

- konfound: An R Sensitivity Analysis Package to
- 2 Quantify the Robustness of Causal Inferences
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DOI: 10.xxxxx/draft

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Editor: Fabian Scheipl ☑ ⑩ Reviewers:

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Submitted: 31 July 2023 **Published:** unpublished

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Quantifying the Robustness of Inferences

Statistical methods which quantify the conditions necessary to alter inferences are important to a variety of disciplines (Razavi et al., 2021). One line of work is rooted in linear models and foregrounds the sensitivity of inferences to the strength of omitted variables (Cinelli & Hazlett, 2019; Frank, 2000). A more recent approach is rooted in the potential outcomes framework for causal inference and foregrounds how hypothetical changes in a sample would alter an inference if such variables or cases were otherwise observed [Frank & Min (2007); Frank et al. (2008); Frank et al. (2013); Xu et al. (2019)). We have implemented two measures from these lines of work within R via the konfound R package. One measure is the Impact Threshold of a Confounding Variable (ITCV), which generates statements such as "to invalidate an inference of an effect, an omitted variable would have to be correlated at ___ with the predictor of interest and with the outcome" (Frank, 2000). This sensitivity analysis can be calculated for any linear model. The second measure is the Robustness of an Inference to Replacement (RIR) which generates statements such as "to invalidate the inference, ___ % of the cases would have to be replaced with counterfactual cases with zero effect of the treatment" (Frank et al., 2013). The RIR represents a more generally applicable approach not limited to linear models, and is recommended for all cases that use binary outcomes (Frank et al., 2021).

Statement of Need: The Need for an R Package

We have implemented these recent developments of sensitivity analysis for causal inferences within R via the konfound R package. In particular, the konfound package is used to calculate two robustness indices: ITCV and RIR.

This paper provides an overview of two core functions within the konfound package: konfound(), pkonfound(). These functions allow users to calculate the robustness of inferences using a model estimated in R in or using information about a model from a published study, respectively. The package is available from the Comprehensive R Archive Network (CRAN) at https://CRAN.R-project.org/package=konfound; it can be installed via the standard install.packages("konfound") function. These two core functions within the konfound package are briefly summarized below along with their functionality.



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Summary and Functionality

1. **konfound**: This function is used for fitted models and calculates the ITCV and RIR. This function currently works for linear models created with lm(), glm(), and lmer() fitted in R. The output printed in the R console is the bias that must be present and the number of cases that would have to be replaced with cases for which there is no effect to invalidate the inference.

Example for linear models fit with Im()

- For this example, we will use the concord1 dataset built into the konfound package. This dataset comes from Hamilton's (1983) study which examines the causal mechanism behind household water conservation in a U.S. city.
- We will model the impact the following variables have on household water consumption in 1981: household water consumption in 1980 (water80), household income (income), education level of household survey respondent (educat), retirement status of respondent (retire), and number of individuals in household in 1980 (peop80).

```
library(konfound)
51
52
   ## Sensitivity analysis as described in Frank, Maroulis, Duong, and Kelcey (2013) and in
53
   ## For more information visit http://konfound-it.com.
   m <- lm(water81 ~ water80 + income + educat + retire + peop80, data = concord1)
56
   summary(m)
57
58
   ##
59
   ## lm(formula = water81 ~ water80 + income + educat + retire + peop80,
61
          data = concord1)
   ##
63
      Residuals:
64
   ##
          Min
                   10
65
   ##
                       Median
                                    30
                                            Max
      -4035.5
               -453.4
                         -62.7
                                 384.2
                                        4995.5
67
   ## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
      (Intercept) 299.7437
                              210.0136
                                         1.427 0.15414
      water80
                    0.4943
                                0.0268
                                        18.445
                                                < 2e-16 ***
   ##
      income
                   22.6031
                                3.5023
                                         6.454 2.62e-10 ***
72
                   -44.2578
                               13.4381
                                        -3.293 0.00106 **
   ## educat
   ## retire
                  155.4727
                               96.3389
                                         1.614 0.10721
                  225.1984
                               28.7048
                                         7.845 2.73e-14 ***
   ## peop80
75
   ##
   ## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
77
   ## Residual standard error: 864.1 on 490 degrees of freedom
79
   ## Multiple R-squared: 0.6653, Adjusted R-squared: 0.6619
   ## F-statistic: 194.8 on 5 and 490 DF, p-value: < 2.2e-16
```

Results indicate that all variables except retire have a significant effect on 1981 household water consumption.



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ITCV example for linear models fit with Im()

```
Now let's examine the robustness of the peop80 effect by calculating the ITCV.
   konfound(m, peop80, index = "IT")
   ## Impact Threshold for a Confounding Variable:
88
   ## The minimum impact of an omitted variable to invalidate an inference for a null hypot
       with the outcome and at 0.52 with the predictor of interest (conditioning on obser
   ## 0.089 for statistical significance (alpha = 0.05).
91
92
   ## Correspondingly the impact of an omitted variable (as defined in Frank 2000) must be
   ## 0.52 \times 0.52 = 0.27 to invalidate an inference for a null hypothesis of 0 effect.
   ## See Frank (2000) for a description of the method.
   ##
   ## Citation:
   ## Frank, K. (2000). Impact of a confounding variable on the
   ## inference of a regression coefficient. Sociological Methods and Research, 29 (2), 147
101
   ## For more detailed output, consider setting `to_return` to table
102
103
   ## To consider other predictors of interest, consider setting `test all` to TRUE.
   The output indicates that in order to invalidate the inference that peop80 has an effect on
105
   water81 using statistical significance as a threshold (e.g., p=.05), an omitted variable would
106
```

have to be correlated at 0.52 with peop80 and 0.52 with water81, conditioning on observed

covariates. Correspondingly, the impact of an omitted variable (as defined in (Frank, 2000))

RIR example for linear models fit with Im()

must be $0.52 \times 0.52 = 0.27$.

```
\,\,^{111}\,\, We can also examine the robustness by calculating the RIR.
```

```
konfound(m, peop80, index = "RIR")
112
113
   ## Robustness of Inference to Replacement (RIR):
114
   ## To invalidate an inference, 74.955 % of the estimate would have to be due to bias.
115
   ## This is based on a threshold of 56.4 for statistical significance (alpha = 0.05).
116
117
   ## To invalidate an inference, 372 observations would have to be replaced with cases
118
      for which the effect is 0 (RIR = 372).
120
   ##
      See Frank et al. (2013) for a description of the method.
121
   ##
122
   ## Citation: Frank, K.A., Maroulis, S., Duong, M., and Kelcey, B. (2013).
   ## What would it take to change an inference?
124
   ## Using Rubin's causal model to interpret the robustness of causal inferences.
125
   ## Education, Evaluation and Policy Analysis, 35 437-460.
   ## For more detailed output, consider setting `to_return` to table
128
129
   ## To consider other predictors of interest, consider setting `test_all` to TRUE.
   The output presents two interpretations of the RIR. First, 74.956% of the estimated effect of
131
   peop80 on water81 would have to be attributed to bias to invalidate the inference. Equivalently,
132
```

we would expect to have to replace 372 out of the 486 households (about 76%) with cases



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for which peop80 had no effect to invalidate the inference. See (Frank et al., 2013, 2021) for guidelines on evaluating the RIR relative to the bias accounted for by observed covariates or published norms.

2. pkonfound: This function quantifies the sensitivity for analyses which have already been conducted, such as in an already-published study or from analysis carried out using other software. This function calculates 1) how much bias there must be in an estimate to invalidate/sustain an inference which can be interpreted as the percentage of cases that would have to be replaced (with cases for which the predictor had no effect on the outcome) to invalidate the inference and 2) the impact of an omitted variable necessary to invalidate/sustain an inference for a regression coefficient (note: impact is defined as the correlation between omitted variable and outcome).

ITCV example for a regression analysis

```
For this example, the following parameters from a regression analysis would be entered into
147
   the pkonfound function: unstandardized beta coefficient for the predictor of interest (B = 2),
   standard error (SE = .4), sample size (n = 100), and the number of covariates (cv = 3).
   pkonfound(2, .4, 100, 3, index = "IT")
150
151
   ## Impact Threshold for a Confounding Variable:
152
   ## The minimum impact of an omitted variable to invalidate an inference for a null hypot
153
       with the outcome and at 0.568 with the predictor of interest (conditioning on obse
154
   ## 0.201 for statistical significance (alpha = 0.05).
156
      Correspondingly the impact of an omitted variable (as defined in Frank 2000) must be
157
      0.568 X 0.568 = 0.323 to invalidate an inference for a null hypothesis of 0 effect.
158
      See Frank (2000) for a description of the method.
   ##
160
   ## Citation:
161
   ## Frank, K. (2000). Impact of a confounding variable on the
162
   ## inference of a regression coefficient. Sociological Methods and Research, 29 (2), 147
   194
164
165
   ## For other forms of output, run ?pkonfound and inspect the to return argument
166
```

For models fit in R, consider use of konfound().

The output indicates that in order to invalidate the inference that the predictor of interest

has a greater than zero effect, an omitted variable would have to be correlated at 0.568 with the outcome and at 0.568 with the predictor of interest, conditioning on observed covariates.

Correspondingly, the impact of an omitted variable (ITCV) must be $0.568 \times 0.568 = 0.323$ to invalidate an inference for a null hypothesis of 0 effect.

RIR example for a regression analysis

```
pkonfound(2, .4, 100, 3, index = "RIR")

## Robustness of Inference to Replacement (RIR):

## To invalidate an inference, 60.29 % of the estimate would have to be due to bias.

## This is based on a threshold of 0.794 for statistical significance (alpha = 0.05).

##

## To invalidate an inference, 60 observations would have to be replaced with cases

## for which the effect is 0 (RIR = 60).

##

##
```



```
## See Frank et al. (2013) for a description of the method.
184
   ##
185
    ## Citation: Frank, K.A., Maroulis, S., Duong, M., and Kelcey, B. (2013).
186
    ## What would it take to change an inference?
187
    ## Using Rubin's causal model to interpret the robustness of causal inferences.
188
   ## Education, Evaluation and Policy Analysis, 35 437-460.
    ## For other forms of output, run ?pkonfound and inspect the to_return argument
191
192
   ## For models fit in R, consider use of konfound().
193
   The output indicates that to invalidate the inference, approximately 60% of the estimated
    effect of the predictor of interest would have to be due to bias in this model to invalidate this
195
   inference. Equivalently, 60 out of 100 cases would have to be replaced with zero effect cases
196
   in order to invalidate this inference. See (Frank et al., 2013, 2021) for guidelines on evaluating
    the RIR relative to the bias accounted for by observed covariates or published norms.
```

Doing and Learning More

We have created a Shiny interactive web application at http://konfound-it.com/ that can be applied to linear models, 2 x 2 tables resulting corresponding to treatment and control by success and failure conditions, and logistic regression models (functionality for designs including mediation, differences in difference, and regression discontinuity are under development). We are also developing extensions of the sensitivity analysis techniques described in this paper, including preserving the standard error (Frank et al., 2023) and calculating the coefficient of proportionality (Frank et al., 2022) for ITCV analyses. Additional documentation on the R package and future extensions will be available at https://konfound-project.github.io/konfound/.

Acknowledgements

The research reported here was supported by the Institute of Education Sciences, U.S. Department of Education, through Grant R305D220022 to Michigan State University. The opinions expressed are those of the authors and do not represent views of the Institute or the U.S. Department of Education.

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