# Introduction to DALES v3.1

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# Chapter 1

# Introduction

This is the introduction of the manual of DALES version 3.1.

## Chapter 2

# Change Log

### Major Changes - Version 3.1

- · Non-equidistant grid for 5th order advection scheme
- · Mixed buoyancy mixing over the wet/dry interface
- · Bulk microphysics implemented
- · Adaptive Timestepping

### Major Changes - Version 3.0

- · 3rd order Runge Kutta integration
- · Several advection schemes: 2nd, 4th and 6th order central as well as 3rd and 5th order schemes that are slightly diffusive and therefore nearly positive. The kappa scheme is also implemented.
- · Allocatable arrays, meaning that new compilation is only necessary for real code changes, and not anymore for changes in resolution or number of processors. The number of processors is now not an input parameter anymore; it is read from MPI.
- · New setup of the namelists; only one namelist (namoptions) file is now necessary.
- · Major cleanup of the main program; most subroutines are now sorted into modules.
- · The modular setup also allows for statistical routines and add-ons.
- · To keep bookkeeping of open files easy, files are always directly closed after use; as an added bonus, results are directly flushed into the files upon closing.
- guard constructions are replaced; thermodynamical 'constants' 0.622, 0.61, 1.61 and 0.378 are replaced with combinations of 1, rv and rd.

## Roadmap / Wish List

- $\cdot$  Chemistry addon
- $\cdot$  Land surface scheme
- $\cdot$  Non-periodic boundary conditions
- $\cdot$  Deep convection / an elastic Navier Stokes solver
- $\cdot$  Block instead of stripe parallelization

## Chapter 3

# **Getting Started**

### 3.1 Installation

...

### 3.2 Namoptions

The model starts by reading options from a file. This file should be included before running the code. The name of the file is namoptions. However, you are free to choose any other name, by changing the command line options at the invocation of DALES:

```
dales3 namoptions.000
```

Some of the options in namoptions are required, while most have default values and are thus optional. The options are divided into different so-called namelists. The standard package contains four of them: run, domain, physics and dynamics. The options belonging to a namelist must be preceded by an ampersand (&) followed directly by the name of the namelist in capitals. There should be a backslash on the line below the last option of a namelist to close it, e.g.:

```
&RUN
option1 = value1
option2 = value2
/
```

The order of the options is not important. In table 3.1 the options required by the model and the most used options are shown. In the examples directory, a namoptions file with this minimalistic set of options is included (namoptions.000). The option isurf requires some extra attention. This option has four possible values, one to four. Each of these values indicates a different method of calculating surface conditions. Therefore, each requires different options to be set correctly:

Table 3.1: Namelists with the most used/required options. The default value gives the value that is incorporated in the model itself. When the options is not included in the namelist, this default value is used. A '-' indicates that the model will not run without setting this value.

Option	Default	Possible values	Description	Unit					
	RUN								
iexpnr	000	any positive integer	Experiment number; every	-					
			output filename ends with						
			[.iexpnr]						
dtmax	20	any positive real	Maximum timestep that is	s					
			used by the model						
runtime	300	any positive real	Total simulation (or: run)	S					
			time						
		DON	AAIN						
xsize	-	any positive real	Horizontal size of the simu-	m					
			lated domain						
ysize	-	any positive real	Horizontal size of the simu-	m					
			lated domain						
		PHY	SICS						
thls	-	any positive real	Liquid water potential tem-	K					
			perature at the surface						
ps	-	any positive real	Pressure at the surface	Pa					
isurf	-	1,2,3,4	Flag for surface parametriza-	-					
			tion						
z0	-	any positive real	Surface roughness	m					
ustin	-	any real	Prescribed friction velocity	$\mathrm{m}\;\mathrm{s}^{-1}$					
wtsurf	-	any positive real	Flux of liq. water pot. temp.	${ m K~m~s^{-1}}$					
			at the surface	_					
wqsurf	-	any positive real	Flux of total water content	$\rm kg~kg^{-1}$					

- $\cdot$  isurf = 1: only z0 is required, this is constant
- $\cdot$  isurf = 2: only z0 is required, this is constant
- $\cdot$  isurf = 3: ustin, wqsurf and wtsurf are required
- $\cdot$  isurf = 4: wqsurf and wtsurf are required

Regarding  $dt\_max$ , it has to be noted that this is a maximum timestep. If necessary for convergence (usually at the start of the simulation) the timestep is significantly smaller. In this version of the model there is also the possibility of adaptive timestepping. The timestep is constantly calculated by means of stability criteria on the basis of the Courant and the Peclet number,  $\frac{u\Delta t}{\Delta x}$  and Re<sub>L</sub>Pr respectively. Table 3.2, at the end of this chapter, contains an extensive list of all available options

Table 3.2, at the end of this chapter, contains an extensive list of all available options in the standard package. Including any of these is optional: when not included in namoptions, the default values are used.

### 3.3 Input files

The DALES model not only needs the namoptions file. For a proper run it also requires initial vertical profiles of different quantities. These profiles are contained in several different input files. At default, only two files are used, namely prof.inp.[iexpnr] and lscale.inp.[iexpnr] (here [iexpnr] denotes the value of iexpnr contained in namoptions. In the rest of this chapter, this extension is omitted). Examples of input files can be found in the examples folder.

### prof.inp

This file contains six columns separated by white spaces and contains the initial vertical profiles of different quantities. The first (leftmost) column contains the height. The information in this column is used to see whether the grid is equidistant. In case of an equidistant grid, the column should start with dz/2 and has kmax entries (see figure 3.1). These levels are the half levels.

Figure 3.1: An example of the first part of a prof.inp input file. In this case kmax = 64 and the domain height is 1600 meters. This results in a vertical spacing dz of 25 meters. The first level is at dz/2 = 12.5m.

		/ -			
ASTEX Flight A209					
height	th_1	qt	u	V	tke
12.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
37.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
62.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
87.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
112.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
137.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
162.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
187.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
212.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
237.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
262.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
287.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
312.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
337.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
362.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
387.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
412.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
437.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
462.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
487.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
512.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
537.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
562.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
587.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
612.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
637.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
662.5000	288.000000	1.020000e-02	-0.700000	-10.000000	1.000000
687.5000	290.750000	9.650000e-03	-1.350000	-10.000000	0.000000
712.5000	293.500000	9.100000e-03	-2.000000	-10.000000	0.000000
737.5000	293.650000	9.030000e-03	-2.000000	-10.000000	0.000000

The following columns contain the profiles at *height* of the following quantities (from left to right):

- · liquid water potential temperature in K,  $\theta_l$
- · total humidity in kg kg<sup>-1</sup>,  $q_t$
- · horizontal wind velocity (in the x-direction) in m s<sup>-1</sup>, u
- · horizontal wind velocity (in the y-direction) in m  $s^{-1}$ , v
- · subfilter scale turbulent kinetic energy in m<sup>2</sup> s<sup>2</sup>, TKE

The first two lines of the file are unimportant and can be used as headers containing experiment information or column descripitions, for instance.

### lscale.inp

This file is made up of eight columns. It contains information about large scale forcings of the simulation. Like the profiles file, it starts with two unimportant header lines. Furthermore, the leftmost column is again the height, the vertical half levels of the domain, with kmax entries. For an example, see figure 3.2.

Figure 3.2: An example of the first few lines of a lscale.inp input file. Here, kmax = 64 and the domain height is 1600 meters. This results in a vertical spacing dz of 25 meters. The first level is at dz/2 = 12.5m. Most forcings are set to zero.

ASTEX Fligh	nt A209 ex	kp nr 000	•				
height	ug	. vg	wfls	datdx	datdu	datdtls	thlpcart
12.5000	-2.000	-10.ŏoo	-6.250000e-05	0.00e+00	0.00e+00	0.00e+00	0.00e+00
37.5000	-2.000	-10.000	-1.875000e-04	0.00e+00	0.00e+00	0.00e+00	0.00e+00
62.5000	-2.000	-10.000	-3.125000e-04	0.00e+00	0.00e+00	0.00e+00	0.00e+00
87.5000	-2.000	-10.000	-4.375000e-04	0.00e+00	0.00e+00	0.00e+00	0.00e+00
112.5000	-2.000	-10.000	-5.625000e-04	0.00e+00	0.00e+00	0.00e+00	0.00e+00
137.5000	-2.000	-10.000	-6.875000e-04	0.00e+00	0.00e+00	0.00e+00	0.00e+00
162.5000	-2.000	-10.000	-8.125000e-04	0.00e+00	0.00e+00	0.00e+00	0.00e+00
187.5000	-2.000	-10.000	-9.375000e-04	0.00e+00	0.00e+00	0.00e+00	0.00e+00
212.5000	-2.000	-10.000	-1.062500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
237.5000	-2.000	-10.000	-1.187500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
262.5000	-2.000	-10.000	-1.312500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
287.5000	-2.000	-10.000	-1.437500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
312.5000	-2.000	-10.000	-1.562500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
337.5000	-2.000	-10.000	-1.687500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
362.5000	-2.000	-10.000	-1.812500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
387.5000	-2.000	-10.000	-1.937500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
412.5000	-2.000	-10.000	-2.062500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
437.5000	-2.000	-10.000	-2.187500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
462.5000	-2.000	-10.000	-2.312500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
487.5000	-2.000	-10.000	-2.437500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00
512.5000	-2.000	-10.000	-2.562500e-03	0.00e+00	0.00e+00	0.00e+00	0.00e+00

Columns two to eight contain the following quantities (from left to right):

- $\cdot$  geostrophic wind in the x-direction in m s  $^{-1},\,u_g$
- geostrophic wind in the y-direction in m s<sup>-1</sup>,  $v_q$
- · large scale subsidence in m s<sup>-1</sup>,  $w_{f,ls}$
- · large scale inflow of moisture in the x-direction in kg kg<sup>-1</sup> s<sup>-1</sup>,  $\frac{dq_t}{dx}$
- · large scale inflow of moisture in the y-direction in kg kg<sup>-1</sup> s<sup>-1</sup>,  $\frac{dq_t}{dy}$
- · additional large scale moisture change in time in kg kg $^{-1}$  s $^{-1}$ ,  $\frac{dq_{t,ls}}{dt}$
- $\cdot$  prescribed temperature tendency due to radiation in K s<sup>-1</sup>

Normally, most of these forcings can be set to zero.

### ls\_flux.inp

In some cases, the large scale forcings need to be varied over time, e.g. when the subsidence at the start of a simulation is much larger than in the end. This is possible, but of course not only the initial forcing must be prescribed. Additional profiles can be 'fed' to the model by using the ls\_flux.inp file. Furthermore, timeseries of different variables

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can be prescribed. This file is only read (and thus required!) when *ltimedep* is set to .true. in namoptions.

The file has a somewhat different lay-out than the others. Like the input files above, it starts with header lines, three this time. The first block of input is made up of five columns separated by white spaces. These columns contain (from left to right):

- $\cdot$  time in s, t
- · liquid water potential temperature flux at time t at the surface in K m s<sup>-1</sup>,  $w\theta_{l,s}$
- · total humidity flux at time t at the surface in kg m s<sup>-1</sup>,  $wq_{t,s}$
- · liquid water potential temperature at the surface in K,  $\theta_{l,s}$
- · total humidity at the surface in kg kg<sup>-1</sup>,  $q_{t,s}$

The routine reads these values into arrays. Then, it interpolates linearly between these given values. Therefore, if a linearly increasing total humidity flux is required, it is sufficient to include only two lines in the first block. One line at time t=0 and one at time t=runtime. By using more entries, complicated changes in time can be made. The last line that is read is the line at time  $t \geq runtime$ .

The second part of the file contains blocks of vertical profiles of large scale forcings. Each block is exactly equal in lay-out to the lscale.inp file. It contains the same information, but not necessarily at time t=0. A profile can be given for every desired t. The model starts reading at a header line directly above the columns, which contains a # followed by a white space and a time in seconds.

Figure 3.3: An example of the first few lines of a ls\_flux.inp input file. Here, the vertical spacing dz is 25 meters. The first level is at dz/2 = 12.5m. To keep the figure small, all vertical levels above 137.50m are truncated off.

[s] [K 0 0.0	nt A209 ex surf m/s] 010000 013000	<pre></pre>	's] [K] Je-05 287		qts [kg/kg] 0.00e+00 0.00e+00		
Large scale	forcing	terms					
height	ug	vg	wfls	dqtd×	dqtdy	dqtdtls	thlpcart
# 0 12.5000 37.5000 62.5000 87.5000 112.5000 137.5000	-2.000 -2.000 -2.000 -2.000 -2.000 -2.000	-10.000 -10.000 -10.000 -10.000 -10.000 -10.000	-6.250000e-0 -1.875000e-0 -3.125000e-0 -4.375000e-0 -5.625000e-0	0.00e+00 0.00e+00 04 0.00e+00 04 0.00e+00	0.00e+00 0.00e+00 0.00e+00 0.00e+00	0.00e+00 0.00e+00 0.00e+00 0.00e+00 0.00e+00 0.00e+00	0.00e+00 0.00e+00 0.00e+00 0.00e+00 0.00e+00
height	ug	vg	wfls	dqtdx	dqtdy	dqtdtls	thlpcart
# 360 12.5000	000 -3.000	-10.000	0.000000e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00
37.5000	-3.000	-10.000	0.000000e+00		0.00e+00	0.00e+00	0.00e+00
62.5000 87.5000	-3.000 -3.000	-10.000 -10.000	0.000000e+00		0.00e+00 0.00e+00	0.00e+00 0.00e+00	0.00e+00 0.00e+00
112.5000	-3.000	-10.000	0.000000e+00		0.00e+00	0.00e+00	0.00e+00
137.5000	-3.000	-10.000	0.000000e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00

The model interpolates the profiles between the different times. So for a linear increase/decrease in time, only two blocks need to be present, one block at time t = 0 and

one at t = runtime. The lines between the end of a block and the line containing the #, are not used. These lines can contain column information for instance. Again, the last block the model reads is that at time  $t \ge runtime$ .

### scalar.inp

It is possible to include scalars in the model, such as concentrations of  $CO_2$  or pollution. These scalars are so-called passive scalars, i.e. they do not influence the model. There is only one-way coupling between the model and the scalars. Initial vertical profiles of these quantities must be included in the input. This is done by using the scalar.inp file. This file is only read (and thus required!) if, in namoptions,  $nsv \neq 0$  (see table 3.1).

The file consists of two unimportant header lines, followed by nsv + 1 columns of kmax entries. The first of these columns is as usual the height, the vertical half levels of the domain. The next columns are the vertical profiles of the scalars.

Figure 3.4: An example of the first few lines of a scalar inp input file. Here, the vertical spacing dz is 25 meters. The first level is at dz/2 = 12.5m. This example gives the necessary scalar fields for the microphysics routine, the initial raindrop (number) concentration  $N_r$  and the rainwater specific humidity  $q_r$  (section 4.1).

ASTEX Flight	A209 exp nr000	
height	Nr	qr
12.5000	0.00e+00	0.00e+00
37.5000	0.00e+00	0.00e+00
62.5000	0.00e+00	0.00e+00
87.5000	0.00e+00	0.00e+00
112.5000	0.00e+00	0.00e+00
137.5000	0.00e+00	0.00e+00
162.5000	0.00e+00	0.00e+00
187.5000	0.00e+00	0.00e+00
212.5000	0.00e+00	0.00e+00

### ls\_fluxsv.inp

When both time dependence is used (ltimedep = .true.) and scalars are included ( $nsv \neq 0$ ), the model requires extra information about the timedependence of the scalar profiles. This information is supplied by the ls\_flux.inp file. This file has a similar build up as the ls\_flux.inp file. It starts with three unimportant header lines.

The first block of data contains in the first column again time. The next nsv columns contain the surface fluxes of the different scalars at the specified time. The model interpolates these surface fluxes linearly between these times, therefore, when a linear time profile is needed, only two lines have to be included. One for the initial surface fluxes and one for the fluxes at runtime. The last line the model reads is where  $t \geq runtime$ . The next block starts with a #, followed by white space and a time. It contains the forcings for each scalar species at the specified time. Only one profile is read per scalar. That means that one block consists of nsv+1 columns, starting with height, the vertical

half levels of the domain. As many blocks can be included as required. The last block the model reads is the one at  $t \ge runtime$ .

NB. Up untill now, the large scale forcings of the scalar concentrations are <u>not</u> used. Including these profiles (these can be equal to zero everywhere) is required however, the model will stop running otherwise.

### 3.4 Output files

The filenames of the files generated by the model all end with a dot followed by the number of the experiment, *iexpnr* (table 3.1). In the standard model, no output data is generated. Only one file is created, namely output, which displays the options and initial profiles that are used by the model in that run. Therefore, it can be used as a check, to see whether or not the used input (namoptions, prof.inp etc.) is read correctly. Also, input/code related warnings are shown in this file.

A large part of the DALES code is devoted to the calculation of useful data and writing it to different output files. The code is divided over several so-called statistical routines and can be activated by adding options in namoptions (see chapter 4).

### 3.5 Run script

Of course, just compiling the source code of DALES is not enough to make it run. A run file (script) has to be used to call the model en perform some other tasks. In this section, a short overview of run scripts is given for Nemo, the computational grid of the TUDelft and for Huygens on the Dutch supercomputer SARA in Amsterdam.

#### Nemo

Figure 3.5 gives the general setup for the script that is needed to run the model on Nemo. Lines 5-8 are not necessary when the input files (here prof.inp, lscale.inp and namoptions), the model (dales3\_1) and the run script are all located in the same

Figure 3.5: An example of a run script for Nemo, the computational grid of the TUDelft. The numbers at the beginning of each line are line numbers and should not be included in the real script.

```
1 #!/bin/bash
2 #
3 #$-pe mpi 4
4
5 cp ... prof.inp.001
6 cp ... lscale.inp.001
7 cp ... namoptions
8 cp ... dales3_1
9
10 ./etc/profile
11
12 mpiexec -n $NSLOTS ./dales3_1
13
14 exit 0
```

directory. Usually, it is more convenient to locate the input files in another directory and possibly with a different name. The copy commands copy all necessary files to the same directory and at the same time give them the appropriate name. Relative paths can be used in these copy commands (for instance ./Input/E001/namoptions.001) or absolute paths (~/Les/Input/E001/namoptions.001). Of course, when extra input files are needed, these need also be copied in a similar way to the active directory. It is important that the destination file has the correct name, ending with a dot and the experiment number.

### Huygens

Figure 3.6 gives the general setup for the script that is needed to run the model on Huygens. Lines 44 to 47 give the copy commands. These are exactly equal to the commands in the run file for Nemo. In the lines below, a temporary directory is created, where all output files are stored for the duration of the run. The actual model is called in line 50. Afterwards, a directory is created whereto all init files are copied.

### 3.6 Warm start

Sometimes, it can be convenient to continue a certain simulation after it has already ended. This is possible with DALES. There are some options in namoptions that are of importance in this context (see section 3.7).

First of all, appropriate initial conditions have to be selected. Luckily, DALES saves profiles once in a certain time. The time interval at which DALES does this is *trestart*. By default, it happens once in a simulated hour. The paralellization of the model requires a restart file for each CPU.

NB. The restart files can take up quite some disk space, up to several megabytes for each file. Therefore, care should be taken in setting a small value for *trestart*, especially when using many CPUs.

DALES automatically assigns names to the restart files. They are as follows: initd00-hxxmxxx.[iexpnr]. The extension is as with all output files the experiment number. The double x in the file name is the number of the restart file, the triple x gives the CPU ID. For example, if trestart = 3600 and four CPUs are being used, then after two simulated hours, eight restart files will have been written, namely:

To continue the simulation, starting after two hours, the appropriate restart files must be copied to the directory of the executable (or, at least, the run script should copy them to the right directory). The *startfile* option should be: initd00h02mxxx.000 and

lwarmstart = .true. The model automatically changes the triple x after the 'm' (places 12 to 14) to the CPU ID.

All output now starts at t = 7200s. Therefore special care should be taken with *runtime*. This is, as the name already says, not the final time of the simulation, but the time the simulation will run. If a simulation is continued after 7200 seconds, and the runtime

Figure 3.6: An example of a run script for Huygens, the computational grid on the SARA, the supercomputer in Amsterdam.

```
#!/bin/bash
    # Loadleveler directives start with # @
3
    # In this job an MPI program is started.
 4
   # This job will run on two nodes, 16 processes on each node, # making a total of 32 processes.
 5
 6
      € job_name - 000.
8
    # @ node - I
9
    # @ tasks_per_node - 32
10
    # Loadleveler can send email, but for this job, we ask Loadleveler not
11
          to send any email:
12
    # @ notification - never
13
14
15
      Define the standard input, output and error for the job:
    # @ input - /dev/null
# @ output - errorfile.$(job_name)
16
17
    # @ error - errorfile.$(job_name)
18
19
20
    # Job will take at most 10 hour wallclock time
21
    # @ wall_clock_limit - 10:00:00
22
      Tell Loadleveler that this is a parallel job, Loadleveler will take care of defining the proper environment for the job
23
24
25
    # @ job_type - parallel
26
27
      The following line ensures that the communication between nodes will
28
      use the infiniband hardware:
    # @ network.MPI = sn_ali,not_shared,US
30
31
    # This ends the instructions for Loadleveler:
32
    # @ queue
33
34
    # Here the shell script starts.
35
    # go to the working directory:
    /bin/bash
36
37
    cd $HOME/Les/Output/H000
    workdir-`pwd`
partition-`uname -n
38
39
40
    TMPDIR-`echo $TMPDIR | sed "s/scratch\/local/gpfs\/mcnl\/${partition}/g"`
    rm -f TMPDIR.$LOADL_JOB_NAME
41
    ln -fs $TMPDIR TMPDIR.$LOADL_JOB_NAME
42
43
44
    cp .../dales3_1 $TMPDIR/dales3_1
45
    cp ... $TMPDIR/namoptions
46
    cp ... $TMPDIR/prof.inp.000
47
    cp ... $TMPDIR/1scale.inp.000
48
49
    cd STMPDIR
    ./dales3 astex >output.000
50
51
    mv * $workdir
   cd $workdir
52
53
    mkdir INIT
54 my init* INIT/.
```

is also 7200 seconds, the end time of the simulation will be 14400 seconds, or, 4 hours. This is particularly important when also working with time dependent input.

### 3.7 List of options

This section contains a list of all options that can be set in the standard model. There are other options in other namelists that can also be usefull. These can be found in chapter 4.

Table 3.2: All options with their default values, possible values, a description and the unit, for all namelists in namoptions. Namelists that are specific for statistical routines or add-ons are not included (see chapter 4).

Option	Default	Possible values	Description	Unit		
RUN						
iexpnr	000	any positive inte-	Experiment number; every out-	-		
		ger	put filename ends with [.iexpnr]			
$\operatorname{dtmax}$	20	any positive real	Maximum timestep that is used	s		
			by the model			
runtime	300	any positive real	Total simulation (or: run) time	s		
lwarmstart	.false.	.false./.true.	Flag for a "cold" or a "warm"	-		
			start			
startfile	-	see section 3.6	Basis for the name of the restart-	-		
			files			
trestart	3600	any positive real	Each <i>trestart</i> seconds, a restart	S		
			file is written to disk			
$dtav\_glob$	60	any positive real	Global value for sampling inter-	S		
			val of statistical routines			
$timeav\_glob$	3600	integer multiple	Global value for writing interval	s		
		of $dtav\_glob$	of statistical routines			
irandom	0	any integer	Number to feed randomnizer	-		
			with			
krand	kmax	any positive inte-	Top vertical full level of random-	-		
		ger	nization			
randqt	1e-5	any positive real	Amplitude of randomnization of	$\rm kg~kg^{-1}$		
			qt			
randthl	0.1	any positive real	Amplitude of randomnization of	K		
			thl			

nsv	0	0-100, integer	Number of additional passive	-
			scalars	
ladaptive	.false.	.false./.true.	If .true., this allows the model	-
			to vary time step, depending on	
			numerical stability criteria	
courant	1.4 or 3	any positive real	Courant number	-
peclet	0.2	any positive real	Peclet number	-
		DOMA	AIN	
imax	64	any positive inte-	Number of horizontal grid points	-
		ger	in x-direction	
jtot	64	any integer multi-	Number of horizontal grid points	-
		ple of number of	in y-direction	
		processors		
kmax	96	any positive inte-	Number of vertical grid points	-
		ger		
xsize	-	any positive real	Horizontal size of the simulated	m
			domain	
ysize	-	any positive real	Horizontal size of the simulated	m
			domain	
xlat	52	-90 - +90	Latitude	0
xlon	0	0 - 360	Longitude	0
xday	1	1 - 365	Number of the day	-
xtime	0	0:00 - 24:00	UTC time of the day	h
ksp	$\min(\frac{3}{4}k\max,$	0 - (kmax - 15)	Lower height of sponge layer	-
	kmax - 15)	DIIXG	LCG	
.1.1	ı	PHYS		77
thls	-	any positive real	Liquid water potential tempera-	K
		• . • 1	ture at the surface	D
ps · · · ·	-	any positive real	Pressure at the surface	Pa
isurf	-	1,2,3,4	Flag for surface parametrization	-
z0	-	any positive real	Surface roughness	m _1
ustin	-	any real	Prescribed friction velocity	${\rm m \ s^{-1}}$
wtsurf	-	any positive real	Flux of liq. water pot. temp. at	${ m K~m~s^{-1}}$
c		•,•	the surface	1 1 -1
wqsurf	-	any positive real	Flux of total water content	$\rm kg \ kg^{-1}$
wsvsurf(1:nsv)	0	any real	Flux of scalar n at the surface	<u> </u>

ltimedep	.false.	.false./.true.	Switch for timedependent fluxes	_
			and large scale forcings	
lcoriol	.true.	.false./.true.	Switch for coriolis force	-
lmoist	.true.	.false./.true.	Switch for calculation of mois-	-
			ture fields	
lneutraldrag	.false.	.false./.true.	Switch for stability correction	-
chi_half	0.5	0 - 1	Fraction determining if a dry or	-
			a moist $\theta_v$ gradient is used to	
			compute the subgrid bouyancy flux at a cloud interface	
			nux at a cioud interrace	
			Flag for radiation calculations	
			0 = No radiation	
			1 = Full radiation (not imple-	
iradiation	2	0, 1, 2, 10	mented yet)	-
			2 = Parametrized radiation	
			10 = User defined radiation (use	
			rad_user.f90)	
timerad	0	any positive real	Value for sampling interval of ra-	S
omici ad	O	any positive rear	diation scheme	5
rad_ls	.true.	.false./.true.	Switch for prescribed radiative	_
		,	forcing	
rad_longw	.true.	.false./.true.	Switch for parametrized long-	-
			wave radiative forcing	
rad_shortw	.true.	.false./.true.	Switch for parametrized short-	-
			wave radiative forcing	
rad_smoke	.false.	.false./.true.	Switch for longwave divergence	-
nlro	130	any positive resi	for smoke cloud	$\mathrm{m^2~kg^{-1}}$
rka	190	any positive real	Extinction coefficient (used if $iradiation = 2$ )	m- kg -
dlwbot	0	any positive real	Longwave radiative flux jump at	${ m W~m^{-2}}$
diw bot		any positive rear	cloud bottom	,, 111
dlwtop	74	any positive real	Longwave radiative flux jump at	${ m W~m^{-2}}$
•			cloud top	
L	ı	1		

sw0	1100	any positive real	Direct solar radiative compo-	${ m W~m^{-2}}$
			nent cloud top (assumes zero dif-	
			fusive contribution)	
gc	0.85	0 - 1	Asymmetry factor of droplet	-
			scattering angle distribution	
$sfc\_albedo$	0.05	0 - 1	Surface albedo	-
reff	1e-5	any positive real	Cloud drop effective radius	m
isvsmoke	1	positive integer $\leq$	Number of passive scalar fields	-
		nsv	to be used for optical depth	
			calculation (not used when	
			$rad\_smoke = .false.)$	
		DYNA	AMICS	
cu	0	any real	Transformation velocity of the	$\mathrm{m}\;\mathrm{s}^{-1}$
			Galilei transformation in x-	
			direction	
cv	0	any real	Transformation velocity of the	${ m m~s^{-1}}$
			Galilei transformation in y-	
			direction	
llsadv	.false.	.false./.true.	Switch for large scale forcings	-
lqlnr	.false.	.false./.true.	Switch for Newton-Raphson ap-	-
			proximation of the liquid water	
			content	
			Advection scheme for momen-	
			tum, TKE, $\theta_l$ , $q_t$ and scalars:	
iadv_mom			1 = 1st order upwind	
iadv_tke			2 = 2nd order central difference	
iadv_thl	5	1,2,4,5,6,7	4 = 4th order central difference	-
iadv_qt			5 = 5th order central difference	
iadv_sv			6 = 6th order central difference	
			7 = kappa scheme	
111		SUBC		
ldelta	.false.	.false./.true.	Switch for diminished sfs in sta-	-
],	6.1		ble flow	
lmason	.false.	.false./.true.	Switch for decreased length scale	-
			near the surface	

cf	2.5	any positive real	Filter constant	-
cn	0.76	any positive real	Subfilter scale parameter	-
Rigc	0.25	any positive real	Critical Richardson number	-
Prandtl	3	any positive real	Prandtl number	_

# Chapter 4

# Statistical Routines and Add-Ons

The DALES code is highly modular. It consists of only a few modules, which in turn consist of a few subroutines per module. The core program makes calls to the subroutines to execute them. This helps to keep the model fast and tidy. Parts of the model can easily be deactivated. This way, everyone can adjust it to his or her purposes. This deactivating can be done by removing the calls inside the main time loop in the code. An easier way, without having to change the code, is by using namelists. Some modules have their own namelist. These modules can be quite useful to some, while being completely unnecessary to others. The namelist of a seperate module contains the options specific for that module, including a switch to activate it. By default, these switches are false. Therefore, namelists of unused modules need not be included in the namoptions file.

A distiction can be made in the modules that are not part of the core. There are modules that have a one way interaction with the model. These modules use information of the model, but do not influence the simulation. These modules are called Statistical Routines. What these routines usually do is create data files with time-averaged output. They have a time sampling interval and a time averaging/writing interval. After every sampling interval, the instantaneous values of certain quantities are taken from the model and, if necessary, calculations are done with them. After a writing interval, these values are averaged and written to a data file. Most of the statistical routines do not write entire 3D fields, but average over the domain, which results in average vertical profiles:

$$\overline{\psi}(z) = \frac{\sum_{n=1}^{N} \sum_{i=1}^{N_x} \sum_{j=1}^{N_y} \psi(x, y, z, t)}{N N_x N_y}$$
(4.1)

where

$$N = \frac{time\_av}{dtav}. (4.2)$$

Preferably, the sampling and averaging time intervals are by default equal to the global values, which can be set in namoptions (see table 3.2). The namelist of the module may contain options to change these intervals to different values.

Other modules incorporate physical processes into the model. This means that there can be two-way coupling between the module and the model. This does not necessarily be the case however. The particles add-on, for instance, that is discussed below does not influence fields of  $q_t$  or temperature, but it still is an add-on because it incorporates the physical process of particle advection. A list of all add-ons that are already available is given in the next section.

The general idea is that the code required to include an extra module into the model is kept at a minimum. Those present now only require a use statement in program.f90 together with three calls: the first call is to the init subroutine in the module, the second calls the execution subroutine while the third finalizes the module by calling the exit subroutine of the module (if necessary). This way, the original code is hardly altered by the addition of the extra module. To ensure that variable or subroutine names are not interfering, a 'private' statement should be included.

### 4.1 Add-Ons

Below, a short description of the available add-on modules is given, together with a list of the associated options.

### modmicrophysics

This module adds microphysical schemes to the code. The available options are summarized in table 4.1.

Up until now the only microphysics scheme is the bulk microphysics scheme. On the list for later versions is a (simpler) drizzle routine and an option for user specified microphysics. The options below the microphysics flag in table 4.1 are only used in the bulk microphysics routine. The bulk microphysics scheme uses two scalars, so when using this scheme, nsv should be at least two. The first scalar represents the particle number concentration  $N_r$ , while the second is the rainwater specific humidity  $q_r$ . The output that is produced by this module are the files associated with the scalar fields. For each scalar a field and a flux file are generated. More output can be generated by activating the special bulk microphysics statistical routine. More information on this scheme can be found under modbulkmicrostat in the next section.

The shape parameter  $\mu_r$  is used to describe the rain drop number density distribution in the microphysics parameterization in the following way (Stevens and Seifert, 2008):

$$f_r(D) = n_r \left(\frac{D}{D_p}\right)_r^{\mu} \frac{exp(-D/D_p)}{D_p\Gamma(\mu_r + 1)}.$$
(4.3)

In this equation  $n_r$  is the rain-drop number mixing ratio,  $\mu$  is the shape parameter,  $D_p$  is a size parameter and  $\Gamma$  is the Gamma function.

		NAMMIC	ROPHYSICS	
			Flag for the microphysical scheme:	
			0 = No microphysics (all-or-nothing	
imicro	0	0,2	scheme)	-
			2 = Bulk microphysics	
l_sb	.true.	.false./.true.	Switch for KK00 (Khairoutdinov and	-
			Kogan, 2000) or SB (Seifert and Be-	
			heng, 2001, 2006) scheme resp.	
$l\_sedc$	.true.	.false./.true.	Switch for cloud droplet sedimentation	-
l_rain	.true.	.false./.true.	Switch for rain formation and evolution	-
l_mur_cst	.false.	.false./.true.	Switch for a constant value of $\mu_r$ (in	-
			raindrop gamma distribution)	
mur_cst	5	any positive real	Value for $\mu_r$ , a shape parameter for the	-
			rain drop number density distribution	
			(used only if $l_mur_cst = .true.$ )	
$Nc_0$	-	any positive real	Initial number of cloud droplets	-
$sig\_g$	_	any positive real	Geometric standard deviation of the	-
			cloud droplet drop size distribution	
sig_gr	_	any positive real	Geometric standard deviation of the	-
			rain droplet drop size distribution	

Table 4.1: Options associated with the microphysics add-on with the default value, possible values, a short description and the unit of the given value.

### modnudge

With this module,  $\theta_l$  en  $q_t$  can be kept at their initial profiles. This is achieved by exerting a source term:  $-\frac{\overline{\phi}-\overline{\phi}_{init}}{\tau}$ . The only options available for this module is tnudge ( $\tau$ , the timescale of the source term), which has a default value of 0. This causes the module not to be used. Setting a different value under the namelist NAMNUDGE automatically activates the module.

### modparticles

The particles module enables one to add massless tracer particles to the simulation. It calculates the Lagrangian tracks of these particles according to a user-specifiable time integration scheme. Unlike the bulk microphysics module, which has a separate statistics module, the particles module has only one namelist where statistics can be switched on and off. All available options for this module are located in table 4.2.

To use the particles routine, an extra input file needs to be included. The name of this input file has to be partstartpos. [iexpnr]. The total number of particles must be on the first line of the file. The rest of the file has the initial conditions of each particle, one line per particle. The first column is the time t in seconds, the second to fourth column are the physical coordinates of the particles: x, y, z respectively.

NAMPARTICLES				
lpartic	.false.	.false./.true.	Switch to enable/disable this routine	-
lpartsgs	.true.	.false./.true.	Switch for subgrid diffusion	-
intmeth	3	0,3	Flag for time integration scheme  0 = particles stand still  3 = Adams-Bashfort second order	_
			scheme	
lstat	.false.	.false./.true.	Switch for particle statistics	_
dtav	60	any positive real	Time interval for sampling of statistics	$\mathbf{s}$
timeav	3600	integer multiple	Time interval for writing statistics	s
		of dtav		
ldump	.false.	.false./.true.	Switch for dump of particle field	-
timedump	3600	any positive real	Time interval for particle field dump	s
npartdump	10	0-10	Number of variables written at	-
			timedump, in order: $x, y, z, u, v, w$ ,	
			$\theta_l,\theta_v,q_t,q_l$	

Table 4.2: Options associated with the particles add-on with the default value, possible values, a short description and the unit of the given value.

The output of this routine can consist of two files: partstat and particles. The first of these is only created if lstat = .true. and it contains the statistics on the particles, like averaged vertical profiles of resolved and subgrid scale velocities and turbulent kinetic energy. The latter file is only created if ldump = .true. and it contains instantanious information of the particles.

#### modtilt

By activating this module, one can create a tilted boundary layer. This can be used to simulate katabatic flow. The options that are available in the namelist associated with this add-on are located in table 4.3.

Table 4.3: Options associated with the tilt add-on with the default value, possible values, a short description and the unit of the given value.

	NAMTILT			
ltilted	.false.	.false./.true.	Switch for a tilted boundary layer	-
alfa	0	$-\frac{\pi}{2} - +\frac{\pi}{2}$	Tilt angle	$\operatorname{rad}$
lstat	.true.	.false./.true.	Switch for statistics	-
dtav	$dtav\_glob$	any positive real	Time interval for sampling of statistics	$\mathbf{s}$
timeav	$timeav\_glob$	integer multiple	Time interval for writing statistics	s
		of dtav		

### 4.2 Statistical Routines

In this section, a short description of all available statistical routines is given, with their associated namelist.

### modbudget

The budget module calculates the terms of the TKE equation: buoyancy, shear, transport etc. terms. Two output files are created, namely budget and sbbudget. The first contains vertical profiles of the resolved TKE terms, while the latter contains the subgrid TKE terms. The options that are available for this routine are given in table 4.4.

Table 4.4: Options associated with the budget statistical routine with the default value, possible values, a short description and the unit of the given value.

	NAMBUDGET			
lbudget	.false.	.false./.true.	Switch for turbulent TKE budget cal-	1
			culation	
dtav	dtav_glob	any positive real	Time interval for sampling of statistics	$\mathbf{S}$
timeav	$timeav\_glob$	integer multiple	Time interval for writing statistics	$\mathbf{S}$
		of dtav		

### modbulkmicrostat

This routine can only be activated if the bulk microphysics add-on is used. It calculates various tendencies and statistics regarding the number of rain and cloud drops, the amount of liquid water in cloud or rain droplets, etc. The output is located in four different files: precep, nptend, qltend and qttend. Table 4.5 contains the options of the namelist associated with this routine.

Table 4.5: Options associated with the bulkmicrostat routine with the default value, possible values, a short description and the unit of the given value.

NAMBULKMICROSTAT				
lmicrostat	.false.	.false./.true.	Switch for microphysics statistics cal-	-
			culation	
dtav	dtav_glob	any positive real	Time interval for sampling of statistics	$\mathbf{S}$
timeav	$timeav\_glob$	integer multiple	Time interval for writing statistics	S
		of dtav		

### modchecksim

This routine calculates the divergence  $\overline{\nabla}\overline{u}$  and the Courant numbers for the different directions  $u_i \frac{\Delta t}{\Delta x}$ . Some of these values are written to the output file (the maximum and

the total divergence, the maximum values of the Courant number in all three directions). The associated namelist is NAMCHECKSIM, the only option contained in this namelist is *tcheck*, which gives the interval between checks. The default value is 3600 s.

### modcloudfield

The cloudfield statistical routine dumps all the wet points (points were  $q_l > 1\text{e-}5 \text{ kg kg}^{-1}$  of the domain into the clouds file. An additional switch controls the output of  $q_l$  and w values. All available options are summarized in table 4.6.

Table 4.6: Options associated with the cloud field statistical routine with the default value, possible values, a short description and the unit of the given value.

NAMCLOUDFIELD				
lcloudfield	.false.	.false./.true.	Switch for cloud field calculations	-
laddinfo	.false.	.false./.true.	Switch to enable writing of $q_l$ and $w$	-
			values	
dtav	dtav_glob	any positive real	Time interval for sampling of statistics	$\mathbf{s}$

#### modcrosssection

This statistical routine dumps instantaneous cross sections of the field. For every variable  $(u, v, w, \theta_l, \theta_v, q_t, q_l)$ , a new file is created for the horizontal and for the vertical crosssection. The available options are given in table 4.7.

Table 4.7: Options associated with the crosssection routine with the default value, possible values, a short description and the unit of the given value.

		*		
NAMCROSSSECTION				
lcross	.false.	.false./.true.	Switch for dumping of crosssections of	-
			the field	
dtav	dtav_glob	any positive real	Time interval for sampling of statistics	$\mathbf{s}$
crossheight	2	1 - kmax, integer	Height of the horizontal crosssection	-
crossplane	2	1- xmax, integer	Location of the vertical (yz) plane on	-
			every processor	

### modfielddump

When this routine is enabled, at regular time intervals, a dump is made of the entire 3d-fields of u, v, w,  $\theta_l$ ,  $\theta_v$ ,  $q_t$ ,  $q_l$  in 2-byte integers. This module's options and the name of the namelist is given in table 4.8

NAMFIELDDUMP Switch for dumping of 3d-fields lfielddump .false. .false./.true. dtav dtav\_glob any positive real Time interval for sampling of statistics ldiracc .false. .false./.true. Switch to dump into direct access files instead of Fortran unformatted files klow 1 1 - khighLowest level of the 3d-field output kmaxklow - kmax Highest level of the 3d-field output khigh

Table 4.8: Options associated with the field dump routine with the default value, possible values, a short description and the unit of the given value.

#### modgenstat

This statistical routine calculates generic slabaveraged statistics, i.e. time averaged fields of the most used variables  $(T, \theta, q_t \text{ etc.})$ , time averaged tendencies of most of these variables, time average turbulent fluxes, variances and skewness of w and  $q_t$ . This output is divided over four files: field, flux1, flux2 and moments. Furthermore, if  $nsv \neq 0$ , for each scalar a field and a flux file is created. The options are the usual and can be found in table 4.9

Table 4.9: Options associated with the genstat routine with the default value, possible values, a short description and the unit of the given value.

-	,	-	g			
	NAMGENSTAT					
lstat	.false.	.false./.true.	Switch for calculating generic slabaver-	-		
			aged statistics			
dtav	dtav_glob	any positive real	Time interval for sampling of statistics	$\mathbf{S}$		
timeav	timeav_glob	integer multiple	Time interval for writing statistics	$\mathbf{S}$		
		of dtav				

### modradstat

This statistical routine calculates slabaveraged vertical profiles of variables concerning radiation, e.g. longwave radiation going up and going down and tendencies of  $\theta_l$  due to short- and longwave radiation. The file that is created to contain the output is radstat. The available options for this module are given in table 4.10.

### modsampling

With this module, conditionally sampled fields can be calculated. The conditions are imposed by switches. For each of these switches that is enabled, two files are created: a field file and a flux file. The names of the available options for this module is given in table 4.11.

Table 4.10: Options associated with the radstat routine with the default value, possible values, a short description and the unit of the given value.

	NAMRADSTAT			
lradstat	.false.	.false./.true.	Switch for calculating slabaveraged ra-	-
			diation statistics	
dtav	dtav_glob	any positive real	Time interval for sampling of statistics	s
timeav	$timeav\_glob$	integer multiple	Time interval for writing statistics	$\mathbf{s}$
		of dtav		

Table 4.11: Options associated with the sampling statistics routine with the default value, possible values, a short description and the unit of the given value.

	=	<u> </u>		
NAMSAMPLING				
dtav	dtav_glob	any positive real	Time interval for sampling of statistics	S
timeav	$timeav\_glob$	integer multiple	Time interval for writing statistics	$\mathbf{S}$
		of dtav		
lsampcl	.false.	.false./.true.	Switch for conditional sampling cloud	-
			$(q_l > 0)$	
lsampco	.false.	.false./.true.	Switch for conditional sampling cloud	-
			core $(q_l > 0, \theta'_v > 0)$	
lsampup	.false.	.false./.true.	Switch for conditional sampling up-	-
			drafts $(w > 0)$	
lsampbuup	.false.	.false./.true.	Switch for conditional sampling of	-
			buoyant updrafts $(w > 0, \theta'_v > 0)$	

### modstattend

The modstattend calculates tendencies of various prognostic variables. It generates five different files: utend, vtend, wtend, tltend and qttend. The options are the usual and can be found in table 4.12

Table 4.12: Options associated with the sampling statistics routine with the default value, possible values, a short description and the unit of the given value.

NAMSTATTEND						
lstattend	.false.	.false./.true.	Switch for calculation of tendencies of			
			prognostic variables			
dtav	dtav_glob	any positive real	Time interval for sampling of statistics	$\mathbf{s}$		
timeav	timeav_glob	integer multiple	Time interval for writing statistics	$\mathbf{s}$		
		of dtav				

### modtimestat

This module calculates timeseries of several variables, among others: cloud cover, cloud bottom and top, inversion height and mean liquid water path. These timeseries can be found in the output file tmser1. The module also calculates several surface variables, like surface temperature and surface fluxes. These timeseries are found in a second file: tmsurf. Several methods are present in the code to calculate the inversion height  $z_i$ , which can be selected by means of options. For all options, see table 4.13.

Table 4.13: Options associated with the time series statistics routine with the default value, possible values, a short description and the unit of the given value.

NAMTIMESTAT						
ltimestat	.false.	.false./.true.	Switch for calculation of time series	-		
dtav	dtav_glob	any positive real	Time interval for sampling of statistics	s		
timeav	timeav_glob	integer multiple of dtav	Time interval for writing statistics	S		
iblh_var	iblh_thv	iblh_thv iblh_thl iblh_qt	Flag for the variable used to calculate boundary layer height iblh_thv = virtual pot. temp. $\theta_v$ iblh_thl = liquid water pot. temp. $\theta_l$ iblh_qt = total humidity $q_t$	-		
iblh_meth	iblh_grad	iblh_flux iblh_grad iblh_thres	Flag for the method used to calculate boundary layer height iblh_flux = use flux of selected variable iblh_grad = use gradient of selected variable iblh_thres = use a threshold (auto or user specified)	-		
blh_thres	automatic	any positive real	Threshold for the selected variable, used only for iblh_thres method	K  or kg $kg^{-1}$		
blh_nsamp	32	any positive integer	Number of levels to integrate over	-		

## Chapter 5

# Model Theory

### 5.1 Governing Equations

After replacement of the conventional temperature in the Navier-Stokes equation with the virtual potential temperature  $\theta_v$ , the Boussinesq approximation can be assumed within the ABL. This results (after application of the LES filter) in:

$$\frac{\partial \widetilde{u}_i}{\partial x_i} = 0, (5.1)$$

$$\frac{\partial \widetilde{u}_i}{\partial t} = -\frac{\partial \widetilde{u}_i \widetilde{u}_j}{\partial x_j} - \frac{\partial \pi}{\partial x_i} + \frac{g}{\theta_0} (\widetilde{\theta}_v - \theta_0) \delta_{i3}$$

$$-2\epsilon_{ijk}\Omega_{j}\widetilde{u_{k}} + F_{i} - \frac{\partial \tau_{ij}}{\partial x_{i}},\tag{5.2}$$

$$\frac{\partial \widetilde{\theta}_l}{\partial t} = -\frac{\partial \widetilde{u}_j \widetilde{\theta}_l}{\partial x_j} + S_{\theta_l} - \frac{\partial R_{u_j, \theta_l}}{\partial x_j}, \tag{5.3}$$

$$\frac{\partial \widetilde{q}_t}{\partial t} = -\frac{\partial \widetilde{u}_j \widetilde{q}_t}{\partial x_j} + S_{q_t} - \frac{\partial R_{u_j, q_t}}{\partial x_j}, \tag{5.4}$$

as basic equations, where the tildes denotes the filtered mean variables. The  $\hat{z}$  direction is taken to be vertical.  $\theta_0$  is the reference state potential temperature and  $\vec{\Omega}$  is the earth's angular velocity. Viscous transport terms are neglected.  $F_i$  represents large scale forcings. With  $\varphi$  one of the scalars, the large scale source terms are  $S_{\varphi}$  and the residuals are denoted by  $R_{u_j,\varphi} = \widetilde{u_j\varphi} - \widetilde{u_j}\widetilde{\varphi}$ . The anisotropic subfilter-stress tensor is defined by

$$\tau_{ij} \equiv \widetilde{u_i u_j} - \widetilde{u}_i \widetilde{u}_j - \frac{2}{3} \delta_{ij} \widetilde{e}, \tag{5.5}$$

where  $\tilde{e} = \frac{1}{2}(\widetilde{u_iu_i} - \widetilde{u_i}\widetilde{u_i})$  is the filtered subfilter-scale turbulent kinetic energy (SFS-TKE). The isotropic part of the subfilter-scale flux is included in the modified pressure

$$\pi = \frac{1}{\rho_0} (\tilde{p} - p_0) + \frac{2}{3} e, \tag{5.6}$$

which is determined by solving a Poisson equation for  $\pi$ 

$$\nabla^{2}\pi = \nabla \left( -\frac{\partial \widetilde{u}_{i}\widetilde{u}_{j}}{\partial x_{j}} + \frac{g}{\theta_{0}} (\widetilde{\theta}_{v} - \theta_{0}) \delta_{i3} -2\epsilon_{ijk} \Omega_{j}\widetilde{u}_{k} + F_{i} - \frac{\partial \tau_{ij}}{\partial x_{j}} \right).$$

$$(5.7)$$

Since computations are performed in a double periodic domain, the Poisson equation is solved with a Fast Fourier transform in the homogenous directions, while for the  $\hat{z}$  direction a tridiagonal system is solved.

### 5.2 Subfilter-Scale Model

The subfilter-scale stresses and residuals are modeled using one-and-a-half order closure (Schmidt and Schumann, 1989). The stress tensor and the subfilter-scale fluxes are modeled by:

$$\tau_{ij} = -K_m \left( \frac{\partial \widetilde{u}_i}{\partial x_j} + \frac{\partial \widetilde{u}_j}{\partial x_i} \right), \tag{5.8}$$

$$R_{u_j,\varphi} = -K_h \frac{\partial \widetilde{\varphi}}{\partial x_j},\tag{5.9}$$

with the eddy diffusivity coefficients  $K_m$  and  $K_h$  a function of  $\tilde{e}$ . The prognostic equation for e:

$$\frac{\partial \widetilde{e}}{\partial t} = -\widetilde{u}_j \frac{\partial \widetilde{e}}{\partial x_j} - R_{u_i, u_j} \frac{\partial \widetilde{u}_i}{\partial x_j} + \frac{g}{\theta_0} R_{w, \theta_v} - \frac{\partial R_{u_j, e}}{\partial x_j} - \frac{1}{\rho_0} \frac{\partial R_{u_j, p}}{\partial x_j} - \varepsilon, \tag{5.10}$$

with  $\varepsilon$  the dissipation. To close Equation 5.10, we need to parameterize all right hand side terms except the first one. The SFS-TKE production by shear (the second term) is closed with Equation 5.8. Following Deardorff (1980), we use for the third term, the production due to buoyancy:

$$\frac{g}{\theta_0} R_{w,\theta_v} = \frac{g}{\theta_0} \left( A R_{w,\theta_l} + B R_{w,q_t} \right), \tag{5.11}$$

with coefficients A and B depending on the local thermodynamic state:

$$\begin{cases}
A = 1 & B = \left(1 - \frac{R_v}{R_d}\right)\theta_0 & \text{for } \widetilde{q}_t < \widetilde{q}_s \\
A = \frac{1 + \frac{R_v}{R_d}\left(\theta_0 \frac{d\widetilde{q}_s}{dT}\right)}{1 + \frac{L}{c_{vd}} \frac{d\widetilde{q}_s}{dT}} & B = \frac{L}{c_{pd}}A - \theta_0 & \text{for } \widetilde{q}_t > \widetilde{q}_s
\end{cases}$$
(5.12)

The fourth and fifth term in Equation 5.10 are together parameterized as:

$$-\frac{\partial}{\partial x_j} \left( R_{u_j,e} + \frac{1}{\rho_0} R_{u_j,p} \right) = 2K_m \frac{\partial \tilde{e}}{\partial x_j}, \tag{5.13}$$

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Under the assumption of 3D homogenous isotropic turbulence, the dissipation rate  $\varepsilon$  can be found by integration of the energy spectrum  $E(k) = \alpha \varepsilon^{2/3} k^{-5/3}$  from a filter wavenumber  $k_f$ , that lies within the inertial subrange, to infinity

$$\varepsilon = \tilde{e}^{3/2} k_f \left(\frac{3}{2}\alpha\right)^{-3/2} = \frac{c_{\varepsilon}}{\lambda} \tilde{e}^{3/2}, \quad \text{with} \quad c_{\varepsilon} = \frac{2\pi}{c_f} \left(\frac{3}{2}\alpha\right)^{-3/2}$$
(5.14)

with  $\alpha=1.5$  the Kolmogorov constant and  $\lambda$  the dominant length-scale of the unresolved flow:  $\lambda=\frac{2\pi}{c_fk_f}$ , where  $c_f$  is chosen to be 2.5 (see Cuijpers 1990). In unstable flow,  $\lambda$  can be taken equal to grid size  $\Delta=(\Delta x\Delta y\Delta z)^{1/3}$ , but this no longer holds for stable flow, where  $\frac{\partial \tilde{\theta_v}}{\partial z}>0$ . In that case, the length scale is taken to be

$$\lambda = \min\left(\Delta, c_N \frac{\tilde{e}^{1/2}}{N}\right),\tag{5.15}$$

with  $N^2 = \frac{g}{\theta_0} \frac{\partial \theta_v}{\partial z}$  the Brunt-Väisälä frequency.

The eddy diffusivity can be found by equating the dissipation  $\varepsilon$  to the production of SFS-TKE:

$$\mathcal{P} = 2K_m \int_0^{k_f} k^2 E(k) dk \tag{5.16}$$

$$= \frac{3}{2} K_m \alpha \varepsilon^{2/3} k_f^{4/3}, \tag{5.17}$$

which yields:

$$K_m = \frac{\tilde{e}^{1/2}}{k_f(\frac{3}{2}\alpha)^{3/2}} = c_m \lambda \tilde{e}^{1/2} \quad \text{with} \quad c_m = \frac{c_f}{2\pi} \left(\frac{3}{2}\alpha\right)^{-3/2}$$
 (5.18)

Similarly,  $K_h = c_h \lambda \tilde{e}^{1/2}$ . Like for  $\lambda$ , a stability correction is also applied on  $c_h$  and  $c_{\varepsilon}$ 

$$c_h = \left(c_{h,1} + c_{h,2} \frac{\lambda}{\Delta}\right) c_m,\tag{5.19}$$

$$c_{\varepsilon} = c_{\varepsilon,1} + c_{\varepsilon,2} \frac{\lambda}{\Delta}. \tag{5.20}$$

Now all parameters of the subfilter-scale parameterization of DALES are defined; they are summarized in Equation 5.2.

Filling the closure relations and parameters into Equation 5.10, we get:

$$\frac{\partial \widetilde{e}^{1/2}}{\partial t} = -\widetilde{u}_{j} \frac{\partial \widetilde{e}^{1/2}}{\partial x_{j}} + \frac{1}{2\widetilde{e}^{1/2}} \left[ K_{m} \left( \frac{\partial u_{j}}{\partial x_{i}} + \frac{\partial u_{i}}{\partial x_{j}} \right) \frac{\partial u_{i}}{\partial x_{j}} \right. \\
+ \left. - K_{h} \frac{g}{\theta_{0}} \frac{\partial A\widetilde{\theta}_{l} + Bq_{t}}{\partial z} \right] + \frac{\partial}{\partial x_{j}} \left( 2K_{m} \frac{\partial \widetilde{e}^{1/2}}{\partial x_{j}} \right) - \frac{c_{\varepsilon}\widetilde{e}}{2\lambda}, \tag{5.21}$$

which closes the system.

$\alpha$	$c_f$	$c_{\varepsilon,1}$	$c_{\varepsilon,2}$	$c_m$	$c_{h,1}$	$c_{h,2}$	$c_N$
1.5	2.5	0.19	0.51	0.12	1	2	0.76

Table 5.1: An overview of the parameters used in the SFS-scheme of DALES model. Not all are independent.

### 5.3 Discretization and Numerical Scheme

A rectangular grid is used, with optional grid stretching in the  $\hat{z}$  direction. For clarity, an equidistant grid is assumed in the discussion of the advection scheme. The grid is staggered in space; if the center of a grid cell of the pressure, the SFS-TKE or the scalars is located at  $\vec{x} + \frac{1}{2}(\Delta x, \Delta y, \Delta z)$ , the  $\tilde{u}$ -grid is centered at  $\vec{x} + \frac{1}{2}(0, \Delta y, \Delta z)$ , and similar for  $\tilde{v}$  and  $\tilde{w}$ .

Time integration is done by a third order Runge-Kutta scheme following Wicker and Skamarock (2002). With  $f^n(\phi^n)$  the right-hand side of the appropriate equation of 5.2-5.4 for variable  $\phi = \{\widetilde{u}, \widetilde{v}, \widetilde{w}, \widetilde{\theta_l}, \widetilde{q_t}\}, \phi^{n+1}$  at  $t + \Delta t$  is calculated in three steps:

$$\phi^* = \phi^n + \frac{\Delta t}{3} f^n(\phi^n)$$

$$\phi^{**} = \phi^* + \frac{\Delta t}{2} f^*(\phi^*)$$

$$\phi^{n+1} = \phi^{**} + \Delta t f^{**}(\phi^{**}),$$
(5.22)

with the asterisks denoting intermediate time steps.

Depending on the desired properties (like high accuracy or monotonicity), several advection schemes are available. With advection in the  $\hat{x}$  direction discretized as

$$\frac{\partial \widetilde{u}_i \phi_i}{\partial x} = \frac{F_{i+\frac{1}{2}} - F_{i-\frac{1}{2}}}{\Delta x},\tag{5.23}$$

with  $F_{i-\frac{1}{2}}$  is the convective flux of variable  $\phi$  through the  $i-\frac{1}{2}$  plane. Since we are using a staggered grid the velocity is available at  $i-\frac{1}{2}$  without interpolation. Second order central differencing can be used for variables where neither very high accuracy or strict monotonicity is necessary:

$$F_{i-\frac{1}{2}}^{2nd} = \widetilde{u}_{i-\frac{1}{2}} \frac{\phi_i + \phi_{i-1}}{2}, \tag{5.24}$$

Higher order accuracy is reached with a sixth order central differencing scheme (see Wicker and Skamarock, 2002):

$$F_{i-\frac{1}{2}}^{6th} = \frac{\widetilde{u}_{i-\frac{1}{2}}}{60} \left[ 37(\phi_i + \phi_{i-1}) - 8(\phi_{i+1} + \phi_{i-2}) + (\phi_{i+2} + \phi_{i-3}) \right]. \tag{5.25}$$

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By adding a small dissipative term to  $F_{i-\frac{1}{2}}^{6th}$ , a fifth order scheme is created that is nearly monotone:

$$F_{i-\frac{1}{2}}^{5th} = F_{i-\frac{1}{2}}^{6th} - \left| \frac{\widetilde{u}_{i-\frac{1}{2}}}{60} \right| [10(\phi_i + \phi_{i-1}) - 5(\phi_{i+1} + \phi_{i-2}) + (\phi_{i+2} + \phi_{i-3})].$$
(5.26)

For advection of scalars that need to be strictly monotone (for example chemically reacting scalars) the  $\kappa$  scheme Hundsdorfer et al. (1995) is implemented:

$$F_{i-\frac{1}{2}}^{\kappa} = \widetilde{u}_{i-\frac{1}{2}} \left[ \phi_{i-1} + \frac{1}{2} \kappa_{i-\frac{1}{2}} \left( \phi_{i-1} - \phi_{i-2} \right) \right], \tag{5.27}$$

in case  $\tilde{u} > 0$ .  $\kappa_{i-1/2}$  serves as a switch between higher order advection and first order upwind in case of strong upwind gradients of  $\phi$ . This makes the scheme monotone, but also rather dissipative.

### 5.4 Condensation Scheme

To calculate the liquid water content  $\tilde{q}_l$  from pressure, temperature and total water content, a condensation scheme has to be included. In the model, it is assumed that there is no liquid water present in a unsaturated grid box, while all moisture above saturation value  $\tilde{q}_s$  is liquid water. To calculate  $\tilde{q}_s$  following Sommeria and Deardorff (1977), first we need to know the liquid water temperature  $\tilde{T}_l$ :

$$\widetilde{T}_l = \left(\frac{p_{ref}}{p_0}\right)^{c_p/R_d} \widetilde{\theta}_l, \tag{5.28}$$

with

$$p_{ref}(z) = p_0 \left( \frac{T_{ref}(0) - (g/c_p)z}{T_{ref}(0)} \right)^{c_p/R_d}.$$
 (5.29)

The saturation vapor pressure  $e_s$  is an empirical function of  $\widetilde{T}_l$ :

$$e_s(\widetilde{T}_l) = e_{s0} \exp\left[a\frac{\widetilde{T}_l - T_{trip}}{\widetilde{T}_l - b}\right],\tag{5.30}$$

with constants  $e_{s0} = 610.78 \,\mathrm{Pa}$ ,  $T_{trip} = 273.16 \,\mathrm{K}$ , a = 17.27 and b = 35.86. For ideal gases, the specific humidity and vapor pressure are related by:

$$q_{sl} = \frac{R_d}{R_v} \frac{e_s}{p_{ref} - (1 - \frac{R_d}{R_v})e_s}.$$
 (5.31)

Using the Clausius-Clapeyron relation:

$$\frac{\mathrm{d}e_s}{\mathrm{d}T} = \frac{Le_s}{R_s T^2},\tag{5.32}$$

with  $R_v = 461.53 \,\mathrm{J\ kg^{-1}\ K^{-1}}$  the gas constant for water vapor, a truncated Taylor expansion now gives a relation for the saturated specific humidity:

$$q_{s} = q_{sl} \left( 1 + \frac{L^{2}}{R_{v} c_{p,d} \tilde{T}_{l}^{2}} q_{t} \right) \left( 1 + \frac{L^{2}}{R_{v} c_{p,d} \tilde{T}_{l}^{2}} q_{sl} \right), \tag{5.33}$$

and finally we obtain for the liquid water content.

$$q_l = \begin{cases} q_t - q_s & \text{if } q_t > q_s \\ 0 & \text{otherwise.} \end{cases}$$
 (5.34)

## 5.5 Boundary Conditions

The computational domain has periodic boundary conditions in the horizontal directions. At the top of the domain, we take:

$$\frac{\partial \widetilde{u}}{\partial z} = \frac{\partial \widetilde{v}}{\partial z} = 0; \qquad \widetilde{w} = 0; \qquad \frac{\partial \widetilde{\theta}_l}{\partial z} = \text{constant}; \qquad \frac{\partial \widetilde{q}_t}{\partial z} = \text{constant}.$$
 (5.35)

Horizontal fluctuations at the top of the domain (e.g. gravity waves) are damped out by a sponge layer through an additional forcing/source term:

$$\frac{1}{\tau_r} \left( \overline{\phi}(z) - \phi \right) \tag{5.36}$$

with  $\overline{\phi}$  the slab averaged value and  $\tau_r$  a relaxation time scale that goes from 1 at the top of the domain to infinity at the bottom of the sponge layer.

#### Surface Model

In order to calculate the subgrid fluxes (Equation 5.9), the vertical gradients of the variables have to be determined. In the mixed layer, the profiles of variables are assumed to be linear, so that they can be simply approximated by finite difference, for instance  $\frac{\partial < u>}{\partial z} = \frac{\Delta < u>}{\Delta z}$ . This is not applicable in the surface layer, where the profiles are characterized by large gradients.

In the surface layer, therefore, the Monin-Obukhov similarity theory is used.

### Monin-Obukhov similarity theory

By defining the horizontal wind speed  $V = \sqrt{\langle u \rangle^2 + \langle v \rangle^2}$ , the general expression for the wind shear in neutral conditions is:

$$\frac{\partial V}{\partial z} = \frac{u_*}{kz} \tag{5.37}$$

where k is the von Karman constant (k = 0.4) and  $u_*$  the friction velocity. Integrating equation 5.37 leads to the logarithmic wind profile

$$V(z) = \frac{u_*}{k} ln \frac{z}{z_0}. ag{5.38}$$

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The Monin-Obukhov similarity theory assumes that the wind shear is scaled by the dimensionless height

$$\zeta \equiv z/L \tag{5.39}$$

where  $L = \frac{-\theta_0 u_*^3}{qw'\theta'}$  is the Monin-Obukhov length.

Expression 5.37 can be generalized for non-neutral stability conditions by introducing a dimensionless wind shear defined as follows:

$$\Phi_m(\zeta) = \frac{kz}{u_*} \frac{\partial V}{\partial z} \tag{5.40}$$

which leads to a general form for the wind shear:

$$\frac{\partial V}{\partial z} = \frac{u_*}{kz} - \frac{1 - \Phi_m}{kz} u_* \tag{5.41}$$

Integrating equation 5.41 between  $z_0$  (height at which  $V(z_0) = 0$ ) and a generic height z, leads to:

$$V(z) = \frac{u_*}{k} \{ \ln \frac{z}{z_0} - \Psi_m(\frac{z}{L}) \}$$
 (5.42)

where

$$\Psi_m(\frac{z}{L}) = \int_0^{z/L} \frac{1 - \Phi_m(\zeta)}{\zeta} d\zeta \tag{5.43}$$

represents the correction to the logarithmic profile due to non-neutral conditions ( $\Psi_m = 0$  in neutral conditions).

Expressions fo  $\Phi_m(\zeta)$  based on field campaigns (Businger et al., 1971; Dyer, 1974; Hogstrom, 1988) are commonly used.

Similarly to momentum, the similarity theory is used to calculate the profiles of the other variables, namely  $<\theta>$  and <q>. By rewriting the expressions for the subgrid fluxes:

$$\langle \theta'' w'' \rangle = -K_h \frac{\partial \langle \theta \rangle}{\partial z} = -u_* \theta_*$$

$$\langle q'' w'' \rangle = -K_q \frac{\partial \langle q \rangle}{\partial z} = -u_* q_*$$
(5.44)

and assuming (Pielke, 1984)  $K_h = K_q$  we obtain an expression similar to (5.40):

$$\Phi_h = \frac{kz}{\theta_*} \frac{\partial \langle \theta \rangle}{\partial z} = \frac{kz}{q_*} \frac{\partial \langle q \rangle}{\partial z},\tag{5.45}$$

which integrated leads to:

$$<\theta(z)> = <\theta(z_0)> +\frac{\theta_*}{k}\{\ln\frac{z}{z_0} - \Psi_h(\frac{z}{L}) + \Psi_h(\frac{z_0}{L})\}$$
 (5.46)

$$\langle q(z) \rangle = \langle q(z_0) \rangle + \frac{q_*}{k} \{ \ln \frac{z}{z_0} - \Psi_h(\frac{z}{L}) + \Psi_h(\frac{z_0}{L}) \}$$
 (5.47)

where

$$\Psi_h(\frac{z}{L}) = \int_0^{z/L} \frac{1 - \Phi_h(\zeta)}{\zeta} d\zeta \tag{5.48}$$

### Surface Layer relationships

The stability functions are parameterized following (Businger et al., 1971; Dyer, 1974; Hogstrom, 1988) as follows:

$$\Phi_{m} = \begin{cases}
(1 - 16\zeta)^{-1/4} & \zeta < 0 \\
1 + 5\zeta & \zeta > 0
\end{cases}$$

$$\Phi_{h} = \begin{cases}
(1 - 16\zeta)^{-1/2} & \zeta < 0 \\
1 + 5\zeta & \zeta > 0
\end{cases}$$

$$\Psi_{m}(\frac{z}{L}) = \begin{cases}
2\ln\left(\frac{1 + \Phi_{m}^{-1}}{2}\right) + \ln\left(\frac{1 + \Phi_{m}^{-2}}{2}\right) - 2\tan^{-1}(\Phi_{m}^{-1}) + \frac{\pi}{2} & \zeta < 0 \\
-5\zeta & \zeta > 0
\end{cases}$$

$$\Psi_{h}(\frac{z}{L}) = \begin{cases}
2\ln\left(\frac{1 + \Phi_{h}^{-1}}{2}\right) & \zeta < 0 \\
-5\zeta & \zeta > 0
\end{cases}$$

The friction velocity is calculated from equation 5.42:

$$u_* = kV \left( \ln \frac{z}{z_0} - \Psi_m(\frac{z}{L}) \right), \tag{5.49}$$

whereas  $\theta_*$  and  $q_*$  are calculated from the known values of the surface fluxes:

$$\theta_* = -\frac{\langle w''\theta' \rangle_0}{u_*} \tag{5.50}$$

(5.51)

$$q_* = -\frac{\langle w''q'' \rangle_0}{u_*} \tag{5.52}$$

(5.53)

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The temperature and humidity surface values are calculated according to equations 5.46 and 5.47

$$<\theta(z_0)> = <\theta(z)> -\frac{\theta_*}{k}\{\ln\frac{z}{z_0} - \Psi_h(\frac{z}{L}) + \Psi_h(\frac{z_0}{L})\}$$
 (5.54)

$$\langle q(z_0) \rangle = \langle q(z) \rangle - \frac{q_*}{k} \{ \ln \frac{z}{z_0} - \Psi_h(\frac{z}{L}) + \Psi_h(\frac{z_0}{L}) \}$$
 (5.55)

using the values of temperature and moisture at the first computational level (z = 1). Finally, the vertical gradients are calculated from equations 5.40 and 5.45 according to:

$$\frac{\partial V}{\partial z} = \Phi_m(\zeta) \frac{u_*}{kz} \tag{5.56}$$

$$\frac{\partial \langle \theta \rangle}{\partial z} = \Phi_h(\zeta) \frac{\theta_*}{kz} \tag{5.57}$$

$$\frac{\partial \langle q \rangle}{\partial z} = \Phi_h(\zeta) \frac{q_*}{kz} \tag{5.58}$$

In the limit of free convection  $(u_* = 0)$  the following relationships are used to calculate the temperature and moisture profiles (Garrat):

$$\frac{\partial <\theta>}{\partial z} = -0.7 < w''\theta'' >_0^{2/3} \left(\frac{g}{\theta_0}\right) z^{-4/3} \tag{5.59}$$

$$\frac{\partial \langle q \rangle}{\partial z} = -0.7 < w'' q'' >_0^{2/3} \left(\frac{g}{\theta_0}\right) z^{-4/3} \tag{5.60}$$

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# Appendix A: The Poisson Solver

In this appendix the Poisson solver is described. As explained in Section 2.4.1, this subroutine needed to be modified in order to use a non-equidistant numerical grid.

### Introduction

The filtered Navier-Stokes equations can be written in the general form as (equation 5.2):

$$\frac{\partial u_i}{\partial t} = -\frac{\partial u_i u_j}{\partial x_j} + g \frac{\theta_l}{\theta_0} \delta_{i3} - 2\epsilon_{ijk} \Omega_j u_k - \frac{\partial \tau_{ij}}{\partial x_j} - \frac{\partial \pi}{\partial x_j}, \tag{5.61}$$

where the angular brackets <> (representing the filter operator) are omitted for sake of clarity.

As explained before, the modified pressure reads

$$\pi = \frac{p}{\rho_0} + 2/3e. \tag{5.62}$$

Equations (5.61) can be split in two contributions according to:

$$\frac{\partial u_i}{\partial t} = -\frac{\partial p}{\partial x_i} + Rem. \tag{5.63}$$

where Rem accounts for all the remaining terms in the r.h.s. of Equation (5.61) (advection, buoyancy, rotation and subgrid stress) except for the pressure gradient. By introducing a fictitious velocity  $u^*$ , Equation (5.63) is decomposed as follows:

$$\begin{cases}
\frac{\partial u^*}{\partial t} = Rem \\
\frac{\partial u}{\partial t} - \frac{\partial u^*}{\partial t} = -\frac{\partial p}{\partial x_i}
\end{cases}$$
(5.64)

Applying the divergence operator to the second equation of the system (5.64) we obtain:

$$\nabla \left( \frac{\partial u}{\partial t} - \frac{\partial u^*}{\partial t} \right) = -\nabla^2 p, \tag{5.65}$$

which becomes, using the continuity equation,

$$\nabla \left(\frac{\partial u^*}{\partial t}\right) = f(u, x, y, z, t) = \nabla^2 p, \tag{5.66}$$

that is a form of the Poisson's equation. Note that  $\nabla u^* \neq 0$  because the fictitious velocity represents all the remaining terms of the Navier-Stokes equation, whose divergence is not necessarily zero.

Assuming that the *Rem* term is known (Equation 5.64), we first calculate the pressure by solving the Poisson's equation (5.66). Once the pressure is known, we can finally solve for  $\frac{\partial u}{\partial t}$  in equation (5.64).

### Time discretization

The discretized form of the l.h.s. of equation (5.63) reads (leap-frog method):

$$\frac{u_i^{n+1} - u_i^{n-1}}{2\Delta t} = -\frac{\partial p}{\partial x_i} + Rem,\tag{5.67}$$

Similarly as above, a fictitious velocity  $u^*$  can be introduced and the equation (5.67) can be split into:

$$\begin{cases}
\frac{u_i^* - u_i^{n-1}}{2\Delta t} = Rem \\
\frac{u_i^{n+1} - u_i^*}{2\Delta t} = -\frac{\partial p}{\partial x_i},
\end{cases} (5.68)$$

which is the equivalent of the system (5.64).

By applying the divergence operator to (5.68) and making use of the continuity equation, we obtain

$$\nabla \left( \frac{u_i^*}{2\Delta t} \right) = \nabla^2 p, \tag{5.69}$$

which is the equation we need to solve, namely the discretized form of the Poisson's equation (5.66).

# Spatial discretization

By defining the quantity

$$u_i^{**} \equiv \frac{u_i^*}{2\Delta t},\tag{5.70}$$

the discretized form of the Poisson's equation (5.69) reads

$$\nabla \left(u_i^{**}\right) = \nabla^2 p. \tag{5.71}$$

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Figure ... shows the numerical grid used in the code, in the vertical direction. The scalar quantities (temperature, humidity, scalar and pressure) are defined in the center of the cell, whereas the wind velocities are defined at the edges, so that p(k) is not at the same level then w(k).

Moreover, referring to Figure ..., it can be noticed that, if a non-equidistant grid is used in the vertical direction, the distance between two adjacent centers  $(\Delta z_h)$  does not coincide with the distance between two edges  $(\Delta z_f)$ .

In discretizing equation (5.71), we have to compute the velocity gradient (l.h.s.) and the pressure Laplacian (r.h.s) at the same level, namely at the center of the cell. Therefore, the l.h.s. can be written in the discrete (centered) form as

$$\nabla u_i^{**} = \frac{u_{i+1}^{**} - u_i^{**}}{\Delta x} + \frac{v_{j+1}^{**} - v_j^{**}}{\Delta y} + \frac{w_{k+1}^{**} - w_k^{**}}{\Delta z_f(k)},\tag{5.72}$$

whereas the pressure Laplacian (at the same level) is

$$\nabla^{2} p = \frac{\partial}{\partial x_{j}} \left( \frac{\partial p}{\partial x_{i}} \right) = \frac{1}{\Delta x} \left[ \left( \frac{\partial p}{\partial x} \right)_{i + \frac{1}{2}} - \left( \frac{\partial p}{\partial x} \right)_{i - \frac{1}{2}} \right] + \frac{1}{\Delta y} \left[ \left( \frac{\partial p}{\partial y} \right)_{j + \frac{1}{2}} - \left( \frac{\partial p}{\partial y} \right)_{j - \frac{1}{2}} \right] + \frac{1}{\Delta z_{f}(k)} \left[ \left( \frac{\partial p}{\partial z} \right)_{k + \frac{1}{2}} - \left( \frac{\partial p}{\partial z} \right)_{k - \frac{1}{2}} \right].$$
 (5.73)

and pressure gradients at the cell's edge (point  $i \pm 1/2$ ) are defined as

$$\begin{cases}
\frac{\partial p}{\partial x}|_{i+\frac{1}{2}} = \frac{p_{i+1} - p_i}{\Delta x} \\
\frac{\partial p}{\partial x}|_{i-\frac{1}{2}} = \frac{p_{i} - p_{i-1}}{\Delta x}.
\end{cases} (5.74)$$

A similar formula holds for the y component.

The vertical pressure gradient reads:

$$\begin{cases}
\frac{\partial p}{\partial z}|_{k+\frac{1}{2}} = \frac{p_{k+1} - p_k}{\Delta z_h(k+1)} \\
\frac{\partial p}{\partial z}|_{k-\frac{1}{2}} = \frac{p_k - p_{k-1}}{\Delta z_h(k)}.
\end{cases} (5.75)$$

As a result, the discretized form of the Laplacian of the pressure reads

$$\nabla^{2} p = \frac{p_{i+1} - 2p_{i} + p_{i-1}}{(\Delta x)^{2}} + \frac{p_{j+1} - 2p_{j} + p_{j-1}}{(\Delta y)^{2}} + \frac{1}{\Delta z_{f}(k)} \left( \frac{p_{k+1} - p_{k}}{\Delta z_{h}(k+1)} - \frac{p_{k} - p_{k-1}}{\Delta z_{h}(k)} \right),$$
(5.76)

and the Poisson equation (5.71) becomes

$$\frac{u_{i+1}^{**} - u_{i}^{**}}{\Delta x} + \frac{v_{j+1}^{**} - v_{j}^{**}}{\Delta y} + \frac{w_{k+1}^{**} - w_{k}^{**}}{\Delta z_{f}(k)} =$$

$$= \frac{p_{i-1} - 2p_{i} + p_{i+1}}{(\Delta x)^{2}} + \frac{p_{j-1} - 2p_{j} + p_{j+1}}{(\Delta y)^{2}} + ap_{k-1} + bp_{k} + cp_{k+1},$$
(5.77)

where

$$a = \frac{1}{\Delta z_f(k)\Delta z_h(k)} \tag{5.78}$$

$$c = \frac{1}{\Delta z_f(k)\Delta z_h(k+1)} \tag{5.79}$$

$$b = -(a+c). (5.80)$$

### Poisson Solver in the LES code

In the code used in this study, the routine FILLPS.F first computes, from Equation (5.68), the sum

$$u_i^{**} = \frac{u_i^*}{2\Delta t} = \frac{u_i^{n-1}}{2\Delta t} + Rem, \tag{5.81}$$

and then solves for the divergence  $\nabla u_i^{**}$  (equation 5.72).

This is followed by the routine SOLMPJ.F that extracts the pressure p solving the Poisson's equation (5.77), given the value of  $\nabla u_i^{**}$  calculated by FILLPS.F, applying a FFT in the two periodic directions (x and y), and solving a tridiagonal matrix in the vertical direction. The routine TDERIVE.F computes the velocity tendency  $\frac{\partial u_i}{\partial t} \equiv u_p$ , from Equation (5.63), namely

$$\frac{\partial u_i}{\partial t} \equiv u_p = Rem - \frac{\partial p}{\partial x_i} = u_i^{**} - \frac{u_i^{n-1}}{2\Delta t} - \frac{p_i - p_{i-1}}{\Delta x} - \frac{p_j - p_{j-1}}{\Delta y} - \frac{p_k - p_{k-1}}{\Delta z_h(k)}, (5.82)$$

where equation (5.81) has been used, and the pressure gradient has been discretized at the same level of the velocity field. Since by definition

$$\frac{\partial u_i}{\partial t} = \frac{u_i^{n+1} - u_i^{n-1}}{2\Delta t},\tag{5.83}$$

the routine TSTEP.F can finally calculate the velocity at the time step n+1

$$u_i^{n+1} = u_p 2\Delta t + u_i^{n-1}. (5.84)$$