

Spin Correlations in the PanScales parton showers and jet observables

Rob Verheyen

With Alexander Karlberg, Gavin Salam, Ludovic Scyboz

2103.16526



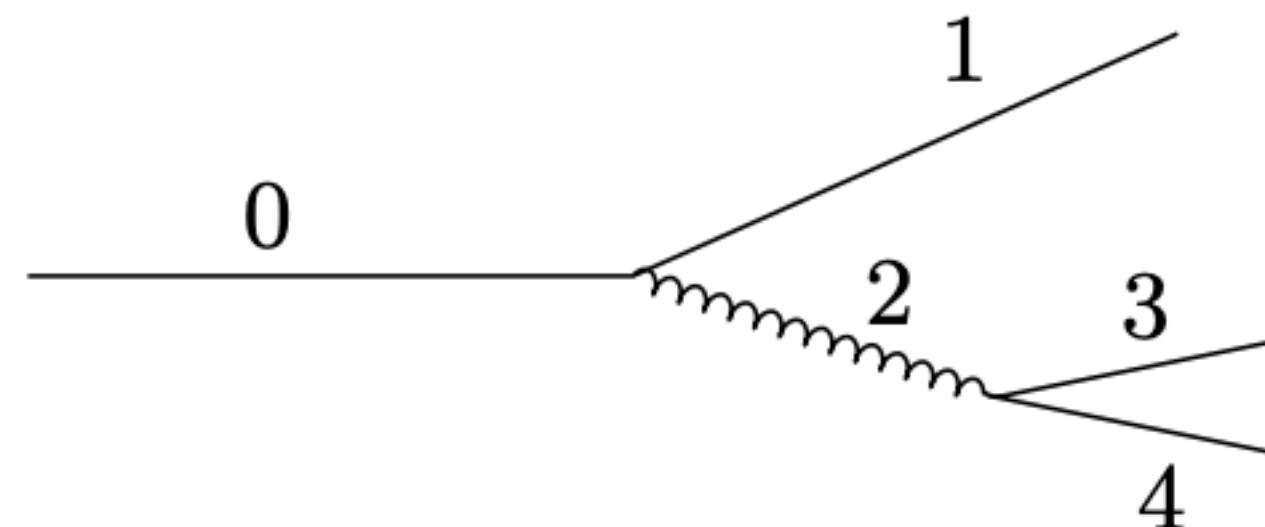
European Research Council

Established by the European Commission

Spin Correlations

PanScales NLL requirement

- Get the ME right for emissions well-separated in Lund plane
- Reproduce NLL resummations of known observables



Collinear
→

Spin interference effects



$$|M|^2 \propto \mathcal{M}_{0 \rightarrow 12}^{\lambda_0 \lambda_1 \lambda_2} \mathcal{M}_{0 \rightarrow 12}^{*\lambda_0 \lambda_1 \lambda'_2} \mathcal{M}_{2 \rightarrow 34}^{\lambda_2 \lambda_3 \lambda_4} \mathcal{M}_{2 \rightarrow 34}^{*\lambda'_2 \lambda_3 \lambda_4}$$

In QCD, spin correlations lead to azimuthal modulation of the form

$$\frac{d\sigma}{d\varphi} \propto a_0 \left(1 + \frac{a_2}{a_0} \cos(2\varphi) \right) \rightarrow \propto \alpha_s^2 L^2$$

$$\ln(\theta_1), \ln(\theta_2) > -|L|$$

$$\ln(z_1), \ln(z_2) \sim 1$$

Spin Correlations

$$|M|^2 \propto \mathcal{M}_{0 \rightarrow 12}^{\lambda_0 \lambda_1 \lambda_2} \mathcal{M}_{0 \rightarrow 12}^{*\lambda_0 \lambda_1 \lambda'_2} \mathcal{M}_{2 \rightarrow 34}^{\lambda_2 \lambda_3 \lambda_4} \mathcal{M}_{2 \rightarrow 34}^{*\lambda'_2 \lambda_3 \lambda_4}$$

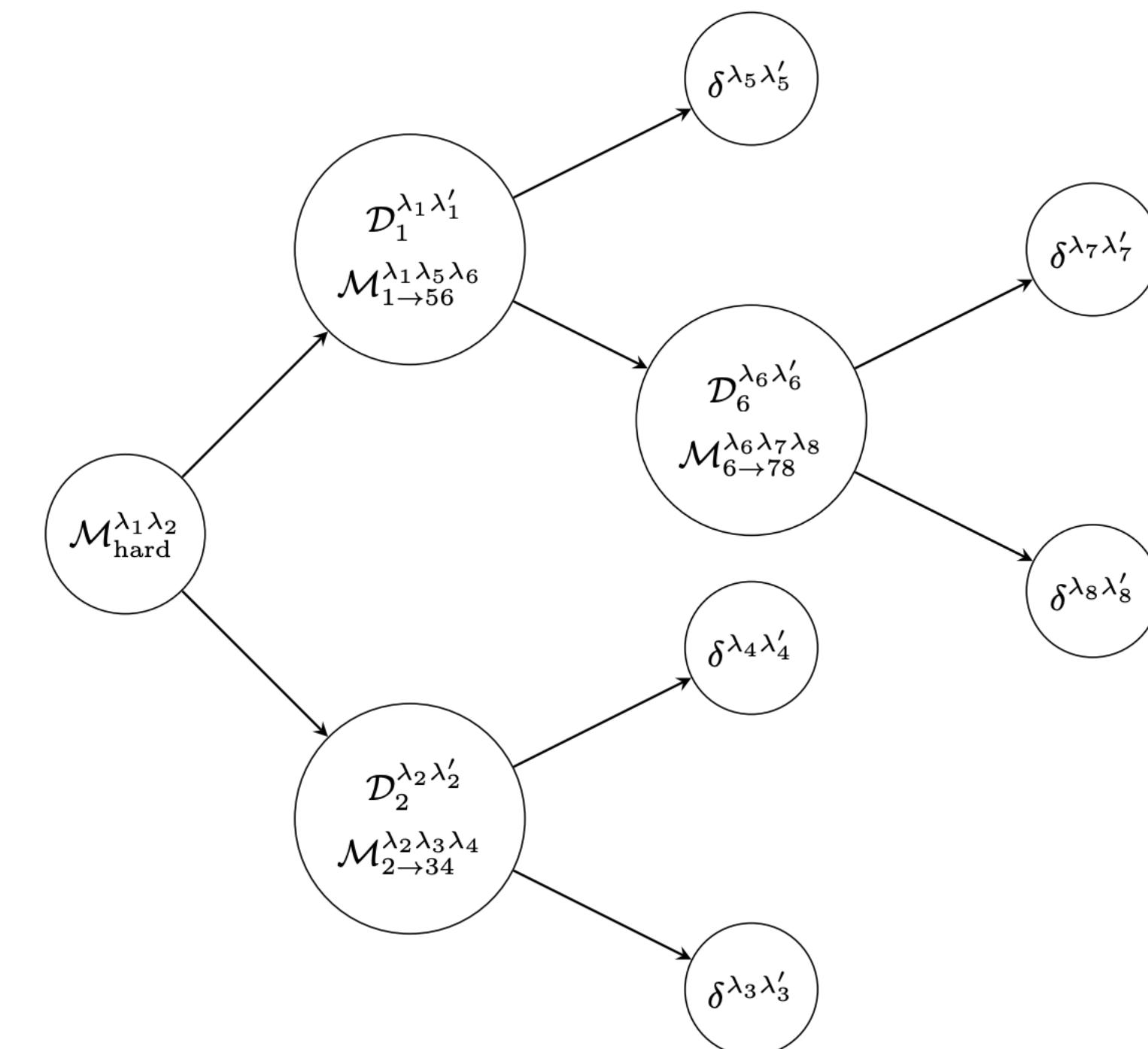
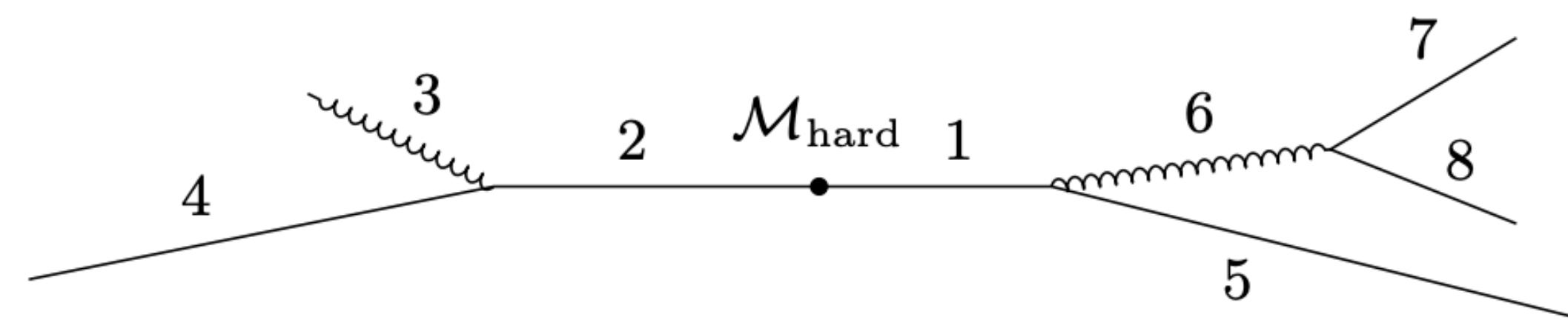
Redoing all spin index contractions at every branching is inefficient

Solution: Collins-Knowles algorithm

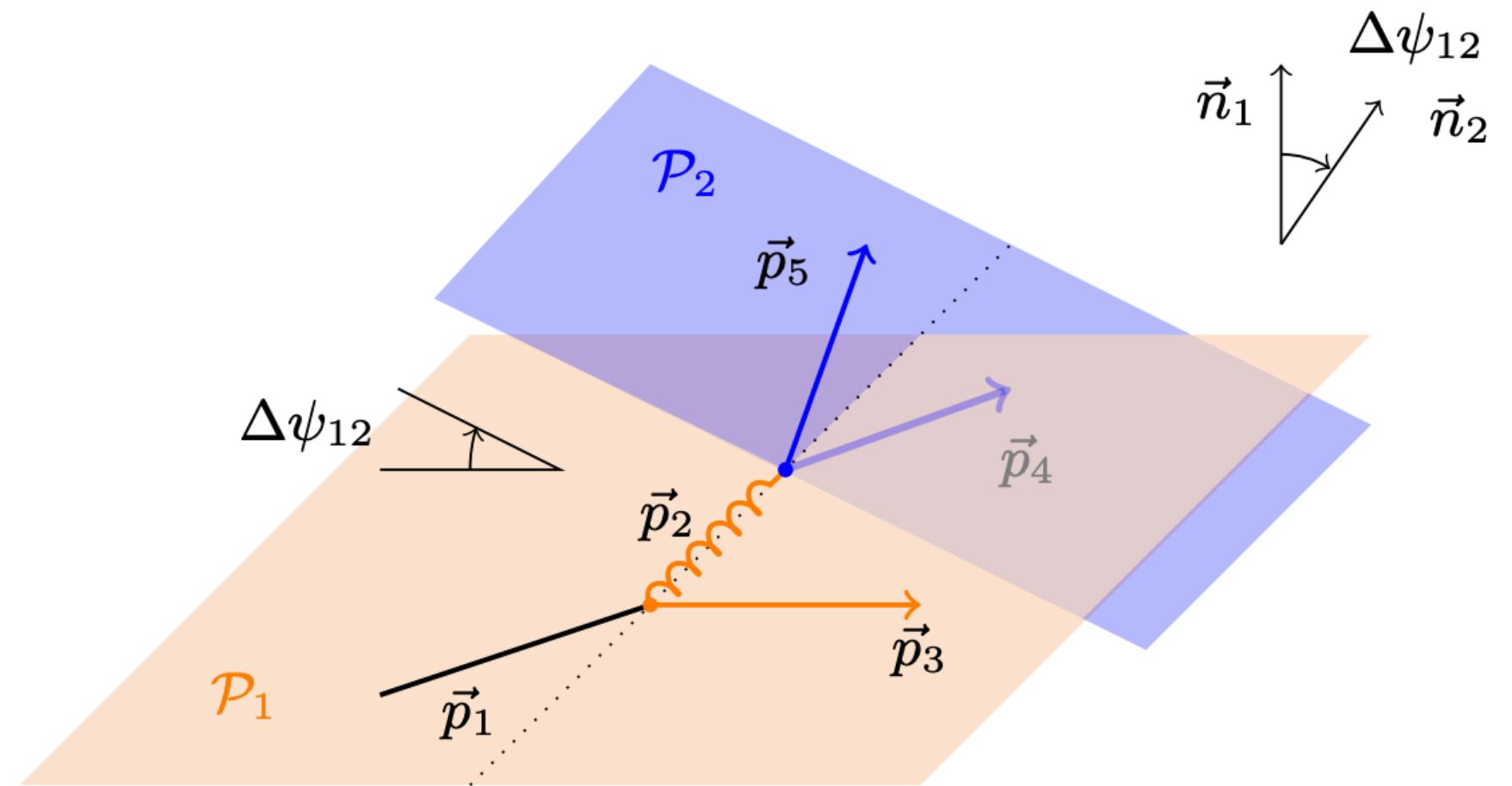
[Collins Nucl.Phys.B 304 \(1988\)](#)

[Knowles Nucl.Phys.B 304 \(1988\)](#)

[Richardson, Webster Eur.Phys.J.C 80 \(2020\)](#)



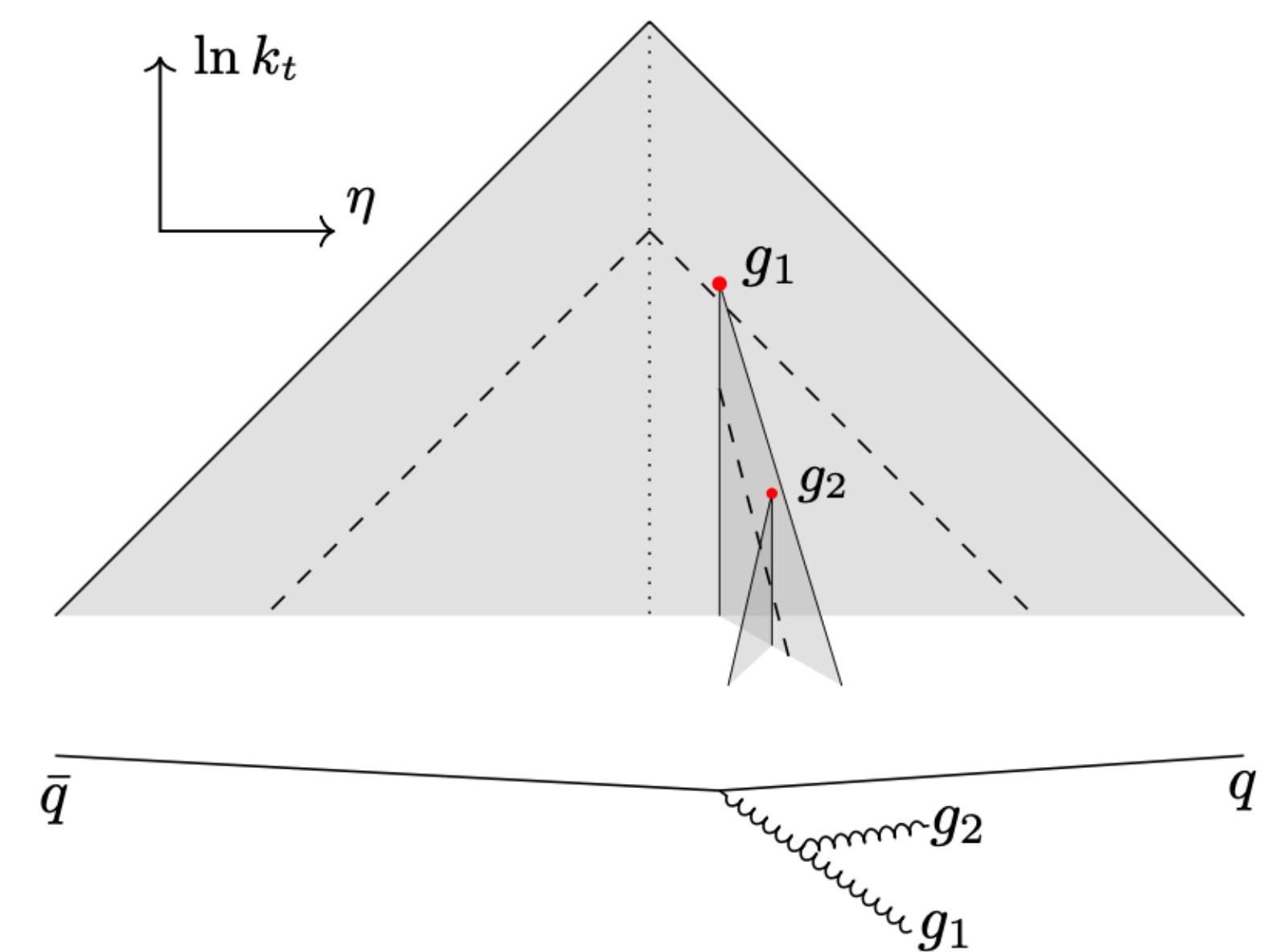
Observables: Lund Declustering



Fixed order:
Angle between the planes of two subsequent branchings

All orders: Lund jet plane [Dreyer, Salam, Soyez JHEP 12 \(2018\) 064](#)

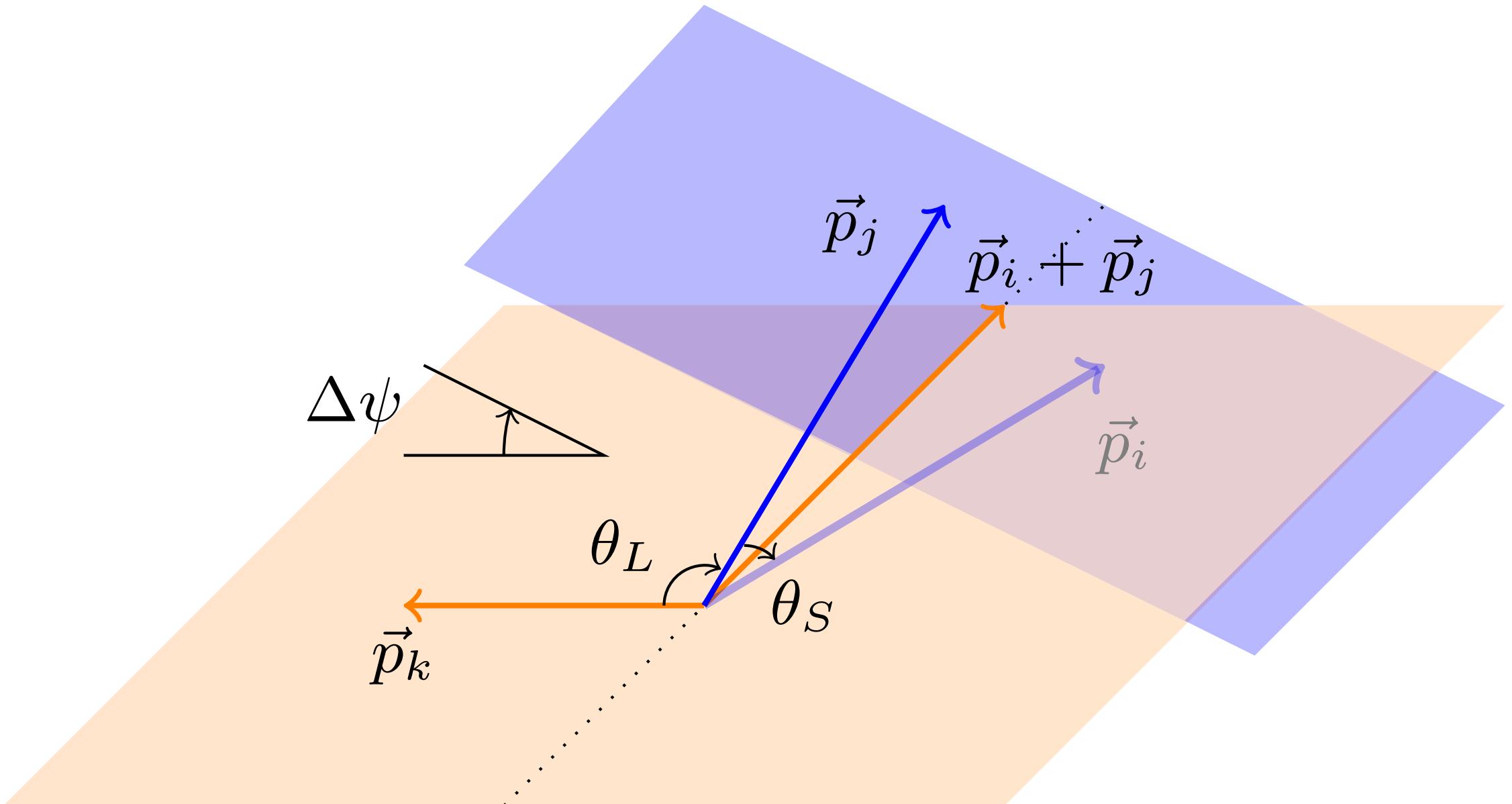
- Decluster with C/A
- Find highest- k_t branching with $z_1 \geq z_{\text{cut}}$
- Follow softest branch
- Find highest- k_t branching with $z_2 \geq z_{\text{cut}}$
- Compute angle $\Delta\psi_{12}$ between two branching planes



Can also be defined *between* jets: EPR-like observable

Observables: EEEC

Recently resummed Chen, Moult, Zhu Phys. Rev. Lett. 126 (2021)



Energy weight removes soft contributions

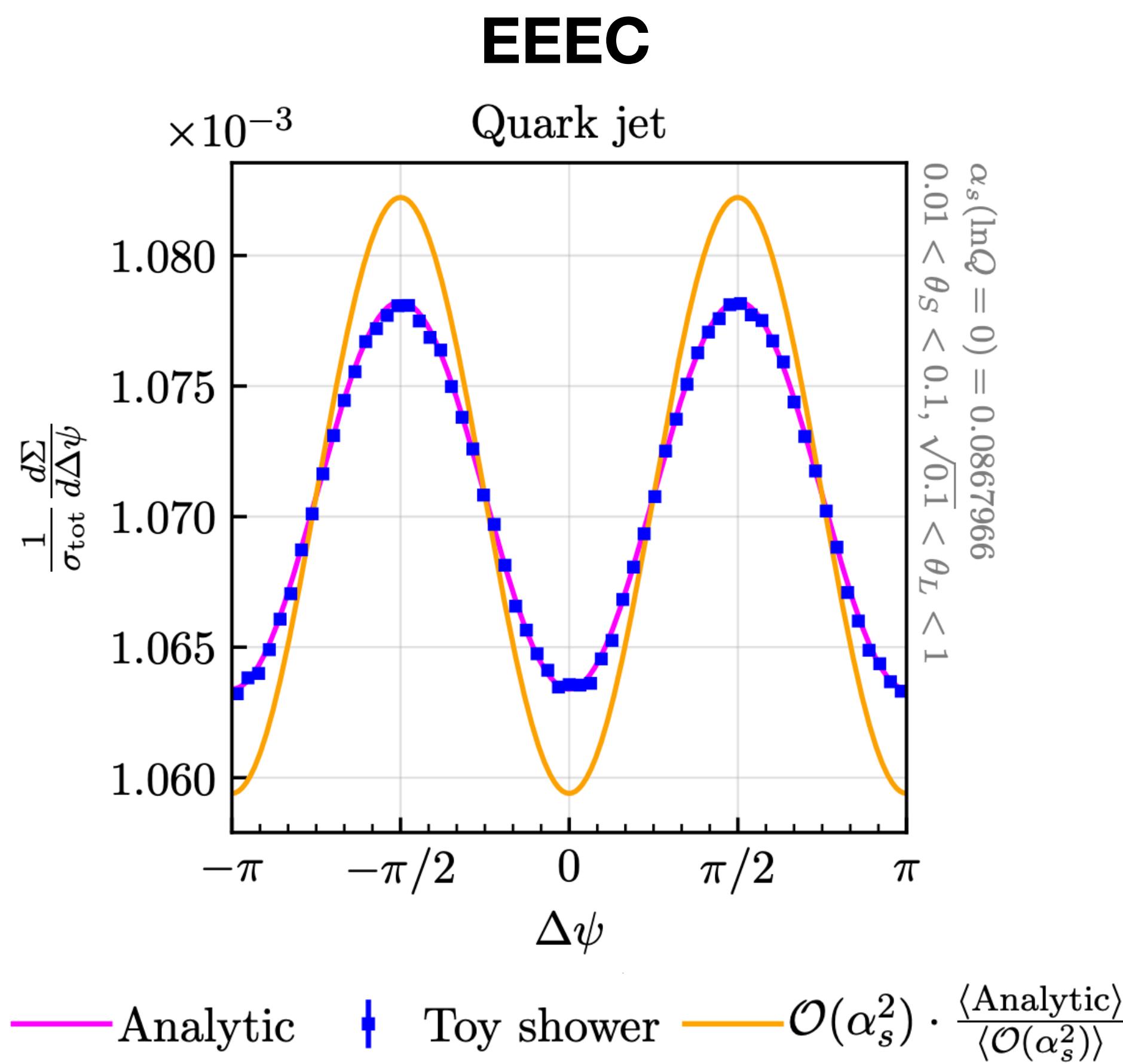
$$\frac{1}{\sigma_{\text{tot}}} \frac{d^3\Sigma}{d\Delta\psi d\theta_S d\theta_L} = \left\langle \sum_{i,j,k=1}^N \frac{8E_i E_j E_k}{Q^3} \delta(\Delta\psi - \phi_{(ij)k}) \delta(\theta_S - \theta_{ij}) \delta(\theta_L - \theta_{jk}) \right\rangle$$

↑

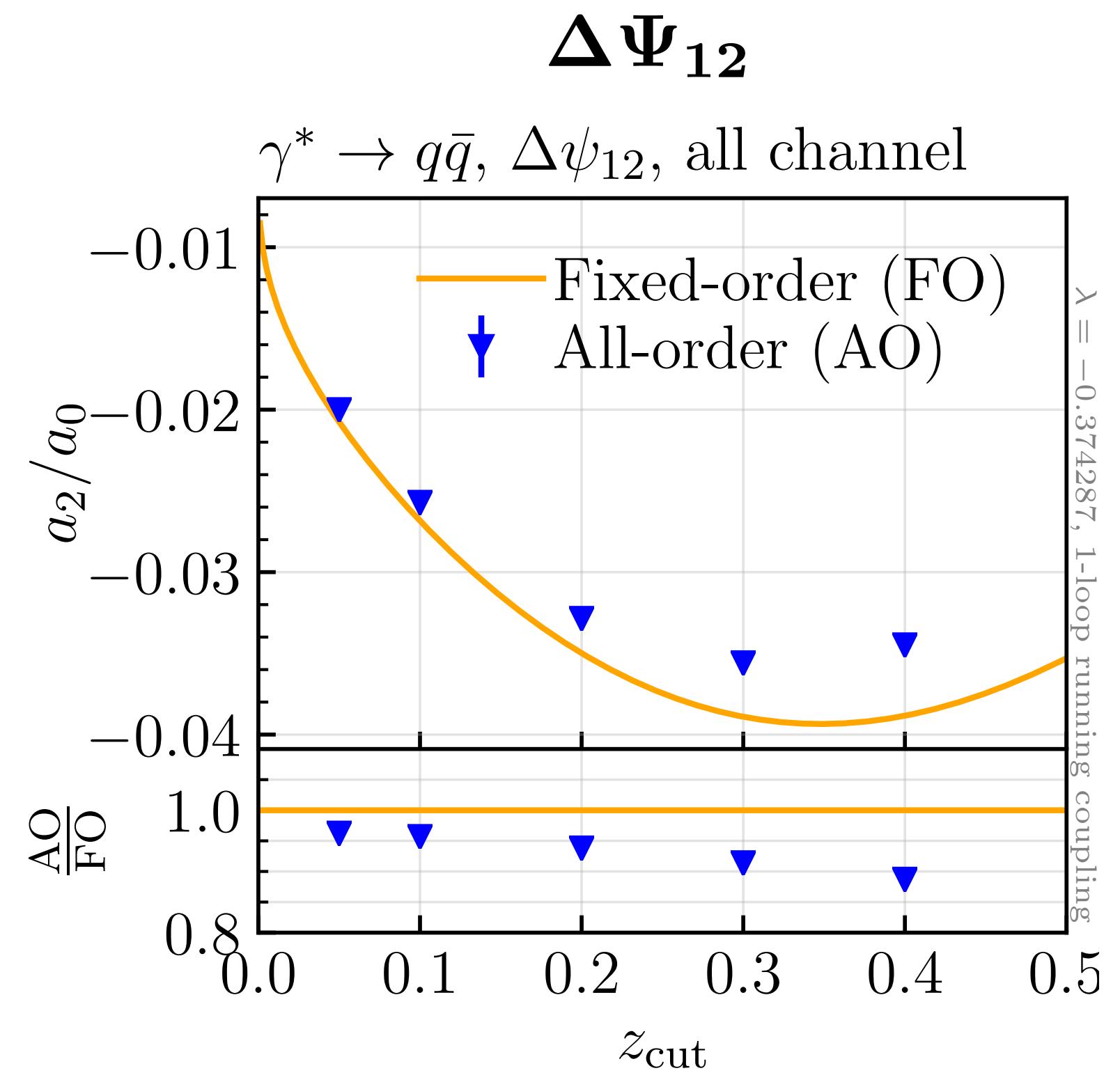
Angle between (p_i, p_j) -plane and $(p_i + p_j, p_k)$ -plane

Effects of resummation

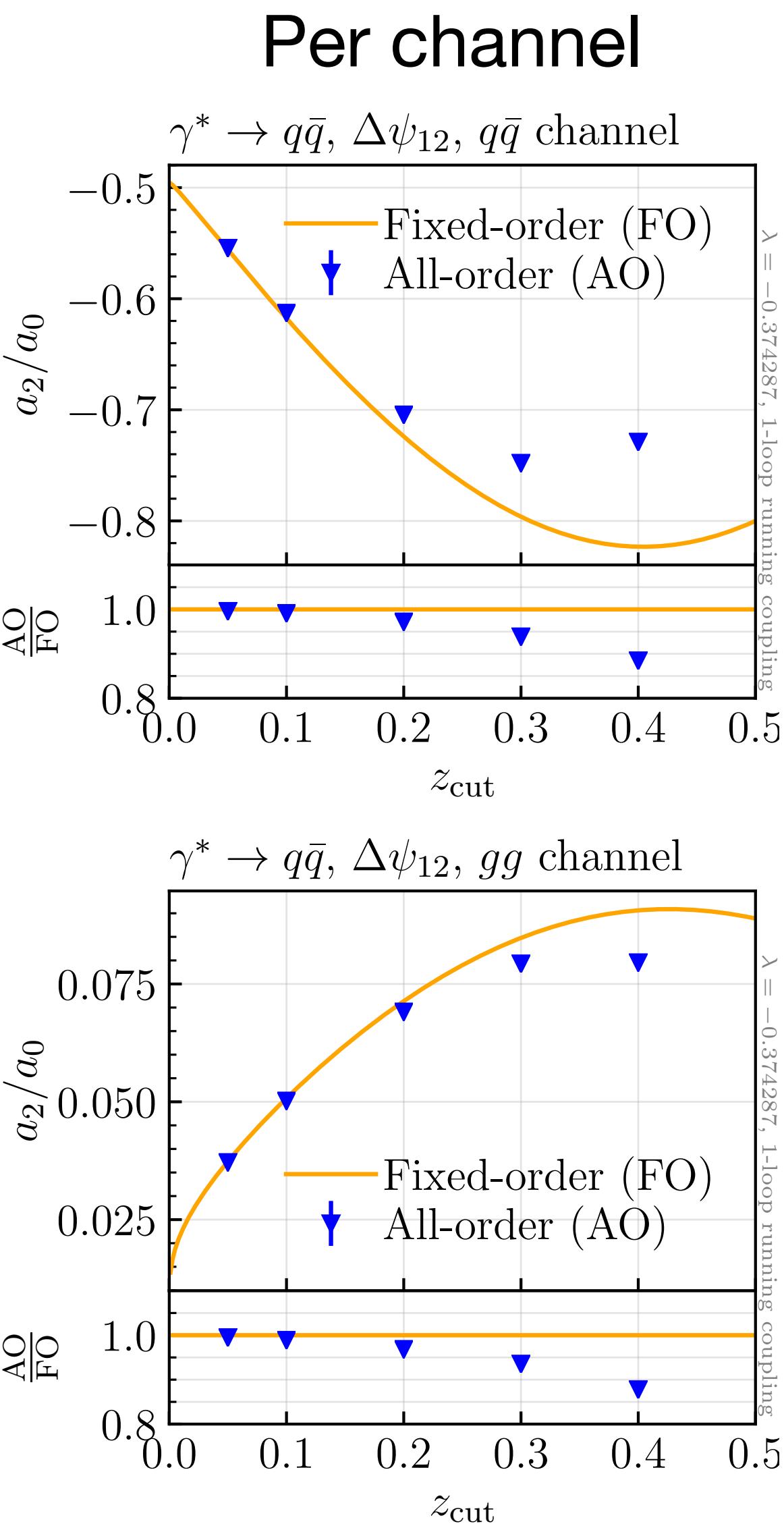
Numerical collinear resummation:
MicroJets (toy shower) + Collins-Knowles



Dasgupta, Dreyer, Salam, Soyez JHEP 04 (2015)
Dasgupta, Dreyer, Salam, Soyez JHEP 06 (2016)



→ Radiation dilutes spin content



All orders: PanScales showers

Comparisons with real showers is technically challenging

Want to send $\alpha_s \rightarrow 0$ while keeping $\alpha_s L$ fixed

→ Run showers to very small cutoff scale

- Shower stores directional differences in dipoles

→ Avoids large cancellation in dot products

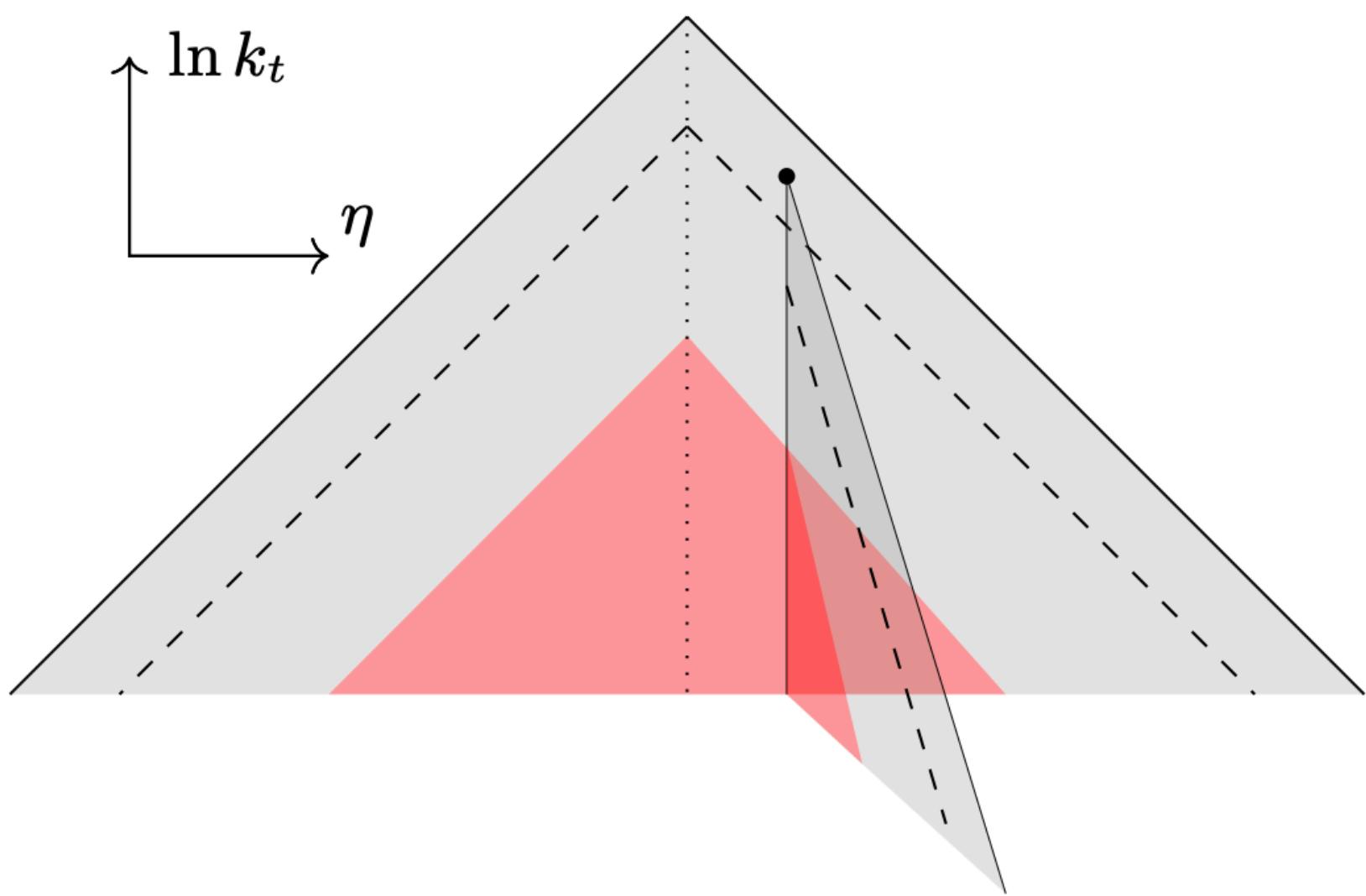
- Dedicated double_exp floating-point type

→ Allows for larger exponent in a double

- Remove soft radiation

→ Avoids multiplicity exploding

→ Thoroughly tested to not alter observable

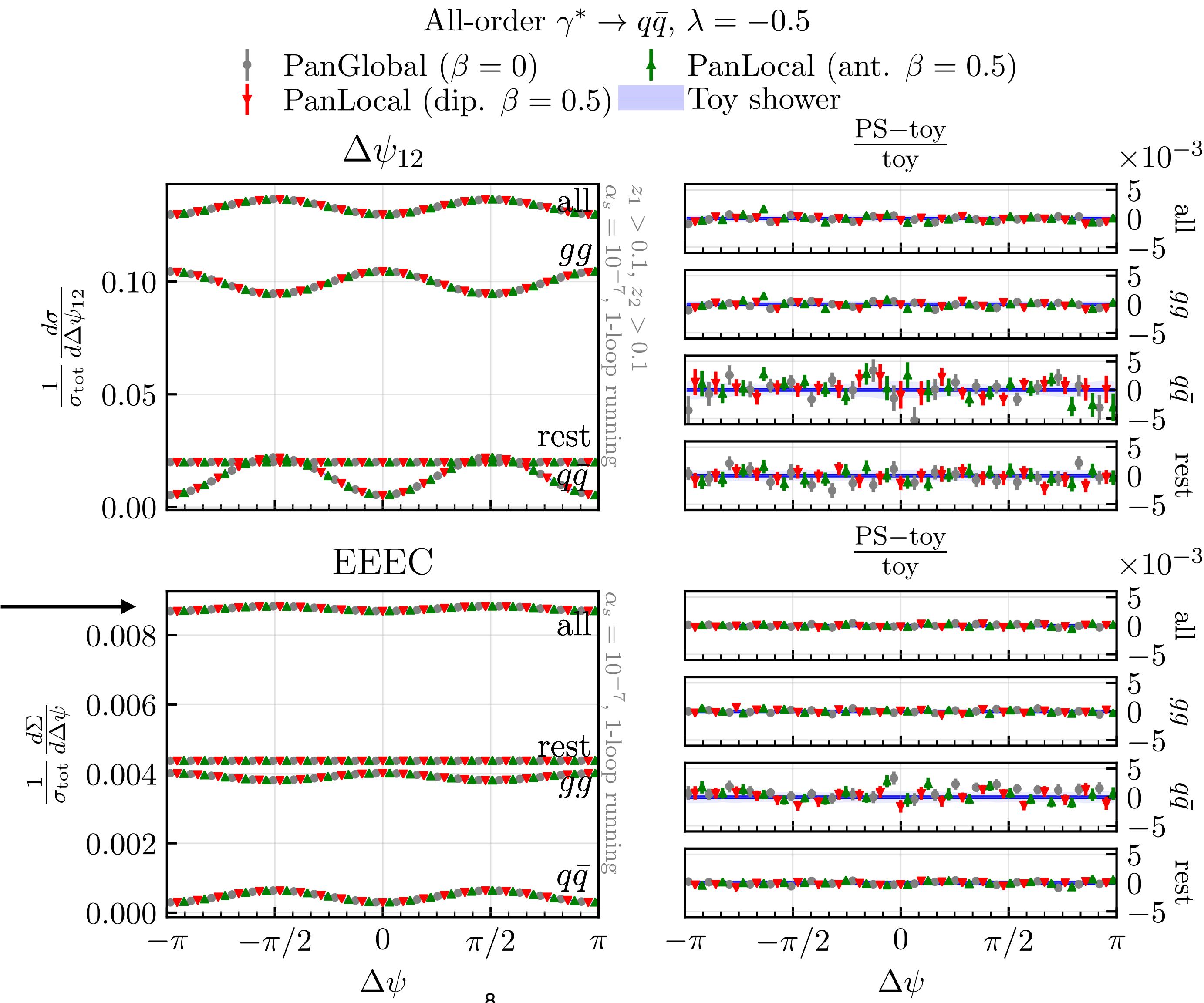


All orders: PanScales Showers vs. Toy Shower

$\lambda \equiv \alpha_s L = -0.5$
 $z_{\text{cut}} = 0.1$

$\alpha_s \rightarrow 0$ limit:
 $\alpha_s = 10^{-7}$
 $L = -5 \cdot 10^6$

Large cancellations between channels



Conclusions & Phenomenology

Phenomenological considerations

- $\Delta\psi_{12}$ generally has larger relative azimuthal modulation
 - Easier to observe experimentally
- Modulations may be enhanced further by adjusting the value of z_{cut}
- There are large cancellations between flavour channels
 - Clear advantage to performing measurements with flavour tagging
- Many subleading effects at LHC energies
 - Quark masses
 - Recoil effects
 - Non-perturbative corrections

- Implementation of Collins-Knowles in PanScales showers
- Definition of spin-sensitive observables
- Validation of NLL resummation

$\lambda = 0.5$	a_2/a_0		
flavour channel for 2 nd splitting	$g \rightarrow q\bar{q}$	$g \rightarrow gg$	all
EEEC	-0.36	0.026	-0.008
$\Delta\psi_{12}, z_1, z_2 > 0.1$	-0.61	0.050	-0.025
$\Delta\psi_{12}, z_1 > 0.1, z_2 > 0.3$	-0.81	0.086	-0.042

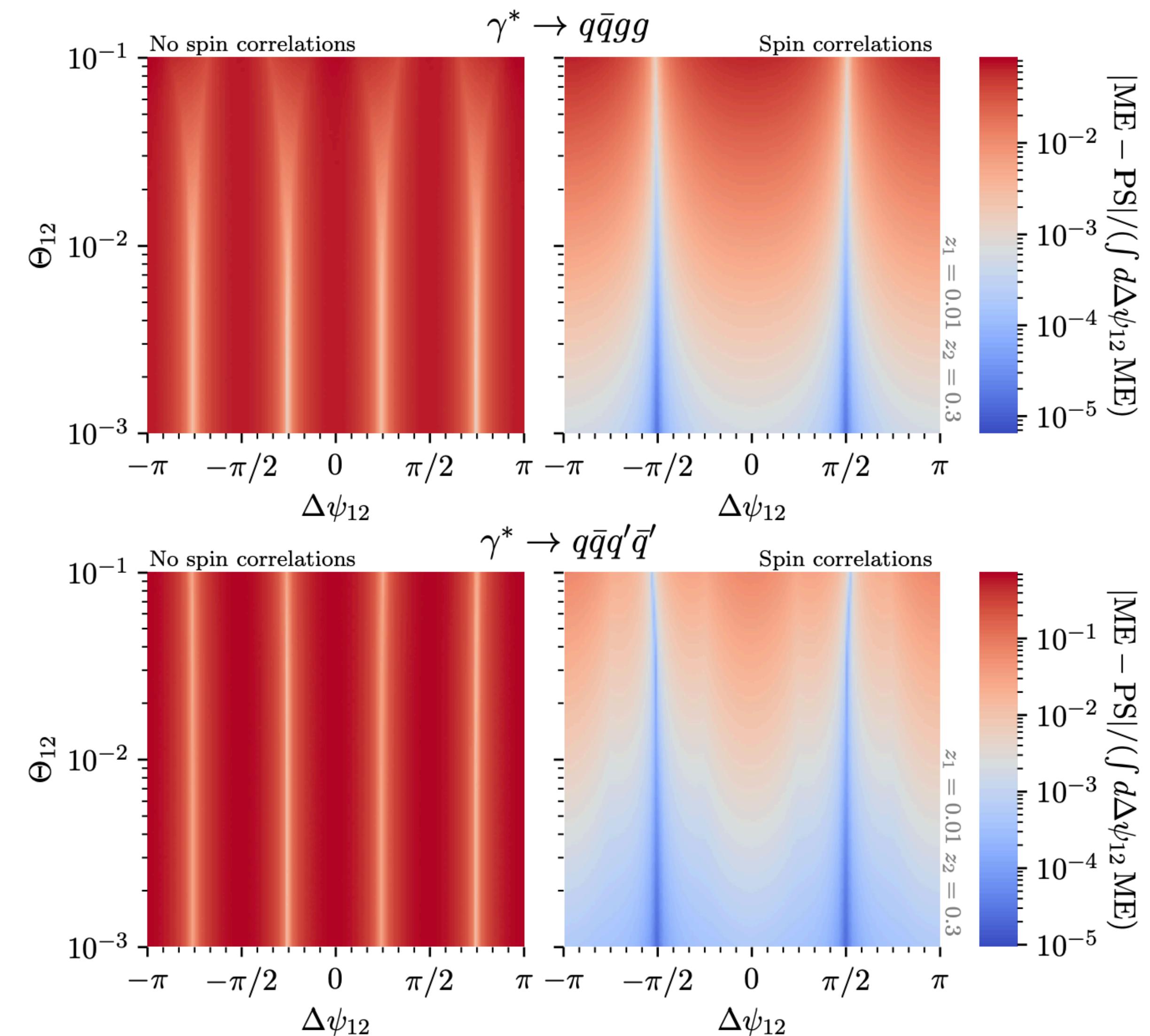
Backup

Matrix Element comparison

$$\Theta_{12} = \max(\theta_1, \theta_2/\theta_1)$$

$$z_1 = 0.01$$

$$z_2 = 0.3$$

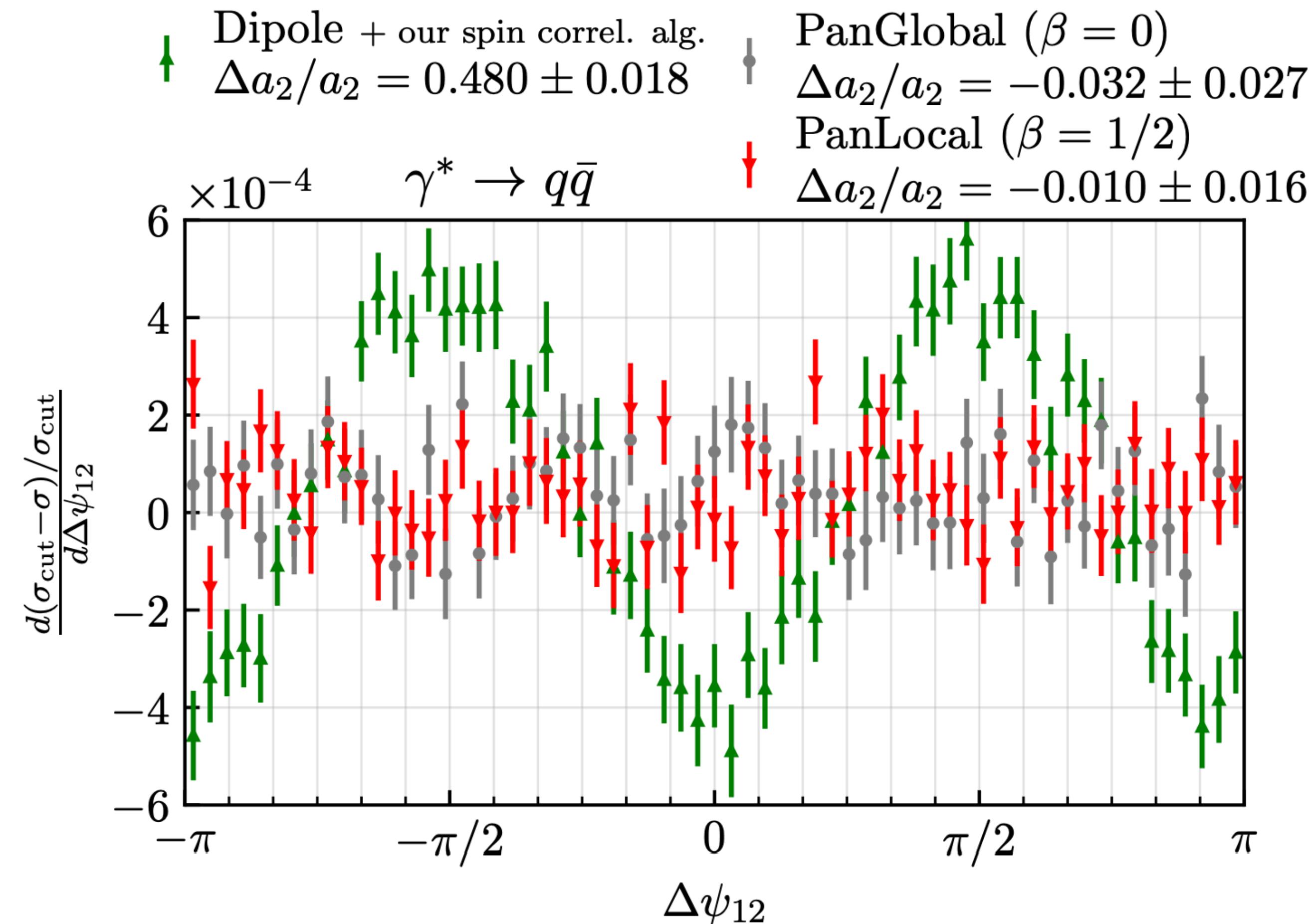


Removing soft radiation

$$\alpha_s = 0.01$$

$$L = -27.5$$

$$\ln z_{\text{cut}}^{\text{PS}} = -10$$



Rotational Invariance of Spinor Products

