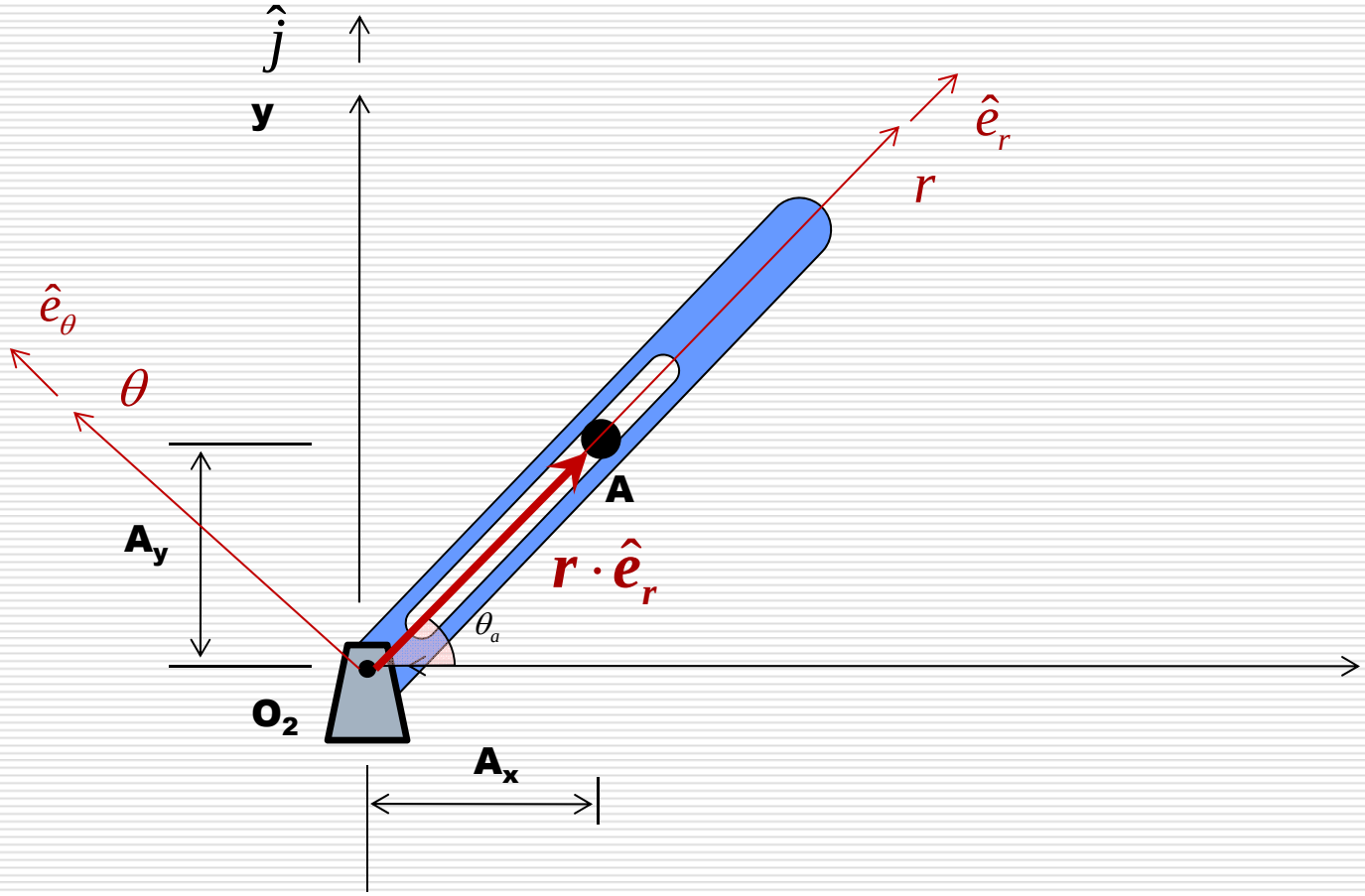
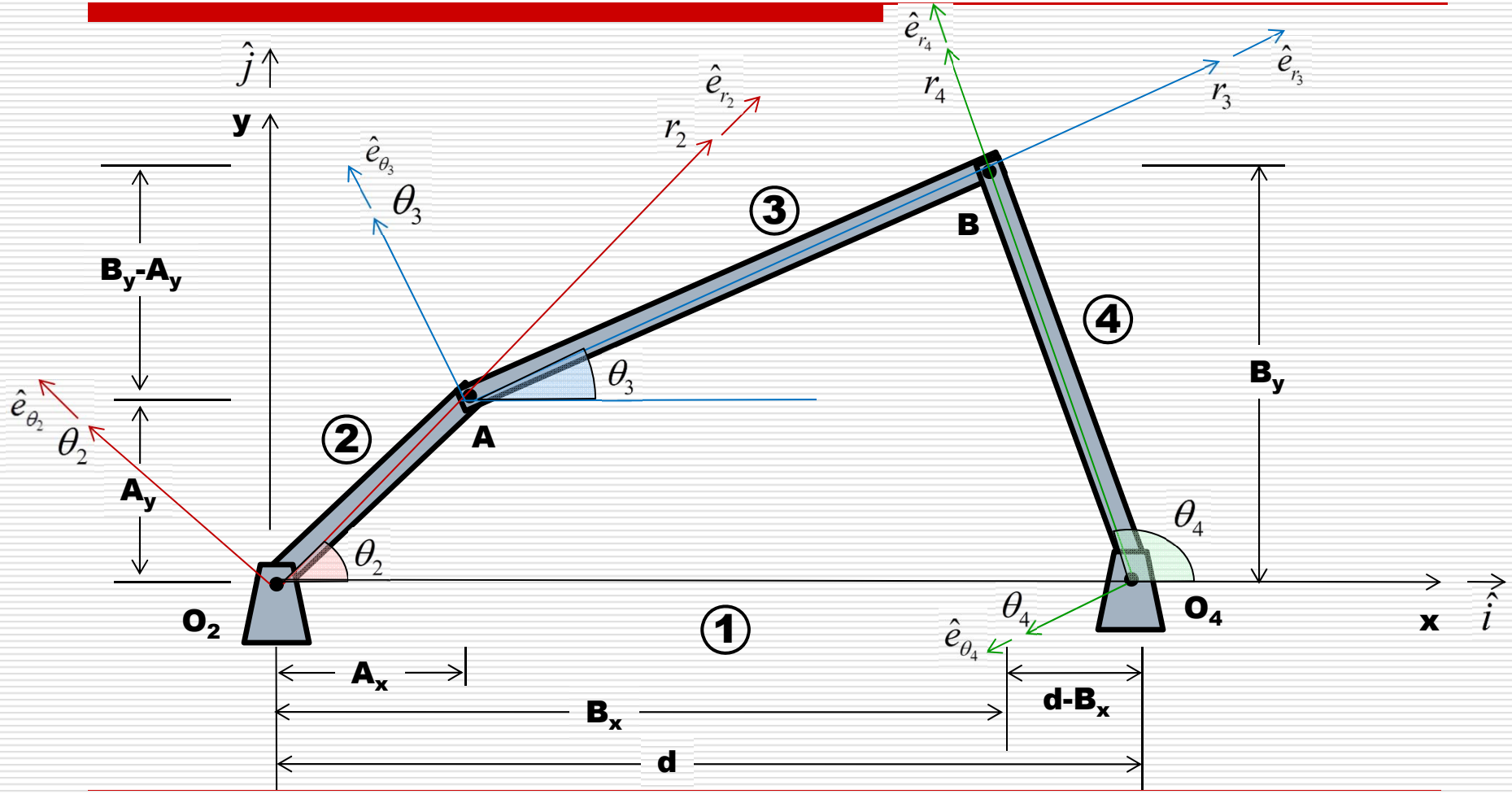
Kinematics Fundamentals

- Acceleration Analysis
- Four Bar Linkage
- Slider Crank
- Inverted Slider Crank

Acceleration Fundamentals



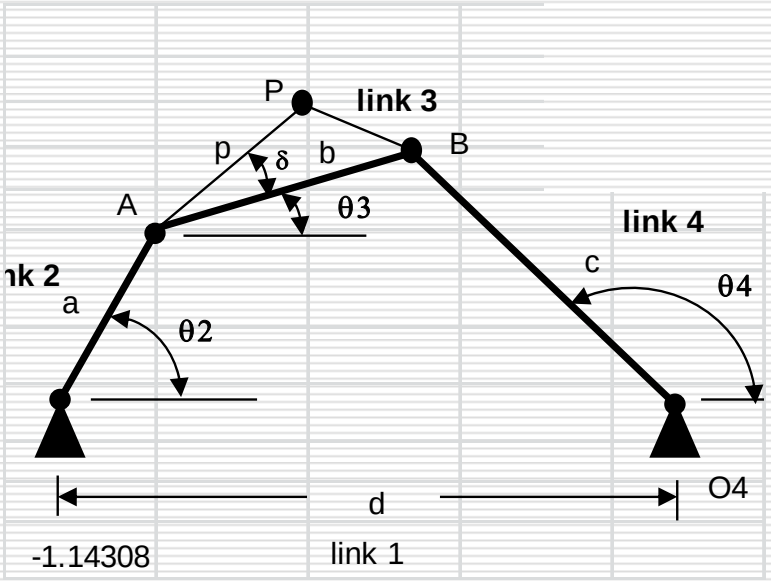
TYPE I: (RRRR)
Four Bar Linkage



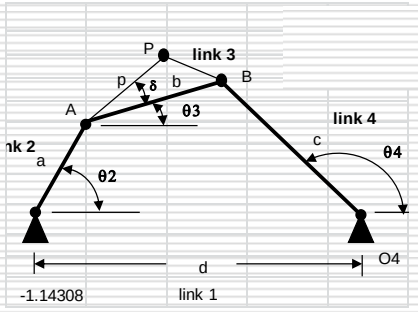
4-Bar Algorithm
Inputs and Initial Calculations

a=	5	Link 2
b=	12	Link 3
c=	10	Link 4
d=	15	Link 1
$\theta_2 =$	60	1.047197551
$\dot{\theta}_2 =$	-25	$1/s$
$\ddot{\theta}_2 =$	-180	$1/s^2$
By=	9.83	-6.59
Bx=	13.17	7.48
$\theta_3 =$	27.3	-65.5
$\theta_4 =$	100.6	-138.8
$\dot{\theta}_3 =$	7.0737E+00	-3.5022E+00
$\dot{\theta}_4 =$	-7.0545E+00	1.0626E+01
$\ddot{\theta}_3 =$	2.2918E+02	3.2675E+02
$\ddot{\theta}_4 =$	2.7146E+02	2.8447E+02

p=	5
δ=	331

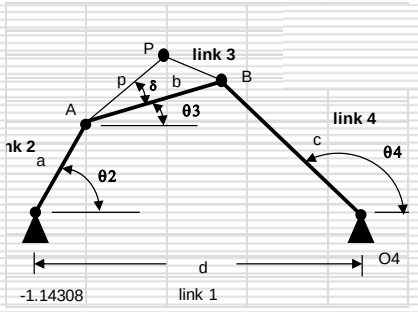


4-Bar Algorithm, (OPEN) Acceleration Vector Results



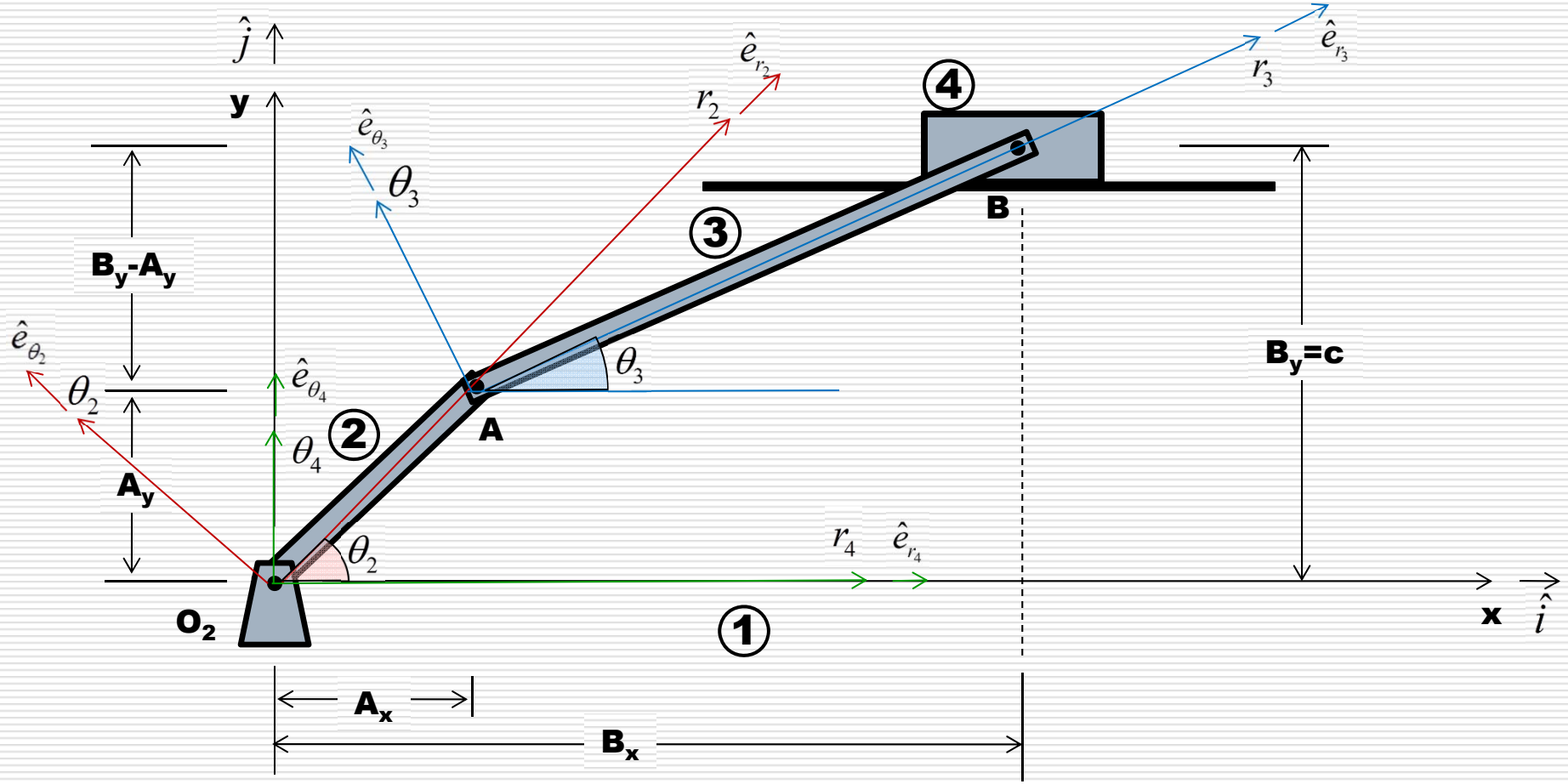
					e_r		e_θ	
	x comp	y comp	mag	angle	i	j	i	j
r04=	**15.00**	**0.00**	**15.000**	**0.0**	**1.000**	**0.000**	**0.000**	**1.000**
rA=	**2.50**	**4.33**	**5.000**	**60.0**	**0.500**	**0.866**	**-0.866**	**0.500**
rBA=	10.67	5.50	12.000	27.3	0.889	0.458	-0.458	0.889
rBO4=	-1.83	9.83	10.000	100.6	-0.183	0.983	-0.983	-0.183
rB=	**13.17**	**9.83**	**16.430**	**36.7**	**0.801**	**0.598**	**-0.598**	**0.801**
rPA=	5.00	-0.15	5.000	-1.7	1.000	-0.030	0.030	1.000
rP=	**7.50**	**4.18**	**8.584**	**29.1**	**0.873**	**0.487**	**-0.487**	**0.873**
vA=	**108.25**	**-62.50**	**125.000**	**-30.0**	**0.866**	**-0.500**	**0.500**	**0.866**
vBA=	-38.91	75.44	84.884	117.3	-0.458	0.889	-0.889	-0.458
vB=	**69.35**	**12.94**	**70.545**	**10.6**	**0.983**	**0.183**	**-0.183**	**0.983**
vPA=	1.06	35.35	35.368	88.3	0.030	1.000	-1.000	0.030
vP=	**109.31**	**-27.15**	**112.635**	**-13.9**	**0.971**	**-0.241**	**0.241**	**0.971**
aA=	**-783.08**	**-3156.33**	**3252.019**	**-103.9**	**-0.241**	**-0.971**	**0.971**	**-0.241**
aBA	-1794.18	2169.07	2814.948	129.6	-0.637	0.771	-0.771	-0.637
aB	**-2577.26**	**-987.26**	**2759.879**	**-159.0**	**-0.934**	**-0.358**	**0.358**	**-0.934**
aPA=	-215.68	1152.89	1172.895	100.6	-0.184	0.983	-0.983	-0.184
aP=	**-998.76**	**-2003.44**	**2238.588**	**-116.5**	**-0.446**	**-0.895**	**0.895**	**-0.446**

4-Bar Algorithm, (CLOSED) Acceleration Vector Results



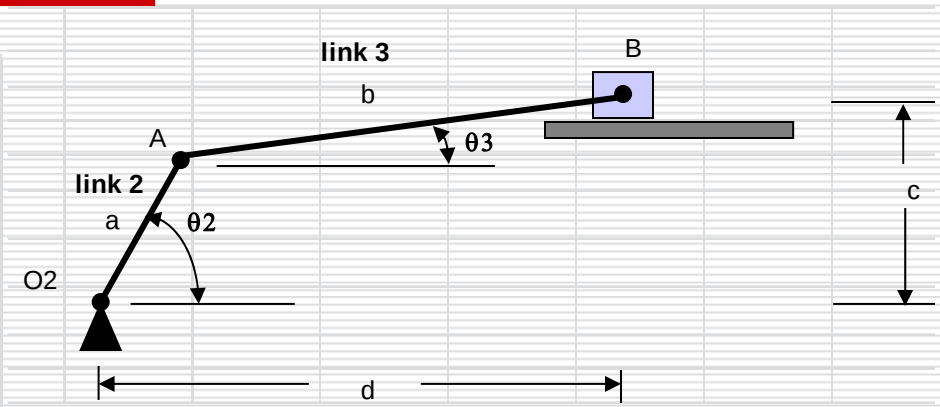
ALT	x comp	y comp	mag	angle	i	j	i	j
rO4=	**15.00**	**0.00**	**15.000**	**0.0**	**1.000**	**0.000**	**0.000**	**1.000**
rA=	**2.50**	**4.33**	**5.000**	**60.0**	**0.500**	**0.866**	**-0.866**	**0.500**
rBA=	4.98	-10.92	12.000	-65.5	0.415	-0.910	0.910	0.415
rBO4=	-7.52	-6.59	10.000	-138.8	-0.752	-0.659	0.659	-0.752
rB=	**7.48**	**-6.59**	**9.966**	**-41.4**	**0.750**	**-0.661**	**0.661**	**0.750**
rPA=	-0.39	-4.98	5.000	-94.5	-0.078	-0.997	0.997	-0.078
rP=	**2.11**	**-0.65**	**2.208**	**-17.2**	**0.955**	**-0.296**	**0.296**	**0.955**
vA=	**108.25**	**-62.50**	**125.000**	**-30.0**	**0.866**	**-0.500**	**0.500**	**0.866**
vBA=	-38.24	-17.43	42.027	-155.5	-0.910	-0.415	0.415	-0.910
vB=	**70.01**	**-79.93**	**106.259**	**-48.8**	**0.659**	**-0.752**	**0.752**	**0.659**
vPA=	-17.46	1.37	17.511	175.5	-0.997	0.078	-0.078	-0.997
vP=	**90.80**	**-61.13**	**109.456**	**-34.0**	**0.830**	**-0.558**	**0.558**	**0.830**
aA=	**-783.08**	**-3156.33**	**3252.019**	**-103.9**	**-0.241**	**-0.971**	**0.971**	**-0.241**
aBA	3506.76	1760.36	3923.805	26.7	0.894	0.449	-0.449	0.894
aB	**2723.68**	**-1395.97**	**3060.583**	**-27.1**	**0.890**	**-0.456**	**0.456**	**0.890**
aPA=	1633.55	-66.86	1634.919	-2.3	0.999	-0.041	0.041	0.999
aP=	**850.47**	**-3223.19**	**3333.504**	**-75.2**	**0.255**	**-0.967**	**0.967**	**0.255**

TYPE II: (RRRP)
Slider Crank Linkage

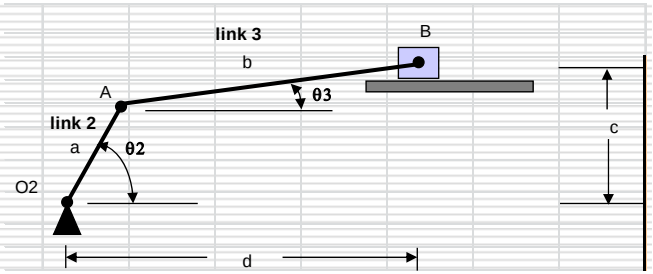


Slider Crank Algorithm
Inputs and Initial Results

a=	5.5	Link 2	
b=	21	Link 3	
c=	2	Offset	
$\theta_2 =$	55		0.959931089
$\dot{\theta}_2 =$	-20	$1/s$	
$\ddot{\theta}_2 =$	5	$1/s^2$	
By=	2.00		2.00
Bx=	24.00		-17.70
$\theta_3 =$	-6.9		-173.1
$\dot{\theta}_3 =$	3.03		-3.03
$\ddot{\theta}_3 =$	84.58		-84.58
vB=	97.69		82.53
aB=	-1263.43		-1305.36



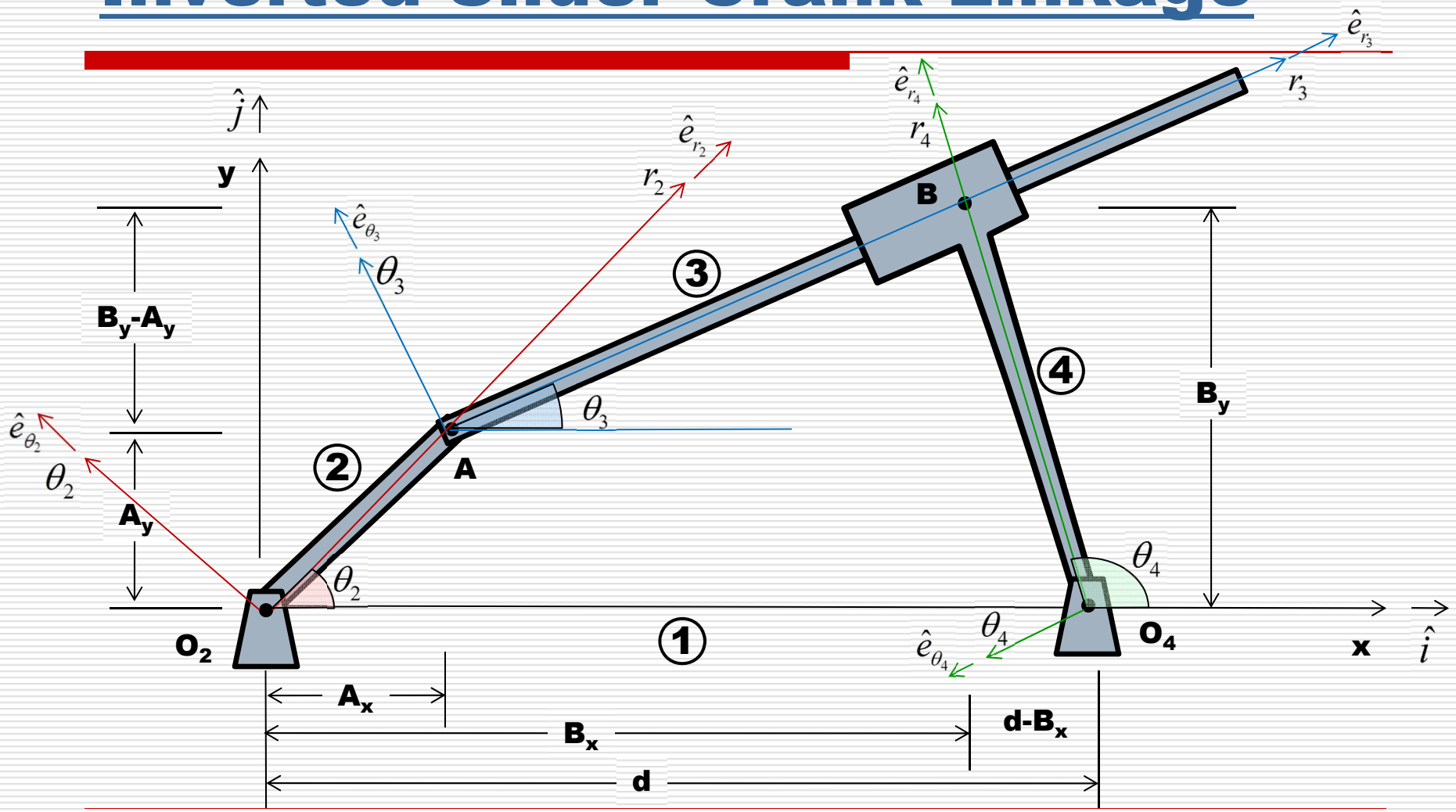
Slider Crank Algorithm Acceleration Results



					e_r		e_θ	
	x comp	y comp	mag	angle	i	j	i	j
rB=	**24.00**	**2.00**	**24.09**	**4.8**	**0.997**	**0.083**	-0.083	0.997
rA=	**3.15**	**4.51**	**5.50**	**55.0**	**0.574**	**0.819**	-0.819	0.574
rBA=	20.85	-2.51	21.00	-6.9	0.993	-0.119	0.119	0.993
vB	**97.69**	**0.00**	**97.69**	**0.0**	**1.000**	**0.000**	0.000	1.000
vA	**90.11**	**-63.09**	**110.00**	**-35.0**	**0.819**	**-0.574**	0.574	0.819
vBA	7.58	63.09	63.55	83.1	0.119	0.993	-0.993	0.119
aB	**-1263.43**	**0.00**	**1263.43**	**180.0**	**-1.000**	**0.000**	0.000	-1.000
aA	**-1284.39**	**-1786.36**	**2200.17**	**-125.7**	**-0.584**	**-0.812**	0.812	-0.584
aBA	20.97	1786.36	1786.48	89.3	0.012	1.000	-1.000	0.012
alt	**x comp**	**y comp**	**mag**	**angle**	**i**	**j**	**i**	**j**
rB=	**-17.70**	**2.00**	**17.81**	**173.6**	**-0.994**	**0.112**	-0.112	-0.994
rA=	**3.15**	**4.51**	**5.50**	**55.0**	**0.574**	**0.819**	-0.819	0.574
rBA=	-20.85	-2.51	21.00	-173.1	-0.993	-0.119	0.119	-0.993
vB	**82.53**	**0.00**	**82.53**	**0.0**	**1.000**	**0.000**	0.000	1.000
vA	**90.11**	**-63.09**	**110.00**	**-35.0**	**0.819**	**-0.574**	0.574	0.819
vBA	-7.58	63.09	63.55	96.9	-0.119	0.993	-0.993	-0.119
aB	**-1305.36**	**0.00**	**1305.36**	**180.0**	**-1.000**	**0.000**	0.000	-1.000
aA	**-1284.39**	**-1786.36**	**2200.17**	**-125.7**	**-0.584**	**-0.812**	0.812	-0.584
aBA	-20.97	1786.36	1786.48	90.7	-0.012	1.000	-1.000	-0.012

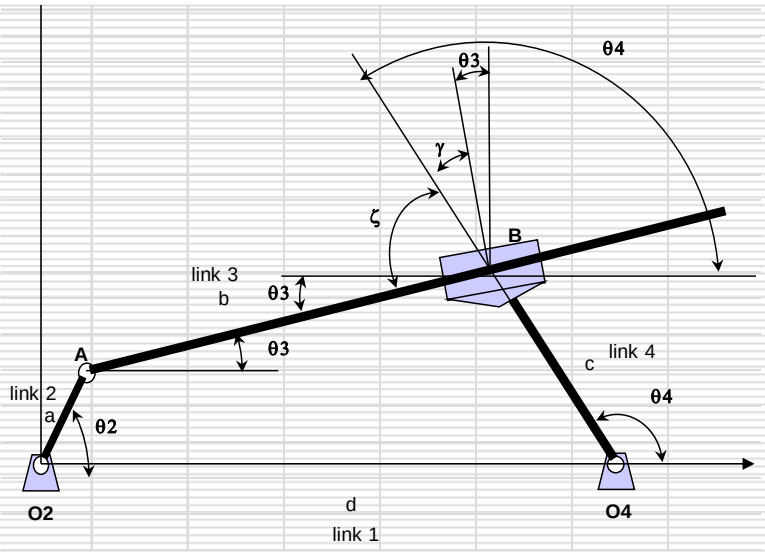
TYPE II: (RRRP)

Inverted Slider Crank Linkage



Slider Crank Algorithm
Inputs and Initial Results

a=	10	Link 2	
c=	6	Link 4	
d=	3	Link 1	
$\theta_2 =$	45		
γ=	45		
$\dot{\theta}_2 =$	100	$1/s$	
$\ddot{\theta}_2 =$	-65	$1/s^2$	
b=	2.73		-11.21
$\theta_4 =$	46.40		163.74
$\theta_3 =$	-88.60		28.74
$\dot{\theta}_4 =$	98.95		137.74
$\dot{\theta}_3 =$	98.95		137.74
b-dot=	304.37		-304.37
$\ddot{\theta}_4 =$	-4276.32		-4588.65
$\ddot{\theta}_3 =$	-4276.32		-4588.65
b-dotdot=	16946.79		-16946.79



ζ=	135
K1=	-7.878679656
K2=	2.121320344
K3=	4.242640687

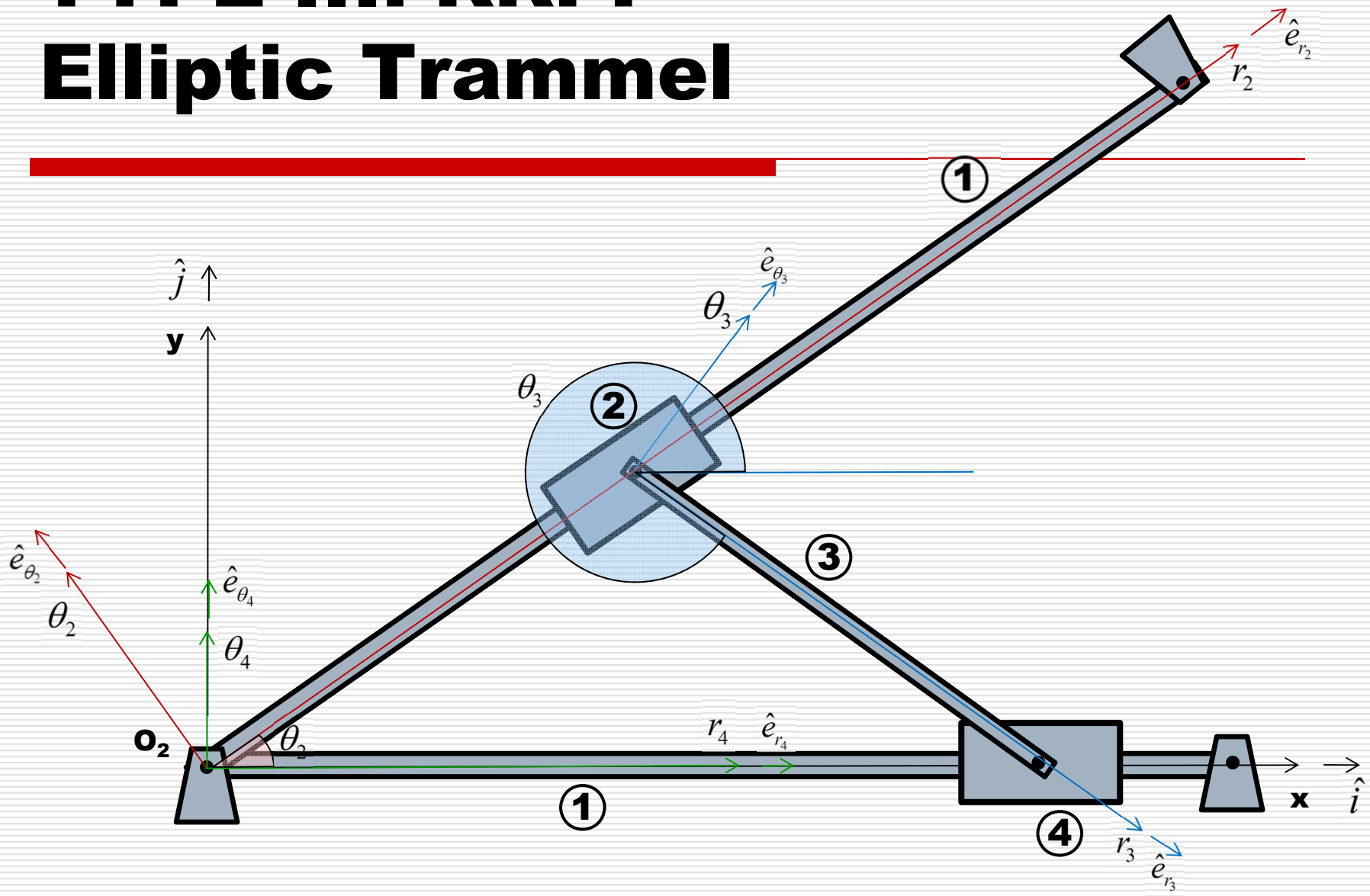
Slider Crank Algorithm (OPEN) Acceleration Vector Analysis

					e_r		e_θ	
	x comp	**y comp**	**mag**	**angle**	**i**	**j**	**i**	**j**
rO4=	**3.00**	**0.00**	**3.00**	**0.0**	**1.000**	**0.000**	0.000	1.000
rA=	**7.07**	**7.07**	**10.00**	**45.0**	**0.707**	**0.707**	-0.707	0.707
rBA=	0.07	-2.73	2.73	-88.6	0.024	-1.000	1.000	0.024
rBO4=	4.14	4.35	6.00	46.4	0.690	0.724	-0.724	0.690
rB=	**7.14**	**4.35**	**8.36**	**31.3**	**0.854**	**0.520**	-0.520	0.854
vA=	**-707.11**	**707.11**	**1000.00**	**135.0**	**-0.707**	**0.707**	-0.707	-0.707
vBA=	277.17	-297.69	406.75	-47.0	0.681	-0.732	0.732	0.681
vB=	**-429.93**	**409.42**	**593.69**	**136.4**	**-0.724**	**0.690**	-0.690	-0.724
aA=	**-70251.06**	**-71170.30**	**100002.11**	**-134.6**	**-0.702**	**-0.712**	0.712	-0.702
aBA=	48320.71	10934.97	49542.55	12.8	0.975	0.221	-0.221	0.975
aB=	**-21930.35**	**-60235.33**	**64103.32**	**-110.0**	**-0.342**	**-0.940**	0.940	-0.342

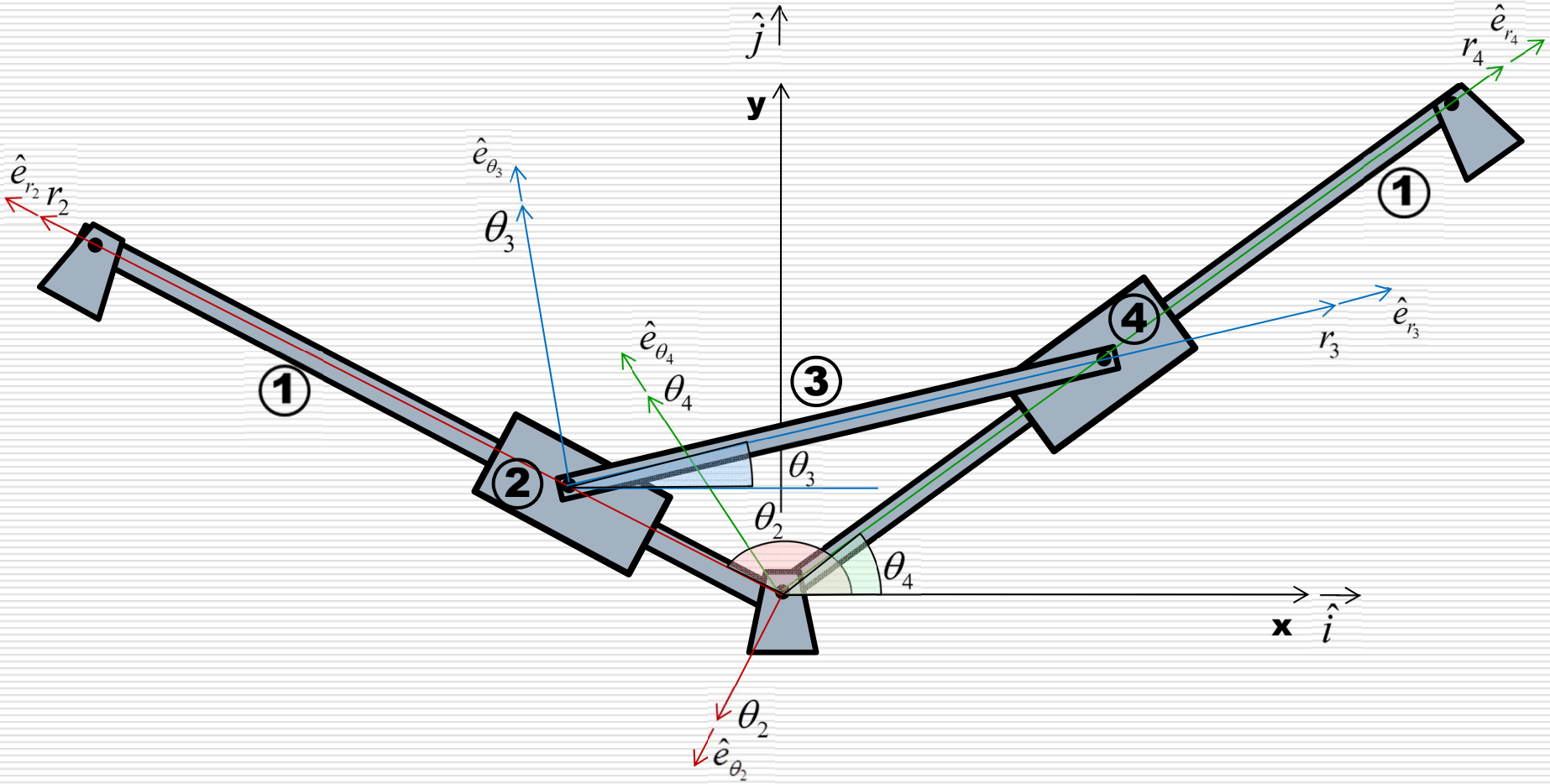
Slider Crank Algorithm (CLOSED) Acceleration Vector Analysis

alt	x comp	y comp	mag	angle	i	j	i	j
rO4=	**3.00**	**0.00**	**3.00**	**0.0**	**1.000**	**0.000**	0.000	1.000
rA=	**7.07**	**7.07**	**10.00**	**45.0**	**0.707**	**0.707**	-0.707	0.707
rBA=	-9.83	-5.39	11.21	-151.3	-0.877	-0.481	0.481	-0.877
rB04=	-5.76	1.68	6.00	163.7	-0.960	0.280	-0.280	-0.960
rB=	**-2.76**	**1.68**	3.23	148.7	-0.854	0.520	-0.520	-0.854
vA=	**-707.11**	**707.11**	**1000.00**	**135.0**	**-0.707**	**0.707**	-0.707	-0.707
vBA=	475.68	-1500.50	1574.09	-72.4	0.302	-0.953	0.953	0.302
vB=	**-231.42**	**-793.39**	**826.46**	**-106.3**	**-0.280**	**-0.960**	0.960	-0.280
aA=	**-70251.06**	**-71170.30**	100002.11	-134.6	-0.702	-0.712	0.712	-0.702
aBA=	187244.61	65723.78	198444.35	19.3	0.944	0.331	-0.331	0.944
aB=	116993.55	-5446.51	117120.26	-2.7	0.999	-0.047	0.047	0.999

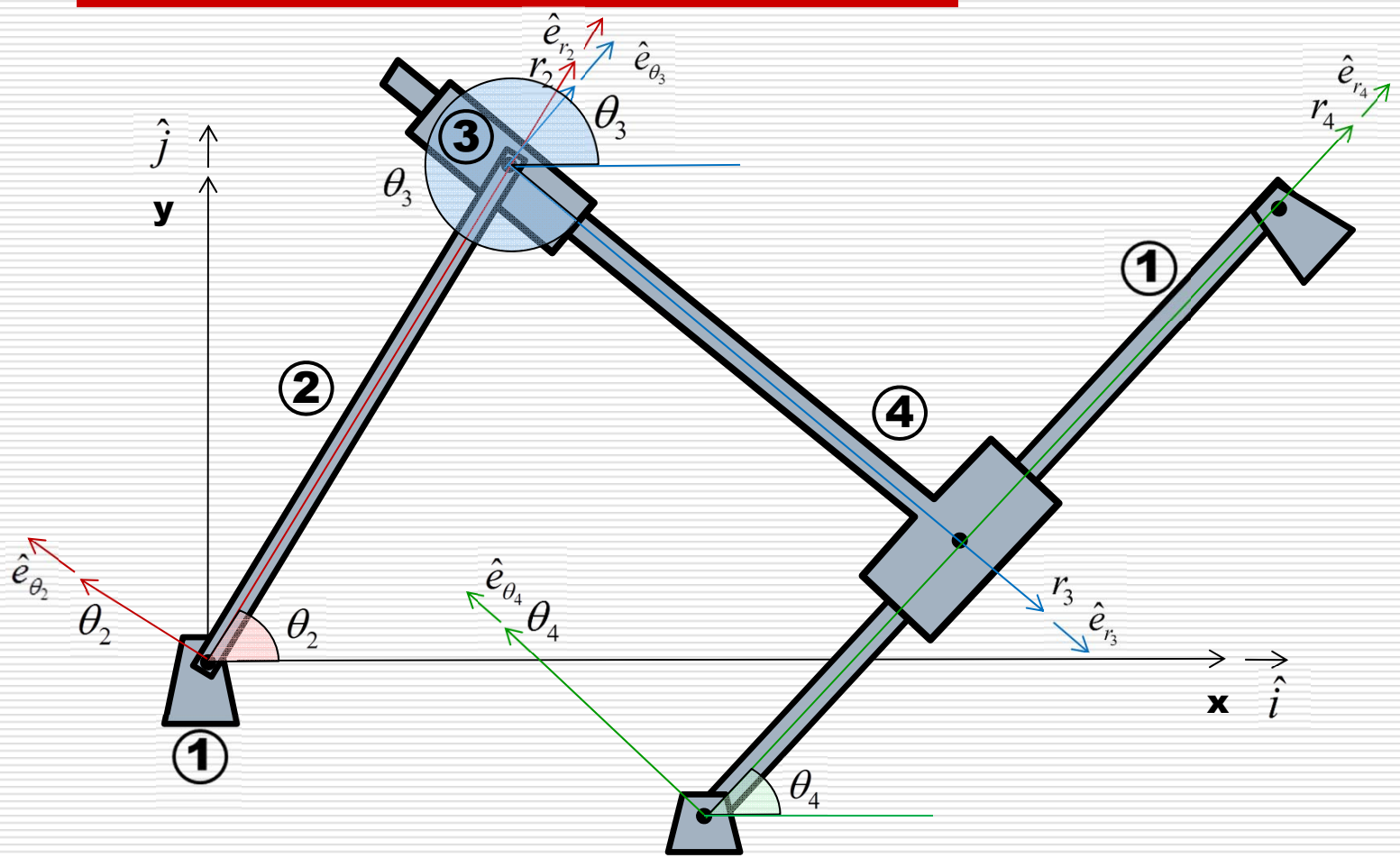
TYPE III: RRPP
Elliptic Trammel



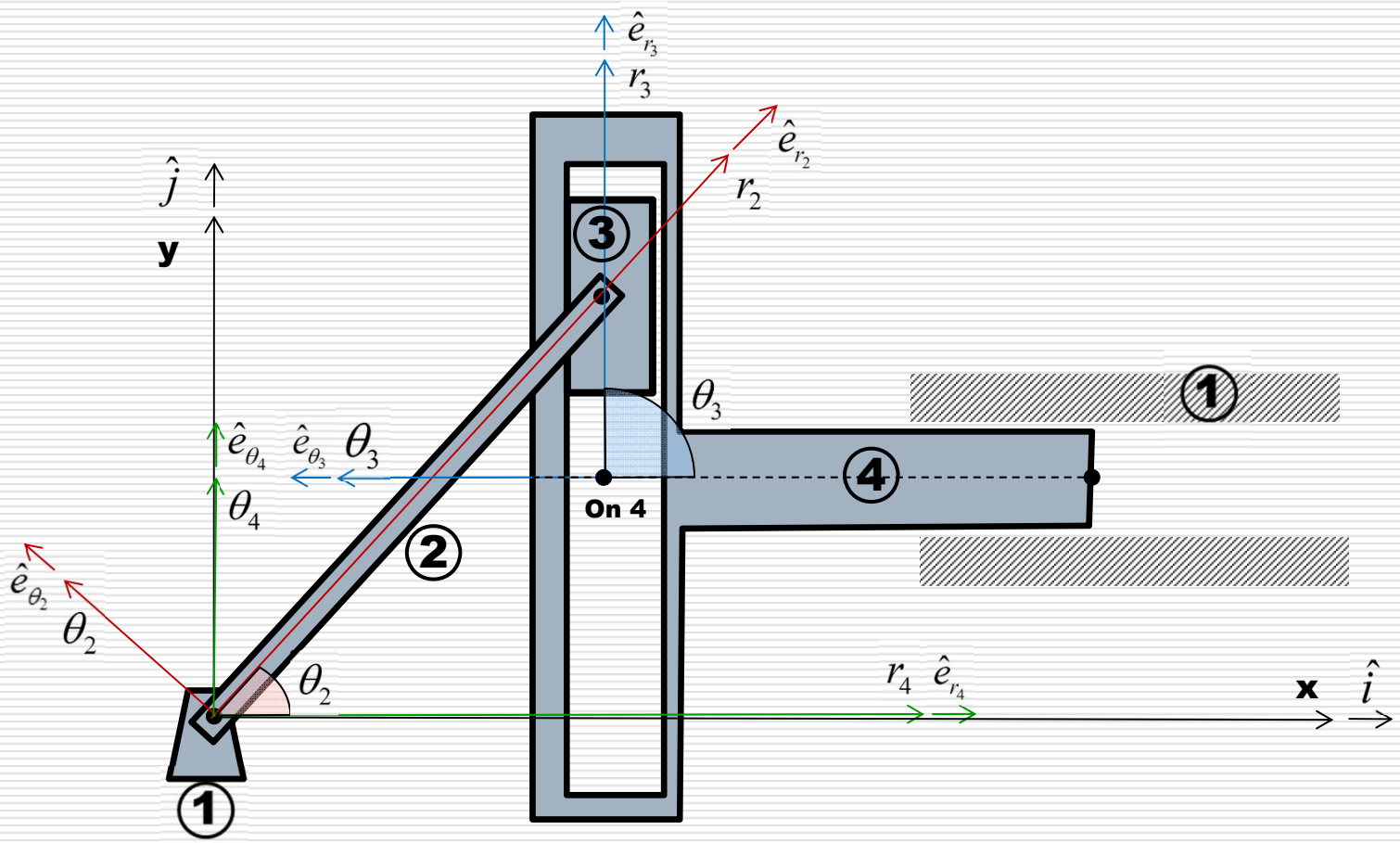
Type III: RRPP
Elliptic Trammel



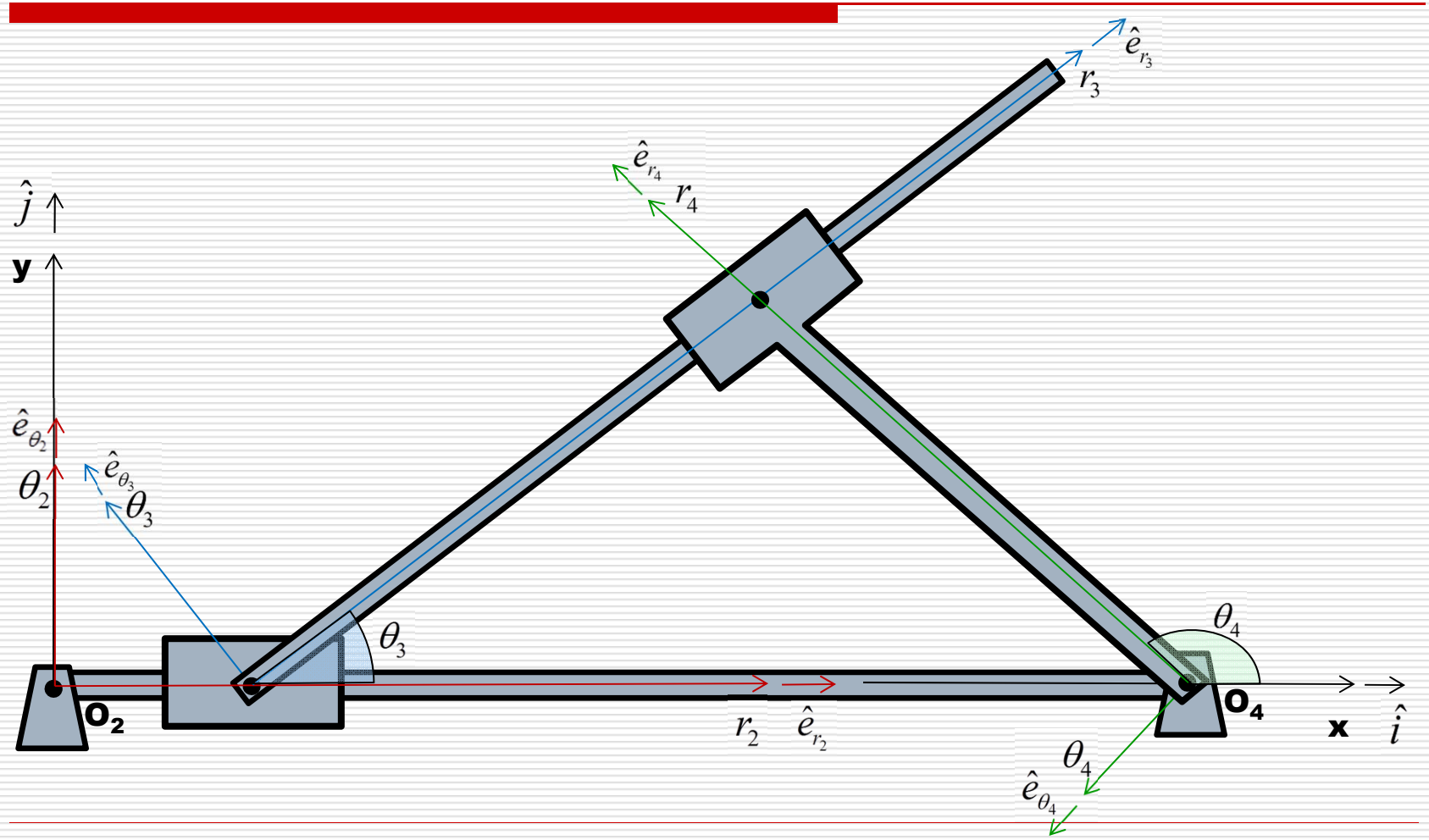
Type III: RRPP
Elliptic Trammel



Type III: RRPP
Elliptic Trammel: Scotch Yoke



Type IV: RPRP
Rapson Slide Linkage



Example 1

Rods "*R*" and "*L*" are pinned at "O" and "O'" to a frame. Rod "*L*" is also pinned to the slotted body "*B*" at "B". ?The upper end of "*R*" is pinned at P to a roller that moves freely in the slot of "*B*". The angular velocities of the rod "*R*" and link "*L*" are constants:

ω_R=-0.2 rad/s

ω_L=-0.4 rad/s

Determine the velocity of "P" and the angular velocity of "B" at the given instant.

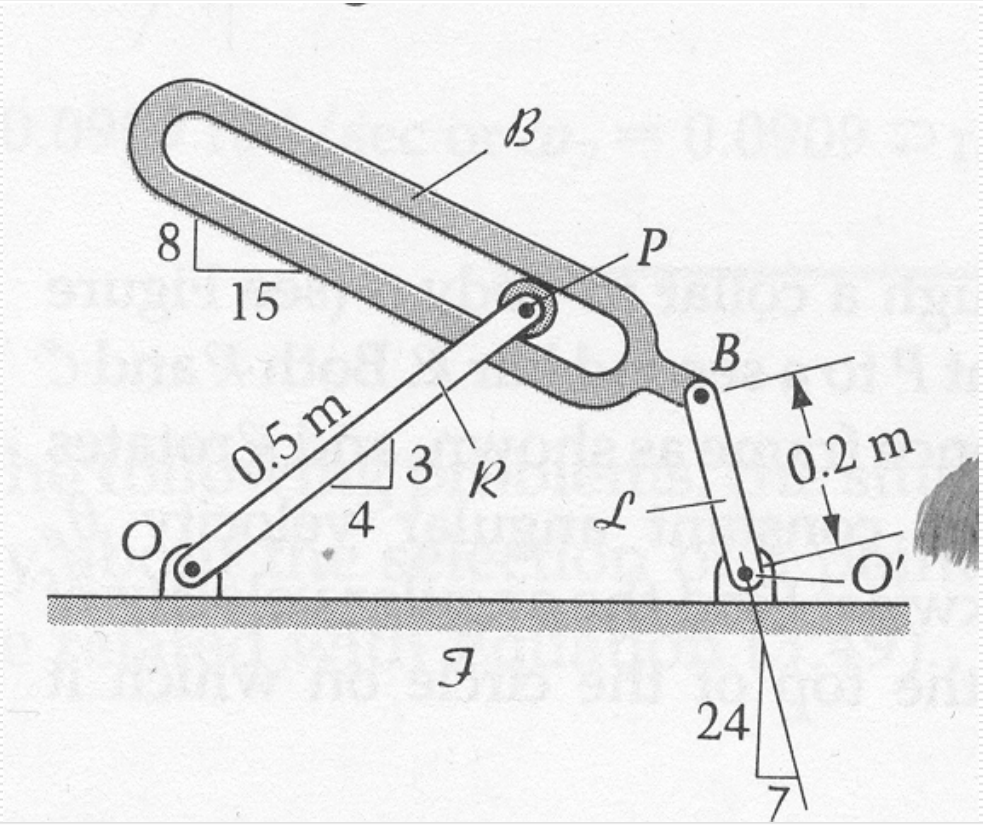
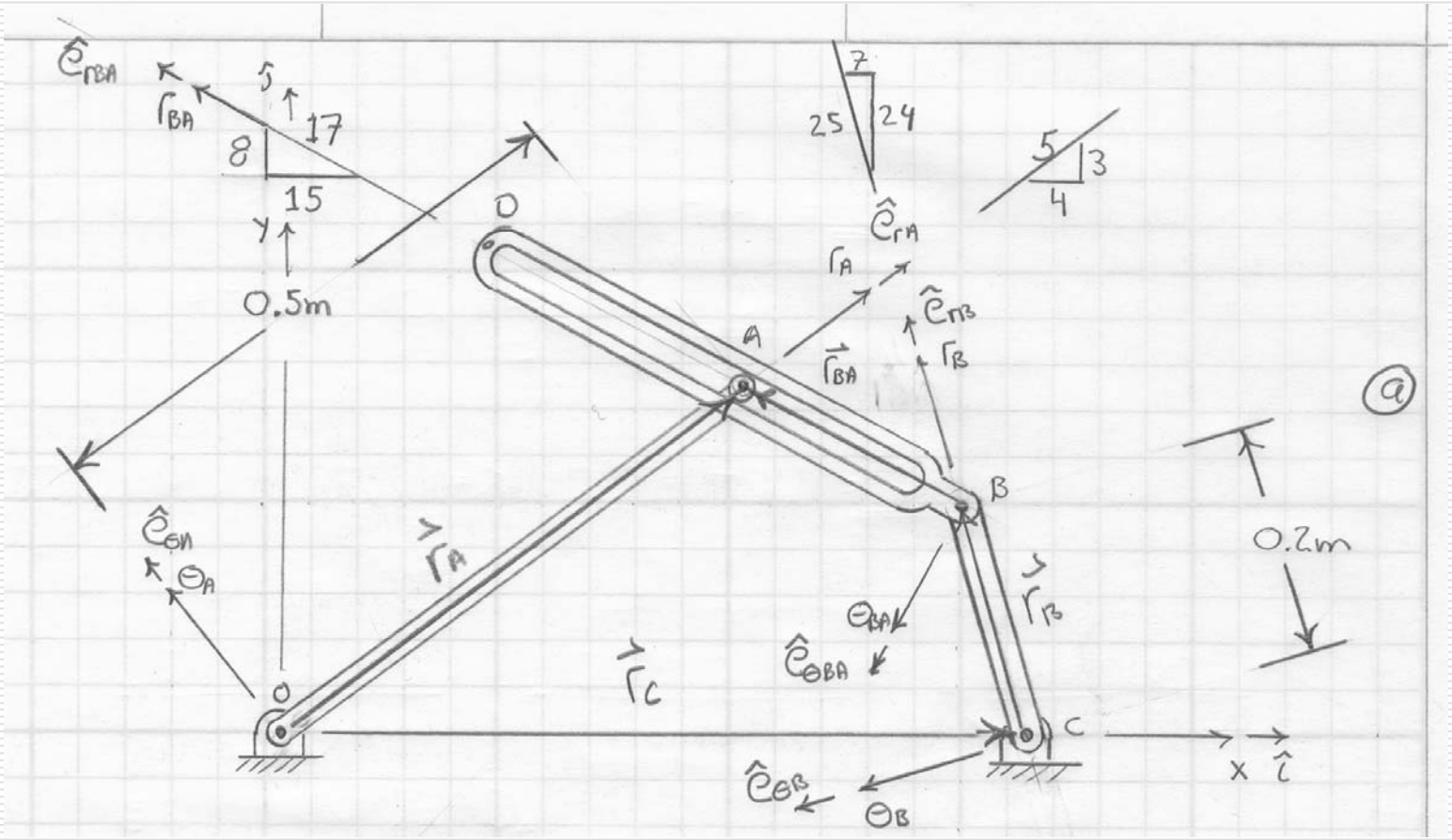


Diagram of Problem



Problem Geometry