



A Measurement of Radius Inflation in the Pleiades and Its Relation to Rotation and Lithium Depletion

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Abstract

Precise measurements of eclipsing binary parameters and statistical studies of young clusters have suggested that some magnetically active low-mass dwarfs possess radii inflated by $\sim 5\%$ – 15% relative to theoretical expectations. If true, this effect should be pronounced in young open clusters, due to the rapid rotation and strong magnetic activity of their most extreme members. We explore this possibility by determining empirical radii for 83 members of the nearby Pleiades open cluster, using spectral energy distribution fitting to establish \mathcal{F}_{bol} with a typical accuracy of $\approx 3\%$ together with color and spectro-photometric indices to determine T_{eff} . We find several Pleiades members with radii inflated above radius- T_{eff} models from state-of-the-art calculations, and apparent dispersions in radii for the K-dwarfs of the cluster. Moreover, we demonstrate that this putative radius inflation correlates strongly with rotation rate, consistent with inflation of young stars by magnetic activity and/or starspots. We argue that this signal is not a consequence of starspot-induced color anomalies, binarity, or depth effects in the cluster, employing *Gaia* DR1 distances as a check. Finally, we consider the lithium abundances of these stars, demonstrating a triple correlation between rotation rate, radius inflation, and enhanced lithium abundance. Our result—already significant to $\sim 99.99\%$ confidence—provides strong support for a magnetic origin of the inflated radii and lithium dispersion observed in young, low-mass stars.

Key words: stars: activity – stars: fundamental parameters – stars: rotation – starspots

Supporting material: figure set, machine-readable tables

1. Introduction

Precise knowledge of the fundamental parameters of stars is of considerable importance for understanding both their exact nature, their exo-planets, and the timescales of diverse astrophysical phenomenon such as star formation and circumstellar disk evaporation. Standard stellar theory has been extremely successful at predicting stellar properties throughout the wide and varied life cycles of stars, but their fidelity with regard to the radii of low mass ($M < 1 M_{\odot}$) stars has been called into question by a consistent trend emerging from direct measurements: young, active stars appear to have radii that are larger than standard predictions by $\sim 5\%$ – 15% . This phenomenon has been claimed in eclipsing binaries (e.g., Popper 1997; Torres & Ribas 2002; López-Morales & Ribas 2005), statistical studies of open clusters (e.g., Jackson et al. 2016), on both sides of the fully convective boundary of $0.35 M_{\odot}$ (e.g., Clausen et al. 2009; Stassun et al. 2012), and on both the pre-main sequence and main sequence (e.g., Torres et al. 2010, 2014; Feiden & Chaboyer 2012; Stassun et al. 2014). Additionally, corresponding anomalies in the T_{eff} s of the afflicted stars have been noted in several instances (e.g., Stassun et al. 2006; Dupuy et al. 2016). While the underlying cause remains controversial, it has been shown that in some cases the degree of radius inflation appears correlated with the strength of surface magnetic activity (e.g., Torres et al. 2006; López-Morales 2007; Morales et al. 2008; Stassun et al. 2012). Newer generations of theoretical models have begun to consider such effects, and ongoing research is studying their impact on the fundamental parameters, abundances, and evolutionary timescales of young stars (e.g., Mullan & MacDonald 2001; Chabrier et al. 2007; Macdonald & Mullan 2010; Feiden & Chaboyer 2013, 2014; Jackson & Jeffries 2014a, 2014b; Somers & Pinsonneault 2014, 2015b, 2015a). Results have been particularly

promising for young stars: the well-known lithium-rotation correlation in pre- and zero-age main sequence clusters (e.g., Soderblom et al. 1993; Bouvier et al. 2016; Messina et al. 2016) is a direct prediction of an activity–radius connection on the pre-main sequence (e.g., Ventura et al. 1998; Somers & Pinsonneault 2015a, 2015b; Jeffries et al. 2017).

If an activity–radius connection truly exists, young ($\lesssim 200$ Myr) main sequence open clusters present a valuable test bed to uncover the nature of the correlation. Young clusters generally contain members with extraordinarily rapid rotation, as the magnetic stellar winds which efficiently break stars on the main sequence have not yet significantly depleted the initial stellar angular momentum (e.g., Pinsonneault et al. 1989; Gallet & Bouvier 2015; Somers & Pinsonneault 2016b). Furthermore, young clusters host large dispersions in rotation rate at fixed mass due to the diversity of rotative initial conditions in star-forming regions, and consequently show a range of activity levels and starspot coverage from moderate to extreme (e.g., Soderblom et al. 1993; O’dell et al. 1995; Gallet & Bouvier 2015; Fang et al. 2016). Such clusters have been the target of several recent statistical studies examining the fundamental parameters of stars (Littlefair et al. 2011; Cottaar et al. 2014; Jackson & Jeffries 2014a, 2014b; Jackson et al. 2016; Lanzafame et al. 2017). In several cases, these studies have concluded both that the average stellar radius is larger compared to standard predictions, and that dispersions likely exist in radius at fixed T_{eff} .

In particular, Jackson & Jeffries (2014a) recently examined the well-studied open cluster, the Pleiades, for signs of radius inflation. By measuring the projected radii of a large sample of its members, and statistically analyzing their results, they found that the average Pleiad radius is $\sim 10\%$ larger than theoretical predictions below $1 M_{\odot}$. The Pleiades is an advantageous

laboratory for such experiments, given its proximity ($d \sim 136$ pc, Melis et al. 2014), near-solar composition of $[\text{Fe}/\text{H}] \sim 0.03$ (Soderblom et al. 2009), and young age of 125 Myr (Stauffer et al. 1998). Furthermore, its members more massive than $\sim 0.6 M_{\odot}$ have reached the main sequence, meaning that the harrowing uncertainties dogging pre-main sequence models can be avoided in comparisons with theory (e.g., Stassun et al. 2014).

In this paper, we apply a distinct method to this same open cluster to search for corroborating signs of radius inflation and dispersion. Our method involves fitting the broadband spectral energy distributions (SEDs) of individual members to establish their bolometric fluxes (\mathcal{F}_{bol}), and combining this result with the known distance of the cluster and an estimate of the T_{eff} , to calculate the stellar radius. This approach is attractive because, in principle, individual stars can be tested for radius inflation, and correlations with non-standard physical effects like activity and rotation can be explored. We devote considerable discussion to the accuracy of our T_{eff} s, as the active and spotted nature of young stars complicates simple extrapolation from photometry. In the end, we find a clear connection between rotation rate and apparent radius inflation above a putative T_{eff} –radius relation.

The paper is organized as follows. In Section 2, we describe our sample selection, our methods for deriving \mathcal{F}_{bol} and T_{eff} for our stars, and our procedure for deriving the corresponding radii. In Section 3, we present these radii and compare them with predictions from theoretical models, looking particular at the influence of rotation on the agreement. In Section 4, we discuss the possible contaminating influence of starspots, binaries, and extinction, and describe the relationship between inflated radii and lithium abundance in this cluster. Finally, we summarize our conclusions in Section 5.

2. Methods

The familiar astrophysical formulation of the Stefan–Boltzmann law defines the effective temperature of a star as a function of radius and luminosity: $L = 4\pi R_*^2 \sigma_{\text{SB}} T_{\text{eff}}^4$. By inverting this equation, the radius of a star can be directly calculated if the T_{eff} and luminosity can be determined with fidelity. This is the fundamental method we employ for this study. In this section, we describe how we infer these two properties, and how the associated uncertainties propagate into radius errors. We first select a sample of Pleiads to study in Section 2.1, requiring accurate BVKs photometry, spectro-photometric T_{eff} s from the *DANCe* collaboration (Bouy et al. 2015; Barrado et al. 2016), and literature lithium abundances. We then discuss our T_{eff} derivations in Section 2.2, describe the broadband photometric data employed to derive the bolometric flux in Section 2.3.1, detail our spectral energy distribution fitting technique in Section 2.3.2, and execute the radius derivations in Section 2.4.

2.1. Sample Selection

We began with the newly assembled catalog of literature lithium measurements reported by Barrado et al. (2016), who accepted only stars with membership probability >0.75 . A small number of Pleiads lie behind an HI cloud, and are thus far more extincted than the rest (e.g., Gordon & Arny 1984); for simplicity, we discard these members. We then cross-correlated this sample with the famous *UBV* photometric catalog of Johnson & Mitchell (1958), who produced homogeneous

photometry for a large sample of Pleiades members. We further selected stars with measured rotation rates, either from the HATNet collaboration (Hartman et al. 2010), or the recent analysis of *K2* data (Rebull et al. 2016a, 2016b; Stauffer et al. 2016), preferring the latter for joint detections. Finally, we queried *VizieR*³ to obtain K_s -band magnitudes from the Two-Micron All-Sky Survey (2MASS) catalog (Skrutskie et al. 2006), which detected every star in our reduced sample. These criteria produced a total of 83 high-probability cluster members, stretching from early-F to late-K type. We refer to these stars as our “sample.” Basic parameters for our sample are listed in Table 1.

For the analysis of Section 3, we exclude known binaries (see Section 4.1.2), and ignore stars warmer than 6250 K, the approximate temperature where the rotative properties of stars change due to their vanishingly small surface convection zones (e.g., Kraft 1967).

2.2. Effective Temperatures

We next establish T_{eff} values for our sample. Accurate T_{eff} s are crucial for this study, as their errors represent the dominant contribution to the uncertainties in our derived radii. This can be understood by considering the equation relating luminosity, radius, and effective temperature. Re-arranging this equation shows that $R \propto T_{\text{eff}}^2 L^{1/2}$, implying that fractional radius errors go like twice the fractional T_{eff} errors, but only as half the fractional luminosity errors. The measured T_{eff} also sets which theoretical radius value to be used as comparison, and also contributes to errors in the bolometric flux derivation (Section 2.3).

There is a well-known problem in the Pleiades related to the colors of the cluster’s K-dwarfs. Going back at least to Herbig (1962), and continuing through the studies of Jones (1972), Stauffer (1980), Mermilliod et al. (1992), Stauffer et al. (2003), and as recently as Covey et al. (2016), it has been shown that the Pleiades K-dwarfs are substantially bluer than expected from a calibrated zero-age main sequence. This is generally attributed to the presence of starspots on the photospheres of the young stars (see the discussion in Stauffer et al. 2003), whose accompanying plages emit substantial short-wavelength radiation, thus altering the relative fractions of photons within the *B* and *V* band-passes. Stauffer et al. (2003) noted a similar but opposite-sign effect for $V - K_s$, which produces a color–magnitude diagram (CMD) too red compared to a less magnetically active cluster (in their case, the ~ 600 Myr old Praesepe), presumably a result of the cool starspot surfaces themselves. They finally note that, perhaps as a result of balance between the cool spots and the hotter photosphere/plage regions, spotted stars generally lie in their “expected” locations in a $V - I_c$ CMD.

To better understand this phenomenon, Somers & Pinsonneault (2015a) constructed evolutionary models of spotted stars and investigated the consequence for different photometric bands. For a 50% spotted star with an 80% temperature contrast between the hot and cool regions, appropriate for the inferred properties of Pleiades stars, they found that the stars would appear bluer in $B - V$, redder in $V - K_s$, and approximately unchanged in $V - I_c$, in good agreement with the empirical Pleiades results. However, they noted that the T_{eff} of a spotted star is always lower than an equivalent star without spots. Consequently, one might expect the true T_{eff} of a spotted star to

³ <http://vizier.u-strasbg.fr/>

Table 1
Basic Pleiades Data

HII	Tycho-2	2MASS	R.A.	Decl.	V_{mag}	$B - V$	$V - K_s$	P_{rot}	Binary?
0025	1803-478-1	03425511 + 2429350	55.729626	+24.493065	9.470	0.48 ± 0.02	1.207 ± 0.029	1.41	N
0034	1803-400-1	03430293 + 2440110	55.762230	+24.669737	12.030	0.94 ± 0.02	2.303 ± 0.028	6.69	N
0097	...	03432662 + 2459395	55.860922	+24.994333	12.500	1.08 ± 0.02	2.705 ± 0.030	6.74947635	Y
0120	1799-118-1	03433195 + 2340266	55.883139	+23.674074	10.790	0.70 ± 0.02	1.687 ± 0.029	3.99	N
0129	1799-1268-1	03433440 + 2345429	55.893373	+23.761917	11.470	0.88 ± 0.02	2.100 ± 0.029	5.44	Y
0152	1799-780-1	03433772 + 2332096	55.907204	+23.536011	10.750	0.70 ± 0.02	1.626 ± 0.029	3.88781400	N
0164	1799-1037-1	03434286 + 2335412	55.928608	+23.594801	9.540	0.48 ± 0.02	1.307 ± 0.033	Y
0174	1803-8-1	03434833 + 2500157	55.951377	+25.004387	11.620	0.85 ± 0.02	2.246 ± 0.028	0.47429706	N
0193	1799-816-1	03435070 + 2414508	55.961274	+24.247465	11.290	0.81 ± 0.02	1.946 ± 0.028	5.36	N
0250	1803-818-1	03440424 + 2459233	56.017681	+24.989822	10.680	0.68 ± 0.02	1.619 ± 0.029	4.23218914	Y
0253	1803-282-1	03440353 + 2430151	56.014746	+24.504206	10.660	0.68 ± 0.02	1.707 ± 0.029	1.48	N
0263	...	03440484 + 2416318	56.020167	+24.275501	11.540	0.88 ± 0.02	2.154 ± 0.029	4.68	Y
0293	1803-812-1	03441391 + 2446457	56.057980	+24.779388	10.800	0.70 ± 0.02	1.738 ± 0.030	4.03	Y
0345	...	03442627 + 2435229	56.109485	+24.589705	11.570	0.84 ± 0.02	2.304 ± 0.028	0.84	N
0380	...	03443741 + 2508160	56.155898	+25.137793	13.330	1.21 ± 0.02	3.091 ± 0.031	9.03288129	N
0405	1803-542-1	03444075 + 2449067	56.169800	+24.818542	9.830	0.54 ± 0.02	1.317 ± 0.031	1.91	N
0430	...	03444398 + 2413523	56.183251	+24.231215	11.400	0.85 ± 0.02	1.931 ± 0.030	5.51856881	N
0470	1799-1157-1	03445123 + 2316082	56.213483	+23.268969	8.950	0.39 ± 0.02	0.966 ± 0.039	Y
0489	...	03445639 + 2425574	56.234988	+24.432623	10.390	0.63 ± 0.02	1.524 ± 0.028	2.78	N
0514	1803-1061-1	03450400 + 2515282	56.266691	+25.257841	10.690	0.69 ± 0.02	1.649 ± 0.028	3.79041574	N
0530	1799-170-1	03450528 + 2342097	56.272009	+23.702707	8.950	0.39 ± 0.02	0.950 ± 0.030	Y
0627	1803-388-1	03452412 + 2453095	56.350531	+24.885977	9.680	0.50 ± 0.02	1.261 ± 0.031	1.81	N
0636	...	03452219 + 2328182	56.342478	+23.471731	12.480	1.06 ± 0.02	2.632 ± 0.027	8.48	N
0708	...	03453539 + 2404595	56.397484	+24.083210	10.130	0.62 ± 0.02	1.568 ± 0.029	1.02	Y
0746	...	03454184 + 2425534	56.424374	+24.431513	11.270	0.92 ± 0.02	1.872 ± 0.030	5.23230299	Y
0879	...	03460649 + 2434027	56.527062	+24.567419	12.790	1.07 ± 0.02	2.677 ± 0.028	6.75	N
0882	...	03460412 + 2324199	56.517177	+23.405537	12.660	1.07 ± 0.02	2.824 ± 0.027	0.58	N
0883	...	03460689 + 2433461	56.528742	+24.562807	13.050	1.08 ± 0.02	2.800 ± 0.031	7.91	N
0916	...	03461174 + 2437203	56.548937	+24.622314	11.710	0.87 ± 0.02	2.165 ± 0.028	5.98	Y
0923	1800-1917-1	03461005 + 2320240	56.541875	+23.340015	10.120	0.62 ± 0.02	1.461 ± 0.026	1.42	Y
0996	...	03462267 + 2434126	56.594480	+24.570177	10.420	0.64 ± 0.02	1.497 ± 0.026	3.23	N
1015	1804-2366-1	03462735 + 2508080	56.613966	+25.135563	10.540	0.65 ± 0.02	1.547 ± 0.026	3.42	N
1032	...	03462841 + 2426021	56.618376	+24.433918	11.340	0.86 ± 0.02	2.181 ± 0.026	1.31	N
1095	...	03463777 + 2444517	56.657390	+24.747698	11.920	0.88 ± 0.02	2.251 ± 0.028	7.18	N
1110	...	03463889 + 2431132	56.662043	+24.520344	13.290	1.19 ± 0.02	3.004 ± 0.027	7.48	N
1122	...	03463932 + 2406116	56.663857	+24.103243	9.290	0.46 ± 0.02	1.099 ± 0.025	0.87	Y
1124	...	03463938 + 2401468	56.664103	+24.029688	12.120	0.92 ± 0.02	2.261 ± 0.029	6.13	N
1132	1800-1574-1	03463839 + 2255112	56.659985	+22.919804	9.420	0.49 ± 0.02	1.267 ± 0.031	6.84	N
1139	1800-1672-1	03463999 + 2306373	56.666655	+23.110371	9.380	0.48 ± 0.02	1.137 ± 0.032	1.82	Y
1182	1800-1774-1	03464706 + 2254525	56.696086	+22.914593	10.460	0.64 ± 0.02	1.532 ± 0.028	3.00	Y
1200	1800-1627-1	03465053 + 2314211	56.710572	+23.239195	9.900	0.54 ± 0.02	1.354 ± 0.029	N
1207	1804-2205-1	03465491 + 2447468	56.728828	+24.796349	10.470	0.62 ± 0.02	1.493 ± 0.028	3.37	Y
1215	1800-1616-1	03465373 + 2335009	56.723910	+23.583599	10.520	0.65 ± 0.02	1.524 ± 0.029	3.59	N
1220	...	03465326 + 2252513	56.721920	+22.880943	11.740	0.88 ± 0.02	2.021 ± 0.028	6.15	N
1298	...	03470678 + 2342546	56.778252	+23.715170	12.180	1.02 ± 0.02	2.341 ± 0.028	8.48	Y
1305	...	03470734 + 2313349	56.780599	+23.226362	13.460	1.18 ± 0.02	3.096 ± 0.028	0.39	N
1309	1800-1935-1	03471005 + 2416360	56.791894	+24.276672	9.460	0.47 ± 0.02	1.178 ± 0.032	0.78	N
1332	...	03471352 + 2342515	56.806374	+23.714310	12.410	1.04 ± 0.02	2.401 ± 0.028	7.85	Y
1454	...	03473367 + 2441032	56.890319	+24.684223	12.780	1.16 ± 0.02	2.652 ± 0.029	8.60	N
1514	...	03474044 + 2421525	56.918539	+24.364594	10.480	0.64 ± 0.02	1.527 ± 0.028	3.25	N
1531	...	03474143 + 2358190	56.922657	+23.971945	13.300	1.15 ± 0.02	2.988 ± 0.029	0.48	N
1593	1800-2170-1	03474811 + 2313053	56.950462	+23.218140	11.120	0.75 ± 0.02	1.796 ± 0.027	5.14	N
1613	...	03475252 + 2356286	56.968837	+23.941282	9.880	0.54 ± 0.02	1.306 ± 0.028	1.40	N
1776	...	03481769 + 2502523	57.073718	+25.047886	10.910	0.72 ± 0.02	1.752 ± 0.028	4.53	N
1794	...	03481712 + 2353253	57.071342	+23.890385	10.360	0.64 ± 0.02	1.469 ± 0.029	3.82	N
1797	...	03481691 + 2338125	57.070459	+23.636806	10.110	0.56 ± 0.02	1.374 ± 0.029	2.45	N
1856	...	03482616 + 2402544	57.109023	+24.048445	10.020	0.56 ± 0.02	1.357 ± 0.027	2.49	N
1883	...	03482802 + 2318027	57.116787	+23.300774	12.600	1.06 ± 0.02	2.764 ± 0.027	0.24	N
1924	...	03483451 + 2326053	57.143806	+23.434818	10.330	0.62 ± 0.02	1.462 ± 0.029	2.88	N
2016	...	03484542 + 2320201	57.189275	+23.338938	13.520	1.22 ± 0.02	3.185 ± 0.027	3.92	N
2034	...	03484932 + 2358383	57.205510	+23.977320	12.570	0.99 ± 0.02	2.578 ± 0.028	0.55	Y
2106	...	03485848 + 2312044	57.243692	+23.201229	11.530	0.86 ± 0.02	2.153 ± 0.027	6.01	Y
2126	...	03490232 + 2315088	57.259705	+23.252468	11.640	0.86 ± 0.02	1.983 ± 0.028	3.08	N
2244	...	03492059 + 2446360	57.335794	+24.776670	12.670	1.04 ± 0.02	2.745 ± 0.030	0.56	N

Table 1
(Continued)

HII	Tycho-2	2MASS	R.A.	Decl.	V_{mag}	$B - V$	$V - K_s$	P_{rot}	Binary?
2284	...	03492405 + 2350214	57.350217	+23.839287	11.350	0.78 ± 0.02	1.972 ± 0.028	5.59	Y
2311	...	03492873 + 2342440	57.369749	+23.712238	11.360	0.83 ± 0.02	1.932 ± 0.030	5.71	N
2341	...	03493312 + 2347435	57.388005	+23.795427	10.870	0.71 ± 0.02	1.656 ± 0.029	4.94	Y
2345	1800-727-1	03493272 + 2322494	57.386341	+23.380413	9.100	0.44 ± 0.02	1.064 ± 0.031	0.24	N
2366	...	03493653 + 2417460	57.402244	+24.296135	11.530	0.82 ± 0.02	1.980 ± 0.028	6.21783952	N
2462	...	03495035 + 2342202	57.459828	+23.705631	11.550	0.83 ± 0.02	1.955 ± 0.028	6.85	N
2506	1800-471-1	03495648 + 2313071	57.485363	+23.218641	10.230	0.60 ± 0.02	1.434 ± 0.028	2.18	N
2644	...	03502089 + 2428003	57.587080	+24.466755	11.030	0.73 ± 0.02	1.723 ± 0.027	5.07153391	N
2665	1800-669-1	03502130 + 2305470	57.588751	+23.096392	11.360	0.83 ± 0.02	1.975 ± 0.029	5.37	N
2741	...	03503457 + 2430281	57.644052	+24.507822	12.600	1.00 ± 0.02	2.520 ± 0.027	5.15798051	N
2786	...	03504007 + 2355590	57.666983	+23.933065	10.310	0.60 ± 0.02	1.457 ± 0.028	2.16	N
2870	1800-586-1	03505143 + 2319447	57.714333	+23.329100	12.450	1.07 ± 0.02	2.435 ± 0.029	8.45	N
2880	...	03505508 + 2411508	57.729525	+24.197466	11.750	0.86 ± 0.02	2.121 ± 0.027	6.28238456	N
3019	...	03512440 + 2405147	57.851675	+24.087425	13.450	1.19 ± 0.02	3.176 ± 0.030	5.46870223	N
3031	1804-67-1	03512722 + 2431072	57.863420	+24.518692	8.830	0.38 ± 0.02	0.953 ± 0.028	N
3063	...	03512993 + 2353572	57.874730	+23.899225	13.520	1.17 ± 0.02	3.224 ± 0.030	0.88393824	N
3163	...	03515338 + 2423132	57.972446	+24.387018	12.690	0.98 ± 0.02	2.807 ± 0.030	0.41747738	N
3179	1800-1415-1	03515685 + 2354070	57.986888	+23.901966	10.040	0.56 ± 0.02	1.408 ± 0.027	4.85456989	Y
3187	...	03515733 + 2320219	57.988895	+23.339439	13.120	1.16 ± 0.02	2.922 ± 0.029	7.30	N

Note. V_{mag} and $B - V$ data from Johnson & Mitchell (1958), K_s data from Skrutskie et al. (2006). Rotation periods with two decimal places are from the K2 Pleiades campaign (Rebull et al. 2016a, 2016b; Stauffer et al. 2016), and those with more decimal places are from the HATNet campaign (Hartman et al. 2010). Sources of binary info are described in Section 4.1.2.

(This table is available in machine-readable form.)

be somewhat cooler than implied by $V - I_c$ and perhaps somewhat warmer or cooler than implied by $V - K_s$ band depending on the properties of the spots, but far cooler than implied by $B - V$.

With these considerations, we believe $V - I_c$ photometry is the ideal photometric index for deriving temperatures for this study, because a $V - I_c$ -derived T_{eff} may be interpreted as a close upper limit to the true temperature. This is advantageous as it results in a *lower limit* on the true radius, useful for detecting radius inflation. However, reliable I_c -band photometry does not exist for the majority of our sample. This is remarkable, given the extensive scrutiny placed on the Pleiades for over a century. The recent and exquisite I_c -band data of Kamai et al. (2014) overlap with only two of our Li-rotation-selected stars, and although there is greater overlap with the comprehensive catalog of Stauffer et al. (2007), many of their reported I_c band values are of mixed origin and uncertain calibration.

Instead, we elected to proceed with T_{eff} s derived from $V - K_s$ photometry. While the above discussion suggests that $V - K_s$ photometry produces T_{eff} s of uncertain accuracy, we find that for Pleiades stars, T_{eff} s derived from $V - K_s$ and $V - I_c$ photometry are quite similar. As we expect these T_{eff} s to approximately bracket the possible T_{eff} range, their similarity is an encouraging sign that our T_{eff} s are reasonable estimates.

As a demonstration, we obtained the BVI_c data set of Kamai et al. (2014), and cross-correlated their members with both 2MASS and the joint HATNet/K2 rotation data set (Section 2.1), to obtain K_s photometry and rotation rates. We assume a reddening of $E(B - V) = 0.04$ (An et al. 2007) and a selective extinction of $R_V = 3.1$ which, with a standard Cardelli et al. (1989) reddening law, gives $E(V - I_c) = 0.06$ and $E(V - K_s) = 0.11$. We then derived T_{eff} s from the infrared flux method (IRFM) calibration of Casagrande et al. (2010, C10 hereafter), and examined the resulting T_{eff} s in

Figure 1. The left column compares $B - V$ and $V - I_c$ T_{eff} s for stars with rotation periods slower than two days (blue points), and faster than two days (red points), in both absolute (top) and differential (bottom) terms. Considering first the left panels, $B - V$ photometry implies substantially higher T_{eff} s than does $V - I_c$ for nearly every star, with the fastest rotating objects showing the greatest departure. Significantly, the dispersion reaches several hundred kelvin between 4500 and 5500 K. This illustrates the adverse impact of magnetic activity on $B - V$ photometry. By contrast, the right compares $V - I_c$ and $V - K_s$ colors, showing good agreement for the slowest rotators, and a far weaker systematic offset among the fastest rotators (65 K on average), below ~ 5800 K. This agreement may be somewhat better than previously thought, perhaps as a consequence of the weaker shift in T_{eff} for a given change in $V - K_s$ when compared to T_{eff} shift for an equal change in $B - V$. The similarity of these two temperatures, in the context of expectations from the Somers & Pinsonneault (2015a) models, gives us confidence in the general reliability of our T_{eff} s. We consider how large the systematic errors bars might be in Section 4.1.1.

As a further test, we fit for the offset between $V - I_c$ and $V - K_s$ -derived T_{eff} s in the combined Kamai et al. (2014) and Hartman et al. (2010) sample as a function of rotation rate, and “corrected” our $V - K_s$ T_{eff} s to the new scale. To do this, we subdivided our stars into a “hot” and “cool” sample, taking 5500 K as the dividing point. This is because the hotter and cooler stars show opposite-sign relationships with rotation (see Section 3.4 in Kamai et al. 2014). We then fit second-order polynomials to the difference between the $V - I_c$ and $V - K_s$ T_{eff} s as a function of the latter. Finally, we applied these offsets to our derived $V - K_s$ T_{eff} s to obtain estimated $V - I_c$ T_{eff} s. Performing the analysis outlined in this paper with these $V - I_c$ values does not influence our results or conclusions in any substantial way, increasing the confidence in our results.

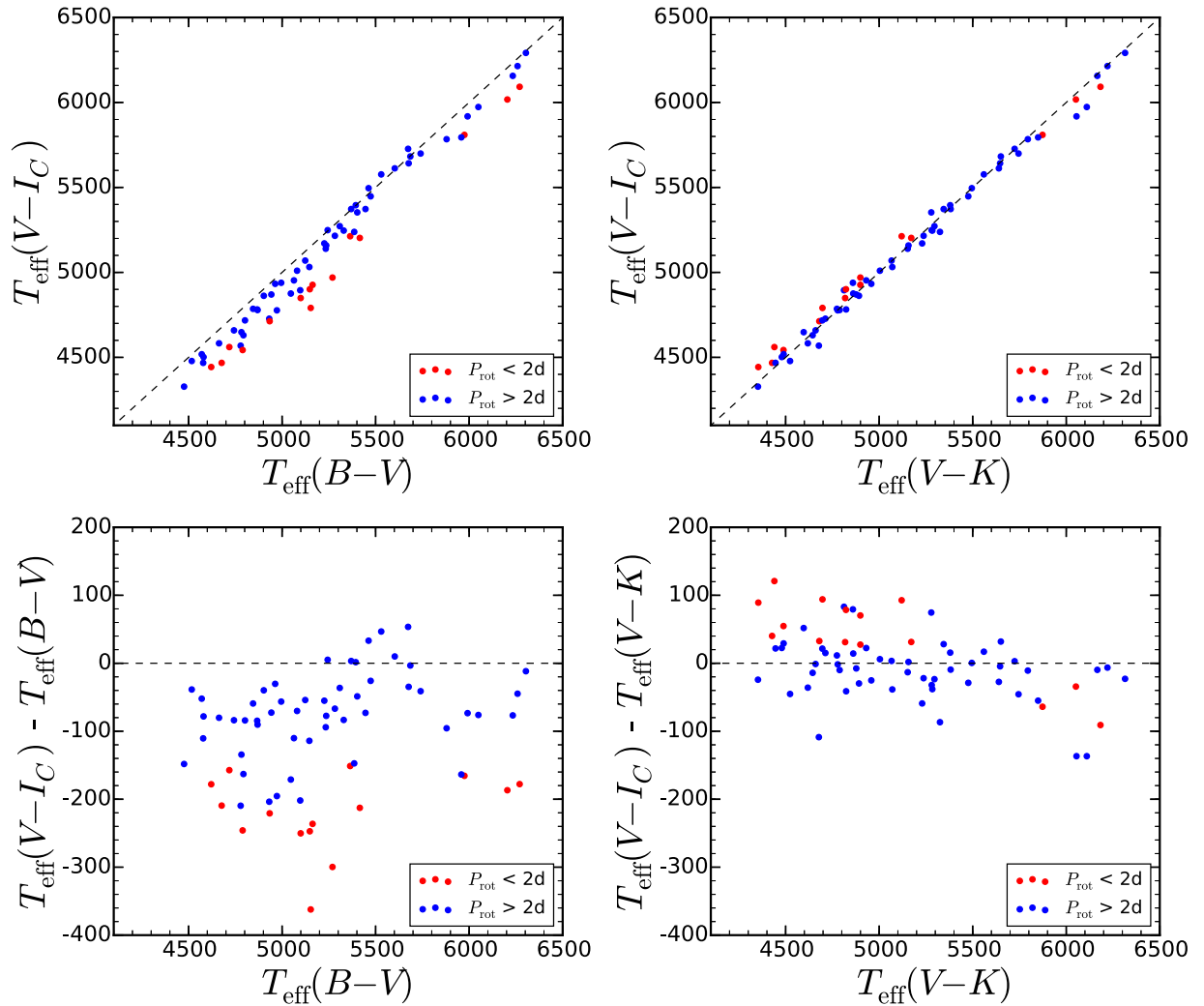


Figure 1. Comparisons between T_{eff} values derived with different color combinations, from the data of Kamai et al. (2014). Top left: $B - V$ and $V - I_c$ T_{eff} s are compared with one another. Each point represents a single star, grouped into fastest (red) and slower (blue) rotators. $B - V$ values are consistently hotter than $V - I_c$ values, and the problem is exacerbated for the fastest rotating stars. Bottom left: the difference between the two T_{eff} derivations as a function of $B - V$ temperature. The agreement is extremely poor overall, demonstrating the unreliability of $B - V$ temperatures of spotted stars. Top right: same as top left, for $V - K_s$ and $V - I_c$. The agreement is generally much better between these bands. Bottom right: same as bottom left, for $V - K_s$ and $V - I_c$. Essentially no systematic offset exists for the slow rotators, and only a mild one for the fastest rotators. This figure attests to the similarity of T_{eff} s derived from $V - I_c$ and $V - K_s$ photometry of spotted stars.

Given these justifications, we proceed with T_{eff} s from the $V - K_s$ data of the combined 2MASS and Johnson & Mitchell (1958) photometric catalogs using the color- T_{eff} relations of C10. For this conversion, we adopt a cluster $[\text{Fe}/\text{H}] = 0.03$ (Soderblom et al. 2009). Propagated errors result from formal uncertainties on the colors, the systematic offsets between the true T_{eff} scale at the C10 scale (quoted at 25 K), and uncertainties on the reddening and metallicity. These are likely lower limits on the errors, as the departure from pristine surfaces will somewhat affect the calibration. Our values are shown in Table 2.

As a check on the validity of our results, we perform in parallel the forthcoming analysis with T_{eff} s derived from an independent method. As a comparison sample, we extract T_{eff} values from the recent *DANCe* analysis of Pleiades members with literature Li values (Barrado et al. 2016). These values were obtained by fitting single-temperature spectral models to the SEDs of their targets, and minimizing the chi-square residual. The authors quote a typical error of 125 K, which we

adopt in every case. These values are listed in Table 3. In what follows, we report results with both $V - K_s$ and *DANCe* T_{eff} s.

2.3. Bolometric Fluxes

Next, we derive bolometric fluxes by considering the full SED of our target stars. In this section, we discuss first the provenance of our SED data, and second our measurement procedure.

2.3.1. Broadband Photometric Data from the Literature

In order to systematize and simplify our procedures, we opted to assemble for each star the available broadband photometry from the following large, all-sky catalogs (listed here in approximate order by wavelength coverage) via the VizieR query service:

1. *GALEX* All-sky Imaging Survey: FUV and NUV at $\approx 0.15 \mu\text{m}$ and $\approx 0.22 \mu\text{m}$, respectively.

Table 2
Derived Stellar Properties ($V - K_s$)

HII	T_{eff} (K)	\mathcal{F}_{bol} $\times 10^{-10}$ (erg cm $^{-2}$ s $^{-1}$)	χ_ν^2	Angular Diameter $\times 10^{-2}$ (mas)	Radius (R_\odot)	Δ Radius (%)
0025	6513 $^{+55}_{-68}$	47.38 $^{+0.59}_{-1.71}$	2.18	8.89 $^{+0.18}_{-0.23}$	1.280 $^{+0.038}_{-0.044}$	6.4 $^{+3.7}_{-3.2}$
0034	5011 $^{+27}_{-34}$	5.77 $^{+0.21}_{-0.15}$	2.45	5.24 $^{+0.12}_{-0.09}$	0.754 $^{+0.024}_{-0.022}$	4.4 $^{+3.0}_{-3.3}$
0097	4658 $^{+23}_{-28}$	4.36 $^{+0.26}_{-0.28}$	7.05	5.27 $^{+0.17}_{-0.18}$	0.759 $^{+0.030}_{-0.031}$	15.4 $^{+4.7}_{-4.5}$
0120	5729 $^{+40}_{-49}$	14.71 $^{+0.29}_{-0.28}$	2.26	6.40 $^{+0.12}_{-0.12}$	0.922 $^{+0.027}_{-0.027}$	3.5 $^{+3.0}_{-3.0}$
0129	5220 $^{+31}_{-38}$	9.06 $^{+0.28}_{-0.27}$	1.99	6.05 $^{+0.12}_{-0.12}$	0.871 $^{+0.026}_{-0.026}$	14.4 $^{+3.4}_{-3.5}$
0152	5816 $^{+41}_{-51}$	15.55 $^{+0.15}_{-0.15}$	0.60	6.39 $^{+0.11}_{-0.11}$	0.920 $^{+0.026}_{-0.026}$	0.3 $^{+2.8}_{-2.8}$
0164	6328 $^{+57}_{-69}$	43.69 $^{+1.14}_{-1.10}$	0.87	9.04 $^{+0.22}_{-0.21}$	1.302 $^{+0.043}_{-0.042}$	16.2 $^{+3.8}_{-3.8}$
0174	5068 $^{+27}_{-34}$	8.23 $^{+0.35}_{-0.33}$	3.14	6.12 $^{+0.15}_{-0.14}$	0.881 $^{+0.029}_{-0.029}$	20.3 $^{+3.9}_{-4.0}$
0193	5396 $^{+32}_{-41}$	10.12 $^{+0.40}_{-0.29}$	2.73	5.99 $^{+0.14}_{-0.12}$	0.862 $^{+0.028}_{-0.026}$	7.9 $^{+3.2}_{-3.5}$
0250	5826 $^{+41}_{-51}$	16.01 $^{+0.32}_{-0.31}$	1.17	6.46 $^{+0.12}_{-0.12}$	0.930 $^{+0.027}_{-0.027}$	1.0 $^{+2.9}_{-3.0}$
0253	5702 $^{+39}_{-48}$	16.17 $^{+0.70}_{-0.49}$	4.30	6.78 $^{+0.18}_{-0.15}$	0.976 $^{+0.034}_{-0.030}$	10.7 $^{+3.5}_{-3.8}$
0263	5163 $^{+30}_{-37}$	8.78 $^{+0.37}_{-0.26}$	1.57	6.09 $^{+0.15}_{-0.12}$	0.877 $^{+0.029}_{-0.026}$	16.9 $^{+3.5}_{-3.9}$
0293	5659 $^{+40}_{-49}$	14.75 $^{+0.30}_{-0.58}$	1.86	6.57 $^{+0.12}_{-0.17}$	0.946 $^{+0.028}_{-0.032}$	8.9 $^{+3.7}_{-3.2}$
0345	5010 $^{+27}_{-34}$	8.94 $^{+0.41}_{-0.48}$	3.51	6.53 $^{+0.17}_{-0.19}$	0.940 $^{+0.032}_{-0.035}$	30.1 $^{+4.8}_{-4.5}$
0380	4380 $^{+20}_{-24}$	2.45 $^{+0.15}_{-0.12}$	5.61	4.47 $^{+0.15}_{-0.12}$	0.643 $^{+0.026}_{-0.023}$	1.7 $^{+3.6}_{-4.1}$
0405	6310 $^{+54}_{-66}$	34.17 $^{+0.39}_{-0.00}$	0.85	8.04 $^{+0.16}_{-0.15}$	1.158 $^{+0.035}_{-0.034}$	4.1 $^{+3.1}_{-3.1}$
0430	5414 $^{+36}_{-44}$	8.89 $^{+0.24}_{-0.31}$	2.43	5.57 $^{+0.11}_{-0.13}$	0.803 $^{+0.024}_{-0.026}$	-0.0 $^{+3.2}_{-3.0}$
0470	7018 $^{+87}_{-101}$	74.86 $^{+0.96}_{-1.86}$	1.95	9.62 $^{+0.27}_{-0.28}$	1.386 $^{+0.049}_{-0.051}$	2.9 $^{+3.8}_{-3.7}$
0489	5968 $^{+43}_{-54}$	20.85 $^{+0.22}_{-0.43}$	1.69	7.02 $^{+0.12}_{-0.14}$	1.011 $^{+0.029}_{-0.030}$	4.3 $^{+3.1}_{-2.9}$
0514	5783 $^{+39}_{-49}$	15.81 $^{+0.32}_{-0.31}$	1.75	6.51 $^{+0.12}_{-0.12}$	0.938 $^{+0.027}_{-0.027}$	3.4 $^{+3.0}_{-3.0}$
0530	7055 $^{+68}_{-84}$	75.16 $^{+0.95}_{-0.93}$	1.51	9.54 $^{+0.21}_{-0.21}$	1.374 $^{+0.044}_{-0.044}$	2.4 $^{+3.2}_{-3.3}$
0627	6412 $^{+57}_{-69}$	39.54 $^{+0.47}_{-0.91}$	0.95	8.38 $^{+0.17}_{-0.19}$	1.206 $^{+0.037}_{-0.039}$	4.3 $^{+3.3}_{-3.2}$
0636	4717 $^{+21}_{-27}$	4.19 $^{+0.24}_{-0.18}$	5.67	5.04 $^{+0.15}_{-0.12}$	0.725 $^{+0.027}_{-0.024}$	8.8 $^{+3.6}_{-4.1}$
0708	5901 $^{+43}_{-53}$	26.88 $^{+0.67}_{-0.96}$	1.65	8.15 $^{+0.17}_{-0.20}$	1.174 $^{+0.036}_{-0.039}$	24.2 $^{+4.1}_{-3.8}$
0746	5486 $^{+37}_{-45}$	9.91 $^{+0.28}_{-0.26}$	2.38	5.73 $^{+0.12}_{-0.12}$	0.825 $^{+0.025}_{-0.025}$	0.7 $^{+3.0}_{-3.1}$
0879	4680 $^{+22}_{-28}$	3.18 $^{+0.22}_{-0.20}$	7.47	4.46 $^{+0.16}_{-0.15}$	0.642 $^{+0.027}_{-0.025}$	-2.9 $^{+3.9}_{-4.1}$
0882	4567 $^{+20}_{-25}$	4.08 $^{+0.17}_{-0.16}$	2.22	5.30 $^{+0.12}_{-0.11}$	0.764 $^{+0.024}_{-0.024}$	17.7 $^{+3.7}_{-3.7}$
0883	4585 $^{+23}_{-28}$	2.55 $^{+0.21}_{-0.19}$	15.80	4.16 $^{+0.18}_{-0.16}$	0.599 $^{+0.029}_{-0.026}$	-8.0 $^{+4.1}_{-4.4}$
0916	5151 $^{+29}_{-36}$	7.56 $^{+0.07}_{-0.07}$	0.31	5.68 $^{+0.08}_{-0.08}$	0.817 $^{+0.021}_{-0.021}$	9.3 $^{+2.9}_{-2.9}$
0923	6067 $^{+41}_{-53}$	26.01 $^{+0.59}_{-0.57}$	2.70	7.59 $^{+0.15}_{-0.15}$	1.093 $^{+0.032}_{-0.032}$	8.5 $^{+3.2}_{-3.2}$
0996	6010 $^{+39}_{-51}$	19.96 $^{+0.20}_{-0.39}$	1.45	6.78 $^{+0.11}_{-0.12}$	0.976 $^{+0.027}_{-0.028}$	-0.9 $^{+2.9}_{-2.7}$
1015	5933 $^{+38}_{-49}$	18.42 $^{+0.18}_{-0.18}$	0.68	6.68 $^{+0.11}_{-0.10}$	0.962 $^{+0.026}_{-0.026}$	0.6 $^{+2.8}_{-2.8}$
1032	5134 $^{+26}_{-34}$	10.92 $^{+0.26}_{-0.12}$	0.51	6.87 $^{+0.11}_{-0.09}$	0.989 $^{+0.028}_{-0.026}$	32.8 $^{+3.4}_{-3.7}$
1095	5063 $^{+28}_{-35}$	6.36 $^{+0.12}_{-0.17}$	1.18	5.39 $^{+0.08}_{-0.10}$	0.776 $^{+0.021}_{-0.022}$	6.0 $^{+3.1}_{-2.9}$
1110	4438 $^{+18}_{-23}$	2.47 $^{+0.13}_{-0.12}$	4.41	4.37 $^{+0.12}_{-0.11}$	0.629 $^{+0.022}_{-0.022}$	-1.4 $^{+3.4}_{-3.5}$
1122	6728 $^{+51}_{-67}$	55.22 $^{+0.68}_{-0.00}$	0.97	8.99 $^{+0.17}_{-0.16}$	1.295 $^{+0.038}_{-0.037}$	0.0 $^{+2.8}_{-2.9}$
1124	5053 $^{+28}_{-35}$	5.14 $^{+0.22}_{-0.21}$	2.97	4.87 $^{+0.12}_{-0.12}$	0.701 $^{+0.023}_{-0.023}$	-4.0 $^{+3.1}_{-3.2}$
1132	6401 $^{+56}_{-69}$	52.38 $^{+3.75}_{-4.65}$	36.26	9.68 $^{+0.40}_{-0.47}$	1.394 $^{+0.065}_{-0.075}$	20.9 $^{+6.5}_{-5.6}$
1139	6651 $^{+63}_{-77}$	51.28 $^{+0.63}_{-0.62}$	0.91	8.87 $^{+0.20}_{-0.20}$	1.277 $^{+0.040}_{-0.040}$	1.1 $^{+3.2}_{-3.2}$
1182	5956 $^{+43}_{-53}$	19.39 $^{+0.40}_{-0.39}$	1.86	6.80 $^{+0.13}_{-0.13}$	0.979 $^{+0.029}_{-0.029}$	1.5 $^{+3.0}_{-3.0}$
1200	6246 $^{+44}_{-61}$	31.51 $^{+0.72}_{-0.35}$	1.76	7.88 $^{+0.17}_{-0.15}$	1.135 $^{+0.035}_{-0.033}$	4.8 $^{+3.1}_{-3.2}$
1207	6016 $^{+44}_{-55}$	18.93 $^{+0.37}_{-0.71}$	3.86	6.58 $^{+0.13}_{-0.17}$	0.948 $^{+0.028}_{-0.032}$	-4.0 $^{+3.2}_{-2.8}$
1215	5968 $^{+44}_{-55}$	18.29 $^{+0.55}_{-0.35}$	2.32	6.58 $^{+0.15}_{-0.13}$	0.947 $^{+0.030}_{-0.028}$	-2.3 $^{+2.9}_{-3.1}$
1220	5309 $^{+32}_{-39}$	6.82 $^{+0.23}_{-0.17}$	1.69	5.07 $^{+0.11}_{-0.09}$	0.731 $^{+0.023}_{-0.021}$	-6.3 $^{+2.7}_{-2.9}$
1298	4975 $^{+26}_{-32}$	4.94 $^{+0.22}_{-0.24}$	5.16	4.92 $^{+0.12}_{-0.13}$	0.709 $^{+0.024}_{-0.025}$	-1.0 $^{+3.5}_{-3.3}$
1305	4376 $^{+18}_{-22}$	2.20 $^{+0.17}_{-0.17}$	9.36	4.24 $^{+0.17}_{-0.17}$	0.611 $^{+0.028}_{-0.028}$	-3.3 $^{+4.4}_{-4.4}$
1309	6569 $^{+61}_{-74}$	47.93 $^{+1.18}_{-1.70}$	2.29	8.79 $^{+0.21}_{-0.24}$	1.265 $^{+0.042}_{-0.045}$	3.1 $^{+3.6}_{-3.4}$
1332	4918 $^{+25}_{-31}$	4.13 $^{+0.14}_{-0.16}$	3.71	4.60 $^{+0.09}_{-0.10}$	0.663 $^{+0.020}_{-0.021}$	-6.0 $^{+2.8}_{-2.8}$
1454	4700 $^{+23}_{-28}$	3.13 $^{+0.24}_{-0.23}$	14.16	4.38 $^{+0.17}_{-0.17}$	0.631 $^{+0.029}_{-0.028}$	-4.9 $^{+2.8}_{-4.3}$
1514	5963 $^{+42}_{-53}$	18.76 $^{+0.19}_{-0.54}$	1.75	6.67 $^{+0.11}_{-0.14}$	0.961 $^{+0.027}_{-0.030}$	-0.7 $^{+3.1}_{-2.8}$
1531	4449 $^{+19}_{-24}$	2.25 $^{+0.19}_{-0.15}$	12.95	4.15 $^{+0.18}_{-0.15}$	0.598 $^{+0.029}_{-0.025}$	-6.4 $^{+3.9}_{-4.5}$
1593	5583 $^{+34}_{-44}$	10.96 $^{+0.20}_{-0.20}$	2.24	5.82 $^{+0.10}_{-0.10}$	0.838 $^{+0.023}_{-0.023}$	-1.0 $^{+2.8}_{-2.8}$
1613	6330 $^{+48}_{-61}$	31.80 $^{+0.35}_{-0.68}$	1.89	7.71 $^{+0.14}_{-0.16}$	1.110 $^{+0.032}_{-0.034}$	-1.0 $^{+3.0}_{-2.9}$
1776	5641 $^{+36}_{-46}$	13.51 $^{+0.13}_{-0.26}$	1.36	6.33 $^{+0.10}_{-0.11}$	0.911 $^{+0.025}_{-0.026}$	5.5 $^{+3.0}_{-2.9}$
1794	6054 $^{+46}_{-57}$	20.82 $^{+0.42}_{-0.21}$	0.79	6.82 $^{+0.14}_{-0.12}$	0.982 $^{+0.029}_{-0.028}$	-2.0 $^{+2.8}_{-2.9}$
1797	6211 $^{+49}_{-60}$	26.01 $^{+0.55}_{-0.53}$	2.16	7.24 $^{+0.15}_{-0.15}$	1.043 $^{+0.032}_{-0.032}$	-2.4 $^{+3.0}_{-3.0}$

Table 2
(Continued)

HII	T_{eff} (K)	\mathcal{F}_{bol} $\times 10^{-10}$ ($\text{erg cm}^{-2} \text{s}^{-1}$)	χ^2_{ν}	Angular Diameter $\times 10^{-2}$ (mas)	Radius (R_{\odot})	ΔRadius (%)
1856	6241 ⁺⁴⁶ ₋₅₈	28.41 ^{+0.31} _{-0.60}	2.13	7.50 ^{+0.13} _{-0.15}	1.080 ^{+0.031} _{-0.032}	-0.1 ^{+3.0} _{-2.8}
1883	4612 ⁺²⁰ ₋₂₆	3.85 ^{+0.30} _{-0.34}	18.99	5.06 ^{+0.21} _{-0.23}	0.728 ^{+0.034} _{-0.036}	11.5 ^{+5.6} _{-5.2}
1924	6066 ⁺⁴⁶ ₋₅₇	21.46 ^{+0.22} _{-0.22}	1.21	6.90 ^{+0.12} _{-0.12}	0.993 ^{+0.028} _{-0.028}	-1.3 ^{+2.8} _{-2.8}
2016	4319 ⁺¹⁶ ₋₂₁	2.29 ^{+0.06} _{-0.08}	1.99	4.44 ^{+0.07} _{-0.08}	0.640 ^{+0.018} _{-0.019}	2.3 ^{+3.0} _{-2.8}
2034	4762 ⁺²³ ₋₂₉	3.94 ^{+0.17} _{-0.13}	2.89	4.79 ^{+0.12} _{-0.10}	0.690 ^{+0.023} _{-0.021}	2.4 ^{+3.1} _{-3.4}
2106	5164 ⁺²⁸ ₋₃₅	8.79 ^{+0.27} _{-0.26}	1.43	6.09 ^{+0.12} _{-0.12}	0.877 ^{+0.026} _{-0.026}	16.9 ^{+3.5} _{-3.5}
2126	5352 ⁺³¹ ₋₄₀	7.26 ^{+0.31} _{-0.24}	3.06	5.15 ^{+0.13} _{-0.11}	0.742 ^{+0.025} _{-0.023}	-6.0 ^{+2.9} _{-3.2}
2244	4627 ⁺²² ₋₂₈	3.86 ^{+0.18} _{-0.14}	2.81	5.02 ^{+0.13} _{-0.11}	0.723 ^{+0.025} _{-0.022}	10.5 ^{+3.4} _{-3.8}
2284	5365 ⁺³² ₋₄₀	9.80 ^{+0.09} _{-0.09}	0.52	5.96 ^{+0.09} _{-0.09}	0.858 ^{+0.023} _{-0.023}	8.4 ^{+2.9} _{-2.9}
2311	5413 ⁺³⁵ ₋₄₃	8.80 ^{+0.24} _{-0.23}	4.16	5.55 ^{+0.11} _{-0.11}	0.799 ^{+0.024} _{-0.024}	-0.4 ^{+3.0} _{-3.0}
2341	5773 ⁺⁴⁰ ₋₅₀	13.31 ^{+0.25} _{-0.12}	1.94	6.00 ^{+0.11} _{-0.10}	0.864 ^{+0.025} _{-0.024}	-4.4 ^{+2.7} _{-2.2}
2345	6802 ⁺⁶⁵ ₋₈₀	64.81 ^{+0.84} _{-0.82}	1.62	9.53 ^{+0.21} _{-0.21}	1.373 ^{+0.043} _{-0.043}	4.1 ^{+3.3} _{-3.3}
2366	5356 ⁺³¹ ₋₄₀	8.22 ^{+0.22} _{-0.28}	1.94	5.48 ^{+0.10} _{-0.12}	0.789 ^{+0.023} _{-0.025}	-0.2 ^{+3.1} _{-2.9}
2462	5385 ⁺³² ₋₄₀	7.98 ^{+0.21} _{-0.20}	1.45	5.34 ^{+0.10} _{-0.10}	0.768 ^{+0.023} _{-0.022}	-3.5 ^{+2.8} _{-2.8}
2506	6111 ⁺⁴⁴ ₋₅₆	23.80 ^{+0.25} _{-0.49}	1.26	7.16 ^{+0.12} _{-0.14}	1.030 ^{+0.029} _{-0.031}	0.5 ^{+3.0} _{-2.8}
2644	5680 ⁺³⁶ ₋₄₆	12.06 ^{+0.22} _{-0.32}	1.15	5.90 ^{+0.10} _{-0.12}	0.849 ^{+0.024} _{-0.025}	-3.0 ^{+2.9} _{-2.7}
2665	5362 ⁺³³ ₋₄₁	9.77 ^{+0.19} _{-0.19}	0.78	5.96 ^{+0.10} _{-0.10}	0.858 ^{+0.024} _{-0.024}	8.4 ^{+3.0} _{-3.1}
2741	4811 ⁺²³ ₋₂₉	3.53 ^{+0.30} _{-0.26}	14.15	4.44 ^{+0.19} _{-0.17}	0.640 ^{+0.031} _{-0.029}	-6.4 ^{+4.2} _{-4.6}
2786	6074 ⁺⁴⁴ ₋₅₅	22.53 ^{+0.23} _{-0.46}	1.11	7.05 ^{+0.12} _{-0.14}	1.015 ^{+0.029} _{-0.030}	0.5 ^{+3.0} _{-2.8}
2870	4887 ⁺²⁶ ₋₃₂	3.92 ^{+0.26} _{-0.21}	8.08	4.54 ^{+0.16} _{-0.13}	0.654 ^{+0.027} _{-0.024}	-6.4 ^{+3.4} _{-3.9}
2880	5198 ⁺²⁸ ₋₃₆	7.12 ^{+0.13} _{-0.19}	0.60	5.41 ^{+0.08} _{-0.10}	0.779 ^{+0.021} _{-0.022}	2.9 ^{+3.0} _{-2.8}
3019	4325 ⁺¹⁸ ₋₂₂	2.33 ^{+0.13} _{-0.12}	9.22	4.47 ^{+0.13} _{-0.12}	0.644 ^{+0.024} _{-0.023}	2.7 ^{+3.6} _{-3.8}
3031	7048 ⁺⁶⁴ ₋₈₁	86.19 ^{+0.00} _{-1.15}	0.68	10.24 ^{+0.21} _{-0.22}	1.474 ^{+0.045} _{-0.046}	9.7 ^{+3.4} _{-3.3}
3063	4295 ⁺¹⁸ ₋₂₂	2.29 ^{+0.15} _{-0.14}	6.12	4.50 ^{+0.15} _{-0.14}	0.647 ^{+0.026} _{-0.025}	4.0 ^{+4.0} _{-4.2}
3163	4579 ⁺²² ₋₂₇	3.87 ^{+0.23} _{-0.25}	7.42	5.14 ^{+0.16} _{-0.17}	0.740 ^{+0.029} _{-0.030}	13.9 ^{+4.6} _{-4.4}
3179	6154 ⁺⁴⁴ ₋₅₆	28.14 ^{+0.32} _{-0.92}	2.34	7.67 ^{+0.13} _{-0.18}	1.105 ^{+0.031} _{-0.036}	5.9 ^{+3.4} _{-3.0}
3187	4495 ⁺²⁰ ₋₂₅	2.70 ^{+0.14} _{-0.13}	7.58	4.45 ^{+0.13} _{-0.12}	0.641 ^{+0.023} _{-0.022}	-0.3 ^{+3.4} _{-3.6}

Note. Derived parameters for our $V - K_s$ T_{eff} s (Section 2). Bolometric flux values are in units of $10^{-10} \text{ erg cm}^{-2} \text{ s}^{-1}$, and angular diameters in units of 10^{-2} mas. (This table is available in machine-readable form.)

2. Catalog of Homogeneous Means in the *UBV* System for bright stars from Mermilliod (1987): Johnson *UBV* bands ($\approx 0.35\text{--}0.55 \mu\text{m}$).
3. *Tycho-2*: Tycho *B* (B_T) and Tycho *V* (V_T) bands ($\approx 0.42 \mu\text{m}$ and $\approx 0.54 \mu\text{m}$, respectively).
4. Strömgren Photometric Catalog by Paunzen (2015): Strömgren *uvby* bands ($\approx 0.34\text{--}0.55 \mu\text{m}$).
5. AAVSO Photometric All-sky Survey DR6 (obtained from the UCAC-4 catalog): Johnson *BV* and SDSS *gri* bands ($\approx 0.45\text{--}0.75 \mu\text{m}$).
6. 2MASS: *JHK_s* bands ($\approx 1.2\text{--}2.2 \mu\text{m}$).
7. All-*WISE*: *WISE1-4* bands ($\approx 3.5\text{--}22 \mu\text{m}$).

We found *BV*, *JHK_s*, and *WISE1-3* photometry—spanning a wavelength range $\approx 0.4\text{--}10 \mu\text{m}$ —for nearly all of the stars in our study sample. Most of the stars also have *WISE4* photometry, and many of the stars also have Strömgren and/or *GALEX* photometry, thus extending the wavelength coverage to $\approx 0.15\text{--}22 \mu\text{m}$. We adopted the reported measurement uncertainties unless they were less than 0.01 mag, in which case we assumed an uncertainty of 0.01 mag. In addition, to account for an artifact in the Kurucz atmospheres at $10 \mu\text{m}$, we artificially inflated the *WISE3* uncertainty to 0.1 mag unless the reported uncertainty was already larger than 0.1 mag. The assembled SEDs are presented in the Appendix.

2.3.2. Spectral Energy Distribution Fitting

We followed the SED fitting procedures described in Stassun & Torres (2016). Briefly, the observed SEDs were fitted with standard stellar atmosphere models from Kurucz (2013). As summarized in Tables 2 and 3, for each star we have T_{eff} , and we assume a main-sequence $\log g$ and solar metallicity. We interpolated in the model grid to obtain the appropriate model atmosphere for each star in units of emergent flux. To redden the SED model, we adopted the interstellar extinction law of Cardelli et al. (1989). We then fitted the atmosphere model to the flux measurements to minimize χ^2 by varying just two fit parameters: extinction (A_V) and overall normalization (effectively the ratio of the stellar radius to the distance, R_*/d^2). (The adopted stellar T_{eff} also has an associated uncertainty; this is handled in a later step via the propagation of errors through the stellar angular radius, Θ ; see Section 2.4.) We allowed the fit to vary A_V within the generally accepted reddening range of $E(B - V) = 0.04 \pm 0.01$ (e.g., An et al. 2007). The best-fit model SED with extinction is shown for each star in the Appendix, and the reduced χ^2 values (χ^2_{ν}) are given in Tables 2 and 3.

The primary quantity of interest for each star is \mathcal{F}_{bol} , which we obtained via direct summation of the fitted SED, *without* extinction, over all wavelengths. The formal uncertainty in \mathcal{F}_{bol}

Table 3
Derived Stellar Properties (*DANCe*)

HII	T_{eff} (K)	\mathcal{F}_{bol} $\times 10^{-10}$ (erg cm $^{-2}$ s $^{-1}$)	χ_{ν}^2	Angular Diameter $\times 10^{-2}$ (mas)	Radius (R_{\odot})	Δ Radius (%)
0025	6481 $^{+125}_{-125}$	46.67 $^{+1.18}_{-1.69}$	2.20	8.91 $^{+0.36}_{-0.38}$	1.283 $^{+0.059}_{-0.062}$	8.0 $^{+5.2}_{-5.0}$
0034	5075 $^{+125}_{-125}$	5.84 $^{+0.26}_{-0.20}$	3.64	5.14 $^{+0.28}_{-0.27}$	0.740 $^{+0.043}_{-0.042}$	0.9 $^{+5.7}_{-5.9}$
0097	4586 $^{+125}_{-125}$	4.26 $^{+0.22}_{-0.20}$	4.73	5.38 $^{+0.32}_{-0.32}$	0.775 $^{+0.050}_{-0.049}$	19.1 $^{+7.6}_{-7.7}$
0120	5683 $^{+125}_{-125}$	14.64 $^{+0.45}_{-0.71}$	2.63	6.49 $^{+0.30}_{-0.33}$	0.935 $^{+0.048}_{-0.051}$	6.7 $^{+5.9}_{-5.5}$
0129	5253 $^{+125}_{-125}$	9.10 $^{+0.28}_{-0.26}$	2.46	5.99 $^{+0.30}_{-0.30}$	0.862 $^{+0.047}_{-0.047}$	12.3 $^{+6.1}_{-6.1}$
0152	5767 $^{+125}_{-125}$	15.40 $^{+0.15}_{-0.15}$	0.52	6.46 $^{+0.28}_{-0.28}$	0.931 $^{+0.046}_{-0.046}$	3.2 $^{+5.1}_{-5.1}$
0164	6405 $^{+125}_{-125}$	45.49 $^{+0.00}_{-0.57}$	0.79	9.01 $^{+0.35}_{-0.36}$	1.297 $^{+0.058}_{-0.059}$	12.4 $^{+5.1}_{-5.1}$
0174	4997 $^{+125}_{-125}$	8.06 $^{+0.27}_{-0.25}$	1.95	6.23 $^{+0.33}_{-0.33}$	0.897 $^{+0.051}_{-0.051}$	24.6 $^{+7.1}_{-7.1}$
0193	5265 $^{+125}_{-125}$	9.79 $^{+0.31}_{-0.39}$	1.95	6.19 $^{+0.31}_{-0.32}$	0.891 $^{+0.049}_{-0.050}$	15.6 $^{+6.5}_{-6.3}$
0250	5655 $^{+125}_{-125}$	15.14 $^{+0.48}_{-0.61}$	1.26	6.67 $^{+0.31}_{-0.32}$	0.960 $^{+0.050}_{-0.051}$	10.7 $^{+5.9}_{-5.8}$
0253	5465 $^{+125}_{-125}$	14.82 $^{+1.05}_{-0.80}$	5.29	7.06 $^{+0.41}_{-0.37}$	1.017 $^{+0.063}_{-0.059}$	24.9 $^{+7.2}_{-7.8}$
0263	5007 $^{+125}_{-125}$	8.25 $^{+0.18}_{-0.09}$	0.41	6.28 $^{+0.32}_{-0.32}$	0.904 $^{+0.050}_{-0.050}$	25.2 $^{+6.9}_{-7.0}$
0293	5565 $^{+125}_{-125}$	13.98 $^{+0.60}_{-0.70}$	2.52	6.61 $^{+0.33}_{-0.34}$	0.952 $^{+0.052}_{-0.053}$	13.3 $^{+6.3}_{-6.2}$
0345	4959 $^{+125}_{-125}$	8.63 $^{+0.51}_{-0.47}$	3.82	6.54 $^{+0.38}_{-0.37}$	0.942 $^{+0.059}_{-0.058}$	32.2 $^{+8.1}_{-8.3}$
0380	4343 $^{+125}_{-125}$	2.43 $^{+0.11}_{-0.10}$	4.18	4.53 $^{+0.28}_{-0.28}$	0.652 $^{+0.043}_{-0.043}$	3.7 $^{+6.8}_{-6.8}$
0405	6194 $^{+125}_{-125}$	33.05 $^{+0.80}_{-0.77}$	0.81	8.21 $^{+0.35}_{-0.34}$	1.182 $^{+0.056}_{-0.056}$	11.5 $^{+5.3}_{-5.3}$
0430	5365 $^{+125}_{-125}$	8.84 $^{+0.16}_{-0.24}$	1.76	5.66 $^{+0.27}_{-0.27}$	0.815 $^{+0.043}_{-0.044}$	2.9 $^{+5.5}_{-5.4}$
0470	7048 $^{+125}_{-125}$	74.70 $^{+0.94}_{-1.83}$	2.15	9.53 $^{+0.34}_{-0.36}$	1.373 $^{+0.058}_{-0.060}$	2.2 $^{+4.5}_{-4.3}$
0489	5851 $^{+125}_{-125}$	20.14 $^{+0.67}_{-0.84}$	1.83	7.18 $^{+0.33}_{-0.34}$	1.034 $^{+0.053}_{-0.054}$	11.4 $^{+5.9}_{-5.7}$
0514	5679 $^{+125}_{-125}$	15.66 $^{+0.33}_{-0.48}$	1.50	6.72 $^{+0.30}_{-0.31}$	0.968 $^{+0.049}_{-0.050}$	10.6 $^{+5.7}_{-5.6}$
0530	6918 $^{+125}_{-125}$	72.92 $^{+2.93}_{-1.86}$	1.53	9.77 $^{+0.40}_{-0.37}$	1.408 $^{+0.066}_{-0.062}$	4.8 $^{+4.7}_{-4.9}$
0627	6413 $^{+125}_{-125}$	39.56 $^{+0.47}_{-0.91}$	0.95	8.38 $^{+0.33}_{-0.34}$	1.207 $^{+0.055}_{-0.056}$	4.2 $^{+4.8}_{-4.7}$
0636	4779 $^{+125}_{-125}$	4.24 $^{+0.27}_{-0.25}$	8.46	4.94 $^{+0.30}_{-0.30}$	0.711 $^{+0.047}_{-0.046}$	5.0 $^{+6.7}_{-6.9}$
0708	5882 $^{+125}_{-125}$	26.39 $^{+0.99}_{-0.94}$	1.72	8.13 $^{+0.38}_{-0.37}$	1.171 $^{+0.060}_{-0.060}$	24.8 $^{+6.4}_{-6.4}$
0746	5465 $^{+125}_{-125}$	9.88 $^{+0.28}_{-0.27}$	2.06	5.77 $^{+0.28}_{-0.28}$	0.830 $^{+0.044}_{-0.044}$	1.9 $^{+5.4}_{-5.4}$
0879	4676 $^{+125}_{-125}$	3.19 $^{+0.19}_{-0.22}$	7.24	4.47 $^{+0.27}_{-0.28}$	0.644 $^{+0.042}_{-0.044}$	-2.5 $^{+6.6}_{-6.4}$
0882	4497 $^{+125}_{-125}$	3.90 $^{+0.16}_{-0.15}$	2.12	5.35 $^{+0.32}_{-0.32}$	0.771 $^{+0.049}_{-0.049}$	19.8 $^{+7.6}_{-7.6}$
0883	4532 $^{+125}_{-125}$	2.55 $^{+0.17}_{-0.14}$	9.55	4.26 $^{+0.27}_{-0.26}$	0.613 $^{+0.042}_{-0.040}$	-5.1 $^{+6.2}_{-6.5}$
0916	5117 $^{+125}_{-125}$	7.49 $^{+0.07}_{-0.14}$	0.27	5.73 $^{+0.28}_{-0.28}$	0.825 $^{+0.044}_{-0.045}$	11.2 $^{+6.1}_{-6.0}$
0923	6051 $^{+125}_{-125}$	25.90 $^{+0.59}_{-0.29}$	2.51	7.61 $^{+0.33}_{-0.32}$	1.096 $^{+0.053}_{-0.052}$	9.6 $^{+5.2}_{-5.3}$
0996	5969 $^{+125}_{-125}$	19.81 $^{+0.20}_{-0.20}$	0.93	6.84 $^{+0.29}_{-0.29}$	0.986 $^{+0.047}_{-0.047}$	1.7 $^{+4.9}_{-4.9}$
1015	5887 $^{+125}_{-125}$	18.37 $^{+0.19}_{-0.37}$	0.63	6.78 $^{+0.29}_{-0.30}$	0.976 $^{+0.047}_{-0.048}$	3.8 $^{+5.1}_{-5.0}$
1032	5309 $^{+125}_{-125}$	11.79 $^{+0.13}_{-0.25}$	0.69	6.67 $^{+0.32}_{-0.32}$	0.961 $^{+0.050}_{-0.051}$	23.3 $^{+6.6}_{-6.5}$
1095	5099 $^{+125}_{-125}$	6.44 $^{+0.12}_{-0.17}$	1.52	5.35 $^{+0.27}_{-0.27}$	0.770 $^{+0.042}_{-0.043}$	4.3 $^{+5.8}_{-5.7}$
1110	4424 $^{+125}_{-125}$	2.44 $^{+0.13}_{-0.12}$	4.13	4.37 $^{+0.27}_{-0.27}$	0.630 $^{+0.042}_{-0.041}$	-1.1 $^{+6.5}_{-6.5}$
1122	6622 $^{+125}_{-125}$	54.60 $^{+0.70}_{-0.68}$	0.49	9.23 $^{+0.35}_{-0.35}$	1.329 $^{+0.059}_{-0.059}$	6.3 $^{+4.7}_{-4.7}$
1124	4875 $^{+125}_{-125}$	4.76 $^{+0.13}_{-0.12}$	1.28	5.03 $^{+0.27}_{-0.27}$	0.725 $^{+0.042}_{-0.042}$	4.1 $^{+6.0}_{-6.0}$
1132	6449 $^{+125}_{-125}$	51.68 $^{+4.37}_{-3.87}$	38.32	9.47 $^{+0.54}_{-0.51}$	1.364 $^{+0.084}_{-0.080}$	16.2 $^{+6.8}_{-7.2}$
1139	6600 $^{+125}_{-125}$	51.63 $^{+0.00}_{-1.26}$	0.70	9.04 $^{+0.34}_{-0.36}$	1.301 $^{+0.057}_{-0.059}$	4.8 $^{+4.8}_{-4.6}$
1182	5879 $^{+125}_{-125}$	19.00 $^{+0.60}_{-0.76}$	2.24	6.91 $^{+0.31}_{-0.32}$	0.995 $^{+0.050}_{-0.052}$	6.1 $^{+5.5}_{-5.4}$
1200	6207 $^{+125}_{-125}$	31.53 $^{+0.37}_{-0.71}$	1.58	7.98 $^{+0.32}_{-0.33}$	1.150 $^{+0.053}_{-0.055}$	7.9 $^{+5.1}_{-5.0}$
1207	5977 $^{+125}_{-125}$	18.98 $^{+0.38}_{-1.08}$	3.91	6.68 $^{+0.29}_{-0.34}$	0.962 $^{+0.047}_{-0.053}$	-1.1 $^{+5.5}_{-4.8}$
1215	5975 $^{+125}_{-125}$	18.39 $^{+0.36}_{-0.53}$	2.37	6.58 $^{+0.28}_{-0.29}$	0.948 $^{+0.046}_{-0.047}$	-2.5 $^{+4.8}_{-4.7}$
1220	5289 $^{+125}_{-125}$	6.78 $^{+0.17}_{-0.17}$	1.48	5.10 $^{+0.25}_{-0.25}$	0.734 $^{+0.040}_{-0.039}$	-5.3 $^{+5.1}_{-5.1}$
1298	4846 $^{+125}_{-125}$	4.77 $^{+0.18}_{-0.13}$	2.46	5.09 $^{+0.28}_{-0.27}$	0.734 $^{+0.043}_{-0.042}$	6.3 $^{+6.1}_{-6.3}$
1305	4288 $^{+125}_{-125}$	2.13 $^{+0.11}_{-0.12}$	5.03	4.35 $^{+0.28}_{-0.28}$	0.627 $^{+0.043}_{-0.043}$	0.8 $^{+6.9}_{-6.8}$
1309	6467 $^{+125}_{-125}$	45.57 $^{+1.74}_{-1.64}$	2.33	8.84 $^{+0.38}_{-0.38}$	1.273 $^{+0.062}_{-0.061}$	7.8 $^{+5.2}_{-5.2}$
1332	4800 $^{+125}_{-125}$	3.99 $^{+0.10}_{-0.10}$	1.75	4.75 $^{+0.25}_{-0.25}$	0.684 $^{+0.040}_{-0.040}$	0.4 $^{+5.8}_{-5.8}$
1454	4669 $^{+125}_{-125}$	3.11 $^{+0.21}_{-0.19}$	12.06	4.43 $^{+0.28}_{-0.27}$	0.638 $^{+0.043}_{-0.042}$	-3.3 $^{+6.4}_{-6.5}$
1514	5897 $^{+125}_{-125}$	18.18 $^{+0.75}_{-0.54}$	2.06	6.72 $^{+0.32}_{-0.30}$	0.967 $^{+0.051}_{-0.049}$	2.5 $^{+5.1}_{-5.4}$
1531	4216 $^{+125}_{-125}$	2.20 $^{+0.06}_{-0.06}$	2.12	4.58 $^{+0.28}_{-0.28}$	0.659 $^{+0.043}_{-0.043}$	7.5 $^{+7.0}_{-7.0}$
1593	5593 $^{+125}_{-125}$	10.97 $^{+0.20}_{-0.29}$	2.33	5.80 $^{+0.26}_{-0.27}$	0.835 $^{+0.042}_{-0.043}$	-1.6 $^{+5.1}_{-5.0}$
1613	6316 $^{+125}_{-125}$	31.74 $^{+0.35}_{-0.69}$	1.71	7.74 $^{+0.31}_{-0.32}$	1.114 $^{+0.051}_{-0.052}$	-0.1 $^{+4.7}_{-4.6}$
1776	5557 $^{+125}_{-125}$	13.17 $^{+0.41}_{-0.39}$	1.38	6.44 $^{+0.31}_{-0.30}$	0.927 $^{+0.049}_{-0.049}$	10.6 $^{+5.8}_{-5.8}$
1794	5995 $^{+125}_{-125}$	20.48 $^{+0.21}_{-0.21}$	0.45	6.90 $^{+0.29}_{-0.29}$	0.993 $^{+0.047}_{-0.047}$	1.5 $^{+4.8}_{-4.8}$
1797	6231 $^{+125}_{-125}$	26.16 $^{+0.55}_{-0.79}$	2.41	7.22 $^{+0.30}_{-0.31}$	1.039 $^{+0.049}_{-0.050}$	-3.5 $^{+4.7}_{-4.6}$

Table 3
(Continued)

HII	T_{eff} (K)	\mathcal{F}_{bol} $\times 10^{-10}$ ($\text{erg cm}^{-2} \text{s}^{-1}$)	χ^2_{ν}	Angular Diameter $\times 10^{-2}$ (mas)	Radius (R_{\odot})	ΔRadius (%)
1856	6161^{+125}_{-125}	$27.99^{+0.63}_{-1.20}$	2.08	$7.64^{+0.32}_{-0.35}$	$1.100^{+0.052}_{-0.056}$	$5.2^{+5.4}_{-5.0}$
1883	4544^{+125}_{-125}	$3.88^{+0.28}_{-0.35}$	16.25	$5.23^{+0.34}_{-0.37}$	$0.753^{+0.052}_{-0.056}$	$16.3^{+8.7}_{-8.1}$
1924	6086^{+125}_{-125}	$21.43^{+0.22}_{-0.21}$	1.43	$6.85^{+0.28}_{-0.28}$	$0.986^{+0.046}_{-0.046}$	$-2.8^{+4.6}_{-4.6}$
2016	4375^{+125}_{-125}	$2.33^{+0.08}_{-0.08}$	2.53	$4.37^{+0.26}_{-0.26}$	$0.629^{+0.040}_{-0.040}$	$-0.5^{+6.3}_{-6.3}$
2034	4669^{+125}_{-125}	$3.81^{+0.14}_{-0.10}$	1.79	$4.91^{+0.28}_{-0.27}$	$0.706^{+0.043}_{-0.042}$	$7.1^{+6.4}_{-6.5}$
2106	5140^{+125}_{-125}	$8.74^{+0.18}_{-0.26}$	1.30	$6.13^{+0.30}_{-0.31}$	$0.883^{+0.048}_{-0.049}$	$18.4^{+6.6}_{-6.5}$
2126	5302^{+125}_{-125}	$7.17^{+0.25}_{-0.24}$	2.24	$5.22^{+0.26}_{-0.26}$	$0.752^{+0.041}_{-0.041}$	$-3.4^{+5.3}_{-5.3}$
2244	4656^{+125}_{-125}	$3.89^{+0.18}_{-0.17}$	3.67	$4.98^{+0.29}_{-0.29}$	$0.718^{+0.045}_{-0.045}$	$9.1^{+6.8}_{-6.8}$
2284	5418^{+125}_{-125}	$9.97^{+0.19}_{-0.19}$	0.82	$5.89^{+0.28}_{-0.28}$	$0.848^{+0.044}_{-0.044}$	$5.6^{+5.5}_{-5.5}$
2311	5438^{+125}_{-125}	$8.87^{+0.24}_{-0.30}$	4.88	$5.52^{+0.26}_{-0.27}$	$0.795^{+0.042}_{-0.043}$	$-1.7^{+5.3}_{-5.2}$
2341	5750^{+125}_{-125}	$13.37^{+0.25}_{-0.12}$	1.58	$6.06^{+0.27}_{-0.26}$	$0.872^{+0.043}_{-0.043}$	$-2.7^{+4.8}_{-4.8}$
2345	6726^{+125}_{-125}	$64.14^{+0.85}_{-2.46}$	1.48	$9.70^{+0.37}_{-0.41}$	$1.397^{+0.061}_{-0.066}$	$8.0^{+5.1}_{-4.7}$
2366	5368^{+125}_{-125}	$8.25^{+0.22}_{-0.28}$	2.05	$5.46^{+0.26}_{-0.27}$	$0.787^{+0.042}_{-0.043}$	$-0.7^{+5.4}_{-5.3}$
2462	5467^{+125}_{-125}	$8.17^{+0.28}_{-0.27}$	2.47	$5.24^{+0.26}_{-0.25}$	$0.755^{+0.041}_{-0.040}$	$-7.4^{+4.9}_{-5.0}$
2506	6005^{+125}_{-125}	$22.96^{+0.50}_{-0.72}$	1.16	$7.28^{+0.31}_{-0.32}$	$1.048^{+0.051}_{-0.052}$	$6.7^{+5.3}_{-5.2}$
2644	5594^{+125}_{-125}	$11.60^{+0.22}_{-0.21}$	0.84	$5.96^{+0.27}_{-0.27}$	$0.859^{+0.044}_{-0.044}$	$1.1^{+5.1}_{-5.1}$
2665	5366^{+125}_{-125}	$9.71^{+0.19}_{-0.18}$	0.79	$5.93^{+0.28}_{-0.28}$	$0.854^{+0.045}_{-0.045}$	$7.8^{+5.7}_{-5.7}$
2741	4792^{+125}_{-125}	$3.52^{+0.27}_{-0.26}$	12.33	$4.48^{+0.29}_{-0.29}$	$0.645^{+0.044}_{-0.044}$	$-5.1^{+6.5}_{-6.5}$
2786	6071^{+125}_{-125}	$22.46^{+0.23}_{-0.46}$	1.13	$7.04^{+0.29}_{-0.30}$	$1.014^{+0.048}_{-0.049}$	$0.6^{+4.8}_{-4.7}$
2870	4840^{+125}_{-125}	$3.89^{+0.20}_{-0.18}$	6.12	$4.61^{+0.27}_{-0.26}$	$0.664^{+0.041}_{-0.041}$	$-3.6^{+5.9}_{-6.0}$
2880	5261^{+125}_{-125}	$7.34^{+0.13}_{-0.13}$	0.55	$5.36^{+0.26}_{-0.26}$	$0.772^{+0.041}_{-0.041}$	$0.3^{+5.3}_{-5.3}$
3019	4192^{+125}_{-125}	$2.26^{+0.09}_{-0.12}$	5.96	$4.68^{+0.29}_{-0.31}$	$0.674^{+0.045}_{-0.047}$	$10.5^{+7.7}_{-7.4}$
3031	6935^{+125}_{-125}	$82.20^{+1.14}_{-1.11}$	0.71	$10.33^{+0.38}_{-0.38}$	$1.487^{+0.064}_{-0.064}$	$10.6^{+4.8}_{-4.8}$
3063	4292^{+125}_{-125}	$2.30^{+0.15}_{-0.14}$	6.03	$4.51^{+0.30}_{-0.30}$	$0.650^{+0.046}_{-0.045}$	$4.4^{+7.2}_{-7.4}$
3163	4456^{+125}_{-125}	$3.71^{+0.11}_{-0.15}$	2.66	$5.31^{+0.31}_{-0.32}$	$0.765^{+0.048}_{-0.049}$	$19.6^{+7.6}_{-7.5}$
3179	6120^{+125}_{-125}	$27.59^{+0.95}_{-0.90}$	2.48	$7.68^{+0.34}_{-0.34}$	$1.106^{+0.055}_{-0.055}$	$7.6^{+5.3}_{-5.3}$
3187	4464^{+125}_{-125}	$2.70^{+0.12}_{-0.13}$	6.60	$4.52^{+0.27}_{-0.28}$	$0.651^{+0.042}_{-0.042}$	$1.7^{+6.6}_{-6.5}$

Note. Derived parameters for the *DANCe* T_{eff} s (Section 2). Bolometric flux values are in units of $10^{-10} \text{ erg cm}^{-2} \text{ s}^{-1}$, and angular diameters in units of 10^{-2} mas . (This table is available in machine-readable form.)

was determined according to the standard criterion of $\Delta\chi^2 = 2.30$ for the case of two fitted parameters (e.g., Press et al. 1992), where we first re-normalized the χ^2 of the fits such that $\chi^2_{\nu} = 1$ for the best fit model. Because χ^2_{ν} is in almost all cases greater than 1 (see Tables 2 and 3), this χ^2 renormalization is equivalent to inflating the photometric measurement errors by a constant factor and results in a more conservative final uncertainty in \mathcal{F}_{bol} according to the $\Delta\chi^2$ criterion.

Figure 2 illustrates the resulting χ^2_{ν} values resulting from the three T_{eff} scales discussed in Section 2.2, distinguishing between the faster (red) and slower (blue) rotating subsets of our sample. The $B - V$ temperatures produce many extremely poor fits, with nearly half the rapid rotators falling above $\chi^2_{\nu} = 20$. By contrast, these outliers generally produce acceptable fits when the $V - K_s$ and *DANCe* scales are employed, showing little difference in the χ^2_{ν} distribution of the slow and rapid rotators. This serves as further justification for our choice of T_{eff} scale.

2.4. Radius Derivation and Errors

Finally, the stellar radius can be derived by combining \mathcal{F}_{bol} and T_{eff} into an angular radius Θ , and multiplying by the

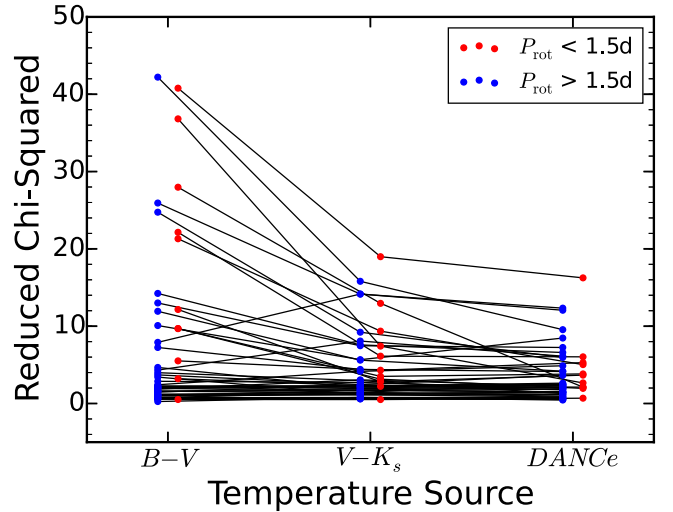


Figure 2. Comparison of the χ^2_{ν} values arising during our SED fitting procedure (Section 2.3.2), for the rapid (red) and slow (blue) members of our sample. Rapid and slow samples have been slightly offset for visibility. $B - V$ temperatures perform the worst on the whole, producing the largest number of extremely poor fits ($\chi_{\nu} < 20$), whereas $V - K_s$ and *DANCe* scales produce far better. This attests to the poor quality of $B - V$ T_{eff} s in spotted stars, and the superiority of the $V - K_s$ and *DANCe* values.

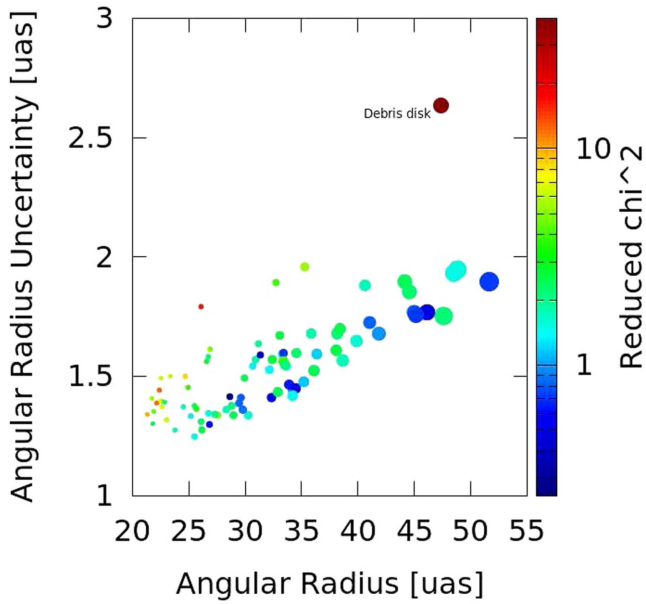


Figure 3. Stellar angular radii, Θ and uncertainties (in units of μas) newly derived in this work. Color represents the χ^2_ν of the SED fit. Symbol size is proportional to \mathcal{F}_{bol} . One star with a debris disk and $\chi^2_\nu > 20$ is labeled and excluded from analysis (see the text).

distance to the star, d_* . Θ is related to our derived quantities by

$$\mathcal{F}_{\text{bol}} = \Theta^2 \sigma_{\text{SB}} T_{\text{eff}}^4, \quad \Theta = \sigma_{\text{SB}}^{-0.5} \mathcal{F}_{\text{bol}}^{0.5} T_{\text{eff}}^{-2}, \quad (1)$$

where σ_{SB} is the Stefan–Boltzmann constant. Contributions to the error budget of R_* thus come from random and systematic errors on T_{eff} , uncertainties in \mathcal{F}_{bol} , and uncertainties in the distances of each individual star. We adopt for our purposes a distance of 134 ± 3 pc, based on Soderblom et al. (2005), where the uncertainty can be thought of as reflecting the depth of the cluster. As we are searching for differential signals, the distance we adopt has very little influence on our results. However, differences in the distances to individual Pleiads can, and do, influence our answer. The recent *Gaia* data release 1 contained distances to several members of our sample, allowing us to verify that no significant distance outliers exist. We discuss this issue in Section 4.1.4. Our final radii are listed in Tables 2 and 3. The formal errors on the radii are typically 3%–5%, though this does not account for potential offsets from the fundamental T_{eff} scale (see Section 4.1.1).

3. Results

3.1. Angular Radii

A fundamental product of this work is a measurement of the angular radius, Θ , of each star in our sample, determined empirically from the measured \mathcal{F}_{bol} and T_{eff} . We report the resulting Θ values and their uncertainties in Tables 2 and 3. Figure 3 presents the distributions of Θ and their uncertainties in relation to the χ^2_ν of the SED fits and the \mathcal{F}_{bol} that result from the SEDs. For simplicity, this figure shows only the *DANCe* T_{eff} sample. The median precision achieved on \mathcal{F}_{bol} is $\approx 3\%$ which, together with the typical uncertainty on T_{eff} of 2%–3%, results in a median precision on Θ for this sample of $1.5 \mu\text{as}$, or $\approx 5\%$, dominated by the uncertainty on T_{eff} . The typical uncertainty

for the $V - K_s$ derivation is closer to $\approx 3\%$, due to the smaller formal T_{eff} errors.

We note that the poor-fit outlier in Figure 3 is HII 1132. This star hosts a well-known debris disk (e.g., Spangler et al. 2001), and the resulting IR-excess is evidently the cause of the poor fit (Figure Set 11). However, given its T_{eff} of 6400–6500 K, it is already excluded from the forthcoming analysis, and thus does not present a problem.

3.2. Stellar Radii

Using these angular sizes, we next derive the radii of the Pleiads using the method describe in Section 2.4, and compare them to the T_{eff} –radius relation from the Padova isochrones⁴ (Bressan et al. 2012; Chen et al. 2014), calculated for Pleiades age and metallicity. These isochrones, like all standard evolutionary tracks, are designed to model stars with negligible magnetic and rotative effects, and have accordingly been calibrated on the relatively quiet, inactive Sun. This procedure generally involves setting the free parameters of the stellar model, namely the convective mixing length and the solar helium abundance, to values which reproduce observed properties of the Sun, like its radius and luminosity (see Bressan et al. 2012 for details). Once calibrated, these models make specific predictions for stellar properties as a function of mass, composition, and age. To verify the reliability of these models, we compared a 1 Gyr, solar metallicity Padova isochrone to the catalogs of single, main sequence stars with interferometric radii from Boyajian et al. (2012, 2013). We found that despite the age, metallicity, evolutionary state, and parallax accuracy variance in the Boyajian sample, the isochrone traced well the lower envelope of stars in the T_{eff} –radius plane, demonstrating the generic reliability of the Padova calibration. In this context, discrepancies between the radii of young, active stars and isochrone predictions could be interpreted as signatures of radius inflation driven by rapid rotation, magnetic activity, and starspots, particularly when radius dispersion is present at fixed T_{eff} .

Our comparison appears in Figure 4. The left panel shows the T_{eff} s and radii derived from $V - K_s$, and the right shows the *DANCe* temperatures and resulting radii. For both temperature scales, the hottest stars ($T_{\text{eff}} > 6000$ K) cluster near the isochrone, and within the errors show little sign of dispersion. This suggests that, at least among the hottest stars, our derived radii are reasonably accurate, and that Pleiads in the mass range ~ 1.1 – $1.2 M_\odot$ are generally un-inflated. For stars cooler than ~ 5700 K, the picture changes. While many of these stars still straddle the T_{eff} –radius relationship predicted by Padova, several lie significantly above this line, and indeed at larger radii than other stars of equivalent T_{eff} .

It is notable that the onset of scatter in stellar radii sets in around the same T_{eff} as in the inflated radii measurements of Jackson & Jeffries (2014a). These authors combined spot modulation periods and $v \sin i$ values to measure the average Pleiad radius from projected stellar radii. They found that the average radius is $\sim 10\%$ larger than stellar models for approximately $1 M_\odot$ and below. This mass corresponds to ~ 5700 K in the Padova isochrones determined for Pleiades parameters, and it is indeed around this temperature at which star-to-star scatter first becomes evident in our derivations, demonstrating good agreement between the methods. This T_{eff}

⁴ <http://stev.oapd.inaf.it/cgi-bin/cmd>

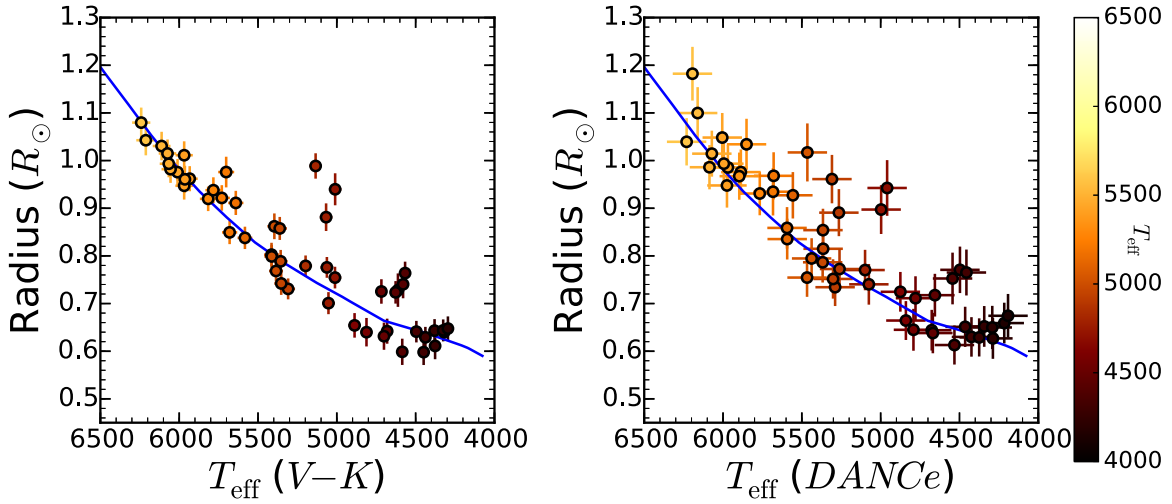


Figure 4. Comparison between the radii of our stars, derived from $V - K_s$ (left) and $DANCe$ (right) temperatures according to the procedure outlined in Section 2, and the stellar isochrones (blue line) of Bressan et al. (2012). There is little evidence for a radius dispersion above ~ 5700 K, but significant scatter below this value for both T_{eff} proxies.

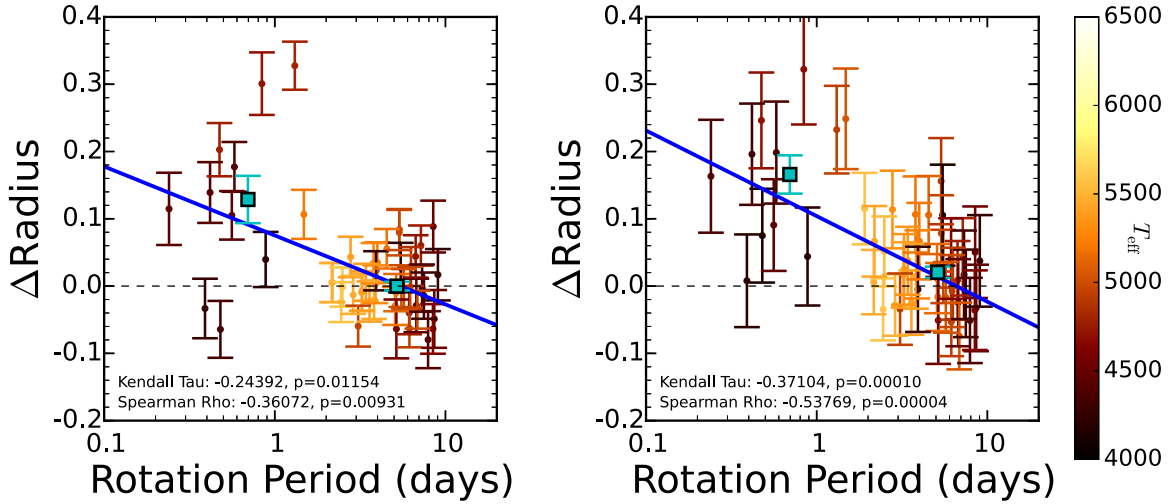


Figure 5. Comparison between the rotation period of stars in our sample and their fractional height above the Bressan et al. (2012) isochrone for $V - K_s$ and $DANCe$ temperatures. In both panels, stars rotating slower than 1.5 days show good agreement with predictions, but faster rotating stars are systematically large by on average 10%–20%. The purple squares show the average ΔR_* among the slower and faster stars, divided at 1.5 days. The trend is statistically significant in both bins according to Kendall’s τ and Spearman’s ρ coefficients. This suggests that rapid rotation drives radius inflation, perhaps through the influence of correlated starspots and magnetic activity.

also corresponds to the onset of extraordinary surface activity among the fastest rotators in the cluster (e.g., Micela et al. 1999). This suggests a connection between activity and the anomalous derived radii, as suggested by many authors (see Section 1). If physical, this could be a consequence of the greater rapidity of rotation among the fastest K-dwarfs when compared to G- and F-dwarfs in the cluster, or could relate to the changing magnetic properties as convection zones deepen.

3.3. Radius Inflation and Its Relation to Rotation

Given this apparent connection with magnetic activity, the exquisite Pleiades rotation data provided by HATNet (Hartman et al. 2010) and K2 (Rebull et al. 2016a, 2016b; Stauffer et al. 2016) offer an interesting comparison point. To explore this, we first calculated the fractional height above the isochrone of

each data point from Figure 4, using

$$\Delta R_* = \frac{R_* - R_{\text{isoc}}}{R_*}, \quad (2)$$

where R_{isoc} is the radius predicted by the Bressan et al. (2012) isochrones at the calculated T_{eff} of each star. We then compared each value to the spot-modulation rotation periods collected in Table 1. The results appear in Figure 5. For stars rotating at slower than 1.5 day periods, the values cluster nicely around $\Delta R_* = 0$, with an average value (cyan square) consistent with standard expectations. The scatter around $\Delta R_* = 0$ is consistent with Poisson noise, with an rms equal to the size of the error bars on the data points. On the other hand, the faster rotating stars show a clear systematic trend toward larger ΔR_* , with values ranging from $\sim 0\%$ to 30% larger than the Padova

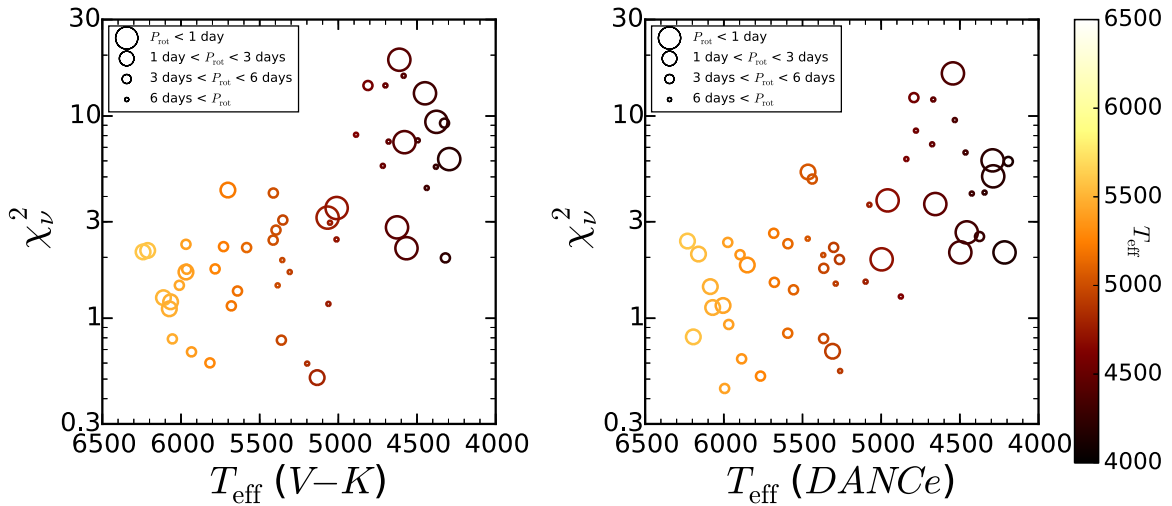


Figure 6. χ^2_ν residuals for our SED fits, plotted as a function of temperature for our $V - K_s$ and $DANCe$ T_{eff} s. The size of the circles reflects rotation rate, as indicated by the key. There is little connection between rotation rate and SED residuals, though a clear connection exists between T_{eff} and the average goodness-of-fit.

prediction. The average calculated radius inflation for those with faster than 2 day rotation periods is $12.3 \pm 3.3\%$ for the $V - K_s$ T_{eff} s, and $15.6 \pm 2.8\%$ for the $DANCe$ T_{eff} s, showing good agreement between our T_{eff} metrics. The significance of the anti-correlation is tested with both Kendall’s τ and Spearman’s ρ tests, showing strong correlations in both panels (blue lines).

These conclusions are unaltered if we transform the $V - K_s$ temperatures into $V - I_c$ temperatures as described in Section 2.2, and redo the analysis. We find in that case an average ΔR_* among the rapid rotators of $10.0 \pm 3.3\%$, with essentially no change in the p -values of the significance tests. The slightly lower average ΔR_* reflects the fact that $V - I_c$ photometry gives marginally higher T_{eff} s for rapidly rotating Pleiades, by about 65 K (Section 2.2). We also re-derived ΔR_* values using the isochrones of Baraffe et al. (2015), and with isochrones derived with our own YREC evolution code (see Somers & Pinsonneault 2015b for details), to determine whether the offset could be due to our choice of comparison models. We find that the overall normalization is affected by isochrone choice, largely as a consequence of the adopted solar abundance, but in each case the rapid rotator average remained larger by $\sim 10\%$ compared to the slow rotators, and the significance of the ΔR_* correlation with rotation rate was unchanged.

To ensure that this result does not stem from systematically poor fitting of the rapid-rotator SEDs, we plot in Figure 6 the χ^2_ν residuals of each \mathcal{F}_{bol} calculation as a function of T_{eff} . The size of each point reflects its rotation rate, given by the inset key. There exists a clear trend of poorer average fits toward lower temperatures. Above ~ 5000 K, the stars show generally good fits, but cooler objects are significantly worse. Whether this is a consequence of generic deficiencies in the atmosphere models or related to intrinsic properties of the SEDs of young, cool stars is not clear, and deserves attention in future work. However, there is little evidence that the fastest rotators have worse \mathcal{F}_{bol} fits, and consequently does not influence our results due to the differential nature of the radius inflation signal.

It is interesting that the rapid rotators do not follow a clear inflationary trend with rotation rate, but instead scatter between consistent with expectations and $\sim 30\%$ inflation. This could

simply be due to observational errors, as the standard deviation about the mean for the fast rotators in the $DANCe$ sample is comparable to the error bar size. This is not the case for the $V - K_s$ values, but these error bars may be under-estimates as the presence of starspots adds additional uncertainty. If indeed there is scatter above a given rotation threshold, this behavior would mirror additional properties of saturated stars, such as their spread in activity (Pizzolato et al. 2003; Wright et al. 2011; Argiroffi et al. 2016), spot modulation amplitudes (Covey et al. 2016), and inferred starspot coverage (Fang et al. 2016). It is also notable that among the inflated stars, none is hotter than ~ 5700 K. This may reflect the fact that higher mass stars are far more likely to have spun down to the slow sequence, leaving a paucity of extremely rapid rotators among the G-dwarfs by Pleiades age.

4. Discussion

4.1. Potential Sources of False Signals

While a truly inflated radius would be the most interesting conclusion of our investigation, it is important to consider potential sources of false positives for over-inflated stars. In this section, we discuss the possibilities of systematic T_{eff} offsets due to starspots, contamination by binaries, and problems with differential extinction.

4.1.1. Starspots and Plages

Perhaps the most pressing concern is the distortion of the stellar SED by starspots and plages. The presence of cool regions on the surface has long been known to alter the shape of the stellar spectrum, thus leading to anomalous colors relative to quiet, inactive stars (see Section 2.2). When using a standard color- T_{eff} transformation, this can result in a systematic T_{eff} offset which depends on the level of spot coverage, the spot temperature distribution, and even the phase of the stellar rotation. In Section 2.2, we discussed in detail our efforts to minimize the impact of these effects, including performing our analysis with two distinct T_{eff} scales, and comparing our resulting values with more reliable $V - I_c$ photometry. However, a strong underlying systematic T_{eff} shift among the fastest rotators could plausibly still impact our

results. In this section, we discuss how large such an offset must be in order to produce a spurious rotation–radius correlation, and estimate whether such an offset is plausible.

For T_{eff} errors to mimic a systematic increase in radius of $\sim 12\%$ among rapid rotators, our derived temperatures for these must be systematically low by $\sim 6\%$, but accurate for stars rotating at slower than 1.5 day periods. Given the typical T_{eff} of our inflated targets of 4750 K, we calculate that this offset must be approximately 230 K on average. This is a rather extreme shift, and in fact approaches the difference in T_{eff} derived between $B - V$ and $V - K_s$ photometric bands for the individual rapid rotators (Figure 1). As $B - V$ T_{eff} s are thought to be the least accurate (Section 2.2), and our rapid rotator $V - K_s$ temperatures only differed from the $V - I_c$ scale by ~ 65 K, this seems an implausibly large shift based on distorted colors. Even taking an average of T_{eff} s derived from $B - V$ and $V - K_s$, and redoing the analysis of Section 3, still produces an average radius inflation of $\sim 7\%$ among rapid rotators and, given the stronger reliability of $V - K_s$ temperatures, one would expect this to represent a lower limit on the true strength of the rotation– ΔR_* correlation.

However, a systematic offset of the required magnitude (~ 230 K) could conceivably arise from a substantial offset in the color– T_{eff} relations from Casagrande et al. (2010) in the regime of highly active stars. This offset would have to affect the most rapidly rotating stars to a much greater degree than those with periods less than 1.5 days, as our inflationary signal is ultimately a differential sign rather than an absolute sign. We cannot exclude this possibility at present, but we can determine whether the Casagrande et al. (2010) scale is uniquely subject to a systematic of this nature. To do this, we re-derived our $V - K_s$ temperatures using the empirically calibrated isochrones of An et al. (2007), and compare them to our adopted values. We find that the new scale produces somewhat cooler T_{eff} s for the lower mass stars and somewhat warmer T_{eff} s for the higher mass stars, a directionality which would actually *enhance* the observed radius–rotation correlation in Figure 5. On the whole, the average offset between the two scales for our sample is 6 ± 52 K, showing overall good agreement. A similar exercise with the empirical isochrones of young stars determined by Peca et al. (2013) again produced commensurate results, with average offsets of -17 ± 6 K and -4 ± 41 K, using their pre-main sequence and main sequence isochrones, respectively. As the Peca et al. (2013) tracks were calibrated on active spotted stars, this agreement greatly strengthens our belief in the accuracy of the IRFM-derived T_{eff} s we have used. Finally, we note that the good agreement between the *DANCe* temperatures and our color-derived temperatures would be surprising if systematic offsets afflicted our color temperatures.

On balance, it is our judgement that starspots have a small impact on our derived T_{eff} s, perhaps as much as 100 K from the $V - K_s$ values, but do not distort our results enough to produce a spurious rotation–radius correlation. However, our analysis would benefit greatly from advances in understanding the SEDs of rapidly rotating, heavily spotted stars.

4.1.2. Binaries

Another false-positive source is binaries, which can impact our radius derivations in two ways. First, for near-equal-mass binaries, \mathcal{F}_{bol} will be significantly increased with little change in inferred T_{eff} . A doubling in \mathcal{F}_{bol} corresponds to a $\sim 40\%$

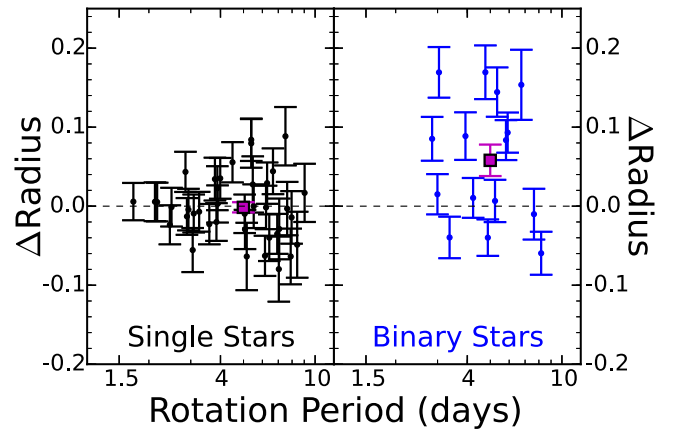


Figure 7. Illustration of the impact of binarity on ΔR_* , as defined in Equation (2). We show slowly rotating single stars (left) and binary stars in our sample (right). The binaries have a larger average ΔR_* by $\sim 6\%$, demonstrating the statistical impact of enhanced bolometric flux at fixed T_{eff} on our calculation. These binaries have been excluded from the analysis of Section 3. The dissimilarity between the two plots suggests that we have filtered binaries out with reasonable completeness.

increase in R_* , thus appearing as an inflated object. Second, for binaries with a significantly lower mass companion, \mathcal{F}_{bol} will be only marginally affected, but the long wavelength emission will be enhanced by the lower mass companion peaking in the near-IR, leading to a lower inferred temperature. Consequently, a larger R_* will be inferred, as a lower T_{eff} star demands a large emitting surface at fixed \mathcal{F}_{bol} .

While these would be extremely problematic in an unfiltered sample, the *DANCe* stars used in our selection already attempted to exclude known binaries. To supplement this initial cut, we searched the literature for additional information on binarity, drawing from Mermilliod et al. (1992), Bouvier et al. (1997), Sestito & Randich (2005), Margheim (2007), and Hartman et al. (2010), some of whom collate previous binary catalogs. We find an additional 22 objects out of our sample of 83 for which one or more of these publications indicates possible binarity. Each of these stars has been excluded from the analysis plots of Section 3. We thus expect the contamination fraction of binaries, or at least of known binaries, to be small. Moreover, as the inflated stars described in Section 3.3 were all among the most rapidly rotating, it would require an extraordinary cosmic conspiracy were the signal a product of unknown binaries.

In the interest of exploring the typical contaminating influence binaries could have on our results, we compare in Figure 7 the derived radii of the slowly rotating binaries to the slowly rotating single stars in our sample. Compared to the single stars, the binaries show a similar ΔR_* floor, but a much higher ceiling as a consequence of the increased bolometric flux due to the blended light of the companions. The average is about 6% higher, showing the likely magnitude of this effect. Visually, it is clear that binaries can produce quite large spurious ΔR_* values, and thus stronger verification of the single-star-nature of our putative inflated stars would be valuable. However, it also appears that there is little clear contamination of the slow-rotator sample with binaries, which may indicate that our binary exclusion is largely complete.

4.1.3. Reddening

Bad measures of extinction could also affect the T_{eff} and \mathcal{F}_{bol} determinations of individual objects. In fact, several Pleiads are

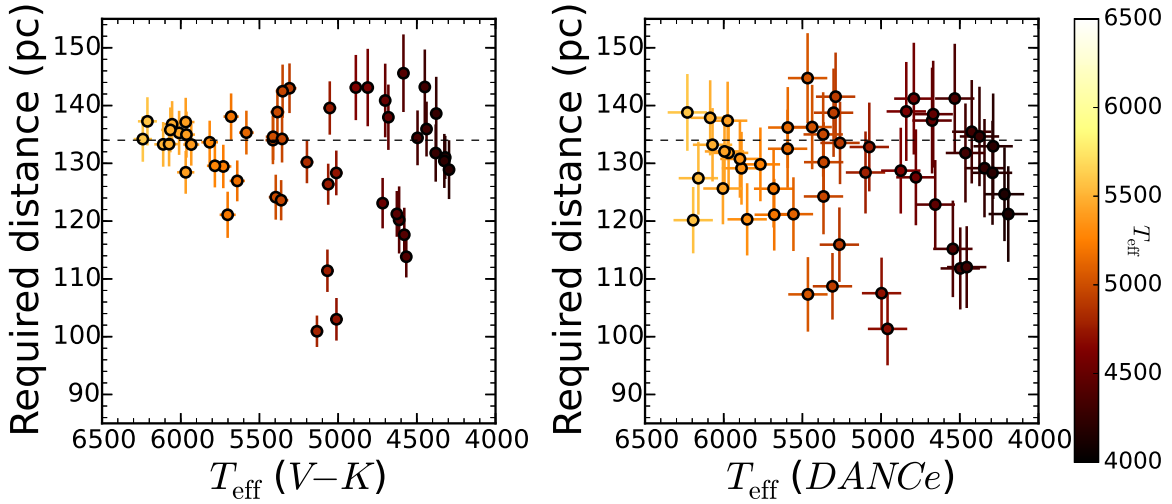


Figure 8. Required distance for each star to lie on the Padova isochrone, given its measured \mathcal{F}_{bol} and T_{eff} . The large required distances from the center of the cluster (~ 134 pc) indicates that in order to not be over-luminous, they must either be non-member interlopers, or members that are currently quite distant from the cluster center.

known to sit behind an area of enhanced extinction, due to an HI cloud occupying a portion of the cluster foreground (e.g., Gordon & Arny 1984). For simplicity, we have excluded these stars from our analysis, and adopt the canonical $E(B - V) = 0.04$ (e.g., An et al. 2007) for the remainder. We do not anticipate that this complicates our results, and again it would be extraordinary were the rapid rotators preferentially distorted by differential reddening.

4.1.4. Distance Errors

A final way that a star might appear spuriously inflated is if its true distance is substantially less than we have assumed (134 ± 3 pc). A closer star, at fixed bolometric luminosity and T_{eff} , obviously requires a lower radius. Given the intrinsic depth of the cluster, it is expected that some stars indeed lie closer than our lower bound of 131 pc, and thus may require some adjustment to their inferred radius. As $\mathcal{F}_{\text{bol}} \propto d_*^2$ and also $\mathcal{F}_{\text{bol}} \propto R_*^2$, a given fractional distance error converts directly into an equivalent fractional radius error. Thus, a three-sigma outlier from the cluster center could induce as much as a 7% increase in inferred radius. Non-member interlopers would also appear as abnormally inflated objects. Each star in our sample has a membership probability $>85\%$, with most $\geq 99\%$, so the membership of our sample is generally secure. However, it is conceivable that a few of our targets are interloper non-members.

Given our measured \mathcal{F}_{bol} and T_{eff} for each star, we can easily determine the distance it must lie at in order to have a normal radius, as defined by the Padova isochrones we have adopted in this paper. Figure 8 shows this calculation for each of our sample stars. Many of the warmest members cluster around the putative Pleiades distance of 134 pc, but as we move to cooler temperatures, more and more scatter far from the mean. In particular, three stars around 5000 K would have to be much closer than the cluster center in order to appear as bright as they are without radius inflation.

Fortunately, *Gaia* has just unveiled its first data release, which includes parallaxes for nearly half of our sample, albeit the brighter half where the putative radius dispersion is not as pronounced. We can use these values to judge whether the most inflated stars could plausibly be interlopers. We compare

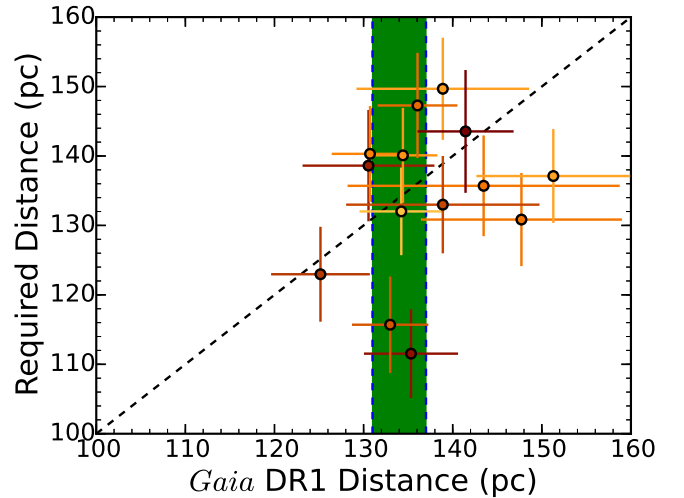


Figure 9. Comparison between the required distances from Figure 8 and the true distances from *Gaia* DR1, for those members of our sample present in the first data release. The stars generally cluster around the true distance to the cluster and not along the one-to-one line, suggesting that distance effects are not responsible for the radius dispersion we find.

our required distances to the measured *Gaia* distances in Figure 9. We find that these stars lie at an average distance of 133 ± 8 pc, nicely consistent with our adopted distance to the center of the cluster of 134 ± 3 pc (green shaded region), indicating that the DR1 Pleiades distances agree well with previous calculations. While many of these stars required distances under 120 pc to agree with the Padova isochrone predictions, none is found to be closer than 125 pc. In particular, two of the three highly inflated stars mentioned above lie right at the adopted Pleiades distance in the *Gaia* determination, whereas they could only be explained with a standard radius if they lay at ~ 105 pc. This strongly demonstrates that interlopers and depth effects cannot account for the radius spread we have inferred. Future *Gaia* data releases will permit similar exercises for the entire sample, and allow us to confirm or refute the inflated nature of the most extreme objects in the cluster.

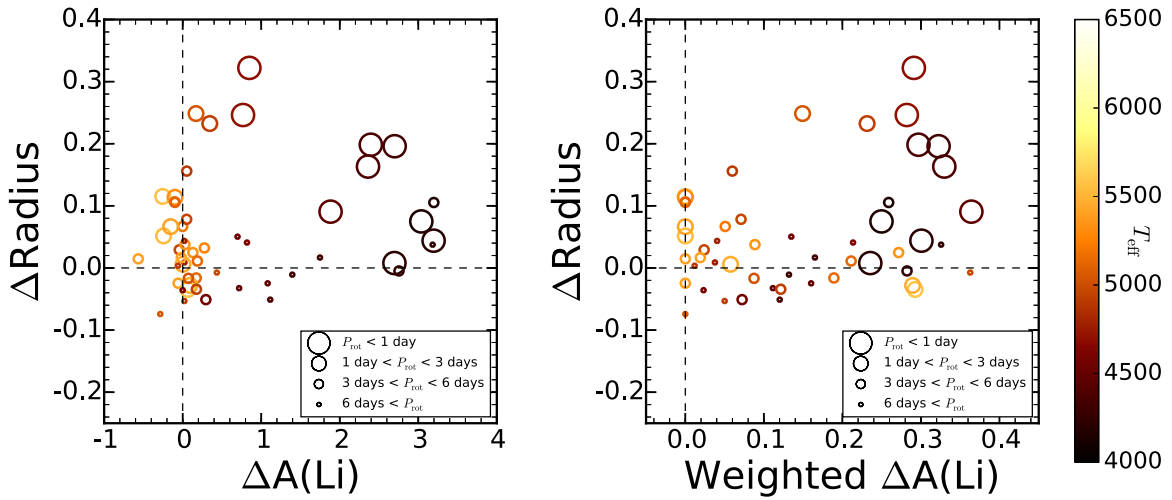


Figure 10. Left: comparison between the height above T_{eff} -radius relation of Bressan et al. (2012), and the height above the standard stellar model lithium predictions of Somers & Pinsonneault (2015a), with rotation rate indicated by point size. Slower rotating stars, and warm stars, tend to cluster near the origin, whereas the rapidly rotating, cooler stars tend to extend to the upper right. This suggests a triple correlation between rotation, radius, and lithium abundance. Right: same as left panel, but the x-axis now reflects how inflated each star must have been on the pre-main sequence in order to possess its current abundance. This panel solidifies the tripartite correlation.

4.2. Connection with Lithium Abundances

There is a well known correlation between rotation rate and lithium abundance in the Pleiades (e.g., Soderblom et al. 1993). The correlation is in the sense that at a given T_{eff} , the most rapidly rotating stars tend to be the richest in lithium. Moreover, equivalent correlations have been found in younger clusters such as the ~ 5 Myr NGC 2264 and the ~ 24 Myr β Pictoris (Bouvier et al. 2016; Messina et al. 2016), suggesting that the Li dispersion sets in during the early pre-main sequence. This picture contradicts standard stellar predictions (e.g., Iben 1965), which anticipate no dispersion in lithium at fixed T_{eff} in a cluster like the Pleiades. Explanations for the origin of this rotationally correlated dispersion in lithium include core–envelope decoupling influencing the rate of rotational mixing (Bouvier 2008), accretion altering the central temperatures of proto-stars (Baraffe & Chabrier 2010), and magnetic activity inducing radius inflation during the pre-main sequence, thus suppressing the central temperatures of stars and slowing the rate of Li destruction (Ventura et al. 1998; Somers & Pinsonneault 2014, 2015a, 2015b).

Given our detection of a correlation between rotation rate and radius, it is interesting to consider whether the ΔR_* we have determined in the Pleiades also correlates with lithium. To this end, we draw lithium abundances for our sample from Barrado et al. (2016). In order to quantify how lithium-rich each star is, we use the lithium depletion models of Somers & Pinsonneault (2015a) to determine the difference in $A(\text{Li})$ between the measured value of each star and the values predicted for its T_{eff} . We refer to this metric as $\Delta A(\text{Li})$, as it is in some ways analogous to our ΔR_* metric. We compare these values to our ΔR_* values in the left panel of Figure 10. Here, the size of the circles reflects the rotation rate, with the largest circles being the most rapidly spinning. The general trend in this panel is for smaller circles to cluster around the origin, and larger circles to be either at high ΔR_* , high $\Delta A(\text{Li})$, or both. At each value of ΔR_* , the fastest rotating stars have the largest $\Delta A(\text{Li})$ values, confirming that the three quantities correlate with one another.

However, we note that there is a strong mass dependence in the largest possible $\Delta A(\text{Li})$. This is because lower mass stars tend to deplete more lithium, thus producing a larger dynamic range with their Li-rich counterparts (see Figure 7 in Somers & Pinsonneault 2015a). To attempt to remove this effect, and thus get a cleaner comparison of lithium and radius anomalies across the full range of T_{eff} , we create a new metric which weights $\Delta A(\text{Li})$ by the width of the lithium dispersion at each T_{eff} . This amounts to determining how much radius inflation is required on the pre-main sequence in order to produce the current day abundance of each star (see Somers & Pinsonneault 2016a for a discussion of this method). We compare these values to ΔR_* in the right panel of Figure 10. Here, the abscissa values correspond to the predicted fraction of the surface covered in starspots, based on the T_{eff} and $A(\text{Li})$ values for each star (Somers & Pinsonneault 2015a). With this metric, essentially all of the rapidly rotating stars now show large lithium anomalies, and (as in Section 3.3) show a range of radius anomalies between 0%–30%. It is clear that there is no one-to-one correspondence between rotation rate, radius, and lithium abundance, but it is clear that the most rapidly rotating, lithium-rich, cool stars are also the most inflated.

5. Summary and Conclusions

Previous studies have reported anomalously large radii among low-mass stars in the Pleiades and other young clusters, using ensemble averages of projected rotation velocity measurements. Here, we have measured the radii of several Pleiades cluster members via the Stefan–Boltzmann law, combining (i) T_{eff} s determined through color and spectrophotometric techniques, (ii) bolometric fluxes determined by summing the observed spectral energy distributions, and (iii) the known cluster distance. Our sample specifically includes stars with previously determined rotation periods and lithium abundances. We compare our radius measurements to literature isochrones, calibrated on older, inactive stars, and find that in many cases the Pleiades radii can be larger by 10%–20% compared to expectations. We further show that this over-

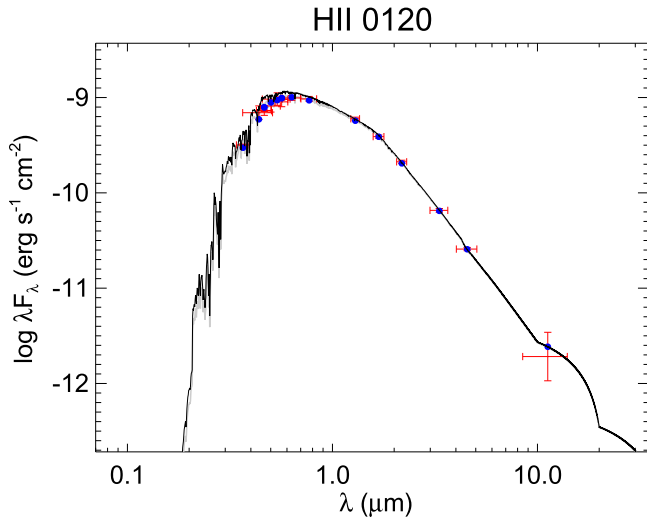


Figure 11. HII 0120 is shown as example of the figure set. Each panel in the figure set is labeled at top by the HII number, and shows the observed fluxes (in units of $\text{erg cm}^{-2} \text{s}^{-1}$) vs. wavelength (in μm) as red error bars, where the vertical error bar represents the uncertainty in the measurement and the horizontal “error” bar represents the effective width of the passband. Also in each figure is the fitted SED model including extinction (light gray curve), on which is shown the model passband fluxes as blue dots. The corresponding un-extincted SED model is also shown (dark black curve); the reported \mathcal{F}_{bol} is the sum over all wavelengths of this un-extincted model (see the text).

(The complete figure set (83 images) is available.)

radius correlates with rapid rotation at greater than 99.99% confidence, strongly suggesting a magnetic origin. We discuss whether this radius–rotation correlation could be a spurious artifact brought on by poorly calculated radii due to the distorted SEDs of rapidly rotating stars. A very large systematic offset in T_{eff} , afflicting only stars which rotate with periods shorter than 1.5 days, would be required to reconcile the rapidly rotating Pleiads with the model expectations. However, our quantitative measures of SED distortion find that this is principally a function of T_{eff} , not rotation, with the coolest stars tending to show modestly distorted SEDs that might be better fit by a two-temperature model. We conclude that the most likely explanation is magnetically driven radius inflation among the most rapidly rotating Pleiads.

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Appendix

Spectral Energy Distribution Measurements and Fits

In Figure Set 11 we present the observed and fitted spectral energy distributions of the stars in our study sample (Tables 2 and 3).

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