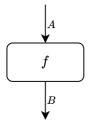
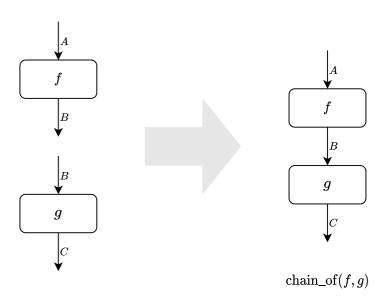
#### **Transformation**



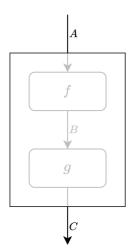
A transformation f maps any input of type A to the output of type B.

## Composition



Transformations with compatible input and output can be composed.

#### **Composition is a Transformation**



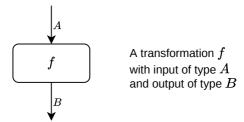
Crucially, composition of transformations is again a transformation.

#### **Composition Combinator**

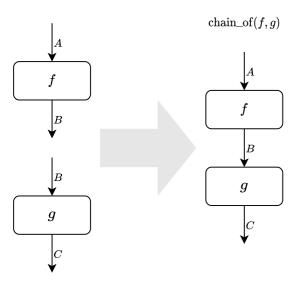


$$\label{eq:composition} \begin{split} & \text{Composition chain\_of}\big([]],[]]\big) \\ & \text{is a transformation combinator} \\ & \text{with two arguments.} \end{split}$$

#### 1. Transformation



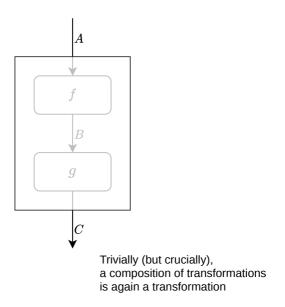
#### 2. Composition

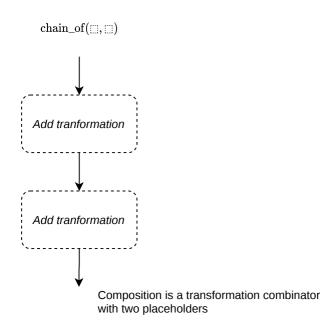


Transformations with compatible input and output can be composed

#### 3. Composition is a Transformation

#### **4. Composition Combinator**

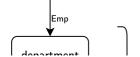


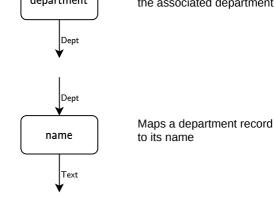


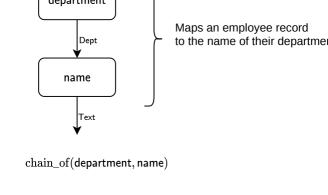
#### **5. Example: Components of a Composition**

#### **6. Example: Composition**

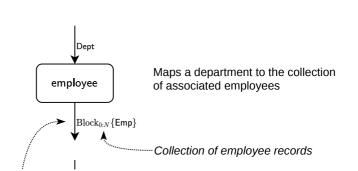




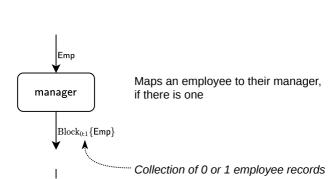




# 7. Counter-example: Plural Component

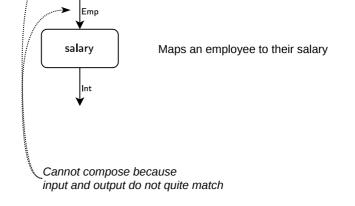


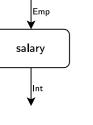
# 8. Counter-example: Optional



t

Component



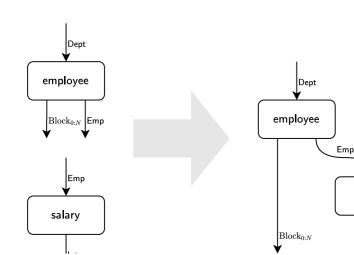


Can we represent composition of these transformations with an intuitive diagrammatic notation?

#### 9. Idea: Unbundle the Wire

# Separate the output wire into two components employee Emp Object wire Intuitively, it signals the number Transmits the output elements

#### **10.** Idea: Compose Using the



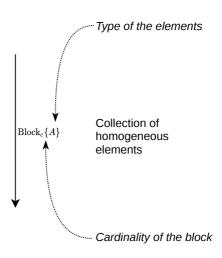
## **Object Wire**



Int

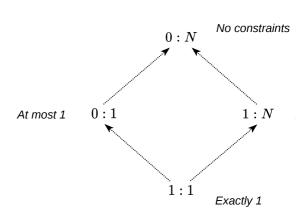
Attaching a transformation to the object wire indicates that the transformation is applied to each element of the collection

#### 11. Block Type



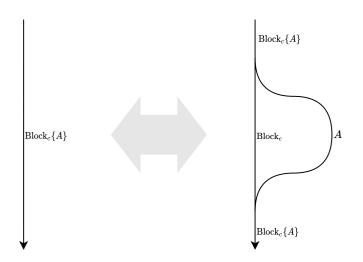
#### 12. Cardinality

Cardinality is a constraint on the number of elem



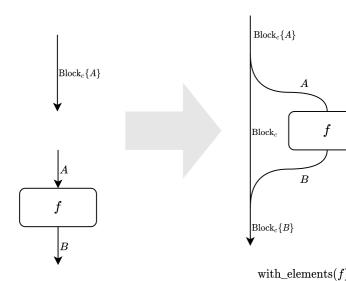


#### 13. Unbundling



We can unbundle a wire of a block type into a functor and object components

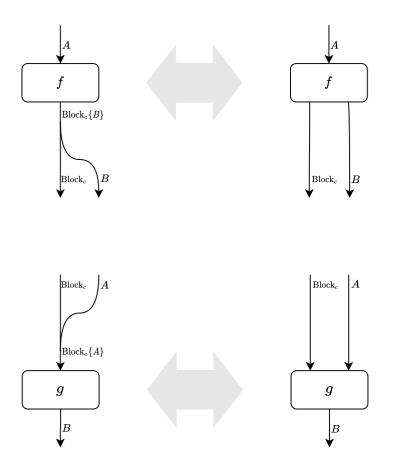
#### **14. Object Transformation**



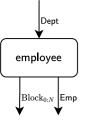
Then any compatible transformation can be applied to the object which indicates that the transformation is applied to every element of the block



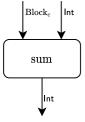
#### 13. Multiwired transformations



#### 14. Example: Multiwired Trans



Maps a department to the collection of associated employees



Produces the sum of a collection of integer

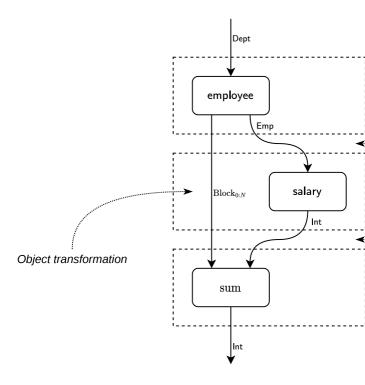
## sformations

...

#### 14. Example: Multiwired Composition

#### Dept Total sum of salaries in a given department employee $\operatorname{Block}_{0:N}$ Emp Dept employee Emp salary salary $Block_{0:N}$ Int sum $\mathrm{Block}_c$ $\operatorname{sum}$ chain\_of(employee, with\_elements(salary), sum) Int

#### 15. Example: Details



chain\_of(employee, with\_elements(salary),



sum)