

welcome <sup>to</sup> back  
ASTR 160

NO SCIENCE MAJORS

FRESH / SOPH  
section sign-up MONDAY

JR / SR  
course & sections TUESDAY

1st problem set now available on  
classes V2

due Thursday (start of class)

PLEASE READ P.S. POLICIES

PLEASE START EARLY

GROUPS STRONGLY ENCOURAGED

but SUBMITTED WORK SHOULD BE  
YOUR OWN

HELP: sections (not this week)

+ on-line  
help  
sheets

office hours (CB STARBUCKS  
M 9:30 - 11 am  
TFs Weds TBA)

classes forum (works well)

cutoff: 8pm Weds

NEED MORE? COME TALK!

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# EXO PLANETS

problem: planets are too close to star

how close is it?

→ planetary orbits

$$a^3 = P^2 M$$

↗ semi-major axis  
(in A.U.)

↘ orbital period (years)

↘ mass (solar masses)

↘ distance from Earth-Sun

↘ constant depends on units

$$a^3 = \frac{P^2 GM}{4\pi^2}$$

if units are  
solar mass  
yrs  
A.U.

$$G = 4\pi^2$$

$$a^3 = p^2 M$$

$$a, M \Rightarrow p \Rightarrow (1.46 \text{ Jupiter})$$

$$\rightarrow a, p \Rightarrow M$$

$$p, M \Rightarrow a$$

Example: what is mass of Sun?

use Earth's  $\rightarrow$  mass of Sun

$$a = 1 \text{ A.U.}$$

$$p = 1 \text{ yr}$$

$$1^3 = 1^2 \times M$$

$$M = 1$$

$\hookrightarrow$  solar masses

mks units  
 $\downarrow$  meter  
 $\downarrow$  seconds  
 $\downarrow$  kilogram

A.U. :  
 150,000,000,000

$$1 \text{ year} = 365.24 \times 24 \times 60 \times 60$$

$$N \times 10^m \rightarrow \text{integer}$$

↓  
decimal

$$10^m = \underbrace{1000000}_{m \text{ zeros}}$$

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$$N \times 10^m \times A \times 10^B = A \cdot N \cdot 10^{m+B}$$

$$(N \times 10^m)^k = N^k \times 10^{m \cdot k}$$

$$(N \times 10^m)^{1/2} = N^{1/2} \times 10^{m/2}$$

$$(N \times 10^m)^{1/2} = (10 \cdot N \times 10^{m-1})^{1/2}$$

$$= (10 \cdot N)^{1/2} \times 10^{(m-1)/2}$$

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$$1 \text{ AU} = 1.5 \times 10^{11} \text{ m}$$

$$1 \text{ yr} = 2.4 \times 10^7 \times 6 \times 10^4 \times 6 \times 10^4$$

$$\times 3.6524 \times 10^2 \text{ s}$$

$$= \underbrace{2.4 \times 6 \times 6 \times 3.6 \dots}_{15 \times 90} \times 10^5$$

$$= 300 \times 10^5$$

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$$1 \text{ yr} = 3 \times 10^7 \text{ s}$$

in mks  $G = 7 \times 10^{-11}$

P.S  $a^3 = \frac{GMp^2}{4\pi^2}$

$$(1.5 \times 10^{11})^3 = \frac{(3 \times 10^7)^2 \cdot 7 \times 10^{-11} M}{4\pi^2}$$

$$(1.5 \times 1.5 \times 1.5) \times 10^{33} = \frac{3^2 \times 10^{14} \times 7 \times 10^{-11} M}{4 \times \pi^2}$$

$$= \frac{7 \times 10^4 M}{4 \times 10^1}$$

$$4 \times 10^{33}$$

$$= 2 \times 10^3 M$$

$$\frac{4}{2} \times 10^{33}$$

$$= M = 2 \times 10^{30} \text{ kg.}$$

$$3 = \pi = \sqrt{10}$$

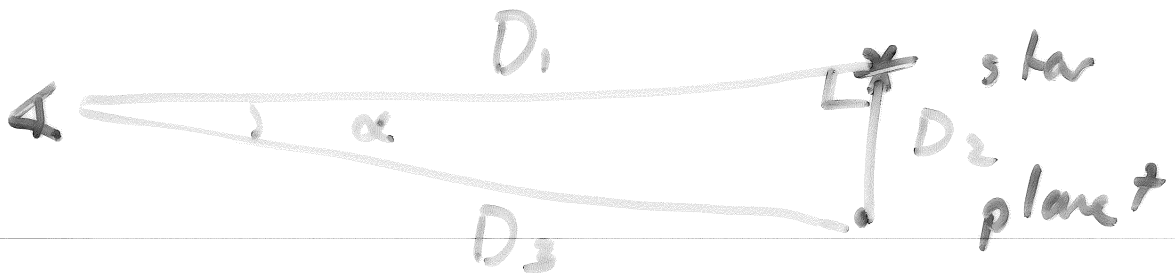

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NO ANDROIDS

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"how close are planets  
to stars"

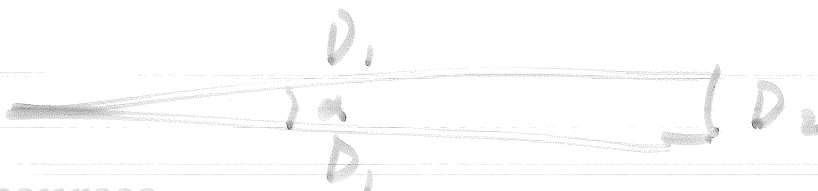
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$$\sin \alpha = \frac{D_2}{D_3}$$

Small angles

$$\sin \alpha = \alpha \rightarrow \text{radians}$$



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**SMALL ANGLE  
FORMULA**

$$\frac{D_2}{D_1} = \alpha$$

$$\frac{D_2}{D_1} = \alpha$$

$D_2, D_1$  same  
unit

$\alpha$  in radians

$2\pi$  radians in  
circle

$360^\circ$  in a circle

$\rightarrow$  AU.

$$\frac{D_2}{D_1} = \alpha$$

$\rightarrow$  arc seconds

$\swarrow$

$$\text{parsecs} = 3 \times 10^{16} \text{ m} = 3 \text{ light years}$$

60 arcsecs = arc minute  
60 arcminutes = 1 degree



## PROBLEM:

a planet with a 40 yr  
period

around a star 3 pc  
away

what is angular separation  
 $T_{\star} \approx 10,000 \text{ K}$

HARD: plug & chug fails  
because no one  
equation

: missing information  
(too much information)



$$P = 40 \text{ yrs} = 40 \times 10^7 \dots$$

$$D = 3 \text{ pc}$$

$$a^3 = P^2 M$$

$\hookrightarrow 1$   
 $\hookrightarrow 40$

$$a^3 = 1600 = 1.6 \times 10^3$$

$$a = (1.6)^{1/3} \times (10^3)^{1/3}$$

$1 \quad 10'$

AU.

$$\alpha = \frac{D_2}{D_1} = \frac{10}{3} = 3.$$

$$\alpha = 3 \text{ arc seconds}$$

Light from observatory of  
Stars is scattered over  
angular sizes of arcseconds

how to think about  
such problems

1) have  $P \Rightarrow$  want  $\alpha$   
have  $D$

2) suppose  $M \sim M_0$

3) Ah ha  $M, P \Rightarrow a$

4) distance between star-planet  
is  $a = D_2$

$$D = D_1$$

5) compute  $\alpha$

$$\alpha = D_2 / D_1$$