



Power Quality Compensation for Smart Grids by Model-based Predictive Control

Carlos Cateriano Yáñez^{1,2}, Kathrin Weihe¹, Georg Pangalos², and Gerwald Lichtenberg¹

¹Hamburg University of Applied Sciences, Faculty Life Sciences, Ulmenliet 20, 21033 Hamburg ²Fraunhofer ISIT, Application Center Power Electronics for Renewable Energy Systems, Steindamm 94, 20099 Hamburg {carlos.caterianoyanez, kathrin.weihe, gerwald.lichtenberg}@haw-hamburg.de, georg.pangalos@isit.fraunhofer.de,

MOTIVATION

- High order harmonics in the electrical grid introduced by switching converters need to be compensated to avoid damage and energy loss
- Classic active power filter (APF) controllers are capable of compensating harmonics but are not flexible under variable load scenarios

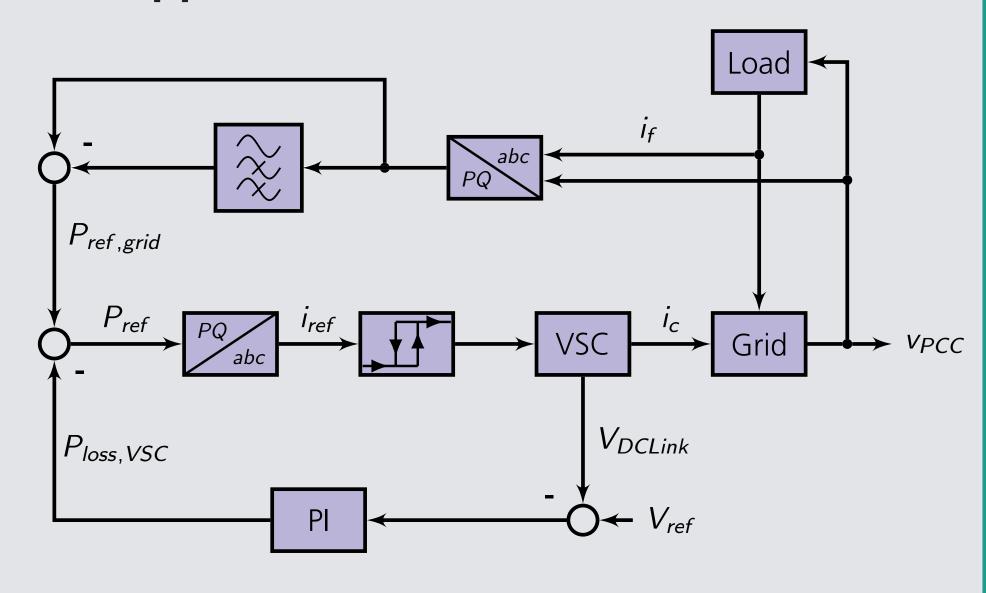
APPLICATION PROBLEM

A novel approach: Linear State Signal Shaping Model Predictive Control (LS³MPC), has been developed to compensate harmonics using shape classes

- Can the LS³MPC improve the grid quality compared to a classic APF controller?
- Can the LS³MPC adapt under variable load scenarios?

CLASSIC IRP CONTROLLER

The instantaneous reactive power (IRP) theory is a state-of-the-art classic APF control approach.



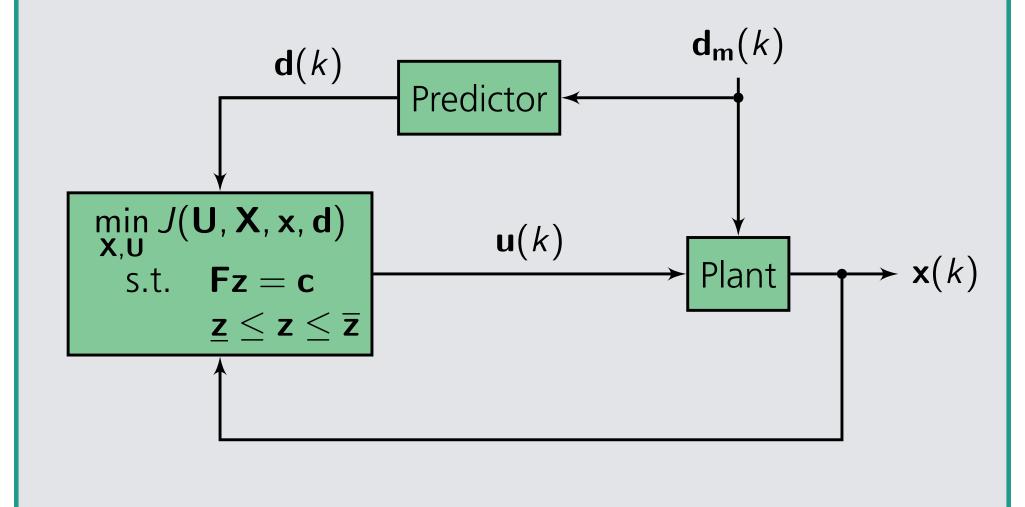
- Clarke and p-q transformation are used
- A high pass filter extracts harmonics
- A hysteresis band controller steers the voltage source converter

PREDICTIVE CONTROLLER

The MPC minimizes the cost function

$$J = \|\mathbf{X}(k) - \Xi(k)\|_{\mathbf{Q}}^{2} + \|\mathbf{U}(k)\|_{\mathbf{R}}^{2}.$$

The optimization problem is solved by formulating it as a constrained sparse quadratic programming (QP) problem, with the following close loop behavior:



LINEAR SHAPE CLASS

A sine wave shape is given by the ODE

$$\frac{\mathrm{d}^2 x(t)}{\mathrm{d}t^2} + \omega^2 x(t) = 0$$

and approximated in discrete time with

$$x(k-1)+((\omega t_s)^2-2)x(k)+x(k+1)=0.$$

From this difference equation the *linear* shape class V is given as

$$\mathbf{V}=\left(\begin{array}{ccc}1&(\omega t_s)^2-2&1\end{array}
ight)\in\mathbb{R}^{1 imes 3}$$
 .

The state error weight matrix Q is built using V by transferring the control goal to the optimization problem

$$\min_{\mathbf{X}(k)} (\mathbf{VX}(k))^2$$
,

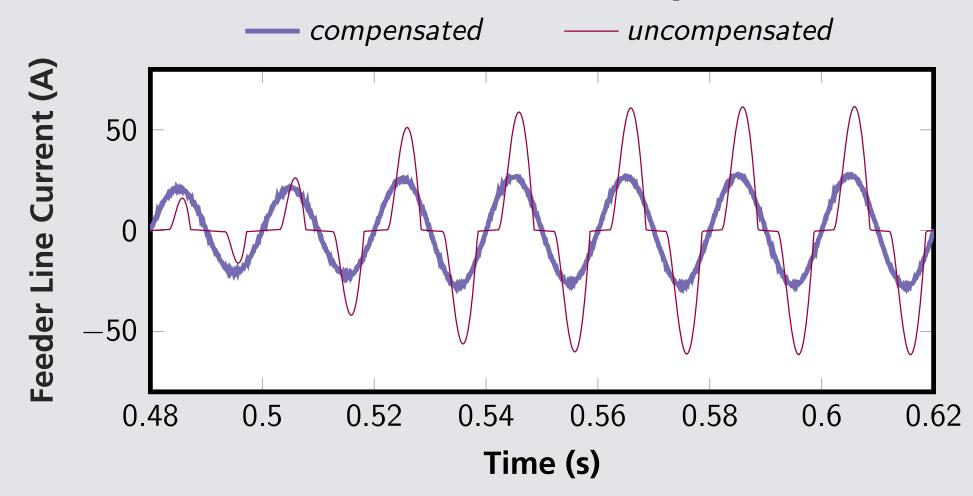
where

$$\mathbf{X}(k) = \begin{pmatrix} x(k-1) & x(k) & x(k+1) \end{pmatrix}^{\mathsf{T}},$$

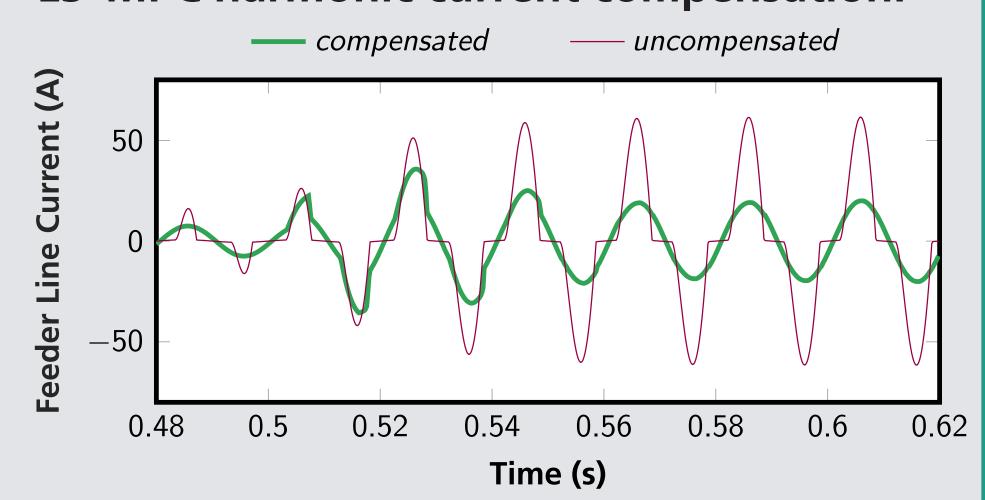
for all times k.

SIMULATION STUDIES

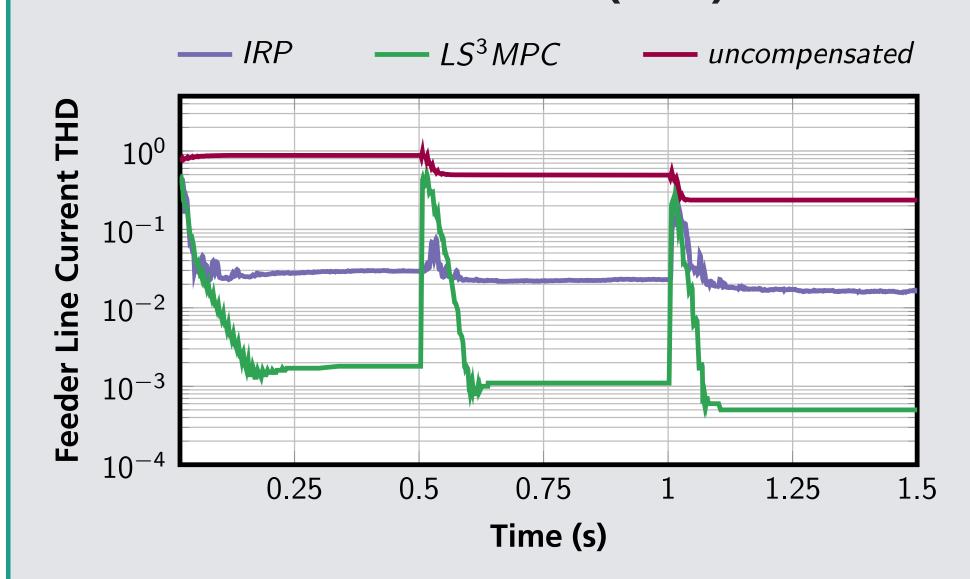
IRP APF harmonic current compensation:



LS³MPC harmonic current compensation:



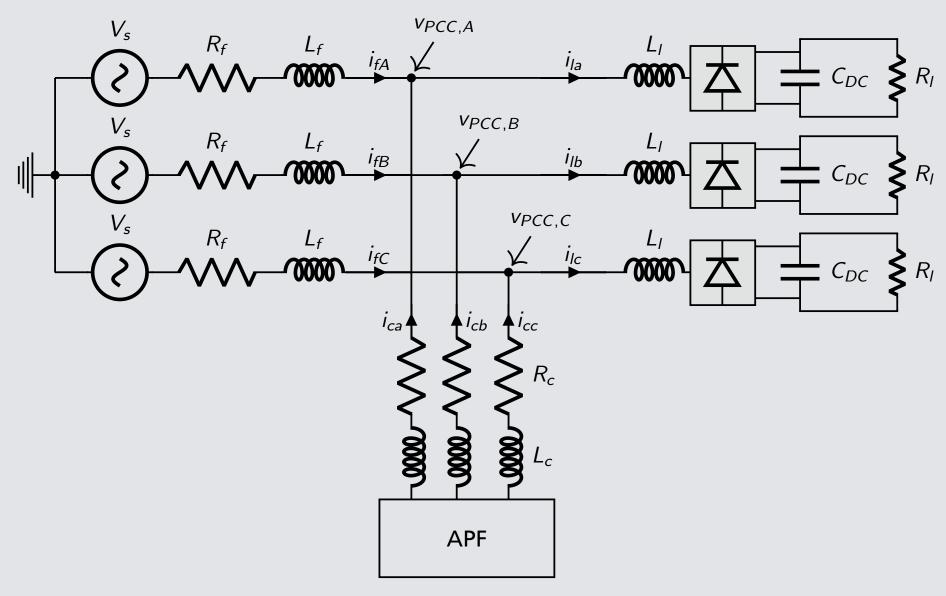
Total harmonic distortion (THD):



Results for different load scenarios:

| Load | THD (v _{PCC}) | | THD (i _f) | |
|----------|-------------------------|---------------------|-----------------------|---------------------|
| scenario | IRP | LS ³ MPC | IRP | LS ³ MPC |
| 100 Ω | 1.07% | 0.01% | 2.92% | 0.18% |
| 9Ω | 0.75% | 0.02% | 2.72% | 0.11% |
| 2Ω | 0.85% | 0.07% | 2.56% | 0.05% |

3-PHASE GRID MODEL



Active power filter in shunt configuration

WHITE-BOX MODELING

Linear state space model per phase

$$x(k+1) = Ax(k) + Bu(k) + Ed_m(k)$$

where

$$\mathbf{x}(k) = \begin{pmatrix} i_f \\ i_c \end{pmatrix} \in \mathbb{R}^2 \qquad \mathbf{u}(k) = i_{c0} \in \mathbb{R}$$
$$\mathbf{d}(k) = \begin{pmatrix} v_s i_{l0} \end{pmatrix}^{\mathsf{T}} \in \mathbb{R}^2$$

and

$$\mathbf{A} \in \mathbb{R}^{2 \times 2}$$
, $\mathbf{B} \in \mathbb{R}^{2 \times 1}$, $\mathbf{E} \in \mathbb{R}^{2 \times 2}$.

CONCLUSION

- The LS³MPC can successfully improve the THD compensation of an APF
- The LS³MPC can inherently adapt to a wider variety of load scenarios
- Current research on LS³MPC focuses on enabling reactive power compensation

PUBLICATIONS

- Cateriano Yáñez, C., Pangalos, G., and Lichtenberg, G. (2018). An approach to linear state signal shaping by quadratic model predictive control. In *European Control Conference (ECC) 2018*
- Weihe, K., Cateriano Yáñez, C., Pangalos, G., and Lichtenberg, G. (2018). Comparison of Linear State Signal Shaping Model Predictive Control with Classical Concepts for Active Power Filter Design. In *Simultech 2018*