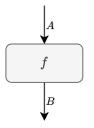
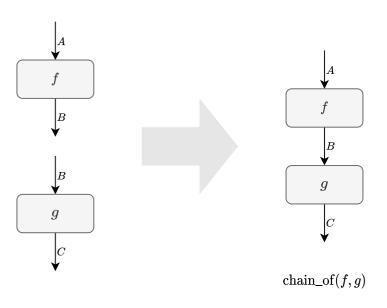
Transformation



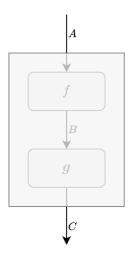
A transformation f maps any input of type A to the output of type B.

Composition



Transformations with compatible input and output can be composed.

Composition is a Transformation



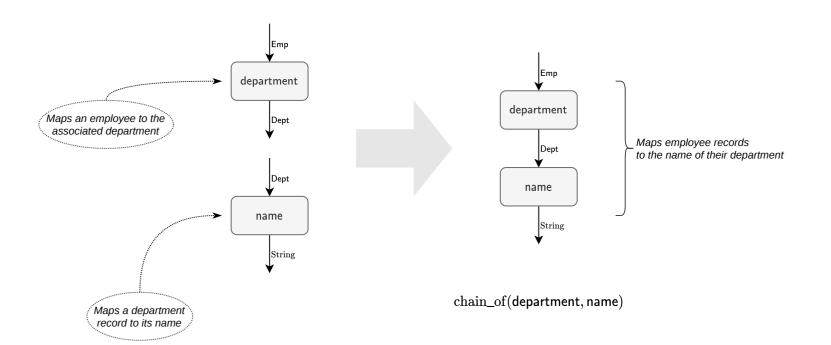
Crucially, composition of transformations is again a transformation.

Composition Combinator

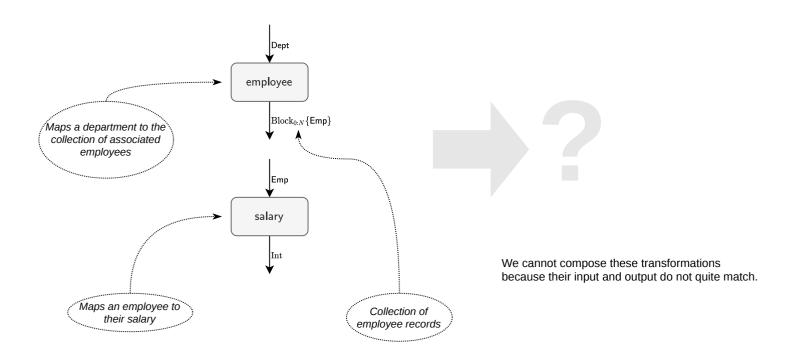


$$\label{eq:composition} \begin{split} & \text{Composition chain_of}\big([]],[]]\big) \\ & \text{is a transformation combinator} \\ & \text{with two arguments.} \end{split}$$

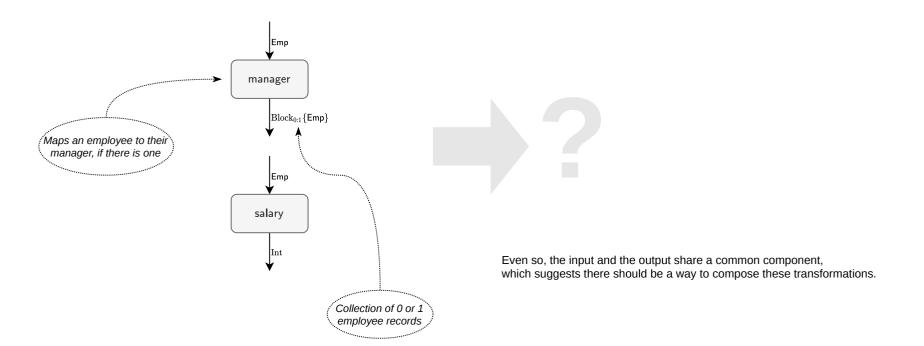
Example: Composition



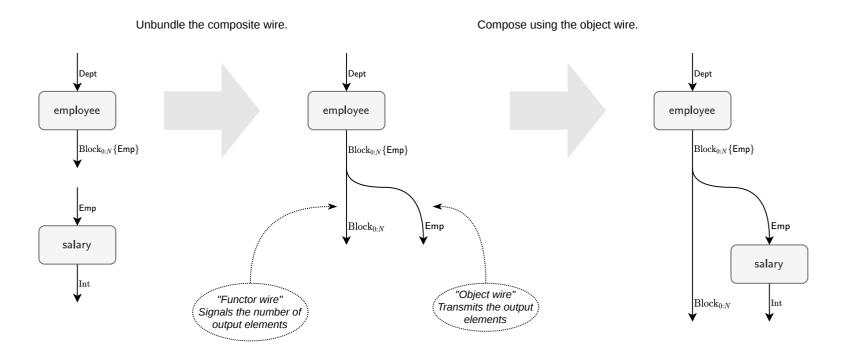
Counter-example: Plural Component



Counter-example: Optional Component



Idea: Unbundle the Wire



Attaching a transformation to the object wire indicates that the transformation is applied to all element of the collection.

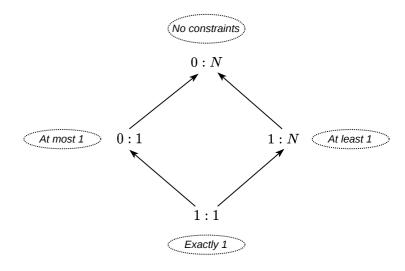
Block Type

A block is a collection of homogeneous elements.

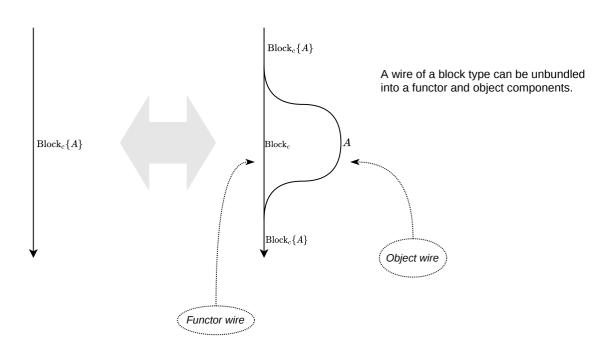
Type of elements

Block $_e\{A\}$ Cardinality of the block

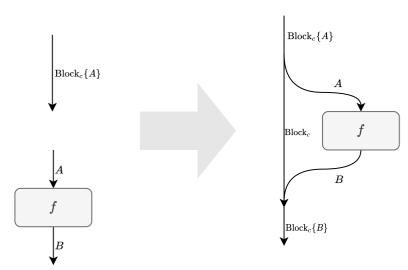
Cardinality is a constraint on the number of elements in a block.



Unbundling



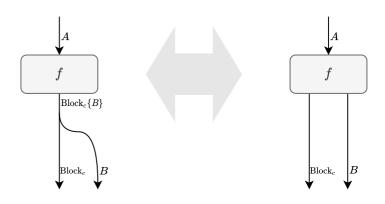
Object Transformation

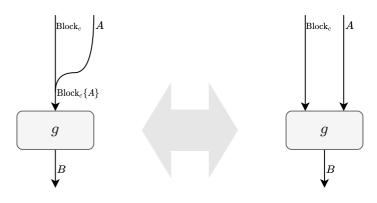


Any compatible transformation can be applied to the object wire, which indicates that the transformation is applied to every element of the block.

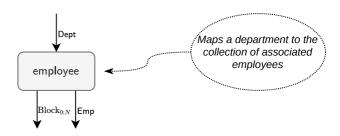
 $with_elements(f)$

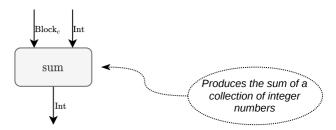
Multiwired Transformations



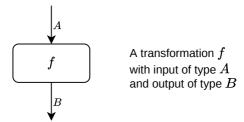


Example: Multiwired Transformations

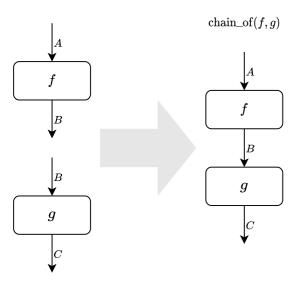




1. Transformation



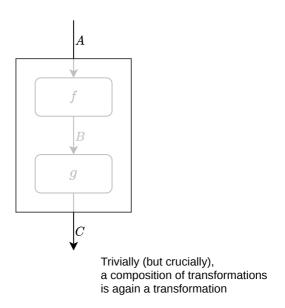
2. Composition

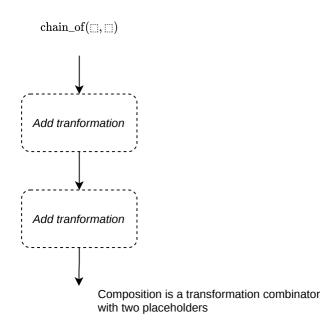


Transformations with compatible input and output can be composed

3. Composition is a Transformation

4. Composition Combinator

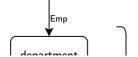


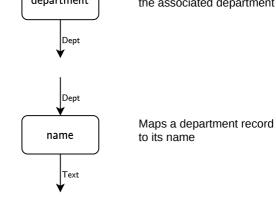


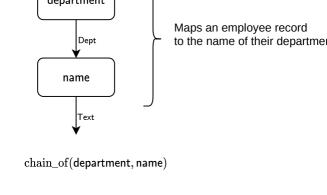
5. Example: Components of a Composition

6. Example: Composition

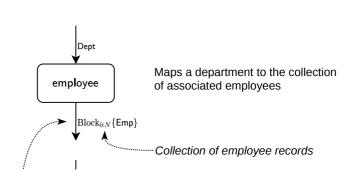




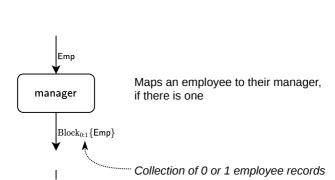




7. Counter-example: Plural Component

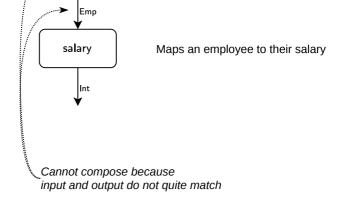


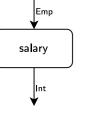
8. Counter-example: Optional



t

Component



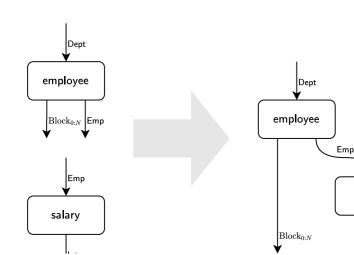


Can we represent composition of these transformations with an intuitive diagrammatic notation?

9. Idea: Unbundle the Wire

Separate the output wire into two components employee Emp Object wire Intuitively, it signals the number Transmits the output elements

10. Idea: Compose Using the



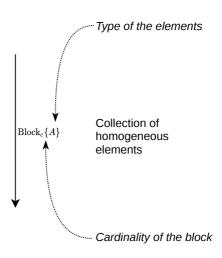
Object Wire



Int

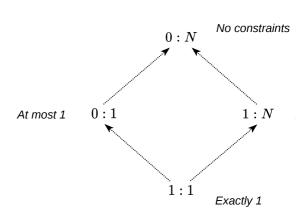
Attaching a transformation to the object wire indicates that the transformation is applied to each element of the collection

11. Block Type



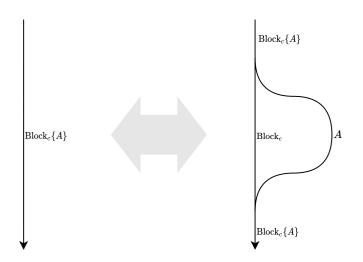
12. Cardinality

Cardinality is a constraint on the number of elem



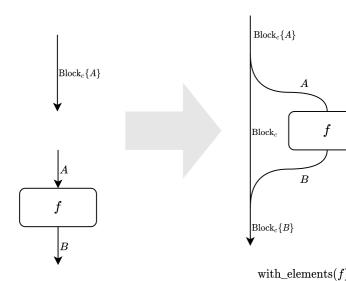


13. Unbundling



We can unbundle a wire of a block type into a functor and object components

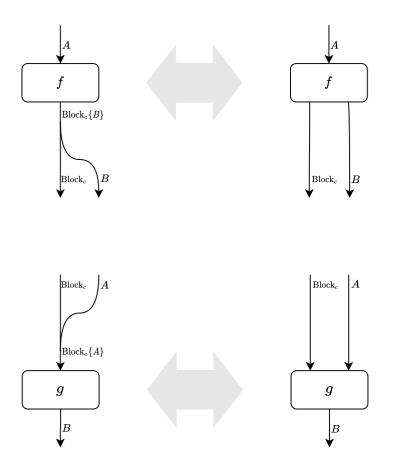
14. Object Transformation



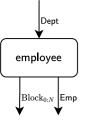
Then any compatible transformation can be applied to the object which indicates that the transformation is applied to every element of the block



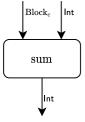
13. Multiwired transformations



14. Example: Multiwired Trans



Maps a department to the collection of associated employees



Produces the sum of a collection of integer

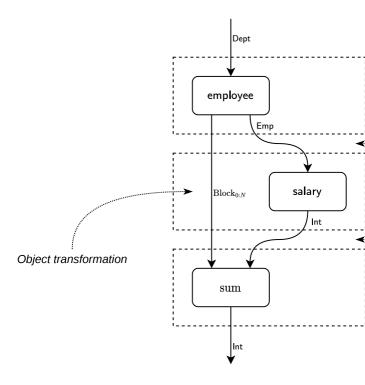
sformations

...

14. Example: Multiwired Composition

Dept Total sum of salaries in a given department employee $\operatorname{Block}_{0:N}$ Emp Dept employee Emp salary salary $Block_{0:N}$ Int sum Block_c sum chain_of(employee, with_elements(salary), sum) Int

15. Example: Details



chain_of(employee, with_elements(salary),



sum)