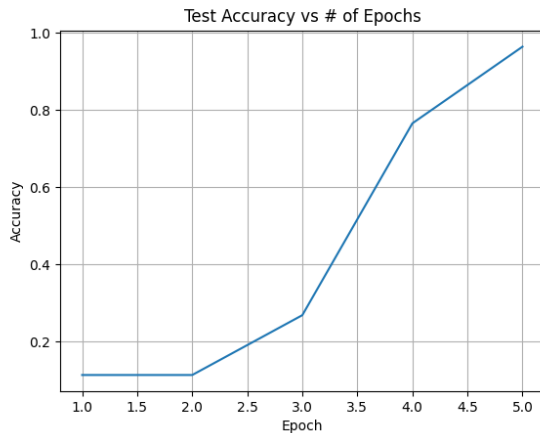


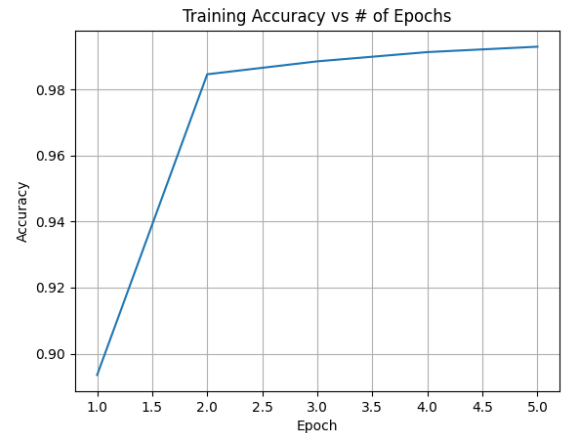
## Exercise # 2

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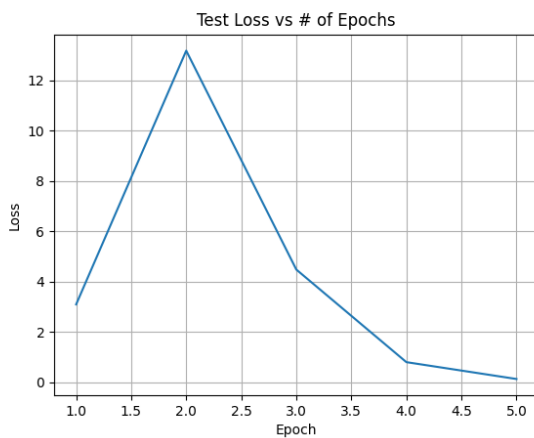
**Q2b)** Below are the 4 graphs each documenting an aspect of the training and testing process for our VG11 net implimention:



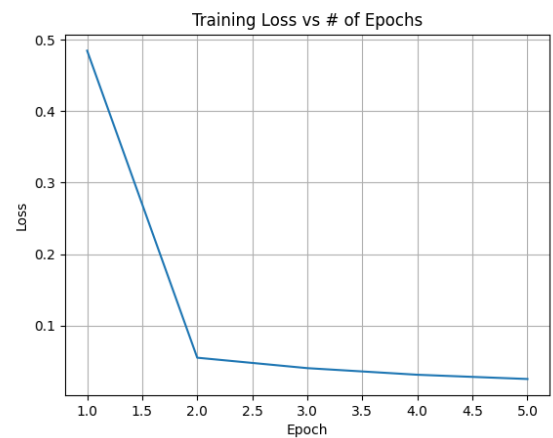
(i) Test accuracy vs the number of epochs



(ii) Training accuracy vs the number of epochs

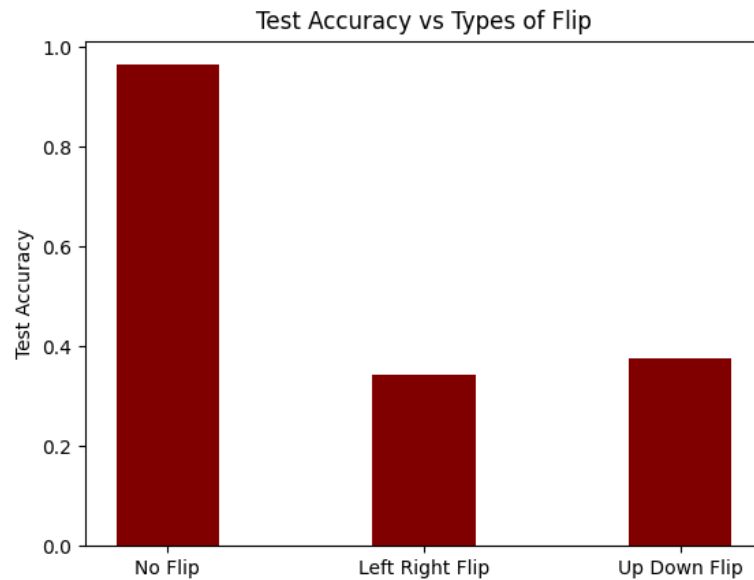


(i) Test loss vs the number of epochs



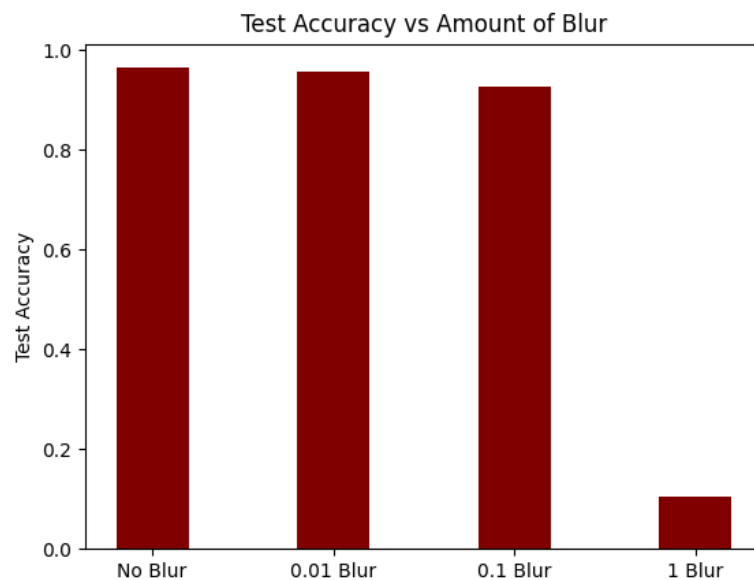
(ii) Training loss vs the number of epochs

**Q2ci)** Below we can see the testing accuracy across each flip:



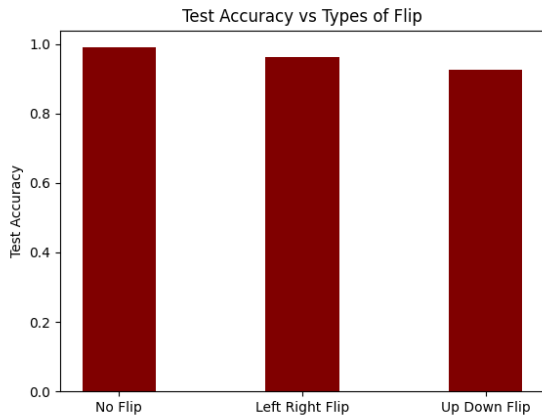
We can see that the updown flip has a higher testing accuracy than the left-right flip, this can be due to the fact that some digits remain more unchanged (like 3) from an updown flip than a right left flip. **Explicit values are provided on the next page.**

**Q2cii)** Below we can see the testing accuracy across each flip:

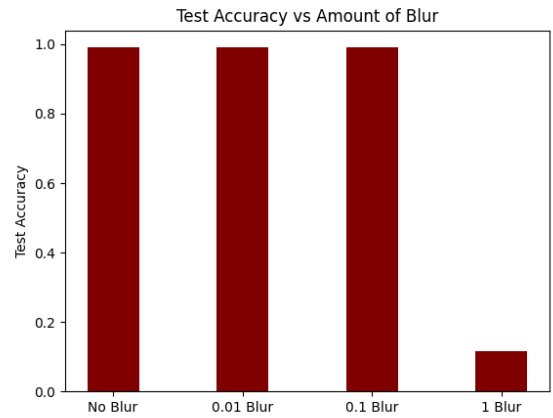


As the amount of blur increases, we can see that testing accuracy decreases. **Explicit values are provided on the next page.**

**Q2d)** By applying the both times of flips, and 0.01 and 0.1 blurring to our original dataset we can retrain for 5 epochs. After which we get the following graphs.



(i) Test accuracy vs flips



(ii) Training accuracy vs blur

We get the following updated test accuracies:

1. No Flip / No Blur: 0.9899
2. Left Right Flip: 0.9635
3. Up Down Flip: 0.9255
4. 0.01 Blur: 0.9905
5. 0.1 Blur: 0.9907
6. 1 Blur: 0.1159

This is comparison to before we did the retraining where we had the following test accuracies:

1. No Flip / No Blur: 0.9784
2. Left Right Flip: 0.3481
3. Up Down Flip: 0.3755
4. 0.01 Blur: 0.9705
5. 0.1 Blur: 0.9503
6. 1 Blur: 0.1139

Below is the code used for this question:

---

```
import tensorflow as tf
import numpy as np
import matplotlib.pyplot as plt
import pandas as pd

from tensorflow.keras import layers, models

# ===== Import MNIST dataset and Normalize =====

def normalize_img(image):
    scaled_image = image / 255. # Scale the image to 0-1

    # Add the top padding to the image
    top = np.zeros((2, 28))
    bottom = top
    image32By28 = np.concatenate([top, scaled_image, bottom], 0)

    left = np.zeros((32, 2))
    right = left
    finalImage = np.concatenate([left, image32By28, right], 1)

    return finalImage # Return image with label

(x_train, y_train), (x_test, y_test) = tf.keras.datasets.mnist.load_data()

updated_train = []
updated_test = []

for i in range(0, len(x_train)):
    updated_train.append(normalize_img(x_train[i]))

for i in range(0, len(x_test)):
    updated_test.append(normalize_img(x_test[i]))

leftRight = []
upDown = []
for i in range(0, len(updated_train)): # Generate Left Right Flip
    leftRight.append(np.fliplr(updated_train[i]))

for i in range(0, len(updated_train)): # Generate Up Down Flip
    upDown.append(np.flipud(updated_train[i]))

var1 = []
var2 = []

for i in range(0, len(updated_train)): # Generate 0.01 Blur
    newDataPoint = []
    for row in updated_train[i]:
        newRow = []
        for element in row:
            element += np.random.normal(0,0.01)
            newRow.append(element)
        newDataPoint.append(newRow)
```

```

var1.append(newDataPoint)

for i in range(0, len(updated_train)):      # Generate 0.1 Blur
    newDataPoint = []
    for row in updated_train[i]:
        newRow = []
        for element in row:
            element += np.random.normal(0,0.1)
            newRow.append(element)
        newDataPoint.append(newRow)
    var2.append(newDataPoint)

var1 = np.array(var1)
var2 = np.array(var2)
leftRight = np.array(leftRight)
upDown = np.array(upDown)

updated_train = np.array(updated_train)
updated_test = np.array(updated_test)

# Combine all of them datasets
updated_train = np.concatenate((updated_train, leftRight, upDown, var1, var2), axis=0)
y_train = np.concatenate((y_train, y_train, y_train, y_train, y_train), axis=0)

# ===== Model Definition =====

model = models.Sequential()

model.add(
    layers.Conv2D(filters=64, kernel_size=3, strides=1, padding="same", activation='relu',
        input_shape=(32, 32, 1)))
model.add(layers.BatchNormalization())
model.add(layers.MaxPooling2D(pool_size=(2, 2), padding="same"))

model.add(layers.Conv2D(filters=128, kernel_size=3, strides=1, padding="same", activation='relu'))
model.add(layers.BatchNormalization())
model.add(layers.MaxPooling2D(pool_size=(2, 2), padding="same"))

model.add(layers.Conv2D(filters=256, kernel_size=3, strides=1, padding="same", activation='relu'))
model.add(layers.BatchNormalization())

model.add(layers.Conv2D(filters=256, kernel_size=3, strides=1, padding="same", activation='relu'))
model.add(layers.BatchNormalization())
model.add(layers.MaxPooling2D(pool_size=(2, 2), padding="same"))

model.add(layers.Conv2D(filters=512, kernel_size=3, strides=1, padding="same", activation='relu'))
model.add(layers.BatchNormalization())

model.add(layers.Conv2D(filters=512, kernel_size=3, strides=1, padding="same", activation='relu'))
model.add(layers.BatchNormalization())
model.add(layers.MaxPooling2D(pool_size=(2, 2), padding="same"))

model.add(layers.Conv2D(filters=512, kernel_size=3, strides=1, padding="same", activation='relu'))
model.add(layers.BatchNormalization())

model.add(layers.Conv2D(filters=512, kernel_size=3, strides=1, padding="same", activation='relu'))
model.add(layers.BatchNormalization())
model.add(layers.MaxPooling2D(pool_size=(2, 2), padding="same"))
model.add(layers.Flatten())

```

```

model.add(layers.Dense(4096, activation='relu'))
model.add(layers.Dropout(.5))

model.add(layers.Dense(4096, activation='relu'))
model.add(layers.Dropout(.5))

model.add(layers.Dense(10))

# ===== Training and Testing =====

model.compile(
    optimizer=tf.keras.optimizers.Adam(),
    loss=tf.keras.losses.SparseCategoricalCrossentropy(from_logits=True),
    metrics=[tf.keras.metrics.SparseCategoricalAccuracy()],
)
trainingAccuracy = []
trainingLoss = []

testAccuracy = []
testLoss = []

for i in range(0, 5):
    history = model.fit(updated_train, y_train, epochs=1, batch_size=512)

    trainingAccuracy.append(history.history["sparse_categorical_accuracy"][0])
    trainingLoss.append(history.history["loss"][0])

    test_loss, test_acc = model.evaluate(updated_test, y_test, verbose=1)

    testAccuracy.append(test_acc)
    testLoss.append(test_loss)
    model.save('q3TrainedExtra'+str(i)+'.keras')

# ===== Graphing =====
x = []
for i in range(0, len(testAccuracy)):
    x.append(i+1)

plt.plot(x, trainingAccuracy)
plt.title('Training Accuracy vs # of Epochs')
plt.ylabel('Accuracy')
plt.xlabel('Epoch')
plt.grid()
plt.show()

plt.plot(x, trainingLoss)
plt.title('Training Loss vs # of Epochs')
plt.ylabel('Loss')
plt.xlabel('Epoch')
plt.grid()
plt.show()

plt.plot(x, testAccuracy)
plt.title('Test Accuracy vs # of Epochs')
plt.ylabel('Accuracy')
plt.xlabel('Epoch')
plt.grid()
plt.show()

```

```

plt.plot(x, testLoss)
plt.title('Test Loss vs # of Epochs')
plt.ylabel('Loss')
plt.xlabel('Epoch')
plt.grid()
plt.show()

trainedModel = tf.keras.models.load_model('q3TrainedExtra4.keras')

_, test_acc = trainedModel.evaluate(updated_test, y_test, verbose=1)

leftRight = []
upDown = []
for i in range(0, len(updated_test)):
    leftRight.append(np.fliplr(updated_test[i]))

for i in range(0, len(updated_test)):
    upDown.append(np.flipud(updated_test[i]))

leftRight = np.array(leftRight)
upDown = np.array(upDown)

_, test_acc_lr = trainedModel.evaluate(leftRight, y_test, verbose=1)
_, test_acc_ud = trainedModel.evaluate(upDown, y_test, verbose=1)

print(test_acc)
print(test_acc_lr)
print(test_acc_ud)

plt.bar(["No Flip", "Left Right Flip", "Up Down Flip"], [test_acc, test_acc_lr, test_acc_ud],
        color='maroon',
        width = 0.4)
plt.ylabel("Test Accuracy")
plt.title("Test Accuracy vs Types of Flip")
plt.show()

var1 = []
var2 = []
var3 = []

for i in range(0, len(updated_test)):
    newDataPoint = []
    for row in updated_test[i]:
        newRow = []
        for element in row:
            element += np.random.normal(0,0.01)
            newRow.append(element)
        newDataPoint.append(newRow)
    var1.append(newDataPoint)

for i in range(0, len(updated_test)):
    newDataPoint = []
    for row in updated_test[i]:
        newRow = []
        for element in row:
            element += np.random.normal(0,0.1)
            newRow.append(element)
        newDataPoint.append(newRow)

```

```

var2.append(newDataPoint)

for i in range(0, len(updated_test)):
    newDataPoint = []
    for row in updated_test[i]:
        newRow = []
        for element in row:
            element += np.random.normal(0,1)
            newRow.append(element)
        newDataPoint.append(newRow)
    var3.append(newDataPoint)

var1 = np.array(var1)
var2 = np.array(var2)
var3 = np.array(var3)

_, test_acc_var1 = trainedModel.evaluate(var1, y_test, verbose=1)
_, test_acc_var2 = trainedModel.evaluate(var2, y_test, verbose=1)
_, test_acc_var3 = trainedModel.evaluate(var3, y_test, verbose=1)

plt.bar(["No Blur", "0.01 Blur", "0.1 Blur", "1 Blur"], [test_acc, test_acc_var1, test_acc_var2,
    test_acc_var3], color='maroon',
    width = 0.4)
plt.ylabel("Test Accuracy")
plt.title("Test Accuracy vs Amount of Blur")
plt.show()
print(test_acc_var1)

```

---