# Sensitivity of Oceanic Fronts to nonlinearities of equation of state investigated using Numerical Experiments

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#### Context

Transition zones between saline warm subtropical water and cold fresh subpolar water arise abruptly. These boundaries are called oceanic front and have similar structures on the North Atlantic Ocean, the North Pacific Ocean and the Southern Ocean, suggesting that the same processes lead to these frontal structures. A hypothesis to study lies in the nonlinearity of the equation of state for seawater, the relation that gives density as a function of pressure, salinity and temperature. To test this hypothesis, we are developing an idealized triple-gyre configuration with the ocean global circulation model NEMO (Nucleus for European Modelling of the Ocean). This configuration includes a continental slope along the coastline with a terrain following coordinate, except at the equator where an open boundary with a no meridional flow condition is imposed.

# Objectives

- We analyzed the sensitivity of transition zones to perturbations of the nonlinear equation of state.
- We ran 5 experiments, perturbing the cabbeling parameter  $\lambda_1$  from  $3.952 \cdot 10^{-2}$  to  $7.952 \cdot 10^{-2}$  (°C)<sup>-1</sup>, and analyzing the resulting stratification and circulation.
- We are building a reference NEMO triple gyre configuration.

#### The basin configuration

#### Description of the grid

- Mercator grid
- Continental slopes (2 km deep at the coast, 4 km deep at the bottom)
- Coarse resolution (for the moment)
- 36 vertical levels
- Terrain following vertical coordinates
- Symmetry condition at the equator (no meridional flux)

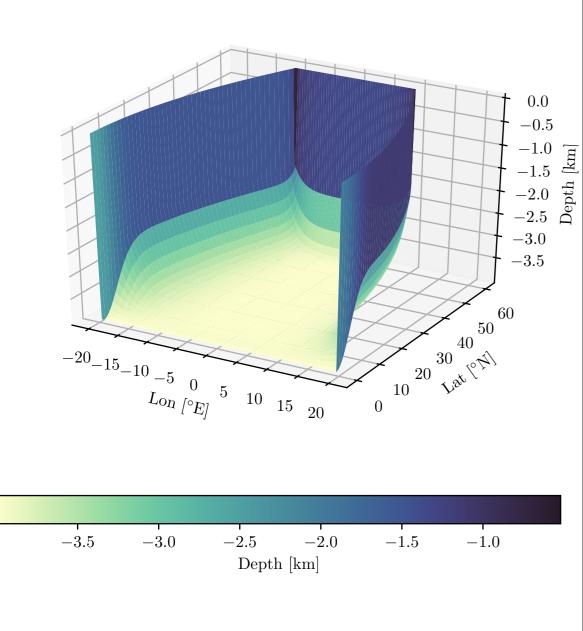


Figure 1. Bathymetry of the basin.

#### Description of the forcing fields

- Restoring temperature
- Penetrative solar radiation
- Restoring salinity (used here) or E-P flux
- Zonal wind stress

# Resulting fields

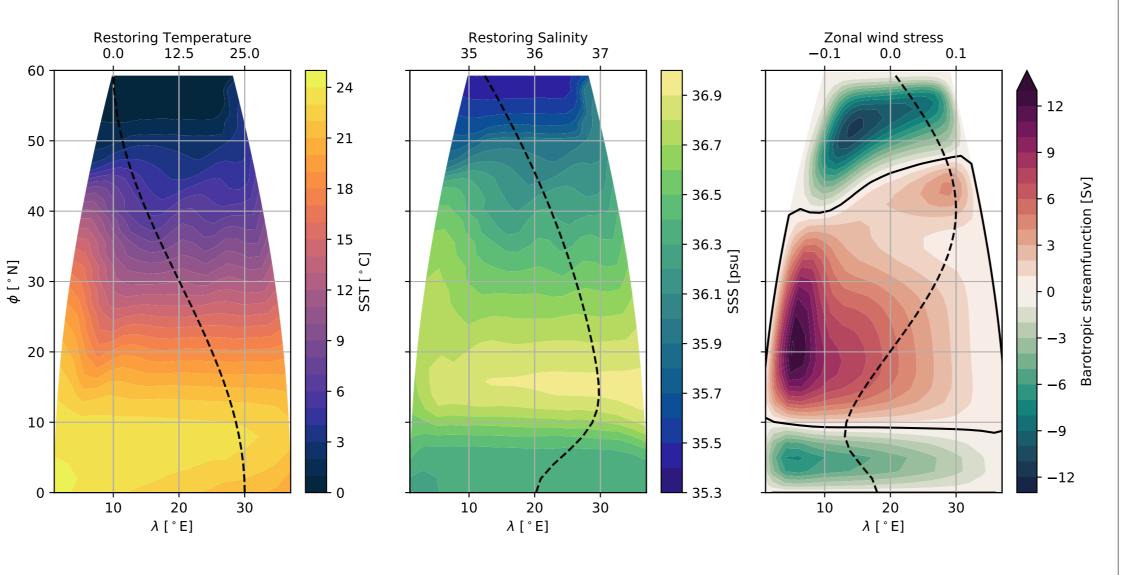
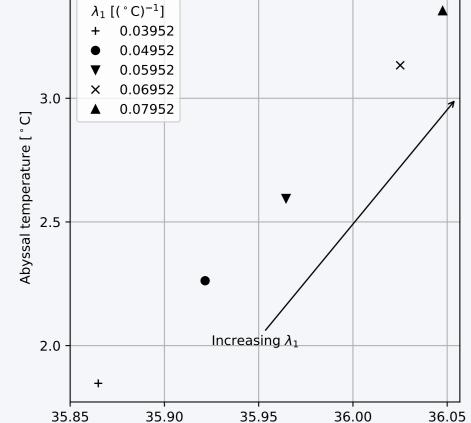


Figure 2. Sea Surface Temperature, Sea Surface Salinity, Barotropic Streamfunction. The forcing fields are represented in dashed lines.

Stratification ratio at  $\lambda = 23.0$  °E

#### 



Abyssal salinity [psu]

Figure 3. T-S diagram for the abyssal water for the fives values of  $\lambda_1$ . Both the temperature and the salinity increase with  $\lambda_1$ : the convective region is displaced to the south.

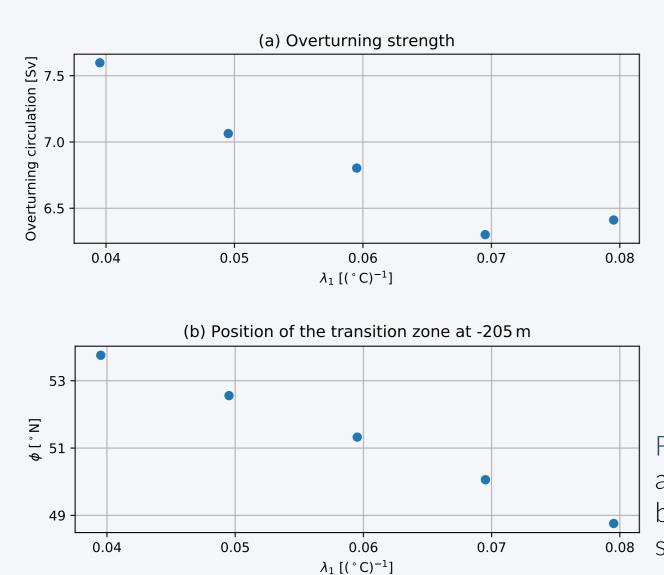


Figure 4. (a) Overturning strength function of the cabbeling term  $\lambda_1$ . The overturning circulation decreases when cabbeling is more important. (b) Position of the transition zone at a depth of 205 m and a longitude of 23 °E. The transition zone corresponds to the northern part of the convective region, and its latitude decreases when  $\lambda_1$  increases, leading to the change of abyssal water properties.

# Results

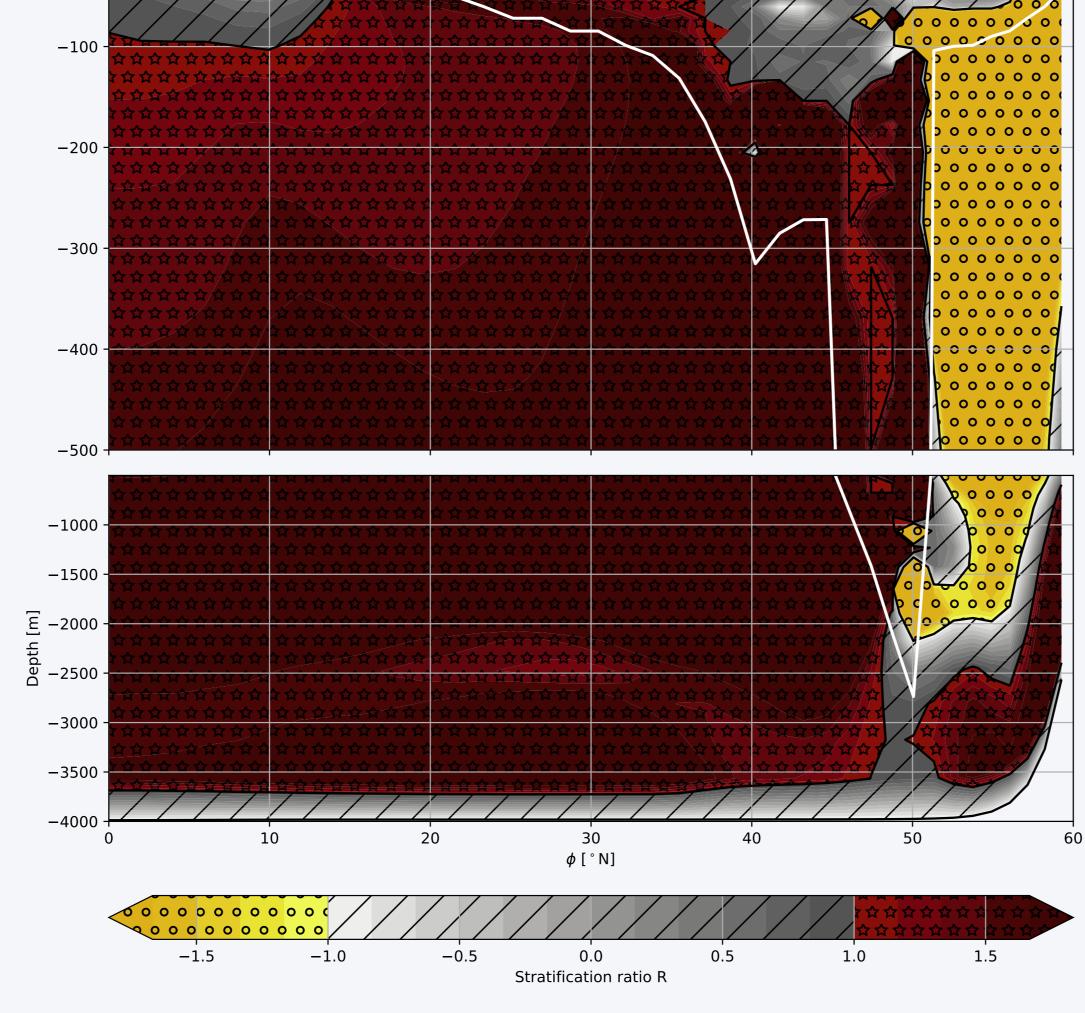


Figure 5. Section of the stratification ratio. The red colors (star background) represent alpha-ocean stratified by the temperature only, the yellow areas (round background) are the beta-ocean stratified by the salinity only and the gray zones (dash background) are doubly stratified. The white line represents the mixed layer depth.

# Take home message

With the increase of the cabbeling parameter  $\lambda_1$ , the stratification becomes sensitive to salinity at higher temperature. As the northern area is stabilized by a strong halocline due to fresh surface water, the salinity takes control of the stratification further south, pushing the transition zone south. This is accompanied by a more southern convection zone and thus a convection of warmer and saltier water. An unexpected effect is the reduction of the overturning strength with cabbeling.

# Thermodynamic properties

#### The nonlinear equation of state

We use the simplified nonlinear equation of state proposed by Roquet et al. (2015).

$$\rho(\Theta, S_A, Z) = \overline{\rho}(Z) - \frac{C_b}{2}(\Theta - \Theta_0)^2 - T_h Z\Theta + b_o S_A \tag{1}$$

$$\overline{\rho}(Z) = \rho_0 - b_0 S_0 + \frac{a_0^2}{2C_b} + T_h Z T_0 \tag{2}$$

$$\alpha = \frac{1}{\rho_0} [C_b(\Theta - \Theta_0) + T_h Z] \quad \text{and} \quad \beta = \frac{b_0}{\rho_0}$$
 (3)

#### Numerical values of the parameters

$$\begin{split} C_b &= 9.851 \cdot 10^{-3} \, \mathrm{kg \, m^{-3} \, K^{-2}} \\ \Theta_0 &= -6.801 \, ^{\circ} \mathrm{C} \\ T_h &= 2.478 \cdot 10^{-5} \, \mathrm{kg \, m^{-4} \, K^{-1}} \\ a_0 &= 1.655 \cdot 10^{-1} \, \mathrm{kg \, m^{-3} \, K^{-1}} \\ b_0 &= 7.6554 \cdot 10^{-1} \, \mathrm{kg \, m^{-3} \, (g \, kg^{-1})^{-1}} \\ \rho_0 &= 1026 \, \mathrm{kg \, m^{-3}} \\ T_0 &= 10 \, ^{\circ} \mathrm{C} \end{split}$$

#### NEMO simplified EOS equivalence (In\_seos=.true.)

$$a_0=a_0$$
 and  $b_0=b_0$   $C_b=a_0\cdot\lambda_1$  and  $\lambda_2=0$   $T_h=a_0\cdot\mu_1$  and  $\mu_2=0$   $\nu=0$  and  $\Theta_0=T_0-1/\lambda_1$ 

#### The stratification ratio

The stratification ratio R determines if the water column is stratified by the temperature only (R>1), by the salinity only (R<-1) or doubly stabilized  $(-1 \le R \le 1)$ .

$$R = \frac{N_{\Theta}^2 - N_{S_A}^2}{N^2} = \frac{\alpha \frac{\partial \Theta}{\partial z} + \beta \frac{\partial S_A}{\partial z}}{\alpha \frac{\partial \Theta}{\partial z} - \beta \frac{\partial S_A}{\partial z}}$$
(4)

The thermal expansion  $\alpha$  is proportional to the temperature (cabbeling effect) while the haline contraction is constant. Thus on warm and tempered regions, the stratification is mainly controlled by the temperature (alpha-ocean (*Carmack*, 2007)). But at high latitude, the lower value of  $\alpha$  associated with the halocline lead to a salinity controlled stratification (beta-ocean).

A T-S profile with a stratification ratio R < -1 can become unstable when the cabbeling term is perturbed, leading to a different polar stratification: the nonlinearities of the equation of state are an essential parameter.

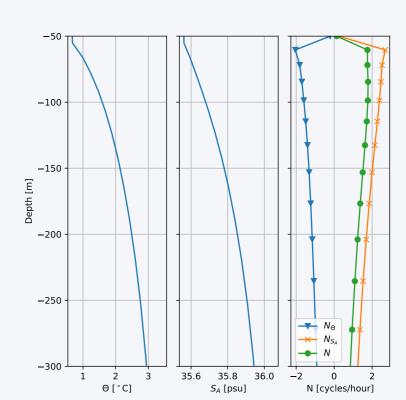


Figure 6. Temperature, salinity and buoyancy frequency profiles in a beta-ocean (19°E, 55°N).

# xbasin and xnemogcm python packages

# xnemogcm

# https://github.com/rcaneill/xnemogcm

Python package interfacing NEMO outputs to xgcm

# xbasin

# https://github.com/rcaneill/xbasin

- Python package used to deal with terrain-following coordinates on idealized configurations
- Based on NumPy, xarray, xgcm, f2py

# Open source projects!

Please feel free to use, fork, and help on these new projects!

# References

Carmack, E. C. (2007), The alpha/beta ocean distinction: A perspective on freshwater fluxes, convection, nutrients and productivity in high-latitude seas, *Deep Sea Research Part II: Topical Studies in Oceanography*, *54*(23-26), 2578–2598.

Roquet, F., G. Madec, L. Brodeau, and J. Nycander (2015), Defining a Simplified Yet "Realistic" Equation of State for Seawater, *Journal of Physical Oceanography*, 45(10), 2564–2579, doi: 10.1175/JPO-D-15-0080.1.