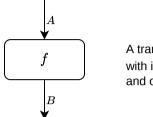
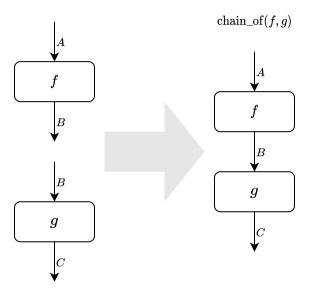
#### 1. Transformation



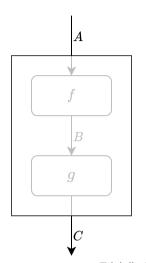
A transformation f with input of type A and output of type B

## 2. Composition



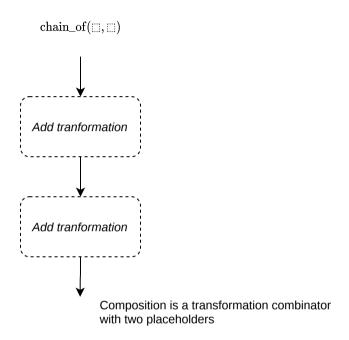
Transformations with compatible input and output can be composed

## 3. Composition is a Transformation

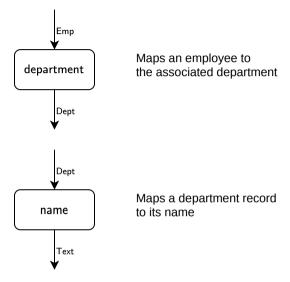


Trivially (but crucially), a composition of transformations is again a transformation

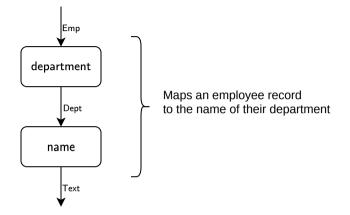
## **4. Composition Combinator**



## **5. Example: Components of a Composition**

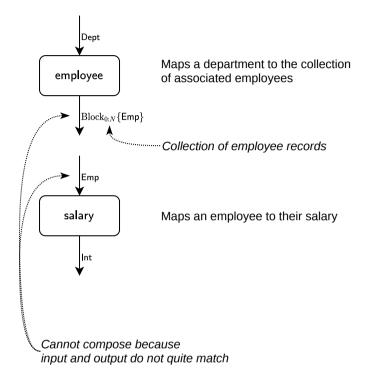


## 6. Example: Composition

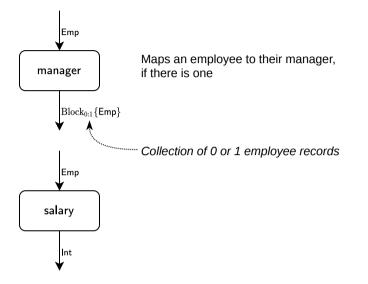


 $chain\_of(\mathsf{department},\mathsf{name})$ 

## 7. Counter-example: Plural Component

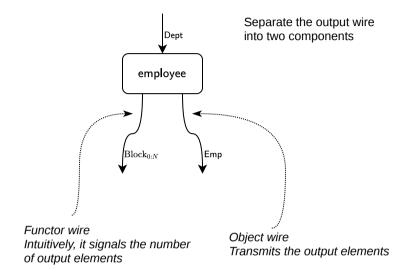


## 8. Counter-example: Optional Component

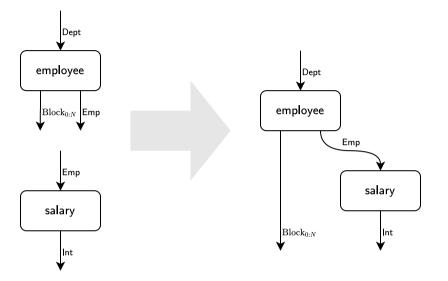


Can we represent composition of these transformations with an intuitive diagrammatic notation?

#### 9. Idea: Unbundle the Wire

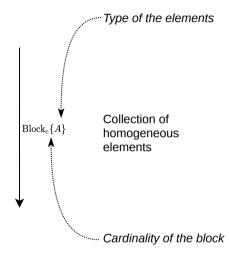


## **10. Idea: Compose Using the Object Wire**



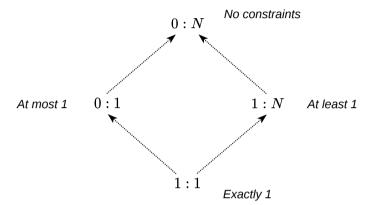
Attaching a transformation to the object wire indicates that the transformation is applied to each element of the collection

#### 11. Block Type

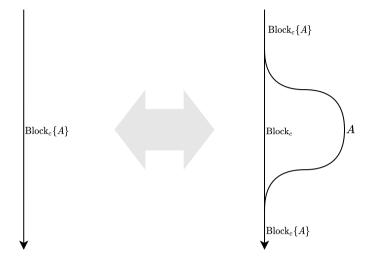


## 12. Cardinality

Cardinality is a constraint on the number of elements in a block

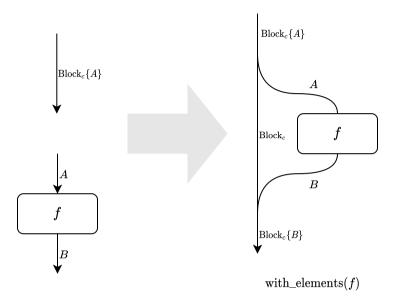


## 13. Unbundling



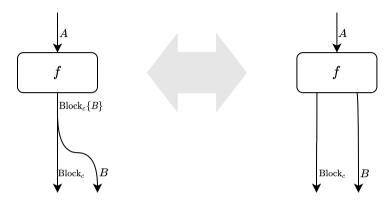
We can unbundle a wire of a block type into a functor and object components

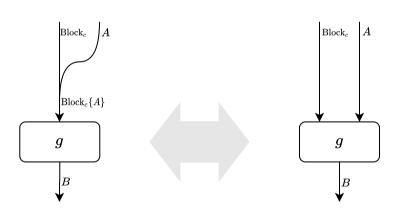
## **14. Object Transformation**



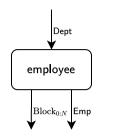
Then any compatible transformation can be applied to the object wire, which indicates that the transformation is applied to every element of the block

#### **13.** Multiwired transformations

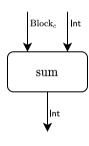




## **14. Example: Multiwired Transformations**

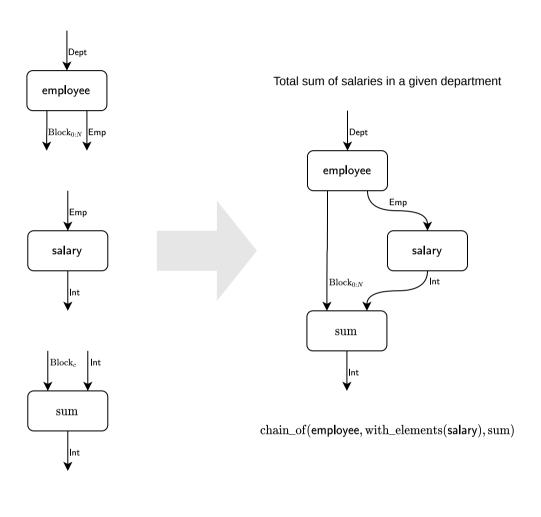


Maps a department to the collection of associated employees



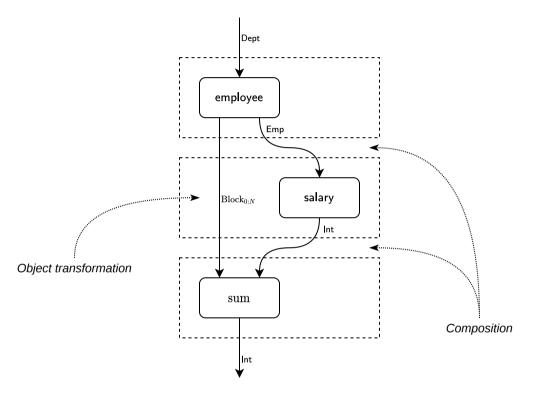
Produces the sum of a collection of integers

## **14. Example: Multiwired Composition**



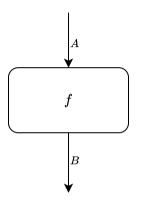


# **15. Example: Details**



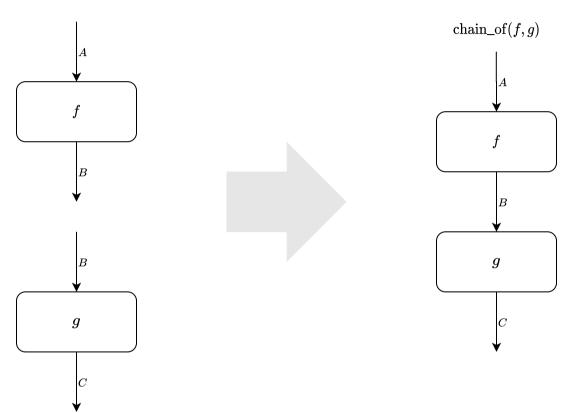
 $chain\_of({\tt employee}, with\_elements({\tt salary}), sum)$ 

#### **Transformation**



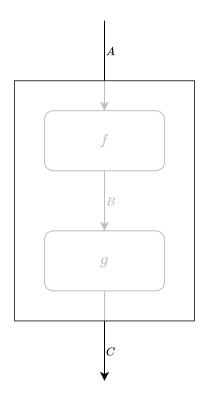
A transformation f maps input of type A to the output of type B.

## Composition



Transformations with compatible input and output can be composed.

# **Composition is a Transformation**



Crucially, a composition of transformations is again a transformation.