

PROBLEM 5.1 A THIN-WALLED STEEL TUBE, 1m LONG, WITH THE CROSS-SECTION SHOWN, IS TRANSMITTING A TORQUE OF 2 kN·m. THE 50mm DIMENSION IS BETWEEN WALL CENTERS. FOR THE MATERIAL LET $E = 210 \text{ GPa}$ AND $\nu = 0.29$. DETERMINE (a) THE AVERAGE SHEAR STRESS IN THE WALL AND (b) THE TOTAL ANGLE OF TWIST OF THE TUBE.

GIVEN:

1. THIN WALLED CROSS-SECTION SHOWN.
2. MATERIAL PROPERTIES $E = 210 \text{ GPa}$, $\nu = 0.29 \Rightarrow G = \frac{E}{2(1+\nu)} = 81.40 \text{ GPa}$
3. APPLIED TORQUE 2 kN·m.
4. LENGTH OF TUBE IS 1m

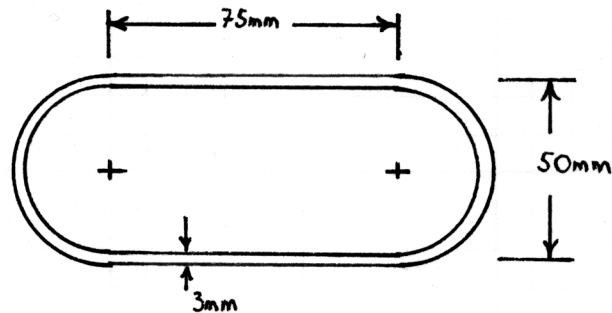
ASSUMPTIONS:

1. SMALL DEFLECTIONS
2. LINEAR-ELASTIC RESPONSE

FIND:

1. AVERAGE SHEAR STRESS IN THE WALLS
2. THE TOTAL ANGLE OF TWIST IN THE TUBE.

FIGURE:



SOLUTION:

THE AVERAGE SHEAR STRESS IS CALCULATED FROM

$$\tau = \frac{2(10^3) \text{ N} \cdot \text{m}}{2 \cdot (0.003 \text{ m}) \cdot [0.05 \text{ m} \cdot 0.075 \text{ m} + \pi \cdot (0.05 \text{ m}/2)^2]} = 58.34 \text{ MPa}$$

THE ANGLE OF TWIST CAN NOW BE CALCULATED.

$$\begin{aligned} \Phi &= \frac{2 \times 10^3 \text{ N} \cdot \text{m} \cdot 1 \text{ m}}{4 \cdot [0.075 \text{ m} \cdot 0.05 \text{ m} + \pi \cdot (0.05 \text{ m}/2)^2] \cdot 81.40 \times 10^9 \frac{\text{N}}{\text{m}^2}} \cdot \left[\frac{2 \cdot \pi \cdot (0.05 \text{ m})}{0.003 \text{ m}} + 2 \cdot 0.075 \text{ m} \right] \\ &= 0.0193 \cdot \frac{180^\circ}{\pi} = 1.10^\circ \end{aligned}$$

SUMMARY: THIS IS A STRAIGHT FORWARD APPLICATION OF THE THEORY PRESENTED. CARE MUST BE TAKEN IN PROPERLY INTERPRETING THE ANGLE OF TWIST CALCULATION TO BE IN RADIANS.