



Power Quality Compensation for Smart Grids by Model-based **Predictive Control**

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MOTIVATION

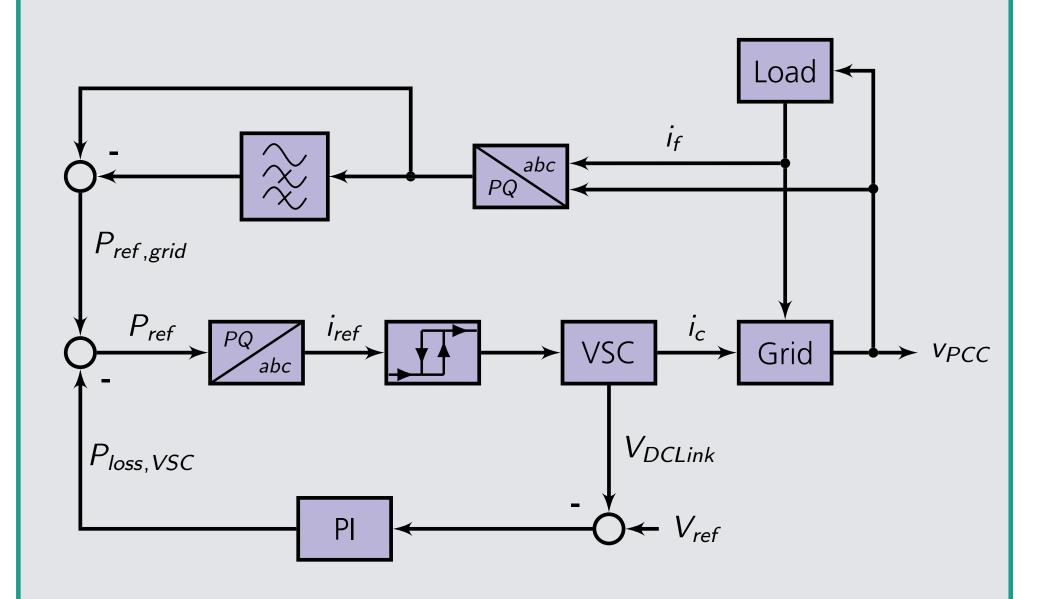
- High order harmonics in the electrical grid introduced by switching converters need to be compensated to avoid damage and energy loss
- Classic active power filter (APF) controllers are capable of compensating harmonics, but are not flexible under variable load scenarios

APPLICATION PROBLEM

A novel approach: "Linear State Signal Shaping Model Predictive Control" (LS³MPC), to compensate harmonics using shape classes has been developed

- Could the LS³MPC improve the grid quality compared to a classic APF controller?
- Could the LS³MPC adapt under variable load scenarios?

CLASSIC IRP CONTROLLER



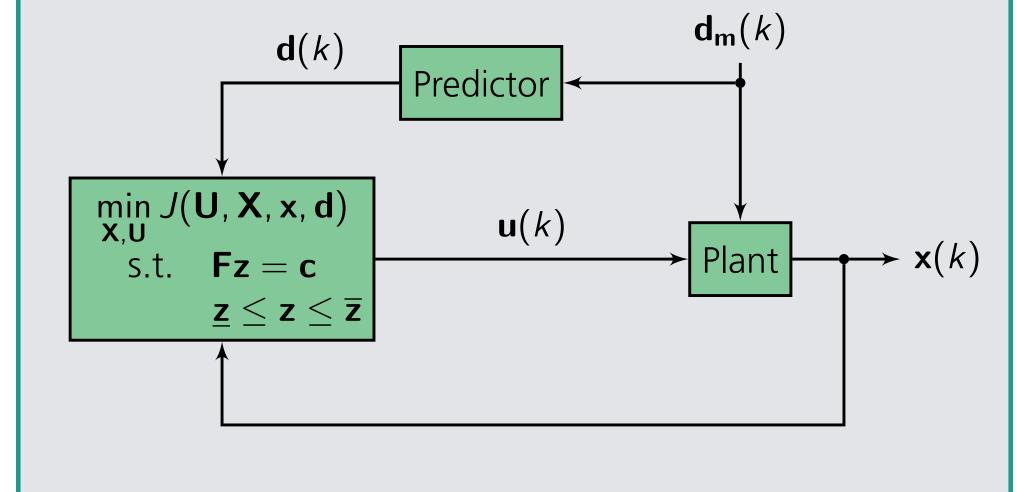
- Clarke and p-q transformation are used
- A high pass filter extracts harmonics
- A hysteresis band controller steers the voltage source converter

PREDICTIVE CONTROLLER

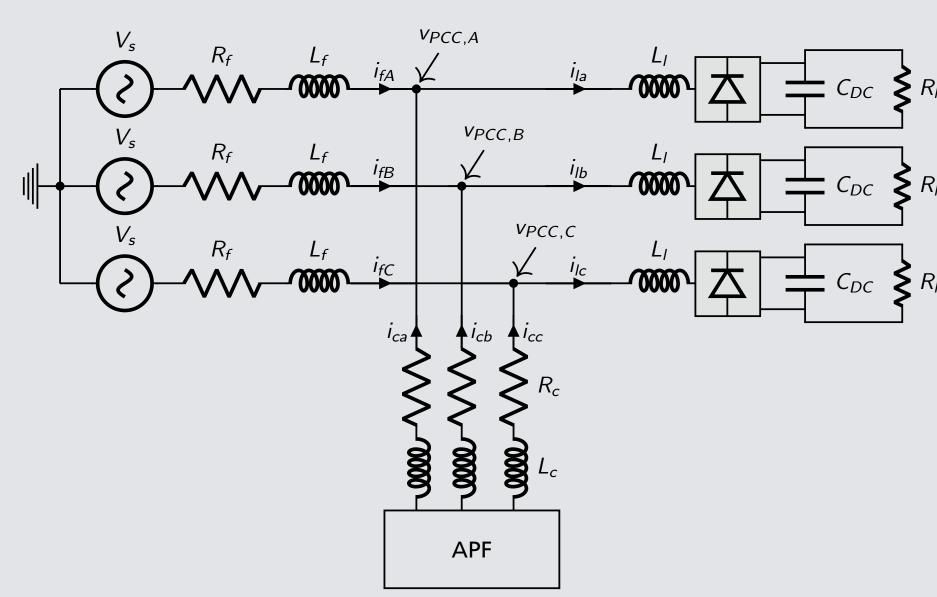
The MPC minimizes the cost function

$$J = \|\mathbf{X}(k) - \Xi(k)\|_{\mathbf{Q}}^{2} + \|\mathbf{U}(k)\|_{\mathbf{R}}^{2}.$$

Solved by constrained sparse quadratic programming (QP), with close loop behavior:



3-PHASE GRID MODEL



Active power filter in shunt configuration

LINEAR SHAPE CLASS

The shape of a sine wave is described by the homogeneous ODE

$$\frac{\mathrm{d}^2 x(t)}{\mathrm{d}t^2} + \omega^2 x(t) = 0$$

and approximated in discrete time with

$$x(k-1) + ((\omega t_s)^2 - 2) x(k) + x(k+1) = 0.$$

From this difference equation the *linear* shape class³ V is given as

$$\mathbf{V}=\begin{pmatrix} 1 & (\omega t_s)^2-2 & 1 \end{pmatrix} \in \mathbb{R}^{1 imes 3}$$
.

The state error weight matrix Q is built using V by transferring the control goal to the optimization problem

$$\min_{\mathbf{X}(k)} (\mathbf{VX}(k))^2$$
,

where

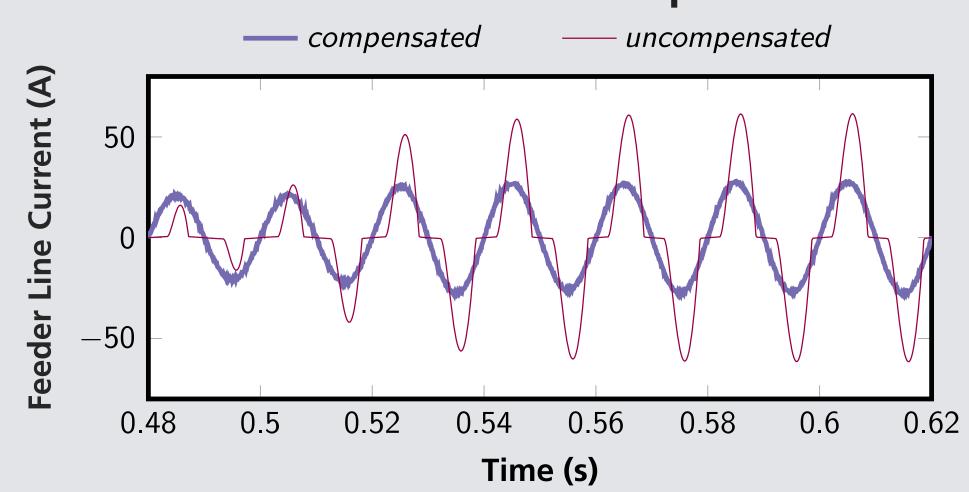
$$\mathbf{X}(k) = \begin{pmatrix} x(k-1) & x(k) & x(k+1) \end{pmatrix}^{\mathsf{T}},$$

for all times k.

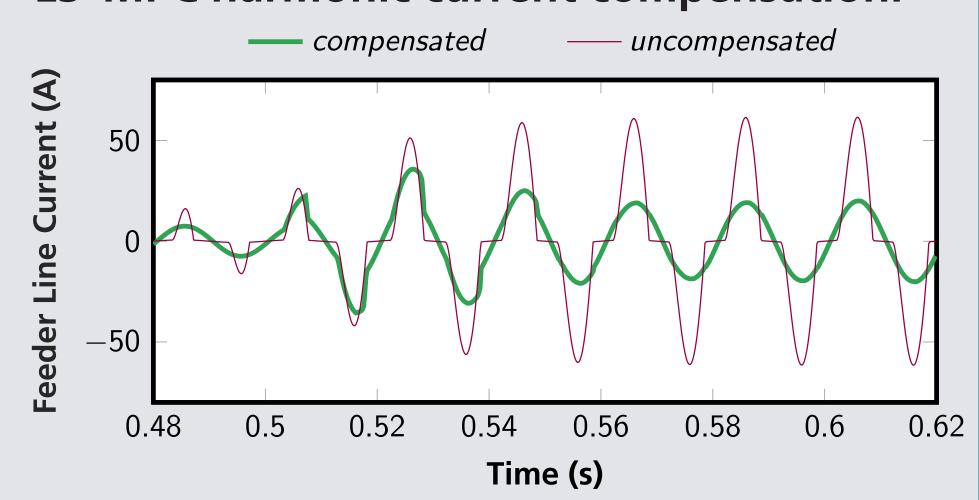
³Cateriano Yáñez, C., Pangalos, G., and Lichtenberg, G. (2018). An approach to linear state signal shaping by quadratic model predictive control. In European Control Conference (ECC) 2018

SIMULATION STUDIES

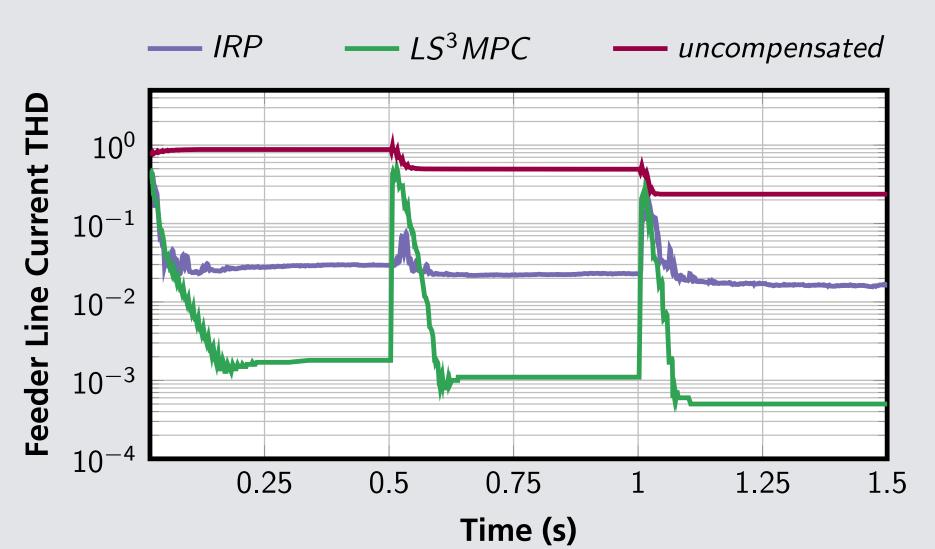
IRP APF harmonic current compensation:



LS³MPC harmonic current compensation:



Total harmonic distortion (THD):

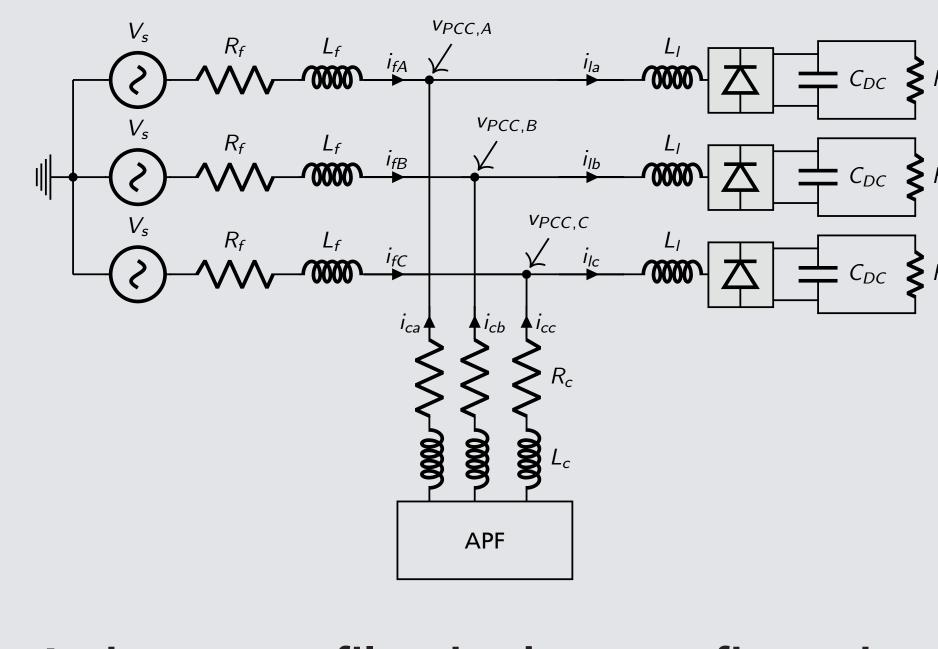


Results for different load scenarios:

Load	THD (VPCC)		THD (<i>i</i> _f)	
scenario	IRP	LS ³ MPC	IRP	LS ³ MPC
100 Ω	1.07%	0.01%	6.68%	0.18%
9Ω	0.75%	0.02%	2.72%	0.11%
2Ω	0.85%	0.07%	2.56%	0.05%

CONCLUSION

- The LS³MPC can successfully improve the THD compensation of an APF
- Classic IRP rely on high pass filter design for a given load scenario, while LS³MPC can inherently adapt to a wider variety
- Current research on LS³MPC focuses on enabling reactive power compensation



WHITE-BOX MODELING

Linear state space model of per phase

$$x(k+1) = Ax(k) + Bu(k) + Ed(k)$$

where

$$\mathbf{x}(k) = \begin{pmatrix} i_f \\ i_c \end{pmatrix} \in \mathbb{R}^2 \qquad \mathbf{u}(k) = i_{c0} \in \mathbb{R}$$
$$\mathbf{d}(k) = \begin{pmatrix} v_s i_{l0} \end{pmatrix}^{\mathsf{T}} \in \mathbb{R}^2$$

and

$$\mathbf{A} \in \mathbb{R}^{2 \times 2}$$
, $\mathbf{B} \in \mathbb{R}^{2 \times 1}$, $\mathbf{E} \in \mathbb{R}^{2 \times 2}$.