22-141 50 SHEETS 22-142 100 SHEETS 22-144 200 SHEETS Problem 7 | Construct the shehr force, Bending moment, curvature and deflection diagrams for this beam. Using the singularity functions discussed in class, write expressions for the shear force, bending moment, curvature, and deplection of the BEAM.

GIVEN: Constraint:

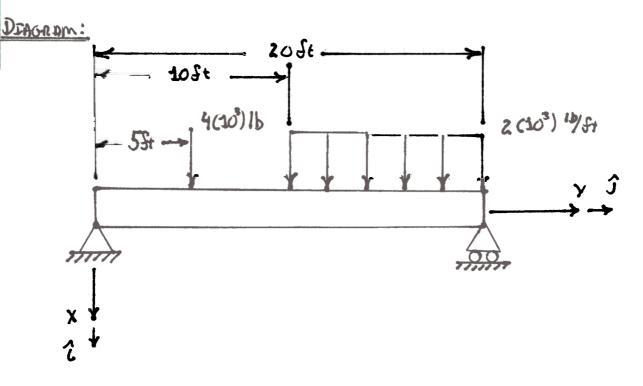
- 1. ZOST BEAM THAT IS PINNED ON ON EMD AND SUPPORTED BY POLLERS ON THE OTHER
- 2. ZC109 16/FT DISTRIBUTED WAD OUTER HALF THE BEAM
- 3. 4(10) ID WAD APPLIED AT A QUATER SPAN ON THE SIDE WITHOUT THE DISTRIBUTED WAD.

Assum PTIONS:

- 1. The Beam Responds In a linear-elastic manner
- 2. THE DEFORMATION IN THE BEAM IS CONSTOENED SMACL
- 3. Strains in the Beam are small
- 4. PINS IN JOINTS ARE PRICTICULESS
- 5. Peller Josny Is precedonless

FINO:

1. Draw shear, bending moment, curvature, and daptecticn diagrams. 2. Write Byressions for the shear, bending moment, corvitors and dievetten diagrams.



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## SOLUTION: STARTING WITH THE CONSTRUCTION OF THE DEAGRAMS. 21/20 = Ax+Bx + 4(10)16 + 20(10)16 200000 2 5d1(602)4 2(103) 1/5+ €5\$t → 0 = Ax+Bx + 24(103)16 () ZMZ/04 =0 = - (55+)- (4x1316) - 16x10 10 C -15fr-20x1016+ 20fr-8x 1-8×103162 Bx = (55+)-(4210 16)+(155+)-(2010)15 1 250 A [BID] Bx=16(103)16 From (1) Ax = - (-16x10316) - 24x10316 LAND ST 64 = -8×1031P 60

STARTING WITH THE CLOSED FORM SOLUTION

$$q(y) = -8(10^{3})|b(y-0)|_{1} + 4(10^{3})|b(y-5)|_{1}$$

$$+ 2(10^{3})|b(y-10)|_{1} + 4(10^{3})|b(y-5)|_{1}$$

$$V(y) = \int -g(y) dy = 8(10^3) |b \langle y - 0 \rangle^0 - 4(10^3) |b \langle y - 5f + \rangle^0$$

$$- 2(10^3) \frac{b}{f +} \langle y - 10 + 1 \rangle^1 + 16(10^3) |b \langle y - 20 + 1 \rangle^0$$

$$M(y) = \int V(y) dy = 8(10^3) |b| \langle y-0 \rangle^2 - 4(10^3) |b| \langle y-5f_1 \rangle^2 - 10(10^3) |b| \langle y-10f_1 \rangle^2 + 16(10^3) |b| \langle y-20f_1 \rangle^3$$

$$U(y) = \int \Theta dy = \frac{1}{EI} \left[ \frac{4}{3} \cdot (10^{3}) | b < y - 0 \rangle^{3} + \frac{2}{3} (10^{3}) | b < y - 55 + \rangle^{3} + \frac{12}{10} (10^{3}) \frac{1}{5} < y - 10 \frac{1}{5} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10^{3}) | b < y - 20 + \gamma^{3} + \frac{2}{3} (10$$

FROM THE BOOWDARY CONDITION U(O)=0

Now considering the SECOND BOUNDARY CONDITION

(L(20ft) = 0 = 
$$\frac{1}{12} \left[ -\frac{4}{12} (10^3) \text{lb} \cdot (20ft)^3 + \frac{2}{3} (10^3) \text{lb} (20ft - SFt)^3 + \frac{10}{12} (10^3) \frac{1}{57} \cdot (20ft - 10ft)^4 - \frac{9}{5} (10^3) \text{lb} (20ft - 20ft)^3 + G \cdot 20ft \right]$$

 $C_{1} = \frac{4(163)16 \cdot (2054)^{3} - \frac{2}{3}(10^{3})16 \cdot (2054 - 1054)^{3} + \frac{2}{3}(10^{3})16 \cdot (2054 - 2054)^{3}}{2054}$   $= 4.167(10^{3})16 \cdot 54^{3}$ 

NOW THE COMPLETE EXPRESSION FOR THE CURVATURE AND DEELECTION CAN BE WRITTEEN

$$\Theta(y) = \frac{1}{ET} \left[ -\frac{4(10^3)}{16} \cdot (y-0)^2 + 2(10^3)}{16} \cdot (y-55t)^2 + \frac{10}{3}(10^3) \frac{1}{5} + (y-105t)^3 - 8(10^3)}{16} \cdot (y-205t)^2 + \frac{1}{3}(10^3) \frac{1}{5} + (y-105t)^3 + \frac{1}{3}(10^3) \frac{1}{5} + (y-105t)^3 + \frac{1}{3}(10^3) \frac{1}{5} + (y-105t)^3 + \frac{1}{3}(10^3) \frac{1}{5} + \frac{1}{3}(10^3) \frac{1$$

$$U(Y) = \frac{1}{61} \left[ -\frac{4}{3} (10^3) | b(y-0)^3 + \frac{3}{3} (10^3) | b(y-5f_1)^3 + \frac{12}{12} (10^3) | b(y-10f_1)^4 \right] -\frac{8}{3} (10^3) | b(y-20f_1)^3 + 4.167(10^3) | b(f_1)^3 \cdot y$$

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