

$$2. D = \{1, 2, 3, 4, 5, 6\}$$

1 bola de u_1 si $D = \{1\} \cup \{2\}$

1 bola de u_2 si $D = D - \{1, 2\}$

$$u_1: 3R, 1N, 6V \quad u_2: 6R, 2N, 2V$$

$$a) P(R) = ?$$

$$\begin{aligned} P(R) &= P(R|u_1)P(u_1) + P(R|u_2)P(u_2) \\ &= \frac{3}{10} \left(\frac{2}{6} \right) + \frac{6}{10} \left(\frac{2}{6} \right) = \frac{1}{10} + \frac{2}{5} = \frac{1}{10} + \frac{4}{10} = \frac{5}{10} = \underline{\underline{\frac{1}{2}}} \end{aligned}$$

$$b) P(N) = ?$$

$$\begin{aligned} P(N) &= P(N|u_1)P(u_1) + P(N|u_2)P(u_2) \\ &= \left(\frac{1}{10} \right) \left(\frac{2}{6} \right) + \left(\frac{2}{10} \right) \left(\frac{4}{6} \right) \\ &= \frac{2}{60} + \frac{8}{60} = \frac{10}{60} = \underline{\underline{\frac{1}{6}}} \end{aligned}$$

$$\begin{aligned} c) P(u_1|N) &= \frac{P(N|u_1)P(u_1)}{P(N|u_1)P(u_1) + P(N|u_2)P(u_2)} \\ &= \frac{\frac{1}{10} \left(\frac{2}{6} \right)}{\frac{1}{10} \left(\frac{2}{6} \right) + \frac{2}{10} \left(\frac{4}{6} \right)} = \frac{\frac{2}{60}}{\frac{2+8}{60}} = \frac{2}{10} = \underline{\underline{\frac{1}{5}}} \end{aligned}$$

$$\begin{aligned} d) P(u_2|N) &= \frac{P(N|u_2)P(u_2)}{P(N|u_2)P(u_2) + P(N|u_1)P(u_1)} \\ &= \frac{\frac{2}{10} \left(\frac{4}{6} \right)}{\frac{2}{10} \left(\frac{4}{6} \right) + \frac{1}{10} \left(\frac{2}{6} \right)} = \frac{\frac{8}{60}}{\frac{10}{60}} = \frac{8}{10} = \underline{\underline{\frac{4}{5}}} \end{aligned}$$