

## CS221 - Indented Outline (Notes 11-18)

Generated from your uploaded lecture PDFs (Overview, Search, MDPs, Logic, ML III).

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## **Notes 11: Lecture 1: Overview**

### **Roadmap**

- A brief history
- Two views
- Course overview
- Course logistics
- Optimization

### **Course plan**

- "Low-level intelligence"
- "High-level intelligence"
- Machine learning

### **Two views of AI**

- AI agents: how can we create intelligence?
- AI tools: how can we benefit society?

### **An intelligent agent**

- Perception
  - Robotics
  - Language
- Knowledge
- Reasoning
- Learning

### **History: early AI**

- 1956: Workshop at Dartmouth College; attendees: John McCarthy, Marvin Minsky, Claude Shannon, etc.
- Aim for general principles:
- Every aspect of learning or any other feature of intelligence can be so precisely described that a machine can be made to simulate it.

### **History: optimism and limits**

- Machines will be capable, within twenty years, of doing any work a man can do. -Herbert Simon
- Within 10 years the problems of artificial intelligence will be substantially solved. -Marvin Minsky
- I visualize a time when we will be to robots what dogs are to humans, and I'm rooting for the machines. -Claude Shannon

### **Modeling paradigm**

- Modeling
- Inference
- Learning

### **State-based models**

- White to move

### **Variable-based models**

- Constraint satisfaction problems:
  - hard constraints (e.g.,
  - Sudoku,
  - scheduling)
  - X1
  - X2
  - X3
  - X4
- Bayesian networks: soft dependencies (e.g., tracking cars from sensors)
  - H1
  - H2
  - H3

### **Knowledge-based systems**

- Expert systems: elicit specific domain knowledge from experts in form
- of rules:
  - if [premises] then [conclusion]

### **Deep learning**

- AlexNet (2012): huge gains in object recognition; transformed computer vision community overnight
- AlphaGo (2016):
  - deep reinforcement learning, defeat
- world champion Lee Sedol

### **Societal impact examples**

- society => data => predictions

### **Summary**

- History: roots from logic, neuroscience, statistics-melting pot!
- Modeling [reflex, states, variables, logic] + inference + learning
- paradigm
- AI has high societal impact, how to steer it positively?

## Notes 12: Lecture 5: Search I

### Roadmap

- Tree search
- Dynamic programming
- Uniform cost search

### Search paradigm

- Modeling
- Inference
- Learning

### State and planning abstraction

- Classifier (reflex-based models):
  - single action  $y$  in  $\{-1, +1\}$
- Search problem (state-based models):
  - action sequence  $(a_1, a_2, a_3, a_4, \dots)$
  - Key: need to consider future consequences of an action!

### Tree search algorithms

- Legend:  $b$  actions/state, solution depth  $d$ , maximum depth  $D$
- Algorithm
- Action costs
- Space
- Time
- $O(bD)$
- Backtracking
- any
- $O(D)$
- $O(bD)$
- DFS
- zero

### Uniform cost search

- Key idea: state ordering
- UCS enumerates states in order of increasing past cost.
- Assumption: non-negativity
- All action costs are non-negative:  $\text{Cost}(s, a) \geq 0$ .
- UCS in action:

### UCS bookkeeping

- Frontier

- Explored
- Unexplored
- Explored: states we've found the optimal path to
- Frontier: states we've seen, still figuring out how to get there
  - cheaply
- Unexplored: states we haven't seen

### **UCS assumptions**

- N total states, n of which are closer than end state
- Algorithm
  - Cycles?
  - Action costs
  - Time/space
- DP
  - no
  - any
  - $O(N)$
  - $\geq 0$
- UCS
  - yes

### **Summary**

- State: summary of past actions sufficient to choose future actions
  - optimally
- Dynamic programming: backtracking search with memoization
  - potentially exponential savings
- cycles?

## Notes 13: Lecture 6: Search II

### Roadmap

- Learning costs
- A\* search
- Relaxation

### General framework: relaxation

- Removing constraints
- (knock down walls, walk/tram freely, overlap pieces)
- Reducing edge costs
- (from  $\infty$  to some finite cost)
- Example:
- Original:  $\text{Cost}((1, 1), \text{East}) = \infty$
- Relaxed:  $\text{Costrel}((1, 1), \text{East}) = 1$

### A\* as UCS with heuristic

- Algorithm: A\* search [Hart/Nilsson/Raphael, 1968]
- Run uniform cost search with modified edge costs:
- $\text{Cost}'(s, a) = \text{Cost}(s, a) + h(\text{Succ}(s, a)) - h(s)$
- Intuition: add a penalty for how much action a takes us away from the
- end state
- Example:
- sstart
- send
- $h(s) =$
- $\text{Cost}'(C, B) = \text{Cost}(C, B) + h(B) - h(C) = 1 + (3 - 2) = 2$

### Heuristic admissibility

- Definition: admissibility
- A heuristic  $h(s)$  is admissible if
- $h(s) \leq \text{FutureCost}(s)$
- Intuition: admissible heuristics are optimistic
- Theorem: consistency implies admissibility
- If a heuristic  $h(s)$  is consistent, then  $h(s)$  is admissible.
- Proof: use induction on  $\text{FutureCost}(s)$

### Heuristic consistency

- Definition: consistency
- A heuristic  $h$  is consistent if
- $\text{Cost}'(s, a) = \text{Cost}(s, a) + h(\text{Succ}(s, a)) - h(s) \geq 0$
- $h(\text{send}) = 0$ .
- Condition 1: needed for UCS to work (triangle inequality).

- $\text{Cost}(s, a)$
- $h(\text{Succ}(s, a))$
- $h(s)$
- send
- Condition 2:  $\text{FutureCost}(\text{send}) = 0$  so match it.

### Search effort vs heuristic quality

- sstart
- send
- $h = 0$  (UCS)
- $h = \text{FutureCost}$
- If  $h(s) = 0$ , then  $A^*$  is same as UCS.
- If  $h(s) = \text{FutureCost}(s)$ , then  $A^*$  only explores nodes on a minimum cost path.
- Usually  $h(s)$  is somewhere in between.

### Learning as inverse problem

- Forward problem (search):
- $\text{Cost}(s, a)$
- $(a_1, \dots, a_k)$
- Inverse problem (learning):
- $(a_1, \dots, a_k)$
- $\text{Cost}(s, a)$

### Cost tweaking intuition

- Costs: {walk:3, tram:2}
- Costs: {walk:1, tram:3}
- Minimum cost path:
- Minimum cost path:
- walk:3
- walk:1
- walk:3
- tram:2
- walk:1
- tram:3
- walk:3
- walk:1

### Simple cost model

- Assume costs depend only on the action:
- $\text{Cost}(s, a) = w[a]$
- Candidate output path:
- $a_1 : w[a_1]$
- $a_2 : w[a_2]$

- $a_3 : w[a_3]$
- $y:$
- $s_0$
- $s_1$
- $s_2$
- $s_3$
- Path cost:

### Structured perceptron learning

- Algorithm: Structured Perceptron (simplified)
- For each action:  $w[a] \leftarrow 0$
- For each iteration  $t = 1, \dots, T$ :
- For each training example  $(x, y)$  in  $D_{\text{train}}$ :
- Compute the minimum cost path  $y'$  given  $w$
- For each action  $a$  in  $y$ :  $w[a] \leftarrow w[a] - 1$
- For each action  $a$  in  $y'$ :  $w[a] \leftarrow w[a] + 1$
- Try to decrease cost of true  $y$  (from training data)
- Try to increase cost of predicted  $y'$  (from search)
- [semi-live solution]

### Applications

- Part-of-speech tagging
- Fruit flies like a banana.
- Noun Noun Verb Det Noun
- Machine translation
- la maison bleue
- the blue house

### Summary

- Structured Perceptron (reverse engineering): learn cost functions
- (search + learning)
- A\*: add in heuristic estimate of future costs
- Relaxation (breaking the rules): framework for producing consistent heuristics
- Next time: when actions have unknown consequences...



## Notes 14: Lecture 7: MDPs I

### Roadmap

- Markov decision process
- Policy evaluation
- Value iteration

### From search to uncertainty

- deterministic
- state  $s$ , action  $a$
- state  $\text{Succ}(s, a)$

### Markov decision process

- Definition: Markov decision process
- States: the set of states
- $s_{\text{start}}$  in States: starting state
- Actions( $s$ ): possible actions from state  $s$
- $T(s'|s, a)$ : probability of  $s'$  if take action  $a$  in state  $s$
- Reward( $s, a, s'$ ): reward for the transition  $(s, a, s')$
- $\text{IsEnd}(s)$ : whether at end of game
- $0 \leq \gamma \leq 1$ : discount factor (default: 1)

### Utility and value

- Definition: utility
- Following a policy yields a random path.
- The utility of a policy is the (discounted) sum of the rewards on the path (this is a random variable).
- Path
- Utility
- [in; stay, 4, end]
- [in; stay, 4, in; stay, 4, in; stay, 4, end]
- [in; stay, 4, in; stay, 4, end]
- [in; stay, 4, in; stay, 4, in; stay, 4, in; stay, 4, end] 16
- Definition: value (expected utility)
- The value of a policy at a state is the expected utility.

### Policy evaluation

- Definition: value of a policy
- Let  $V_{\pi}(s)$  be the expected utility received by following policy  $\pi$  from state  $s$ .
- Definition: Q-value of a policy
- Let  $Q_{\pi}(s, a)$  be the expected utility of taking action  $a$  from state  $s$ , and then following policy  $\pi$ .

- $Q_{\pi}(s, \pi(s))$
- $V_{\pi}(s')$
- $s'$
- $T(s'|s, \pi(s))$
- $V_{\pi}(s)$
- $\pi(s)$

### Summary so far

- MDP: graph with states, chance nodes, transition probabilities,
- rewards
- Policy: mapping from state to action (solution to MDP)
- Value of policy: expected utility over random paths
- Policy evaluation: iterative algorithm to compute value of policy

### Optimality: values and policies

- Goal: try to get directly at maximum expected utility
- Definition: optimal value
- The optimal value  $V^*(s)$  is the maximum value attained by any
- policy.

### Value iteration

- Algorithm: value iteration [Bellman, 1957]
- Initialize  $V^*(0)(s) \leftarrow 0$  for all states  $s$ .
- For iteration  $t = 1, \dots, t_{VI}$ :
- For each state  $s$ :
- $V^*(t)(s) \leftarrow$
- $T(s'|s, a)[\text{Reward}(s, a, s') + \gamma V^*(t-1)(s')]$
- max
- $a \in \text{Actions}(s)$
- $s'$
- $Q^*(t-1)(s, a)$
- Time:  $O(t_{VI} |S|)$
- [semi-live solution]

## Notes 15: Lecture 8: MDPs II

### Roadmap

- Reinforcement learning
- Model-based value iteration
- Model-free policy evaluation & learning
- Covering the unknown
- Summary

### From MDPs to reinforcement learning

- Markov decision process (offline)
- Have mental model of how the world works.
- Find policy to collect maximum rewards.
- Reinforcement learning (online)
- Don't know how the world works.
- Perform actions in the world to find out and collect rewards.

### RL template

- action  $a$
- agent
- environment
- reward  $r$ , new state  $s'$
- Algorithm: reinforcement learning template
- For  $t = 1, 2, 3, \dots$
- Choose action  $a_t = \text{piact}(s_{t-1})$  (how?)
- Receive reward  $r_t$  and observe new state  $s_t$
- Update parameters (how?)

### Model-based value iteration

- Data:  $s_0; a_1, r_1, s_1; a_2, r_2, s_2; a_3, r_3, s_3; \dots; a_n, r_n, s_n$
- Key idea: model-based learning
- Estimate the MDP:  $T(s'|s, a)$  and  $\text{Reward}(s, a, s')$
- Transitions:
  - $\hat{T}(s'|s, a) = \# \text{ times } (s, a, s') \text{ occurs}$
  - $\# \text{ times } (s, a) \text{ occurs}$
- Rewards:
  - $\text{Reward}(s, a, s') = r \text{ in } (s, a, r, s')$

### Model-free Monte Carlo

- Data (following policy  $\pi$ ):
- $s_0; a_1, r_1, s_1; a_2, r_2, s_2; a_3, r_3, s_3; \dots; a_n, r_n, s_n$

- Recall:
- $Q_{\pi}(s, a)$  is expected utility starting at  $s$ , first taking action  $a$ , and then following policy  $\pi$
- Utility:
- $u_t = r_t + \gamma V_{t+1} - V_t$
- Estimate:
- $\hat{Q}_{\pi}(s, a) = \text{average of } u_t \text{ where } s_{t-1} = s, a_t = a$
- (and  $s, a$  doesn't occur in  $s_0, \dots, s_{t-2}$ )

## Q-learning

- Problem: model-free Monte Carlo and SARSA only estimate  $Q_{\pi}$ , but
- want  $Q^*$  to act optimally
- Output
- MDP
- reinforcement learning
- $Q_{\pi}$
- policy evaluation
- model-free Monte Carlo, SARSA
- $Q^*$
- value iteration

## Exploration/exploitation

- Key idea: balance
- Need to balance exploration and exploitation.
- Examples from life: restaurants, routes, research

## Epsilon-greedy

- Algorithm: epsilon-greedy policy
- $\arg \max_a Q(s, a)$
- probability  $1 - \epsilon$ ,
- $\pi_{\text{act}}(s) =$
- random from  $\text{Actions}(s)$
- probability  $\epsilon$ .
- 99.8
- 99.6
- (2,1)
- 50
- Run (or press ctrl-enter)
- 50

## Function approximation

- Key idea: linear regression model
- Define features  $\phi(s, a)$  and weights  $w$ :
- $\hat{Q}(s, a; w) = w \cdot \phi(s, a)$

- Example: features for volcano crossing
- $\phi_7(s, a) = 1[s = (5, *)]$
- $\phi_1(s, a) = 1[a = W]$
- $\phi_8(s, a) = 1[s = (*, 6)]$
- $\phi_2(s, a) = 1[a = E]$

## Deep reinforcement learning

- just use a neural network for  $\hat{Q}^*(s, a)$ ,  $\pi^*$ ,  $T$ , etc
- Playing Atari [Google DeepMind, 2013]:
- last 4 frames (images)  $\Rightarrow$  3-layer NN  $\Rightarrow$  keystroke
- ■-greedy, train over 10M frames with 1M replay memory
- Human-level performance on some games (breakout), less good on others (space invaders)

## Summary so far

- Online setting: learn and take actions in the real world!
- Exploration/exploitation tradeoff
- Model-Based RL: estimate transitions & rewards, and use that model of the MDP to find optimal policy
- Model-Free Monte Carlo: estimate Q-values from data
- Model-Free Bootstrapping: update towards target that depends on estimate rather than just raw data

## Notes 16: Lecture 16: Logic I

### Motivation

- Tell information
- Ask questions
- Use natural language!
- [semi-live demo]
- Need to:
  - Digest heterogenous information
  - Reason deeply with that information

### Logic in the AI stack

- question
- data
- Learning
- model
- Inference
- answer
- Examples: search problems, MDPs, games, CSPs, Bayesian networks

### Ingredients of propositional logic

- Syntax
- Semantics
- formula
- models
- Inference
- rules

### Syntax

- Propositional symbols (atomic formulas): A, B, C
- Logical connectives: not, and, or,  $\rightarrow$ ,  $\leftrightarrow$
- Build up formulas recursively-if f and g are formulas, so are the following:
- Negation: not f
- Conjunction: f and g
- Disjunction: f or g
- Implication:  $f \rightarrow g$
- Biconditional:  $f \leftrightarrow g$

### Semantics: truth and models

- $\{f : KB \models f$

### Model checking

- Checking satisfiability (SAT) in propositional logic is special case of solving CSPs!
- Mapping:
  - $\Rightarrow$
  - propositional symbol
  - variable
  - $\Rightarrow$
  - formula
  - constraint
  - model
  - assignment

### Knowledge bases

- $M(\text{Rain})$
- $M(\text{Rain} \rightarrow \text{Wet})$
- $\text{Wet}$
- $\text{Wet}$
- $\text{Rain}$
- $\text{Rain}$
- Intersection:
  - $M(\{\text{Rain}, \text{Rain} \rightarrow \text{Wet}\})$
  - $\text{Wet}$
  - $\text{Rain}$

### Entailment and queries

- $M(\text{KB})$
- $M(f)$
- Intuition:  $f$  added no information/constraints (it was already known).
- Definition: entailment
- $\text{KB}$  entails  $f$  (written  $\text{KB} \models f$ ) iff
- $M(\text{KB}) \subseteq M(f)$ .
- Example:  $\text{Rain and Snow} \models \text{Snow}$

### Tell/Ask interface

- $\text{Tell}[f]$
- $\text{KB}$
- Tell: It is raining.
- $\text{Tell}[\text{Rain}]$
- Possible responses:
  - Already knew that: entailment ( $\text{KB} \models f$ )
  - Don't believe that: contradiction ( $\text{KB} \models \text{not } f$ )
  - Learned something new (update  $\text{KB}$ ): contingent

### Satisfiability

- Definition: satisfiability
- A knowledge base KB is satisfiable if  $M(KB) \neq \emptyset$ .
- Reduce Ask[f] and Tell[f] to satisfiability:
  - Is  $KB \cup \{\text{not } f\}$  satisfiable?
  - yes
  - no
  - Is  $KB \cup \{f\}$  satisfiable?
  - entailment
  - no
  - yes
  - contradiction
  - contingent

### Inference rules

- Example of making an inference:
  - It is raining. (Rain)
  - If it is raining, then it is wet. (Rain  $\rightarrow$  Wet)
  - Therefore, it is wet. (Wet)
  - Rain  $\rightarrow$  Wet
  - Rain,
  - (premises)
  - (conclusion)
  - Wet
- Definition: Modus ponens inference rule
- For any propositional symbols p and q:
- $p \rightarrow q$

### Soundness and completeness

- The truth, the whole truth, and nothing but the truth.
- Soundness: nothing but the truth
- Completeness: whole truth

### Historical note

- Logic was dominant paradigm in AI before 1990s
- Problem 1: deterministic, didn't handle uncertainty (probability addresses this)
- Problem 2: rule-based, didn't allow fine tuning from data (machine learning addresses this)
- Strength: provides expressiveness in a compact way

### Summary

- Syntax
- Semantics
- formula



- models
- Inference
- rules

## Notes 17: Lecture 17: Logic II

### Roadmap

- Resolution in propositional logic
- First-order logic

### Limits of propositional logic

- Alice and Bob both know arithmetic.
- AliceKnowsArithmetic and BobKnowsArithmetic
- All students know arithmetic.
- AliceIsStudent  $\rightarrow$  AliceKnowsArithmetic
- BobIsStudent  $\rightarrow$  BobKnowsArithmetic
- ...
- Every even integer greater than 2 is the sum of two primes.
- ???

### First-order logic ingredients

- Syntax
- Semantics
- formula
- models
- Inference
- rules

### Syntax of FOL

- Terms (refer to objects):
- Constant symbol (e.g., arithmetic)
- Variable (e.g.,  $x$ )
- Function of terms (e.g.,  $\text{Sum}(3, x)$ )
- Formulas (refer to truth values):
- Atomic formulas (atoms):
- predicate applied to terms (e.g.,  $\text{Knows}(x, \text{arithmetic})$ )
- Connectives
- $\rightarrow$
- applied
- to

### Quantifiers

- Universal quantification (forall):
- Think conjunction: forall  $x$   $P(x)$  is like  $P(A)$  and  $P(B)$  and \* \* \*
- Existential quantification (exists):
- Think disjunction: exists  $x$   $P(x)$  is like  $P(A)$  or  $P(B)$  or \* \* \*

- Some properties:
- not forall x P(x) equivalent to exists x not P(x)
- forall x exists y Knows(x, y) different from exists y forall x Knows(x, y)

## Models in FOL

- Recall a model represents a possible situation in the world.
- Propositional logic: Model w maps propositional symbols to truth values.
- $w = \{\text{AliceKnowsArithmetic} : 1, \text{BobKnowsArithmetic} : 0\}$
- First-order logic: ?

## Definite clauses

- forall x forall y forall z (Takes(x, y) and Covers(y, z))  $\rightarrow$  Knows(x, z)
- Note: if propositionalize, get one formula for each value to (x, y, z), e.g.,
- Definition: definite clause (first-order logic)
- A definite clause has the following form:
- forall x1 \* \* \* forall xn (a1 and \* \* \* and ak)  $\rightarrow$  b
- for variables x1, . . . , xn and atomic formulas a1, . . . , ak, b (which contain those variables).

## Substitution

- $\text{Subst}[\{x/\text{alice}, P(x)\}] = P(\text{alice})$
- $\text{Subst}[\{x/\text{alice}, y/z, P(x) \text{ and } K(x, y)\}] = P(\text{alice}) \text{ and } K(\text{alice}, z)$
- Definition: Substitution
- A substitution theta is a mapping from variables to terms.
- $\text{Subst}[\text{theta}, f]$  returns the result of performing substitution theta on f.

## Unification

- $\text{Unify}[\text{Knows}(\text{alice}, \text{arithmetic}), \text{Knows}(x, \text{arithmetic})] = \{x/\text{alice}\}$
- $\text{Unify}[\text{Knows}(\text{alice}, y), \text{Knows}(x, z)] = \{x/\text{alice}, y/z\}$
- $\text{Unify}[\text{Knows}(\text{alice}, y), \text{Knows}(\text{bob}, z)] = \text{fail}$
- $\text{Unify}[\text{Knows}(\text{alice}, y), \text{Knows}(x, F(x))] = \{x/\text{alice}, y/F(\text{alice})\}$
- Definition: Unification
- Unification takes two formulas f and g and returns a substitution
- theta which is the most general unifier:
- $\text{Unify}[f, g] = \text{theta}$  such that  $\text{Subst}[\text{theta}, f] = \text{Subst}[\text{theta}, g]$
- or "fail" if no such theta exists.

## Modus ponens

- Definition: modus ponens (first-order logic)
- a'
- 1, . . . , a'
- forall x1 \* \* \* forall xn (a1 and \* \* \* and ak)  $\rightarrow$  b
- b'

- Get most general unifier theta on premises:
  - $\theta = \text{Unify}[a'$
  - $1 \text{ and } * * * \text{ and } a'$
  - $k, a1 \text{ and } * * * \text{ and } ak]$
- Apply theta to conclusion:
  - $\text{Subst}[\theta, b] = b'$

## CNF conversion

- Input:
  - $\text{forall } x (\text{forall } y \text{ Animal}(y) \rightarrow \text{Loves}(x, y)) \rightarrow \text{exists } y \text{ Loves}(y, x)$
- Output:
  - $(\text{Animal}(Y(x)) \text{ or } \text{Loves}(Z(x), x)) \text{ and } (\text{not Loves}(x, Y(x)) \text{ or } \text{Loves}(Z(x), x))$
- New to first-order logic:
  - All variables (e.g.,  $x$ ) have universal quantifiers by default
  - Introduce Skolem functions (e.g.,  $Y(x)$ ) to represent existential quantified variables

## Resolution

- Recall: First-order logic includes non-Horn clauses
  - $\text{forall } x \text{ Student}(x) \rightarrow \text{exists } y \text{ Knows}(x, y)$
- High-level strategy (same as in propositional logic):
  - Convert all formulas to CNF
  - Repeatedly apply resolution rule

## Resolution algorithm

- Recall:
  - relationship between entailment and contradiction (basically
  - "proof by contradiction")
  - $\text{KB} \models f$
  - $\text{KB} \cup \{\text{not } f\}$  is unsatisfiable
  - Algorithm: resolution-based inference
  - Add not  $f$  into KB.
  - Convert all formulas into CNF.
  - Repeatedly apply resolution rule.
  - Return entailment iff derive false.

## Complexity

- $\text{forall } x \text{ forall } y \text{ forall } z \text{ P}(x, y, z)$
- Each application of Modus ponens produces an atomic formula.
- If no function symbols, number of atomic formulas is at most
  - $(\text{num-constant-symbols})(\text{maximum-predicate-arity})$
- If there are function symbols (e.g.,  $F$ ), then infinite...
  - $* * *$
- $Q(a)$

- $Q(F(a))$
- $Q(F(F(a)))$
- $Q(F(F(F(a))))$

### **Summary**

- Horn clauses
- any clauses
- modus ponens
- resolution
- linear time
- exponential time
- less expressive
- more expressive

## Notes 18: Lecture 4: Machine learning III

### Roadmap

- Generalization
- Unsupervised learning
- Summary

### Evaluation and test discipline

- $D_{\text{train}}$
- Learner
- How good is the predictor  $f$ ?
- Key idea: the real learning objective
- Our goal is to minimize error on unseen future examples.
- Don't have unseen examples; next best thing:
  - Definition: test set
  - Test set  $D_{\text{test}}$  contains examples not used for training.

### Generalization

- When will a learning algorithm generalize well?
- $D_{\text{train}}$
- $D_{\text{test}}$

### Bias/variance lens

- All predictors
- Learning
- $f^*$
- approx. error
- Feature extraction
- est. error
- $\hat{f}$
- Approximation error: how good is the hypothesis class?
- Estimation error: how good is the learned predictor relative to the potential of the hypothesis class?
- $\text{Err}(\hat{f}) - \text{Err}(g)$
- $+ \text{Err}(g) - \text{Err}(f^*)$

### Controlling model capacity

- All predictors
- Learning
- $f^*$
- approx. error
- Feature extraction
- est. error

- $\hat{f}$
- As the hypothesis class size increases...
- Approximation error decreases because:
  - taking min over larger set
- Estimation error increases because:
  - harder to estimate something more complex

### Mitigation: dimensionality

- $w$  in  $R^d$
- Reduce the dimensionality  $d$ :

### Mitigation: regularization

- $w$  in  $R^d$
- Reduce the norm (length)  $\|w\|$ :
- [whiteboard:  $x^T w \rightarrow w^T x$ ]

### Hyperparameters and tuning

- Definition: hyperparameters
- Properties of the learning algorithm (features, regularization parameter  $\lambda$ , number of iterations  $T$ , step size  $\eta$ , etc.).
- How do we choose hyperparameters?
- Choose hyperparameters to minimize  $D_{\text{train}}$  error? No - solution would be to include all features, set  $\lambda = 0$ ,  $T \rightarrow \infty$ .
- Choose hyperparameters to minimize  $D_{\text{test}}$  error? No - choosing based on  $D_{\text{test}}$  makes it an unreliable estimate of error!

### Development cycle

- Problem: simplified named-entity recognition
- Input: a string  $x$  (e.g., Governor [Gavin Newsom] in)
- Output:  $y$ , whether  $x$  contains a person or not (e.g., +1)
- Algorithm: recipe for success
- Split data into train, val, test
- Look at data to get intuition
- Repeat:
  - Implement feature / adjust hyperparameters
  - Run learning algorithm
  - Sanity check train and val error rates, weights
  - Look at errors to brainstorm improvements
- Run on test set to get final error rates

### Unsupervised learning overview

- Data has lots of rich latent structures; want methods to discover
- this structure automatically.

## Clustering

- Definition: clustering
- Input: training set of input points
- $D_{\text{train}} = \{x_1, \dots, x_n\}$
- Output: assignment of each point to a cluster
- $[z_1, \dots, z_n]$  where  $z_i \in \{1, \dots, K\}$
- Intuition: Want similar points to be in same cluster, dissimilar points to be in different clusters
- [whiteboard]

## K-means objective

- Setup:
- Each cluster  $k = 1, \dots, K$  is represented by a centroid  $\mu_k$  in  $\mathbb{R}^d$
- Intuition: want each point  $\phi(x_i)$  close to its assigned centroid  $\mu_{z_i}$
- Objective function:
- $\|\phi(x_i) - \mu_{z_i}\|^2$
- $\text{Loss}_{\text{kmeans}}(z, \mu) =$
- $\sum_{i=1}^n$
- Need to choose centroids  $\mu$  and assignments  $z$  jointly

## K-means algorithm

- $\min_z$
- $\min_{\mu}$
- $\mu \text{ Loss}_{\text{kmeans}}(z, \mu)$
- Key idea: alternating minimization
- Tackle hard problem by solving two easy problems.

## Local minima

- K-means is guaranteed to converge to a local minimum, but is not guaranteed to find the global minimum.
- [demo: getting stuck in local optima, seed = 100]
- Solutions:
- Run multiple times from different random initializations
- Initialize with a heuristic (K-means++)

## Embeddings and vectors

- [Mikolov et al., 2013]

## Challenges

- Capabilities:
- More complex prediction problems (translation, generation)
- Unsupervised learning: automatically discover structure
- Responsibilities:



- Feedback loops: predictions affect user behavior, which generates
- data
- Fairness: build classifiers that don't discriminate?
- Privacy: can we pool data together
- Interpretability: can we understand what algorithms are doing?

## Summary

- Feature extraction (think hypothesis classes) [modeling]
- Prediction (linear, neural network, k-means) [modeling]
- Loss functions (compute gradients) [modeling]
- Optimization
  - (stochastic
  - gradient,
  - alternating
  - minimization)
- [learning]
- Generalization (think development cycle) [modeling]