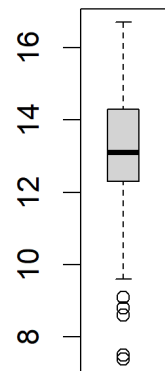


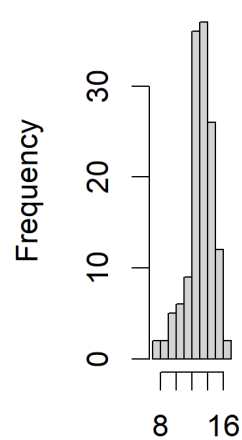
Distribution shape

Shape of the frequency distribution

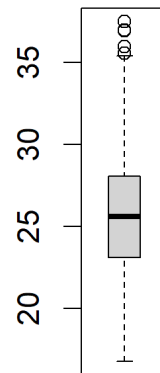
The shape of the frequency distribution can appear different for several aspects over and above location and variability



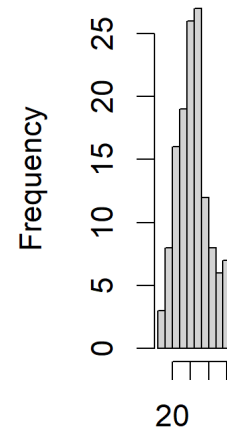
HBG



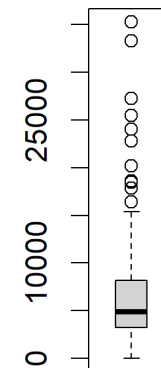
HBG



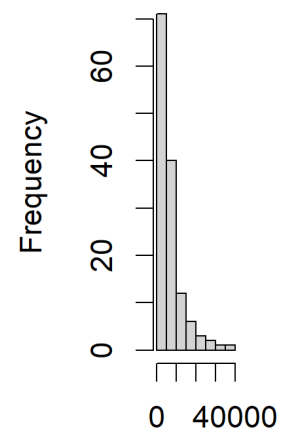
MBI



MBI



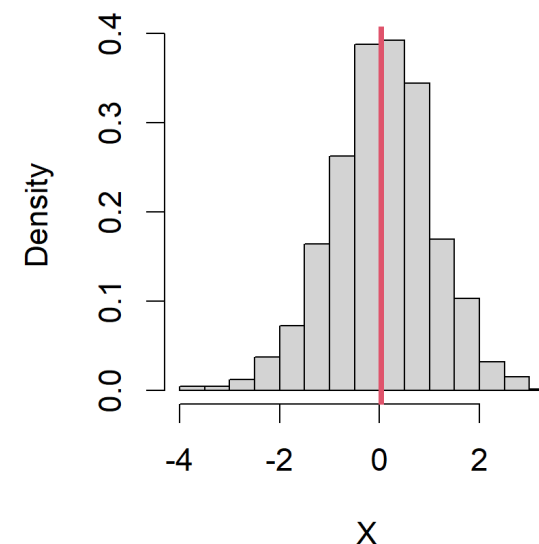
Neutrophils



Neutrophils

Symmetric versus asymmetric distribution

Geometrically, a frequency distribution is symmetric if the right half of the distribution is the mirror image of the left half.



This implies that, for symmetric distribution we get

$$\bar{X} = Me$$

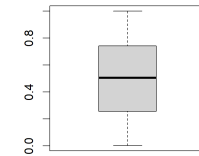
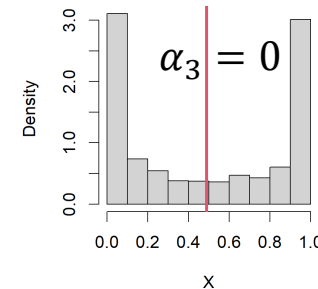
Hence an index for skewness is

$$\alpha_3 = \frac{(\bar{X} - Me)^3}{\tilde{s}^3}$$

Symmetric versus asymmetric distribution

$\alpha = 0 \rightarrow$ symmetric distribution

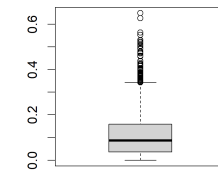
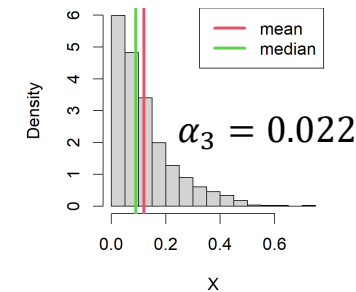
in this case $Me - Q_1 \approx Q_3 - Me$



$\alpha > 0 \rightarrow$ *positive* skewed distribution

$\rightarrow \bar{X} > Me$

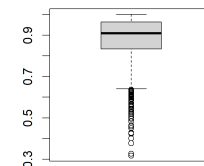
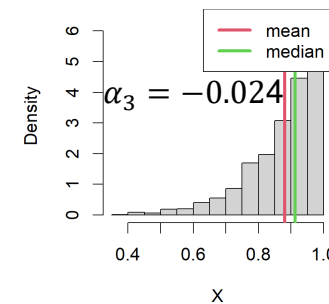
In this case $Me - Q_1 < Q_3 - Me$



$\alpha < 0 \rightarrow$ *negative* skewed distribution

$\rightarrow \bar{X} < Me$

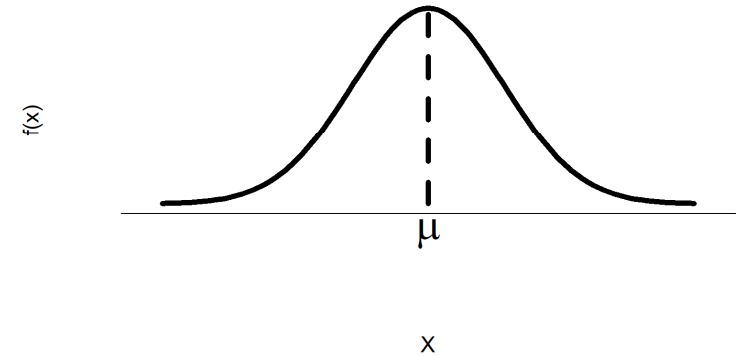
In this case $Me - Q_1 > Q_3 - Me$



Kurtosis

Kurtosis measures how much the distribution peaks around its mode.

It is defined as the degree of departure of the observed frequency distribution from the normal or *Gaussian distribution*, which is assumed as a benchmark.



The *normal distribution* is a mathematical model often adopted to describe many phenomena in real life.

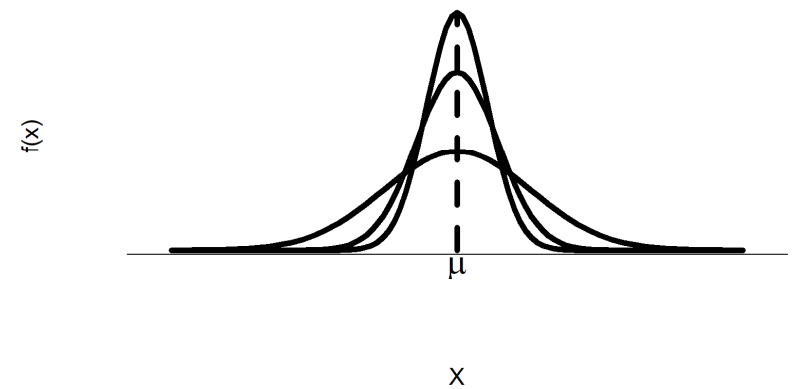
The Normal distribution is defined by the following equation

$$f(x; \mu, \sigma^2) = \frac{1}{\sqrt{2\pi} \sigma} e^{-\frac{1(x-\mu)^2}{2 \sigma^2}} \quad x \in \mathbb{R}, \mu \in \mathbb{R}, \sigma > 0$$

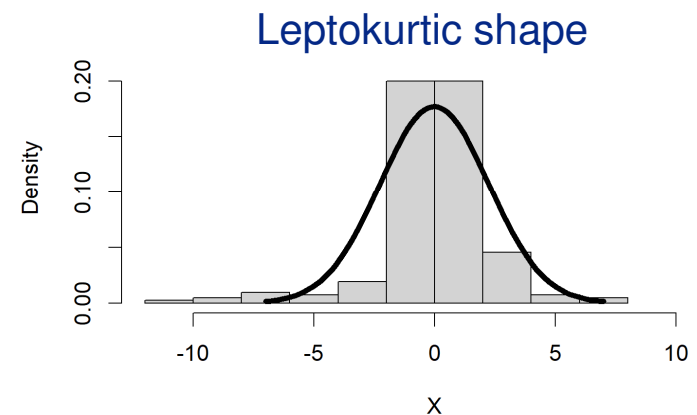
Kurtosis cont'd

μ is the maximum of the function.

σ determines the narrowness of the curve as σ decreases, the curve becomes more peaked around μ .



The observed distribution is called *leptokurtic* if, compared to the normal, it has fatter tails, whereas it is called *platykurtic* if it has thinner tails.



Kurtosis cont'd

The kurtosis index is defined by

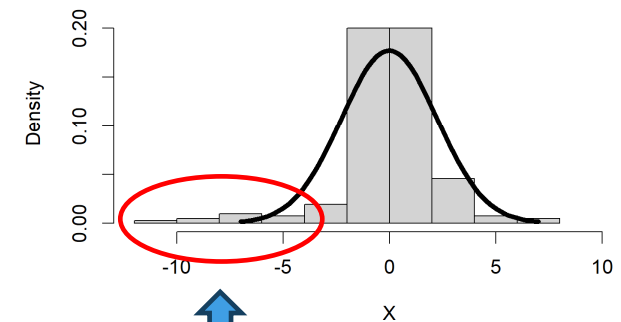
$$\gamma = \frac{1}{\tilde{S}^4} \left[\frac{1}{n} \sum_{i=1}^n (x_i - \bar{X})^4 - 3 \right]$$

$\gamma \approx 0 \rightarrow$ the distribution is close to
the normal shape

$\gamma > 0 \rightarrow$ the distribution is leptokurtic
(heavy tails)

$\gamma < 0 \rightarrow$ the distribution is platykurtic (thin tails)

$$\gamma = 9.4$$



Summarising...description of a variable: BMI

Min.	0
Q1	23.10
Median	25.58
Mean	25.78
Q3	28.07
Max.	37.50
sd	4.97
asimmetry	0
kurt	7.26
NA	2

