**Q1A.** For S to be a subset of T it would imply that every element of S belongs to T. To show this is the case, I will demonstrate that every solution to S is also solution to T.

To start we know that the solution set of S is given by (where for some  $s \in \mathbb{Z}$ ):

$$c = 8s \pmod{12}$$

Congruent To Remainder (CTR), tells us that:

$$12|(c-8s)$$

From definition of divisibility we can rewrite this as (for some  $t \in \mathbb{Z}$ ):

$$12t = c - 8s$$
$$12t - 8s = c$$

$$2(6t - 4s) = c$$

Therefore we will let some integer n = 6t - 4s, we thus find that:

$$2n = c$$

By definition we find that:

Which shows that every solution to S is a solution to T, and thus S is a subset of T.

**Q1B.** Lets look at the element e = 2 in set T, we know that:

Thus we know that e=2 is a element of T. We know that the solutions (c) to S are of the form (for some integer s):

$$c = [8][s] \pmod{12}$$

Notice that  $0 \le [s] \le 11$ , thus we can construct a table that gives all possible values of c:

[s]	0	1	2	3	4	5	6	7	8	9	10	11
[s][8] (mod 12)	0	8	4	0	8	4	0	8	4	0	8	4

Therefore we notice that e=2 never coursers as a solution for any value of s. Therefore we know that the set S does not contain e=2.

Thus we have shown that the element e=2 exists within T but not within S.