

# GRAVITATIONAL LENSING



*R. Benton Metcalf*  
*2022-2023*

# BRIEF COURSE OUTLINE

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BASIC GRAVITATIONAL LENSING THEORY

APPLICATIONS:

MICROLENSING IN OUR GALAXY

DARK MATTER IN COMPACT OBJECTS

PLANETS & BINARY STARS

STRONG LENSING OF QUASARS AND GALAXIES BY GALAXIES

LENS MODELS

FITTING LENS MODELS

MICROLENSING

TIME-DELAYS AND COSMOLOGICAL PARAMETERS

LENSING BY GALAXY CLUSTERS

MASS DENSITY RECONSTRUCTION

WEAK LENSING : COSMIC SHEAR

CONSTRAINING COSMOLOGY & DARK MATTER

PYTHON EXAMPLES

# COURSE MATERIALS

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PRIMARY TEXT : “INTRODUCTION TO GRAVITATIONAL LENSING WITH PYTHON EXAMPLES”, by Massimo Meneghetti, Springer

AVAILABLE COURSE MATERIALS : <https://virtuale.unibo.it>

LECTURE SLIDES

PYTHON NOTEBOOKS from Menenghetti

OTHER SUGGESTED TEXTS :

“GRAVITATIONAL LENSING: STRONG, WEAK & MICRO”, Schneider, Kochanek & Wambsganss

“PRINCIPLES OF GRAVITATIONAL LENSING”, Congdon & Keeton

“GRAVIATATIONAL LENSING”, Dodelson

# GRAVITATIONAL LENSING

## 1 – Deflection of Light I

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# LECTURES THIS WEEK

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SOME HISTORY

DEFLECTION OF LIGHT IN THE NEWTONIAN LIMIT

DEFLECTION OF LIGHT IN GENERAL RELATIVITY

DEFLECTION OF LIGHT BY THE SUN

# CORPUSCULAR THEORY OF LIGHT

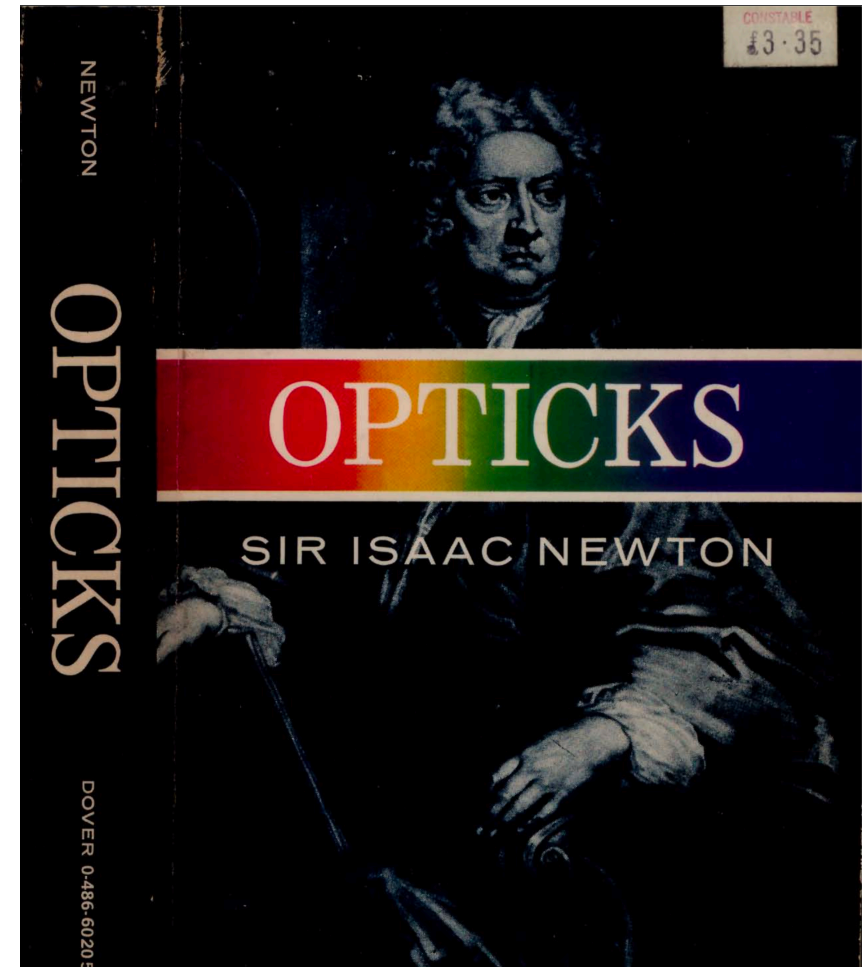
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- I. Newton, Opticks (1704-1730)
- Third volume ends with 31 queries:

*Query 1.* Do not Bodies act upon Light at a distance, and by their action bend its Rays; and is not this action (*cæteris paribus*) strongest at the least distance?

*Qu. 29.* Are not the Rays of Light very small Bodies emitted from shining Substances? For such Bodies will pass through uniform Mediums in right Lines without bending into the Shadow, which is the Nature of the Rays of Light. They will also be capable

- 1678: wave theory, Huygens



# TIMELINE

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- 1783: John Michell writes to Henry Cavendish. A light corpuscle might not be capable of escaping a massive star if

$$E \equiv \frac{1}{2}mv^2 - \frac{GmM}{R} \leq 0 \quad v = c \quad R < R_s \equiv \frac{2GM}{c^2} .$$

- 1784: Henry Cavendish calculates the deflection of a light corpuscle by a mass M. Unpublished until beginning of '900.
- 1801: Johan Soldner independently repeats the same calculation and publish it
- 1801: Thomas Young demonstrates the wave nature of light using diffraction

# DEFLECTION OF A PHOTON GRAZING THE SURFACE OF THE SUN

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**“Newtonian”  
approximation**

$$G = 6.67 \times 10^{-11} N m^{-2} kg^{-2}$$

$$c = 299792 \text{ km } s^{-1}$$

$$R_{\odot} = 695700 \text{ km}$$

$$M_{\odot} = 1.989 \times 10^{30} \text{ kg}$$



$$\hat{\alpha}(R_{\odot}) = \frac{2GM_{\odot}}{c^2 R_{\odot}} = 0.875''$$



# TIMELINE

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- 1907-1911: Einstein resumes the idea of light deflection using special relativity and equivalence principle: *“In an arbitrary gravitational field, at any given spacetime point, we can choose a locally inertial reference frame such that, in a sufficiently small region surrounding that point, all physical laws take the same form they would take in absence of gravity, namely the form prescribed by Special Relativity”*