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In [1]: # Standard imports
import numpy as np
np.seterr(all='ignore'); # allows floating-point exceptions
import matplotlib.pyplot as plt
```

Q3: FPNS $\mathcal{F}(6, 6, -6, 6)$

(a)

The largest value in \mathcal{F} is:

$$0.555555 \times 6^6$$

(b)

The value in our number system is:

$$0.545335 \times 6^{-2}$$

(c)

From class we learned that we can express the machine epsilon as:

$$E = \frac{1}{2} B^{1-t}$$

Plugging in our values give us:

$$E = \frac{1}{2} \times 6^{1-6}$$

$$E = 0.500000 \times 6^5$$

(d)

The total number of normalized numbers that can be expressed is:

$$= 2 \text{ (sign)} \times 5 \text{ (first digit)} \times 6^5 \text{ (next 5 digits)} \times 13 \text{ (exponent)}$$

$$= 1010880$$

Therefore we need to calculate the amount of normalized numbers that are less than:

$$= 0.100000 \times 6^1$$

will be greater than 1. The number of combinations is:

$$= 2 \text{ (sign)} \times 5 \text{ (first digit)} \times 6^5 \text{ (next 5 digits)} \times 7 \text{ (exponent)}$$

$$= 544320$$

Which gives us a fraction of:

$$= \frac{544320}{1010880}$$

$$= \frac{7}{13}$$

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