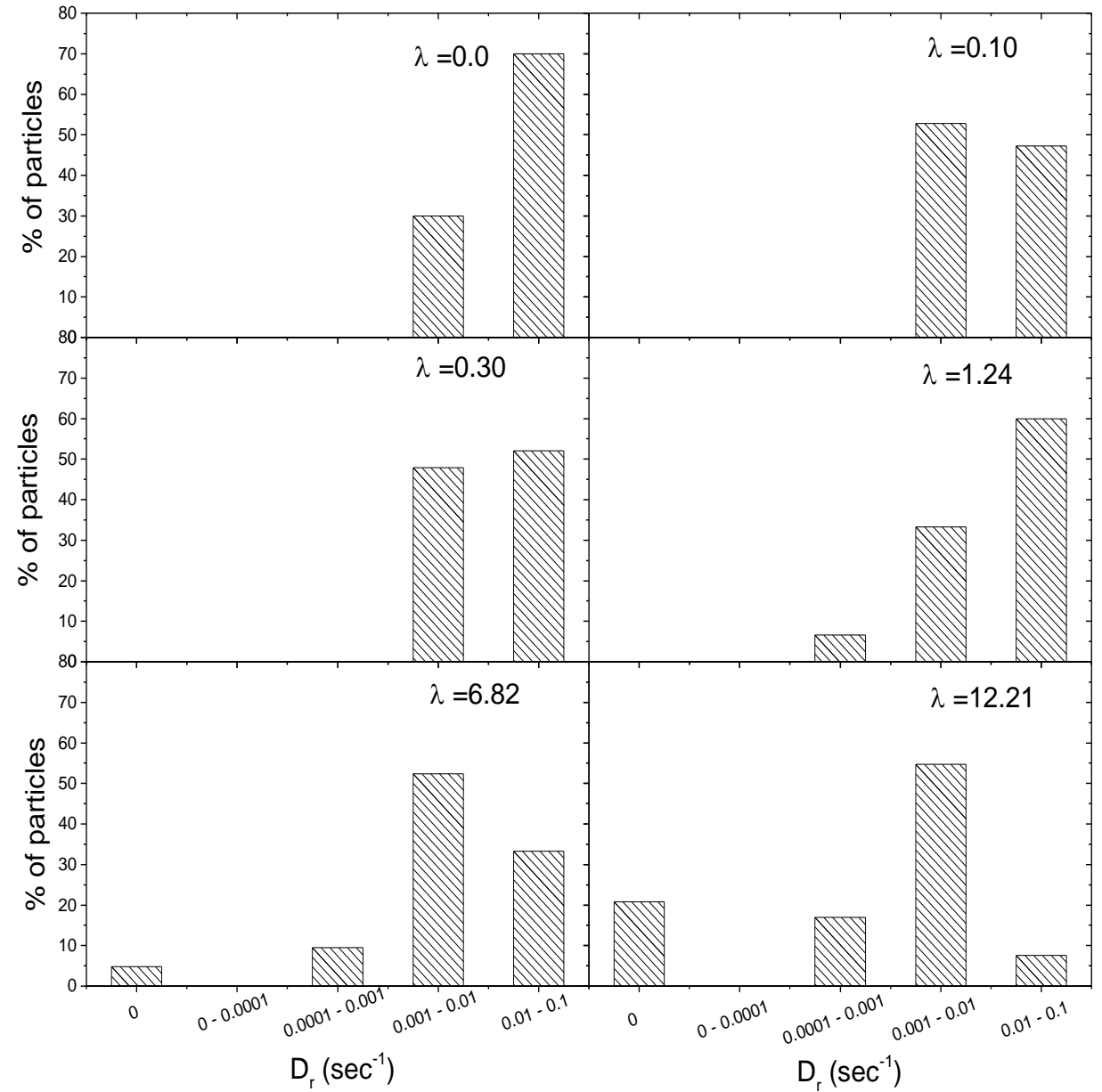
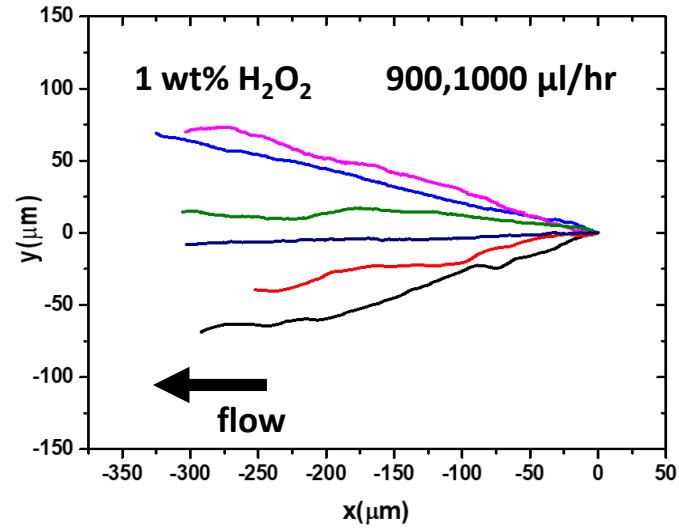
Variation with λ



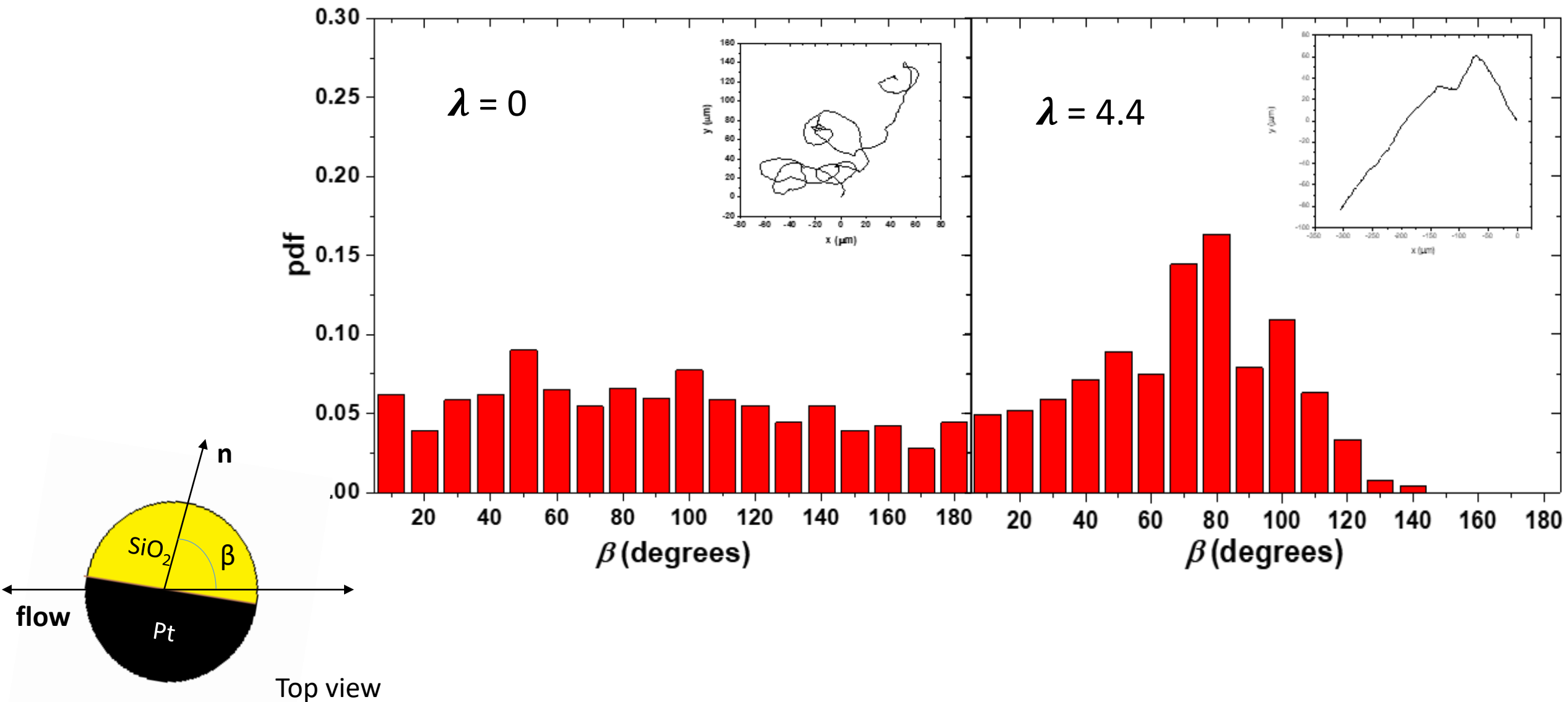
Variation of D_r with λ



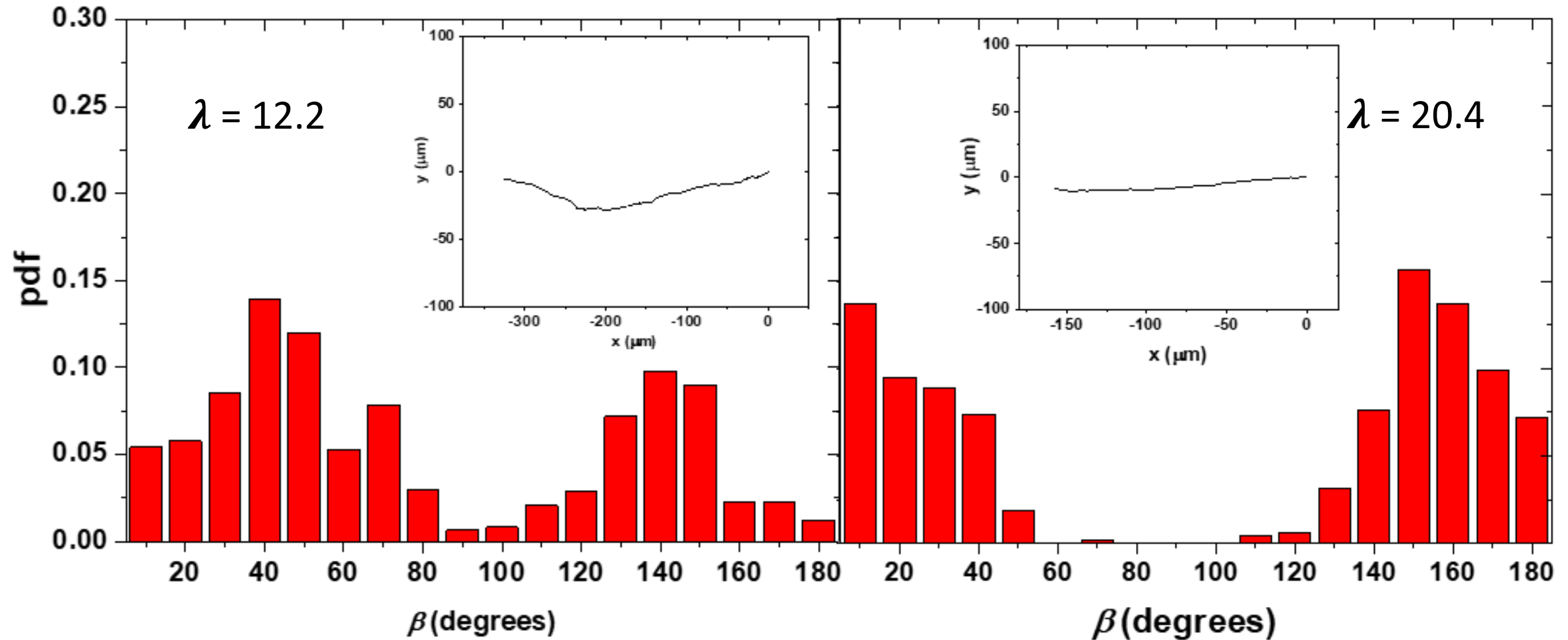
$$D_r = \frac{1}{\tau_r}$$



Angle β as a function of λ

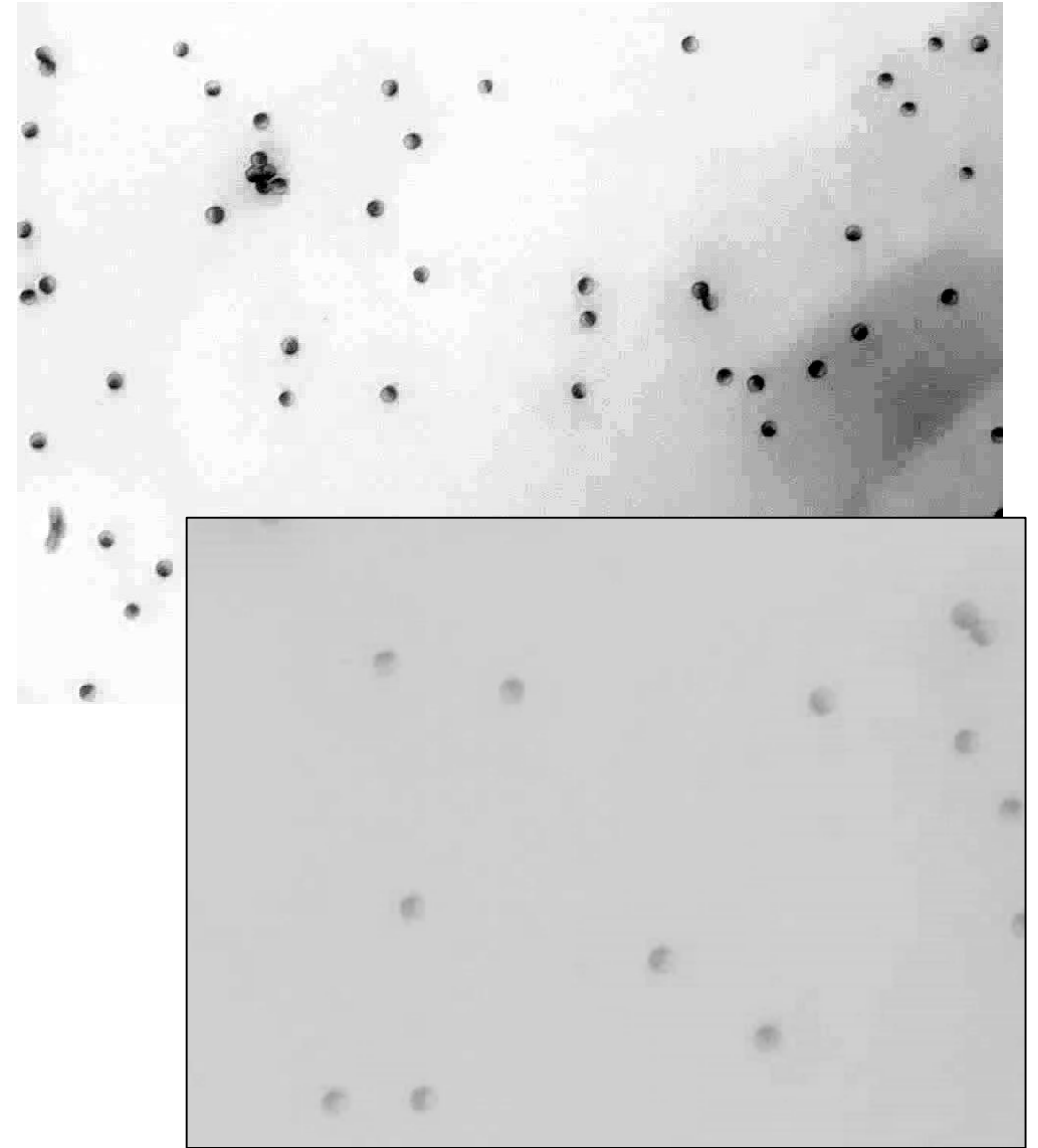
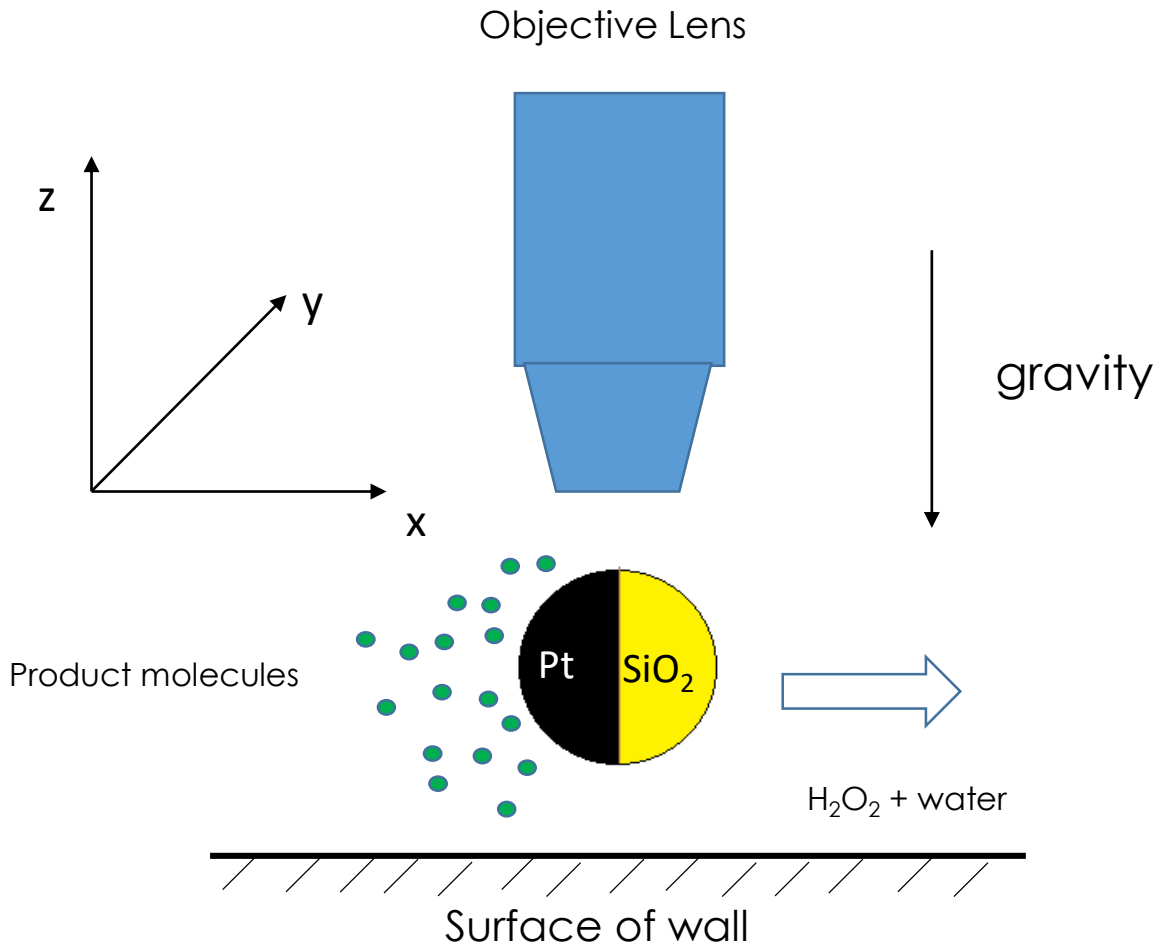


Angle β as a function of λ

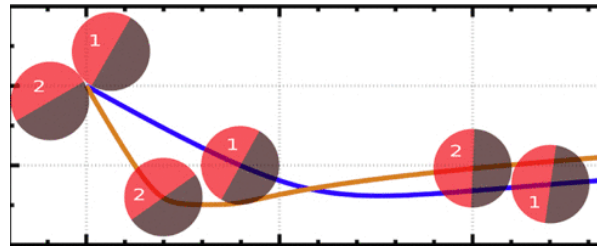


Locked out of plane rotation due to activity

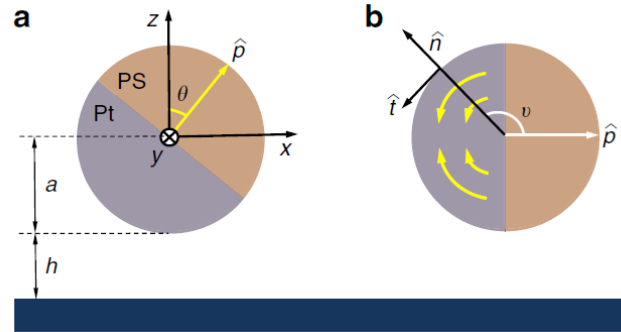
Active motion



No flow + Active motion



Maldreli et al. Phy. Of. Fluid.,(2016)



Das et al. Nature Comm.,(2015)

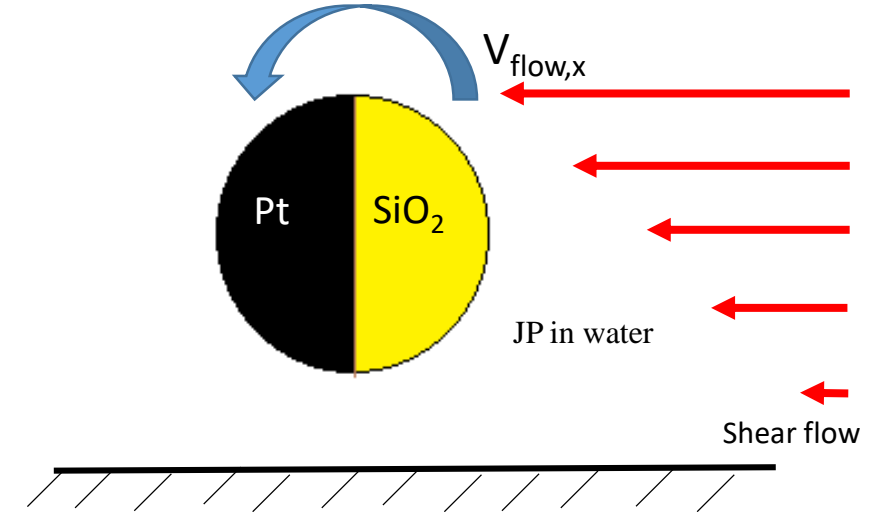
Restoring rotation to bring the Janus boundary perpendicular to the plane

$$\Omega_y(\theta) = -\Gamma(\theta - \theta_s)$$

$$\Gamma_{activity} \sim \frac{v_{activity}}{a}$$

$$\frac{\Gamma_{shear}}{\Gamma_{activity}} \sim \frac{v_{x,flow}}{v_{activity}} = \lambda$$

No Activity + Shear flow

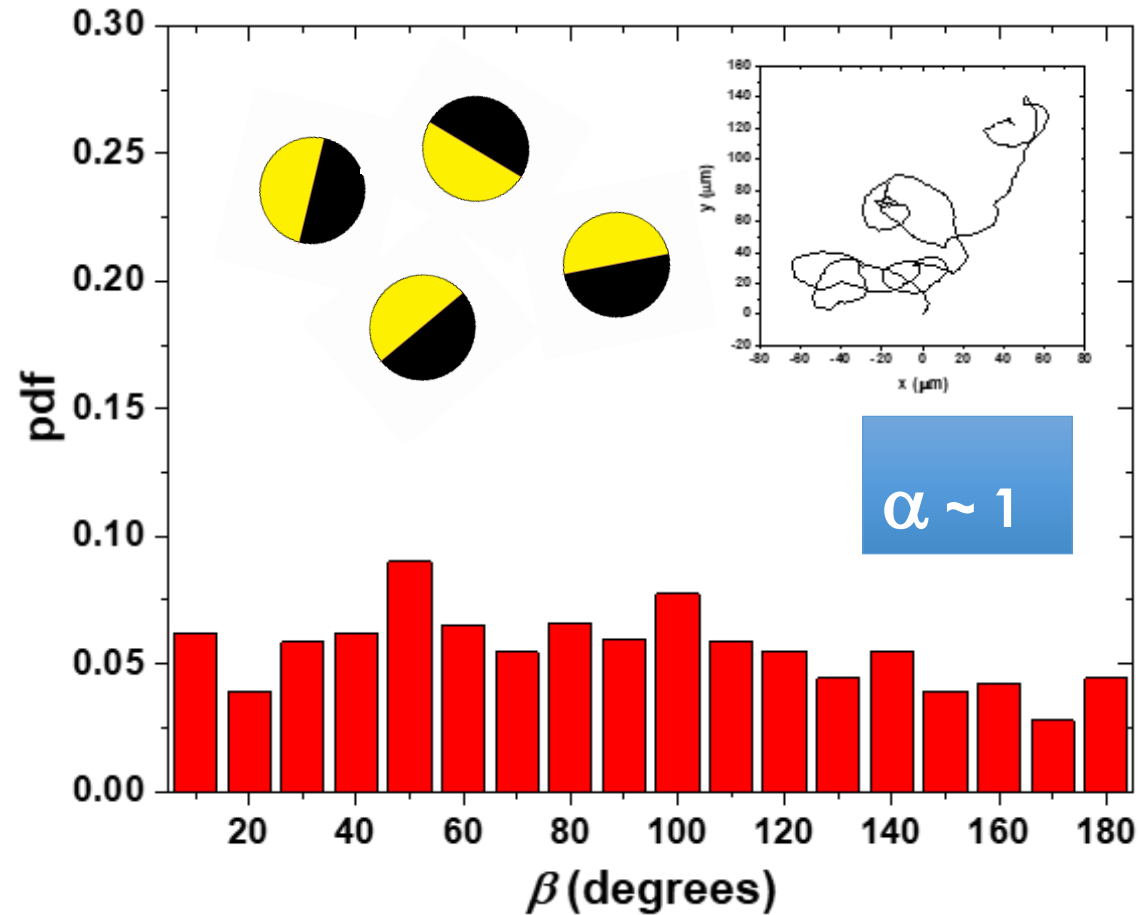


Out of plane rotation of Janus boundary

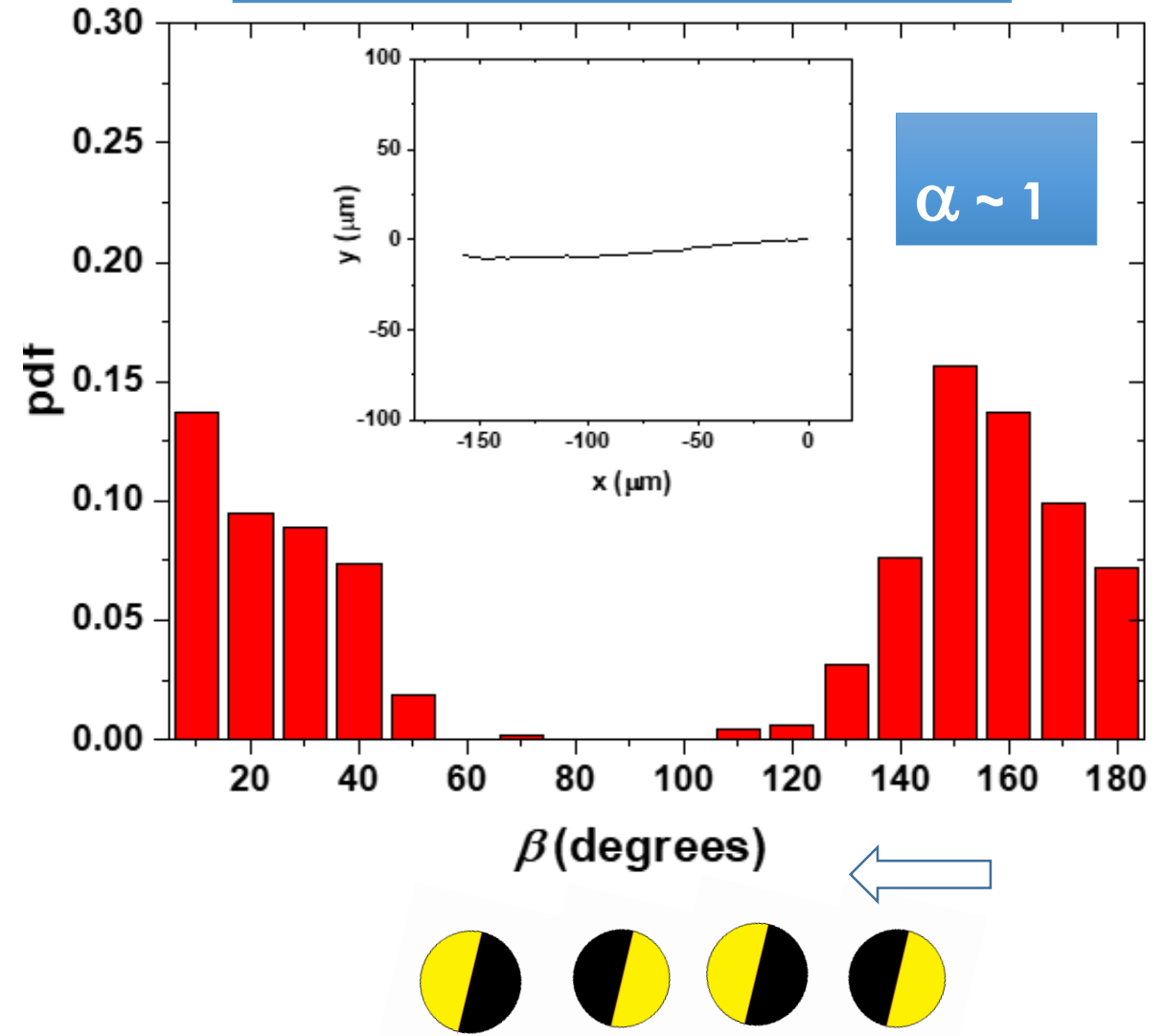
$$\Gamma_{shear} \sim \frac{v_{x,flow}}{a}$$

Random motion and migration along flow

$$\lambda \ll 1 \quad \Gamma_{\text{activity}} \gg \Gamma_{\text{flow},x}$$



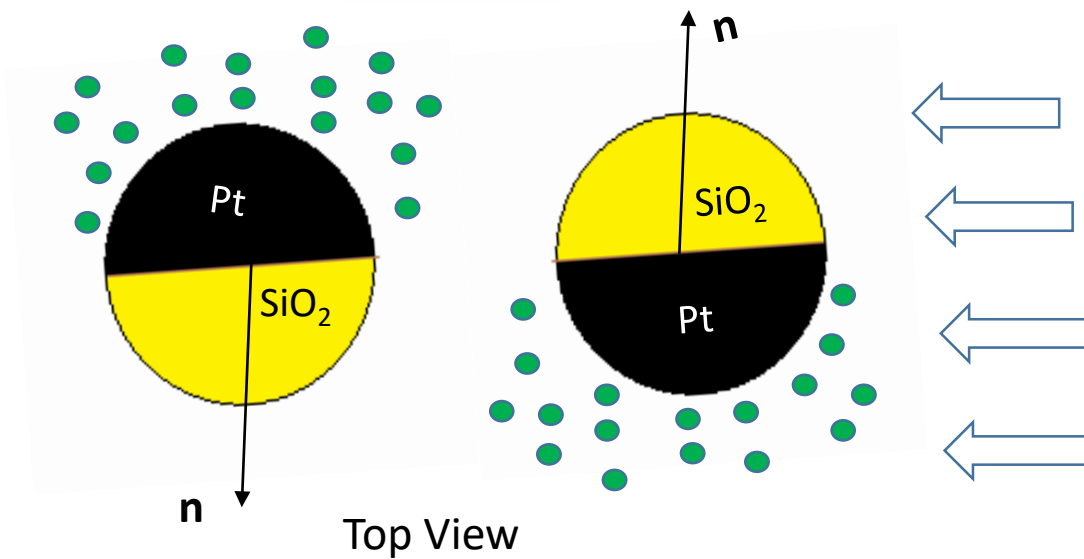
$$\lambda \gg 1 \quad \Gamma_{\text{activity}} \ll \Gamma_{\text{flow},x}$$



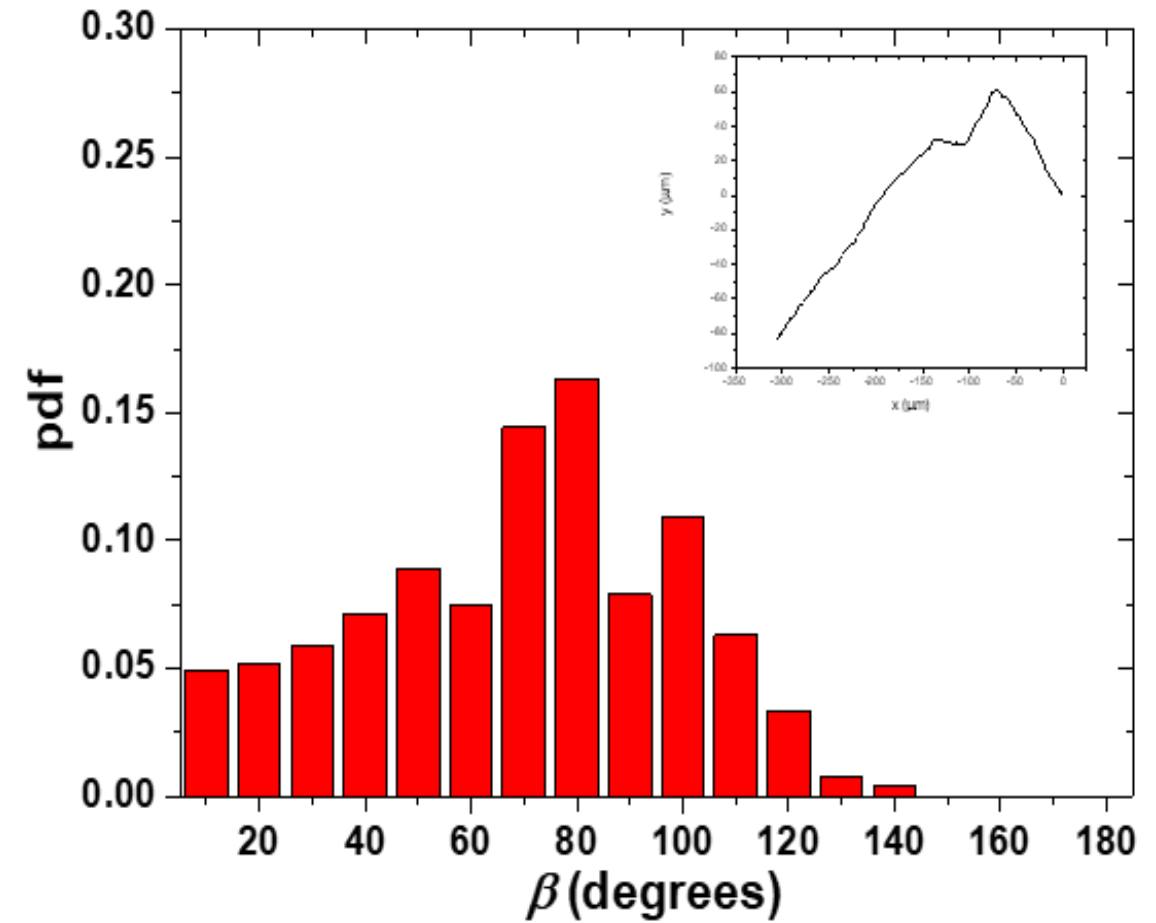
Migration across Stream Lines

$$\lambda \sim 1 \quad \Gamma_{\text{activity}} \sim \Gamma_{\text{flow},x}$$

$$\beta \sim 90^\circ$$



$$\alpha > 1$$



Conclusions

Because of presence of wall Active Propulsion brings the Janus boundary perpendicular to the plane

Shear flow tries to rotate the Janus boundary out of plane

Low Flow rates restoring rotation due to activity is quick compared to rotation due to flow
→ Random motion

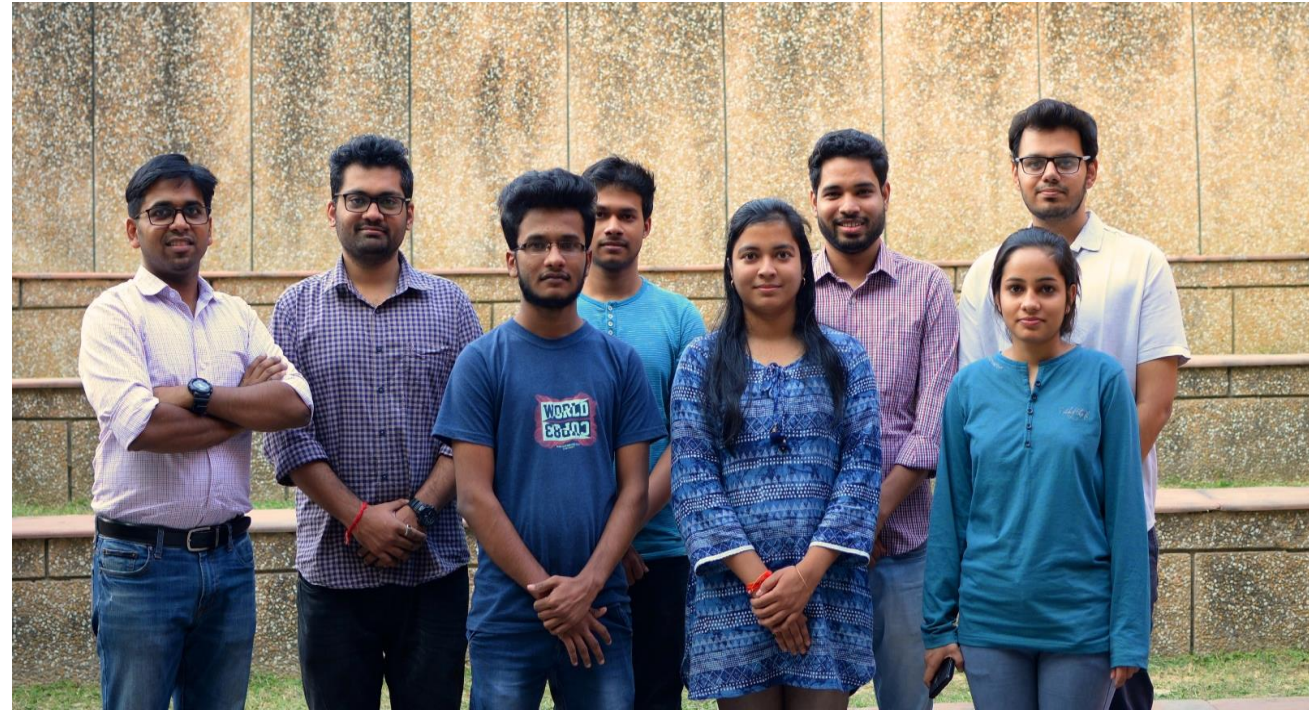
High Flow rates rotation due to flow is quicker than restoring rotation due to activity
→ Migration along flow

Moderate flow rates due to competing rotational mechanisms → Particles migrate across streamlines

Non-dimensional parameter λ explains the observations universally

Colloids And Polymer Physics Group

- Dr. Rahul Mangal, Principal Investigator
- Fellow lab members



Special thanks to:

- Dr. Asish Garg, MSE IITK
- Dr. Shashank Sekhar, MSE IITK
- Dr. Animangsu Ghatak, CHE IITK
- ACMS, IITK
- Nanoscience, IITK