

Akantu: an HPC finite-element library for contact and dynamic fracture simulations

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Summary

Complex, nonlinear and transient phenomena are at the heart of modern research in mechanics of materials. For example, the buildup and release of elastic energy at geological fault is what causes earthquakes, and the intricate details of the slip zone, the propagation of slip fronts and waves radiated through the various geological media are still active areas of research (David S. Kammer et al., 2012; D. S. Kammer et al., 2014; Roch et al., 2022). Similarly, understanding fracture in heterogeneous materials such as concrete, masonry or ceramics necessitates the modeling of interaction of crack fronts with complex materials (A. I. Cuba Ramos et al., 2018; Taheri Mousavi et al., 2015; Yilmaz et al., 2017), the representation of residual shear stresses in the contact of newly-formed crack surfaces (Pundir & Anciaux, 2021; Zhang et al., 2017), and the accurate characterization of transient dynamics (Corrado & Molinari, 2016; Vocialta et al., 2018) and material structure evolution (A. I. Cuba Ramos et al., 2018; Gallyamov et al., 2020).

The finite-element method is now ubiquitous in virtually all areas of solid mechanics. With meticulous care on code architecture and performance, we show that our finite-element library Akantu can handle the requirements mentioned above for state-of-the-art research in mechanics of materials. Akantu is designed from the ground up for high-performance, highly distributed computations, while retaining the necessary flexibility to handle:

- crack propagation with cohesive elements
- non-local damage models
- plastic and visco-plastic constitutive laws
- large deformations
- contact constraints (including rate and state friction)
- interaction between contact and cohesive elements (residual crack shear strength)

Statement of need

Understanding the interplay between material constitutive behavior and interface processes such as crack propagation, contact and friction is fundamental to a number of application domains. Thanks to its versatility, the finite-element method (FEM) has become an essential

42 tool in these areas. However, codes that can handle cutting edge simulations with interaction
43 of material behavior and interface processes in a high-performance computing (HPC) setting
44 are rare, particularly in the open-source space. Being able to simulate the aforementioned
45 interface processes in an efficient manner is the primary *raison d'être* of Akantu. Even though
46 Akantu is meant to be a generic FEM library, the physics currently implemented, all serve the
47 goal to get a better understanding of fracture, contact and friction mechanism at a continuum
48 scale.

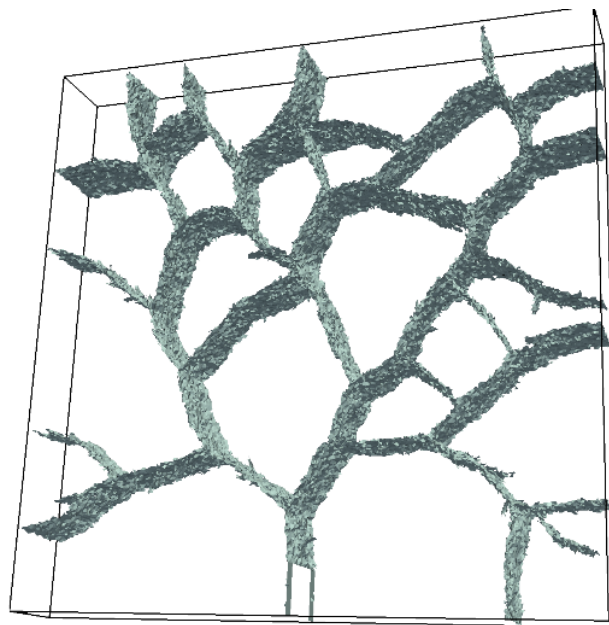


Figure 1: Dynamic fragmentation of a tempered glass pane using cohesive elements.

49 At its heart, Akantu leverages a SOA (structure of array) architecture in order to take advantage
50 of an object-oriented high-level abstraction, and maintains performance in the critical areas of
51 the code. In addition, Akantu benefits from distributed memory parallelization using state-of-
52 the-art domain decomposition methods. A distinguishing feature is its communication strategy,
53 which relies on a layer of ghost elements instead of the more conventional ghost nodes. This
54 choice simplifies the implementation of algorithms involving topological changes of the meshes
55 in parallel, such as the dynamic insertion of cohesive elements. The [Figure 1](#) taken from
56 Vocialta et al. (2018) illustrates the usage of cohesive elements to simulate the dynamic
57 fragmentation of tempered glass panes.

58 Akantu differs from other existing codes in its ability to combine fracture dynamics and contact
59 mechanics by introducing new free surfaces through cohesive elements insertion strategy. Other
60 open-source parallel finite-element codes are capable of performing fracture and/or contact
61 mechanics simulations: among others, the most well-known that can be cited are deal.II
62 (Arndt et al. (2023)), FEniCS (Baratta et al. (2023)), GetFEM (Renard & Poulios (2021)),
63 MFEM (Anderson et al. (2021)), MoFEM (Kaczmarczyk et al. (2020)), Moose (Lindsay
64 et al. (2022)), OOFEM (Patzák (2012)). These codes can do fracture mechanics through
65 continuum damage modeling, phase-field and in some cases, X-FEM. Some of them implement
66 traction-separation laws (cohesive elements) by means of a discontinuous Galerkin formulation.
67 Only a subset of these codes is capable of performing contact mechanics computations. If
68 we consider the dynamic insertion of cohesive elements, which avoids the burden of having
69 interface elements pre-inserted everywhere and allows representing explicitly the newly formed
70 cracked surfaces, there is only one other code capable of doing such simulations in parallel
71 (Espinha et al. (2013)), to our best knowledge. However this software is not distributed as
72 open-source.

73 Scaling analysis

74 High performance and scalability is a necessity for the resolution of fracture and contact
75 simulations. To illustrate the possibilities offered by Akantu, a 3D simulation is presented
76 where a cube composed of 4'392'180 tetrahedra and 734'594 nodes is being compressed and
77 sheared (cf Figure 2). This simulation only serves to demonstrate how Akantu behaves in
78 a situation where massive fragmentation takes place: about 460'000 cohesive elements are
79 inserted during the run. This simulation was run on 1 up to 720 cores, on a cluster composed
80 of Intel Xeon nodes with 2 sockets of 36 cores, 512Gb of RAM and dual 25Gb Ethernet links.
81 The time to solution (TTS) averaged over six different runs is computed for each core count
82 on the x -axis in Figure 3. The overhead due to cohesive element insertion is also highlighted
83 by providing the TTS when cohesive element insertions are precluded.

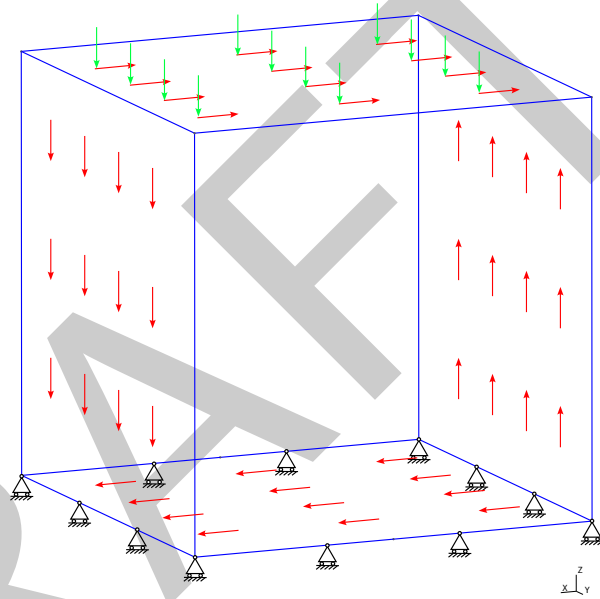


Figure 2: Numerical setup.

84 When cohesive element insertion is not active, (cf. Figure 3 'no insertion'), the time to solution
85 scales well up to ~576 cores. The simulations are running on a newly installed machine and
86 the impact of the network on the loss of scalability is not fully understood, the min and
87 max measures vary a lot after 288 cores (4 nodes). The scalability with insertion of cohesive
88 elements (Figure 3 'insertion') decreases, and starts to plateau at around 288 cores: this is
89 due to the extra communications needed to change the topology of the mesh.

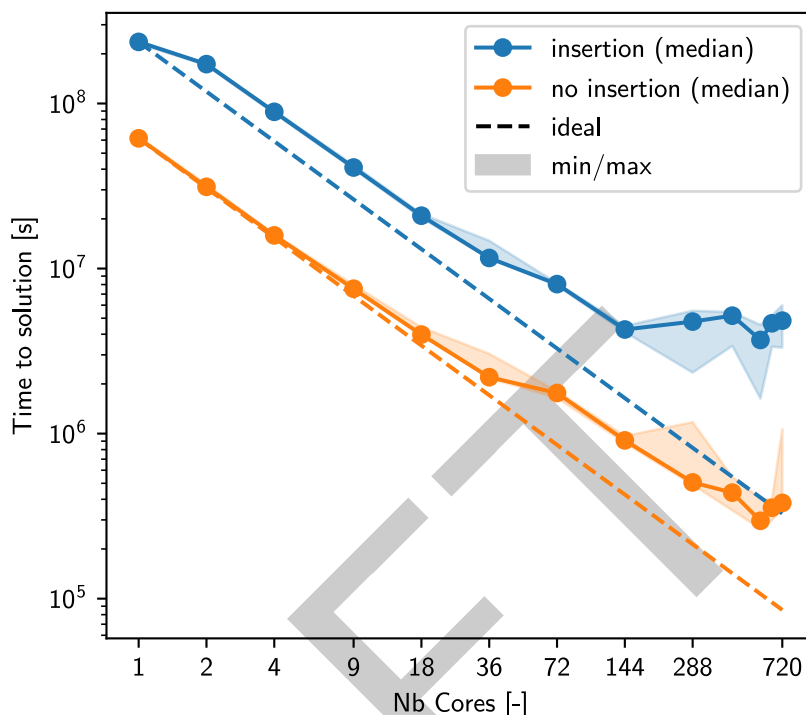


Figure 3: Time to solution with and without cohesive insertion.

Publications

The following publications have been made possible with Akantu:

- David S. Kammer et al. (2012)
- D. S. Kammer et al. (2014)
- Wolff et al. (2014)
- Richart & Molinari (2015)
- Taheri Mousavi et al. (2015)
- A. Cuba Ramos et al. (2015)
- Radiguet et al. (2015)
- Vocialta & Molinari (2015)
- Corrado & Molinari (2016)
- D. S. Kammer et al. (2016)
- Svetlizky et al. (2016)
- Vocialta et al. (2016)
- Yilmaz & Molinari (2017)
- Yilmaz et al. (2017)
- Zhang et al. (2017)
- A. I. Cuba Ramos et al. (2018)
- Vocialta et al. (2018)
- Yilmaz et al. (2018)
- Zhang et al. (2018)
- Zhang & Beyer (2019)
- Frérot et al. (2019)
- Gallyamov et al. (2020)
- Milanese & Molinari (2020)
- Albertini et al. (2021)

- 116 ■ Brun et al. (2021)
- 117 ■ Rezakhani et al. (2021)
- 118 ■ Pundir & Anciaux (2021)
- 119 ■ Roch et al. (2022)
- 120 ■ Gallyamov, Leemann, et al. (2022)
- 121 ■ Gallyamov, Shakoorioskooie, et al. (2022)
- 122 ■ Gallyamov et al. (2023)

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