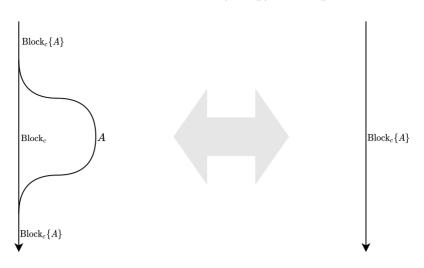
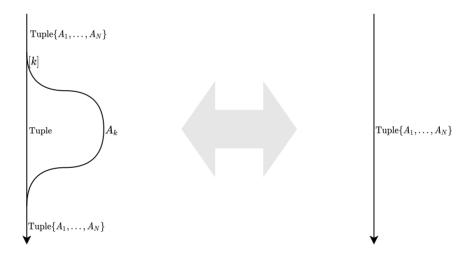
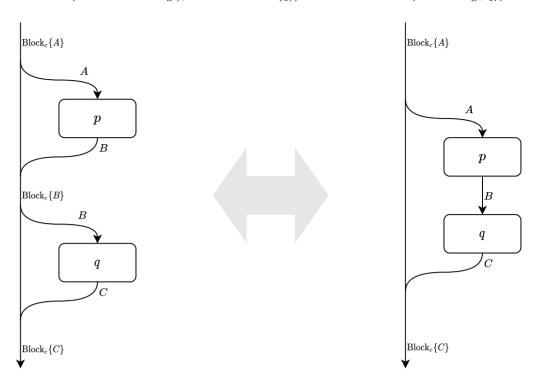
$with_elements(pass()) \Leftrightarrow pass()$



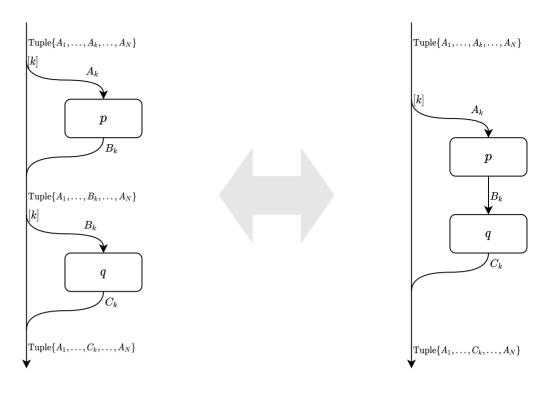
$with_column(k, pass()) \Leftrightarrow pass()$



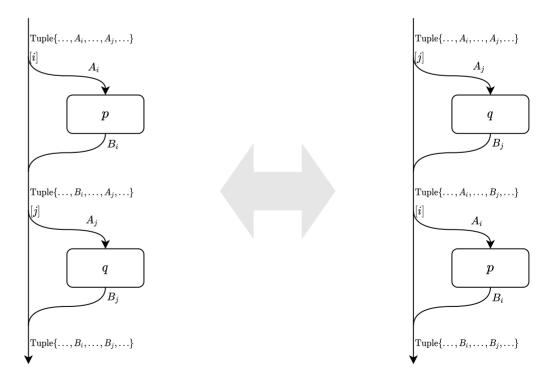
 $\texttt{chain_of}(\texttt{with_elements}(p), \texttt{with_elements}(q)) \Leftrightarrow \texttt{with_elements}(\texttt{chain_of}(p,q))$



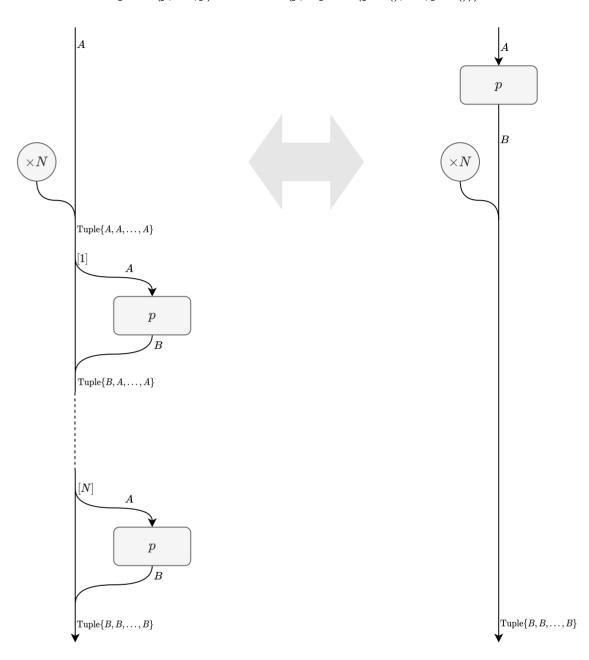
 $\texttt{chain_of}(\texttt{with_column}(k,p), \texttt{with_column}(k,q)) \Leftrightarrow \texttt{with_column}(k,\texttt{chain_of}(p,q))$

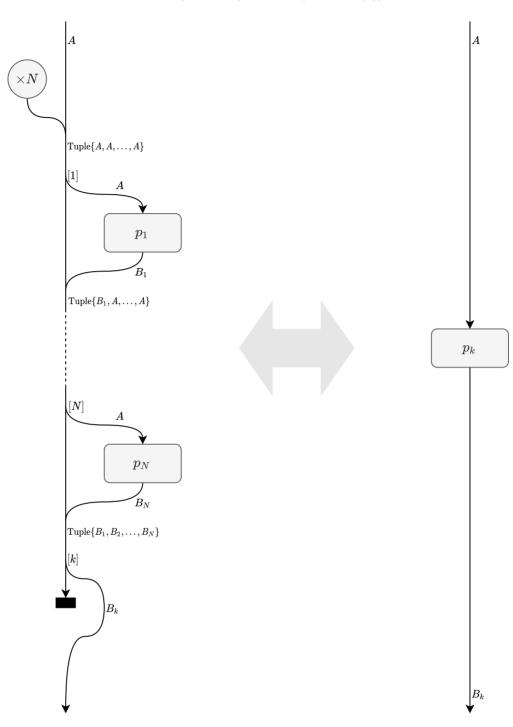


 $\texttt{chain_of}(\texttt{with_column}(i,p), \texttt{with_column}(j,q)) \Leftrightarrow \texttt{chain_of}(\texttt{with_column}(j,q), \texttt{with_column}(i,p)) \qquad i \neq j$









 $\operatorname{chain_of}(\operatorname{wrap}(),\operatorname{lift}(f)) \Leftrightarrow \operatorname{lift}(f)$

