

**Q03** To start we know that  $z$  (and thus  $|z|$ ) can be expressed as:

$$z = a + bi \text{ (for } a, b \in \mathbb{R})$$

$$|z| = \sqrt{a^2 + b^2}$$

We thus can plus this equation into the bounds of  $|z|$ :

$$1 < \sqrt{a^2 + b^2} < 4$$

$$1 < a^2 + b^2 < 16$$

Let the outer bounds (values  $a$  and  $b$  must be less then) be in the form  $(a, b)$ , they can be represented as:

$$[0, 4), [0, -4), (4, 0], (-4, 0]$$

Let the inner bounds (values  $a$  and  $b$  must be greater then) be in the form  $(a, b)$ , they can be represented as:

$$[0, 1), [0, -1), (1, 0], (-1, 0]$$

Thus we can see the graph for  $|z|$  would be the graph of a circle with radius 4 with a hole in the shape of a circle with radius 1.

Shown as the first graph

Adding  $i$  would be an upward shift of 1 in the imaginary direction, thus resulting in the second graph where the shaded region of the complex plane represents  $\{i + \bar{z} : 1 < |z| < 4, z \in \mathbb{C}\}$ .