

# Transformation



A transformation  $f$   
maps any input of type  $A$   
to the output of type  $B$ .

# Composition



Transformations with compatible input and output can be composed.

# Composition is a Transformation



Crucially, composition of transformations is again a transformation.

# Composition Combinator



Composition `chain_of([], [])`  
is a transformation combinator  
with two arguments.

## Example: Composition



## Counter-example: Plural Component



We cannot compose these transformations because their input and output do not quite match.

## Counter-example: Optional Component



Even so, the input and the output share a common component, which suggests there should be a way to compose these transformations.

# Idea: Unbundle the Wire



Attaching a transformation to the object wire indicates that the transformation is applied to all element of the collection.



# Block Type

A block is a collection of homogeneous elements.



Cardinality is a constraint on the number of elements in a block.



# Unbundling



# Object Transformation



Any compatible transformation  
can be applied to the object wire,  
which indicates that the transformation  
is applied to every element of the block.

# Multiwired Transformations



## Example: Multiwired Transformations



# Example: Multiwired Composition



# Example: Multiwired Composition Details



# Challenge: Functor Transformation

So far we have seen different combinations of transformations and wires:  
transformations that are applied to the object wire, as well as  
transformations that consume or produce both functor and object wires.



What we miss is a notion of a transformation applied to the functor wire.



# Functor Transformation

Since a functor transformation does not act on the object wire, it cannot interfere with any transformations applied to the object wire.



How to define a functor transformation?



This property can be taken as a definition of a functor transformation.

# Definition: Functor Transformation



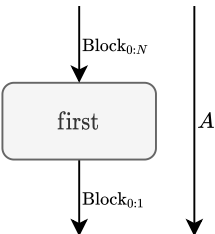
Such transformations are also called *natural*.

Branch of mathematics that studies natural transformations is called the *category theory*.

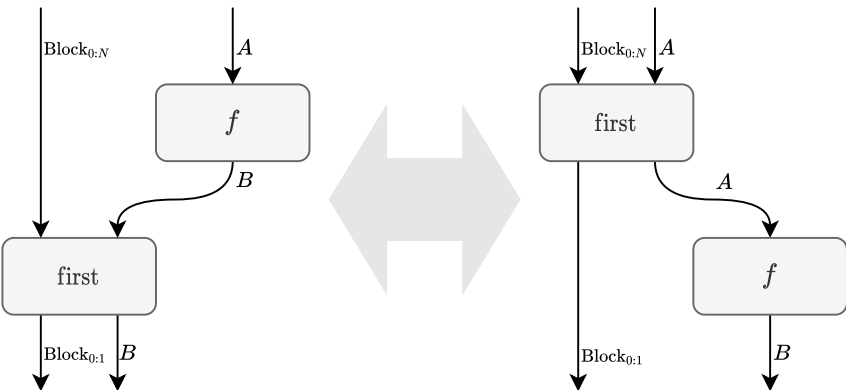
# Example: Functor Transformation



This is, in fact, a natural transformation.



Indeed, for any  $f : A \rightarrow B$ ,



$$\text{chain\_of}(\text{with\_elements}(f), \text{first}) \equiv \text{chain\_of}(\text{first}, \text{with\_elements}(f))$$