COMP8620: MC-AIXI-CTW Group 3

Jarryd Martin, John Aslanides, Yadunandan Sannappa, Nrupendra Rao, Cheng Yu, Ryk Budzynski

October 2015

Abstract

We outline an implementation of Veness et al.'s Monte Carlo AIXI approximation[?] (MC-AIXI-CTW), and report our simulation results on a number of toy domains.

Contents

1 Introduction							
2 User Manual							
3	MC 3.1	C-AIXI-CTW Implementation Agent-environment interaction loop	2 2				
	3.2	Monte Carlo Tree Search (MCTS) Algorithm	3				
	0.2	3.2.1 High level description	3				
		3.2.2 Class structure	3				
		3.2.3 Other Considerations	3				
		3.2.4 Efficiency/performance	4				
	3.3	Context Tree Weighting (CTW)	4				
	0.0	3.3.1 High level description of algorithm	4				
		3.3.2 Class structure	4				
		3.3.3 Code snippets	4				
		3.3.4 Efficiency/performance	4				
4	Env	vironments	4				
	4.1	Cheese Maze	4				
	4.2	Extended Tiger	4				
	4.3	Tic-Tac-Toe	5				
	4.4	Biased Rock-Paper-Scissors	6				
	4.5	PacMan	6				
5	Exp	periments	6				
	5.1	Experimental Setup	6				
	5.2	Experiment Summary	6				
	5.3	Cheesemaze	7				
	5.4	Extended Tiger	7				
	5.5	TicTacToe	8				
	5.6	Biased Rock-Paper-Scissors	9				
	5.7	Pacman	9				
6	Cro	oss Domain Simulation Results	10				

7	Discussion and Conclusions	10
A	Files	10
В	Graphs	11

1 Introduction

Recall that the AIXI agent is defined by its actions, which for each cycle k are given by

$$a_k^{\text{AIXI}} = \arg\max_{a_k} \sum_{o_k r_k} \cdots \max_{a_m} \sum_{o_m r_m} \left[r_k + \cdots + r_m \right] \xi \left(o_1 r_1 \dots o_m r_m | a_1 \dots a_m \right),$$

where the o_n and r_n are the observation and reward provided by the environment at cycle n, and ξ is a Bayesian mixture model for the environment.

Following Veness et al., we approximate a_k^{AIXI} using Monte Carlo tree search (upper confidence bound) to approximate the expectimax, and we compute a mixture over variable-order Markov models using the context-tree weighting algorithm.

We present a lightweight C++ implementation of MC-AIXI-CTW, along with implementations of a number of simple games: Pacman, Tic-Tac-Toe, Biased Rock-Paper-Scissor, Extended-Tiger, and Cheesemaze.

2 User Manual

15: end while

To build from source on linux, run g + + - std = c + +0x * .cpp - o aixi **TODO** check To run, invoke ./aixi \$ENVNAME.conf.

3 MC-AIXI-CTW Implementation

3.1 Agent-environment interaction loop

For each agent-environment interaction cycle, we run the following for each experiment (see Algorithm ??):

```
Algorithm 1 Main loop.
 1: while cycle < max cycles do
2:
       while environment is not finished do
           generate (o, r) from environment
3:
          update agent model with (o, r)
4:
5:
          if explore then
              a \leftarrow randomAction()
6:
7:
          else
              a \leftarrow MCTS()
                                                                                                 ⊳ Monte Carlo Tree Search
8:
          end if
9:
          perform action a
10:
           update agent history with a
11:
12:
           cycle + +
13:
       end while
       reset environment
14:
```

The MCTS algorithm follows as in Algorithms 1-4 in Veness et al., and is found in search.cpp. Model updates are handled in methods in agent.cpp, which interfaces with the context tree defined in predict.cpp.

3.2 Monte Carlo Tree Search (MCTS) Algorithm

3.2.1 High level description

Since the environment is only partially observable, we have no explicit notion of state; instead, we only have a history of actions and percepts $h = (a_1 o_1 r_1 \dots a_n o_n r_n)$. For the purposes of choosing the optimal action, we treat each possible (hypothetical) history as a node in the search tree, with the root being the tip of the current (realised) history.

The search tree is comprised of alternate layers of decision nodes and chance nodes with the root being a decision node. The maximum branching possible from decision nodes is the number of available actions in the given environment while the maximum branching possible from chance nodes is equal to the number of possible observations times the number of possible rewards. We do however restrict branching in general to 100 to avoid memory issues. This number is configurable in search.cpp.

Each node is implicitly labelled by its history as chance nodes record the hypothetical action taken while decision nodes record the hypothetical observation and reward from the environment. The expected value of each node in the search tree is equal to the expected total (non-discounted) reward that would be accumulated from that node, where the expectation is under the agent's current policy and the agent's current model for the behavior of the environment.

Thus, for each node we keep a value estimate \hat{V} , and a count of the number of times T that node has been visited in search. This is used to determine how we explore the search space using the UCB algorithm, which, for each decision node picks (assuming T(ha) > 0 for all actions)

$$a_{\text{UCB}} = \arg\max_{a \in \mathcal{A}} \left\{ \frac{1}{m\left(\beta - \alpha\right)} \hat{V}\left(ha\right) + C\sqrt{\frac{\log T\left(h\right)}{T\left(ha\right)}} \right\},\,$$

where \mathcal{A} is the set of all permissible actions, m is the search horizon, $\beta - \alpha$ is the difference between the minimal and maximal instantaneous reward, and C is a parameter controlling the propensity of the agent to explore less frequently-seen histories.

Note that the expectimax is a stochastic, partially observable game between the agent and its environment. In the following, call nodes corresponding to agent moves 'decision nodes', and nodes corresponding to Nature's moves 'chance nodes'.

3.2.2 Class structure

To represent our search nodes, we define a base SearchNode class, from which ChanceNode and DecisionNode inherit. ChanceNode and DecisionNode each have a sample method defined on them; each of these methods is mutually recursive. For a given node n, we keep its children in a dictionary keyed on the action or (observation,reward) used to generate each child.

3.2.3 Other Considerations

In addition to the psuedocode presented in Veness et al., we implemented a solution to allow us to decide on a per cycle basis whether or not to build a search tree from scratch. In addition, we constructed routines which given an action taken by the agent and an observation/reward received from the environment, would prune the search tree accordingly.

The pruning of the search tree removes all subtrees begining with the chance nodes directly below the root which correspond to the actions not taken by the agent and as such are impossible future paths. Additionally, all subtrees begining with descision nodes below the chance node (corresponding to the action taken) that do not match the observation/reward received from the environment are pruned. As cycles progress throughout an experiment, this represents a significant reduction in memory consumption.

Our final solution however did not implement pruning as our experimental results showed unusual behaviour whereby the agent would appear to get stuck in certain game states.

3.2.4 Efficiency/performance

Between calls to search, we retain much of the search tree, pruning those nodes that are now inaccessible from the realised (a, o, r) tuple that happened during the cycle. This allows us to avoid re-generating similar search trees from similar positions.

- 3.3 Context Tree Weighting (CTW)
- 3.3.1 High level description of algorithm
- 3.3.2 Class structure
- 3.3.3 Code snippets
- 3.3.4 Efficiency/performance

4 Environments

To test the effectiveness of the agent we developed 5 environment simulations which range in complexity from the relatively simple cheese maze to the much more complicated partially observable pacman game. The details of these environments with respect to their behaviour and implementation is discussed below. For all environments to avoid negative rewards to the agent we have added a constant to all rewards such that the minimum reward received by the agent is 0. Since the difference between the rewards is the same this will not affect the behaviour of the agent in any way.

4.1 Cheese Maze

This is a environment in which the agent is a mouse trying to find a piece of cheese in an two dimensional maze. The actions of the agent are:

Action	Code
Move Up	0
Move Right	1
Move Left	2
Move Down	3

The rewards have been adjusted as

Action effect	Reward
Agent bumps into wall	0
Agent moves into free cell	9
Agent finds cheese	20

The details of the maze and the starting positions of the agent and the cheese are read from the configuration file. The maze is represented as the list of nodes as they would be visited by the depth first search algorithm. Mouse position and cheese position are simply the order of the node.

Each node of the maze is a structure which stores the percept of that node and an array of pointers which point to its neighbours. In case there is a wall on a particular side of the node then that pointer will be NULL.

In terms of an optimal agent strategy, an upper bound on reward per cycle for Cheesemaze is 2 given that the best possible reward for an episode is 8 and there are a minimum of 4 moves (including the start) to reach the goal state.

4.2 Extended Tiger

This environment simulates two doors. At the start of each game the tiger is behind one of the doors with probability of 0.5 and behind the other door, there is a pot of gold. The agent begins sitting down and it can perform the following actions:

Action	Code
Stand	0
Listen	1
Open left door	2
Open right door	3

When the agent tries to listen the environment provides it with an observation which correctly describes where the tiger is with a probability as defined in the configuration file. Until the listen action is performed the observation remains 0.

Observation	\mathbf{Code}
Agent has not performed listen action yes	0
Tiger behind left door	1
Tiger behind right door	2

The rewards the agent receives in this environment are as follows

State	Action	Reward
sitting	stand	99
sitting	open door	90
sitting	listen	99
standing	stand	90
standing	open door with tiger	0
standing	open door with gold	30
standing	listen	90

In terms of an optimal agent strategy, an upper bound on reward per cycle for Extended Tiger is derived as follows. Firstly note that an optimal strategy will be to start, listen n times, stand, open. Letting a false observation probability be q, we wish to maximise the following w.r.t. n

$$\mathbb{E}[r_{\text{avg}}] = \frac{30(1-q)^n - 100(1 - (1-q)^n) - n - 1}{n+3}$$

where the denominator is equal to the number of actions taken. For example, with q = 0.15, the optimal n is 2.

4.3 Tic-Tac-Toe

In this game, the agent plays games of TicTacToe against an opponent who makes random moves. The agent moves are coded as 0-8 referring to the different positions of the board.

$$\begin{array}{c|cccc}
0 & 1 & 2 \\
\hline
3 & 4 & 5 \\
\hline
6 & 7 & 8 \\
\end{array}$$

Observation completely describes the current state of the board using 2 bits for each cell of the board.

00 | Cell empty 01 | Agent's cell

02 | Environment's cell

The agent rewards are as follows:

Status	Reward
Illegal move	0
Game is a draw	4
Game won by agent	5
Agent lost	1

In terms of an optimal agent strategy, an upper bound on reward per cycle is 0.5 given that the minimu number of cycles required for the agent to win the game is 4.

4.4 Biased Rock-Paper-Scissors

The agent will play games of Rock-Paper-Scissors against an opponent who plays the same action every time it wins the game, and otherwise plays a random move. For this agent we encoded the actions of the agent and the environment as

The agent receives a reward of 1 for a win, 0 for a draw and -1 for a loss.

In terms of an optimal agent strategy, an upper bound on reward per cycle for Biased Rock-Paper-Scissors is derived as follows.

Let X_t be a R.V. representing the outcome of cycle t. Under an optimal strategy, the agent will win after the environment won in cycle t-1 as the environments action in cycle t is predictable. Otherwise, the agent plays randomly. As such we have

$$P(X_t = \text{win}) = \sum_{X_{t-1}} P(X_t = \text{win}, X_{t-1}) = \sum_{X_{t-1}} P(X_t = \text{win}|X_{t-1})P(X_{t-1})$$

which is a 1st order Markov chain with the following right stochastic transition matrix

$$\mathbf{P} = \begin{bmatrix} \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \\ 1 & 0 & 0 \\ \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \end{bmatrix} \tag{1}$$

Therefore, we want a steady state distribution for \mathbf{P} , i.e. a solution to $\boldsymbol{\pi} = \mathbf{P}\boldsymbol{\pi}$, which is an eigenvector $\boldsymbol{\pi}^*$. The average reward at time t is then

$$\mathbb{E}[r_{\text{avg}_t}] = 1 \cdot P(X_t = \text{win}) + 0 \cdot P(X_t = \text{draw}) - 1 \cdot P(X_t = \text{lose}) = \pi_0^* - \pi_2^* = 0.25$$

4.5 PacMan

This is game of PacMan in which the agent can only partially observe the environment unlike the classic game in which the entire game state is known to the player at any given time. The agent does not know the structure of the maze but only receives a 4 bit wall configuration of the node it is currently in. The agent also receives a 4 bit observation of the presence of any ghosts in its direct line of sight. The location of food pellets can change every episode as every free cell has a 50% chance of having food in it. The agent receives a 3 bit observation indicating the presence of food within a Manhattan distance of 2, 3 or 4. It also receives a 4 bit string indicating food in its line of sight similar to the ghosts. The agent also knows when it is under the effect of the power pill.

Action	Reward
Agent runs into a wall	-10
Agent caught by a ghost	-50
Agent moves into empty cell	-1
Agent eats a food pellet	10
Agent collects all the food	100

To calculate the actual reward, the rewards from the above table are added to 60. This is because the agent can potentially be affected by multiple rewards e.g. it can run into a wall and get caught by a ghost in the same turn.

In terms of an optimal agent strategy, an upper bound on reward per cycle for Pacman is unknown.

5 Experiments

5.1 Experimental Setup

5.2 Experiment Summary

Following is a complete summary of all experiments conducted

	Bits^1	CT-depth	Cycles	Timeout ²	Horizon	Exp. Rate	ExpDecay	UCB-weight ³
Cheesemaze	11	96	10	0.5	8	0.999	0.999769818	1.4
	11	96	10	1.6	6	0.999	0.999769818	1.4
	11	144	2.5	3	8	0.999	0.9990795899	1.4
	11	48	10	0.1	4	0.999	0.999769818	1.4
	11	96	10	0.5	8	0.999	0.999769818	1.4
Biased Rock-Paper-Scissors	6	32	10	2.5	4	0.999	0.999769818	1.4
	6	48	5	5	8	0.999	0.999539689	1.4
	6	96	4.5	4	4	0.999	0.9994885564	1.4
	6	96	10	0.5	4	0.999	0.999	1.4
Extended Tiger	13	96	16	2.5	6	0.999	0.99985613	1.4
_	13	96	2.5	12	4	0.999	0.9990795899	1.4
	13	96	25	0.8	4	0.999	0.9999079208	1.4
	13	52	5	8	4	0.999	0.999539689	1.4
Tic-Tac-Toe	25	96	4.5	4	9	0.9999	0.9994884564	1.4
	25	192	5	8	9	0.9999	0.999539599	1.4
	25	256	20	8	9	0.9999	0.9998848799	1.4
	25	512	25	3	9	0.9999	0.9999079028	1.4
	25	512	30	2	9	0.9999	0.9999232518	1.4
Pacman	26	256	10	4	8	0.99	0.999	1.5
	26	512	20	2	4	0.9999	0.9998848799	1.4
	26	320	10	4	8	0.99	0.999	1.4
	26	256	10	1	6	0.9999	0.999769773	1.4

Table 1: MC-AIXI-CTW Experiments

5.3 Cheesemaze

Here we present the environmental setup and learning rate of our best results training AIXI on the Cheesemaze environment.

Interpreting the results, we conclude that ...

B	its	CT-depth	Cycles	Timeout	Horizon	Exp. Rate	ExpDecay	UCB-weight
1	1	96	10	0.5	8	0.999	0.999769818	1.4

Table 2: Environment Setup

5.4 Extended Tiger

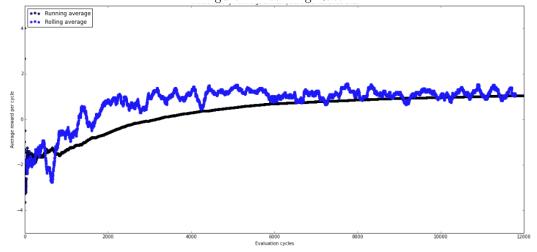
Here we present the environmental setup and learning rate of our best results training AIXI on the Extended Tiger environment.

Interpreting the results, we conclude that ...

 $^{^{1}}$ total bit length of an ora cycle

²timeout value for each select action ³UCB exploration bias parameter

Figure 1: Learning Rate



Bits	CT-depth	Cycles	Timeout	Horizon	Exp. Rate	ExpDecay	UCB-weight
11	96	10	0.5	8	0.999	0.999769818	1.4

Table 3: Environment Setup

Figure 2: Learning Rate

5.5 TicTacToe

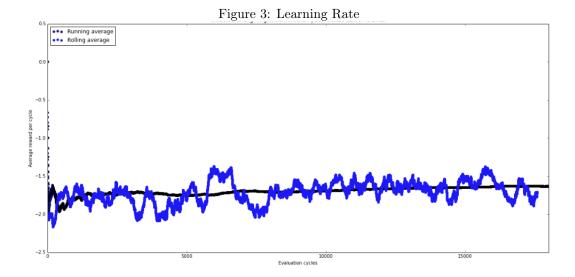
Here we present the environmental setup and learning rate of our best results training AIXI on the Tic-Tac-Toe environment.

Evaluation cycles

Interpreting the results, we conclude that ...

Bits	CT-depth	Cycles	Timeout	Horizon	Exp. Rate	ExpDecay	UCB-weight
11	96	10	0.5	8	0.999	0.999769818	1.4

Table 4: Environment Setup



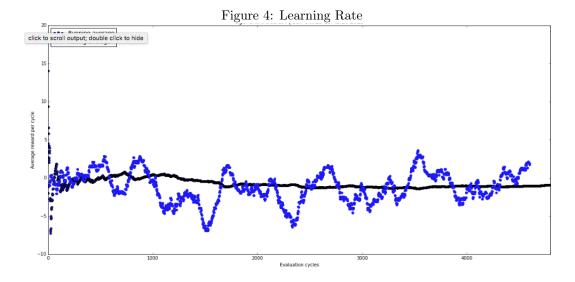
5.6 Biased Rock-Paper-Scissors

Here we present the environmental setup and learning rate of our best results training AIXI on the Biased Rock-Paper-Scissors environment.

Interpreting the results, we conclude that \dots

Bits	CT-depth	Cycles	Timeout	Horizon	Exp. Rate	ExpDecay	UCB-weight	
11	96	10	0.5	8	0.999	0.999769818	1.4	

Table 5: Environment Setup



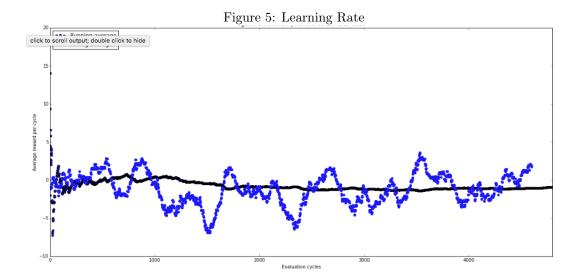
5.7 Pacman

Here we present the environmental setup and learning rate of our best results training AIXI on the Pacman environment.

Interpreting the results, we conclude that \dots

Bits	CT-depth	Cycles	Timeout	Horizon	Exp. Rate	ExpDecay	UCB-weight
11	96	10	0.5	8	0.999	0.999769818	1.4

Table 6: Environment Setup



6 Cross Domain Simulation Results

- \diamond Cheesemaze and Extended Tiger
- ♦ Cross domain simulation on more difficult environments...
- $\diamond\,$ Separate CTW for Obs and Rews...

7 Discussion and Conclusions

Appendix

A Files

The report archive should contain the following:

```
MC-AIXI-CTW-Grp3.zip
  \report
    report.pdf // this report
    report.tex
    cheesemaze_best.png // results plots
    tiger_best.png
    rockpaper_best.png
    tictactoe_best.png
    pacman_best.png
    \src
```

```
main.hpp
main.cpp
environment.hpp
environment.cpp
agent.hpp
agent.cpp
search.hpp
{\tt search.cpp}
predict.hpp
predict.cpp
util.hpp
util.cpp
{\tt README.md}
{\tt cheesemaze.conf~//~environment~configuration~files}
rockpaper.conf
tictactoe.conf
coinflip.conf
tiger.conf
```

B Graphs..