Universidade Federal de Ouro Preto Lecture Notes Graphs

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Source

• Super Study Guide - Graphs (https://superstudy.guide/algorithms-data-structures/graphs-trees/graphs)

1 Graphs

2 Graphs in C++

2.1 Adjacency list

```
1 #include <iostream>
2 #include <unordered_map>
3 #include <vector>
4 #include <stack>
5 #include <algorithm>
7 using namespace std;
9 class Graph {
10 private:
      unordered_map < string , vector < pair < string , int >>> adj_list;
12
13 public:
      void add_node(string node) {
14
          if (adj_list.find(node) == adj_list.end()) {
15
16
               adj_list[node] = {};
17
      }
18
19
      void add_edge(string node1, string node2, int weight = 1) {
20
21
           add_node(node1);
22
           add_node(node2);
           adj_list[node1].push_back({node2, weight});
23
           adj_list[node2].push_back({node1, weight});
24
26
      void remove_edge(string node1, string node2) {
27
28
           auto it = find_if(adj_list[node1].begin(), adj_list[node1].end(),
                              [node2](const pair<string, int>& p) {
29
                                  return p.first == node2;
                              });
31
           if (it != adj_list[node1].end()) {
32
               adj_list[node1].erase(it);
33
34
           it = find_if(adj_list[node2].begin(), adj_list[node2].end(),
35
                         [node1](const pair<string, int>& p) {
36
                             return p.first == node1;
```

```
});
          if (it != adj_list[node2].end()) {
39
40
               adj_list[node2].erase(it);
41
42
43
      void remove_node(string node) {
44
          adj_list.erase(node);
          for (auto& [other_node, neighbours] : adj_list) {
46
               auto it = find_if(neighbours.begin(), neighbours.end(),
                                 [node](const pair<string, int>& p) {
48
                                     return p.first == node;
49
50
                                 });
               if (it != neighbours.end()) {
51
52
                   neighbours.erase(it);
               7
53
54
          }
      }
55
      bool is_path(string node1, string node2) {
58
          unordered_set < string > visited;
          stack<string> st;
59
60
          st.push(node1);
          while (!st.empty()) {
61
62
               string node = st.top();
               st.pop();
63
               if (node == node2) {
                  return true;
65
66
               if (visited.find(node) == visited.end()) {
67
                  visited.insert(node);
68
69
                   for (auto& [neighbour, weight] : adj_list[node]) {
                       st.push(neighbour);
70
71
72
              }
73
74
          return false;
      }
75
76 };
77
78 int main() {
79
      Graph g;
      80
81
      for (auto& [node, neighbours] : g.adj_list) {
82
83
          cout << node << ": ";
          for (auto& [neighbour, weight] : neighbours) {
84
               cout << "(" << neighbour << ", " << weight << ") ";
85
86
          cout << endl;</pre>
87
88
      // Output: A: (B, 1)
89
                 B: (A, 1) (C, 1)
90
      //
      //
                 C: (B, 1)
91
92
      g.add_edge("A", "D"); // add an edge between nodes 'A' and 'D'
93
      for (auto& [node, neighbours] : g.adj_list) {
94
          cout << node << ": ";
95
          for (auto& [neighbour, weight] : neighbours) {
96
               cout << "(" << neighbour << ", " << weight << ") ";
97
98
          cout << endl;</pre>
99
      }
```

2.2 Adjacency matrix

```
#include <iostream>
2 #include <vector>
3 using namespace std;
5 class Graph {
6 public:
      Graph(int num_nodes) : num_nodes(num_nodes), adj_matrix(num_nodes, vector<int>(
      num_nodes, 0)) {}
      void add_node() {
9
           num_nodes++;
10
11
           for (auto& row : adj_matrix) {
               row.push_back(0);
12
13
           adj_matrix.push_back(vector<int>(num_nodes, 0));
14
15
16
      void add_edge(int node1, int node2, int weight = 1) {
17
           adj_matrix[node1][node2] = weight;
18
           adj_matrix[node2][node1] = weight;
19
20
21
      void remove_edge(int node1, int node2) {
22
23
           adj_matrix[node1][node2] = 0;
           adj_matrix[node2][node1] = 0;
24
25
26
      void remove_node(int node) {
27
28
           num_nodes--;
           adj_matrix.erase(adj_matrix.begin() + node);
29
30
           for (auto& row : adj_matrix) {
               row.erase(row.begin() + node);
31
32
      }
33
34
      bool is_path(int node1, int node2) {
35
           vector < bool > visited(num_nodes, false);
36
37
           vector < int > queue;
           queue.push_back(node1);
38
           visited[node1] = true;
39
40
           while (!queue.empty()) {
41
               int current_node = queue.front();
               queue.erase(queue.begin());
43
               if (current_node == node2) {
44
45
                   return true;
46
               for (int neighbor = 0; neighbor < num_nodes; neighbor++) {</pre>
47
                   int weight = adj_matrix[current_node][neighbor];
48
49
                   if (weight > 0 && !visited[neighbor]) {
                        visited[neighbor] = true;
50
51
                        queue.push_back(neighbor);
                   }
               }
53
           }
55
           return false;
56
      }
57
58
```

```
59 private:
       int num_nodes;
60
61
       vector < vector < int >> adj_matrix;
62 };
63
64 int main() {
       Graph g(3); // create a graph with 3 nodes
65
       g.add_edge(0, 1); // add an edge between nodes 0 and 1
       g.add_edge(1, 2); // add an edge between nodes 1 and 2
67
68
       for (auto row : g.adj_matrix) {
           for (auto val : row) {
69
                cout << val << " ";
70
71
           cout << endl;</pre>
72
       } // print the adjacency matrix
73
       // Output: 0 1 0
74
75
                   1 0 1
       //
                   0 1 0
76
       g.add_node(); // add a node to the graph
       g.add_edge(0, 3); // add an edge between nodes 0 and 3
79
       for (auto row : g.adj_matrix) {
80
81
           for (auto val : row) {
                cout << val << " ";
82
83
           cout << endl;</pre>
84
       } // print the adjacency matrix
       // Output: 0 1 0 1
86
87
       //
       //
                   0 1 0 0
88
       //
                   1 0 0 0
89
90
       g.remove_edge(0, 3); // remove the edge between nodes 0 and 3 g.remove_node(2); // remove node 2 from the graph
91
92
93
       for (auto row : g.adj_matrix) {
           for (auto val : row) {
94
95
                cout << val << " ";
96
            cout << endl;</pre>
97
       } // print the adjacency matrix
98
99 }
```

Listing 2: Example 1 - Graph as Adjacency List C++

3 Graphs in Python

3.1 Adjacency list

```
1 class Graph:
      def __init__(self):
          self.adj_list = {}
      def add_node(self, node):
           if node not in self.adj_list:
6
               self.adj_list[node] = []
      def add_edge(self, node1, node2, weight=1):
          self.add_node(node1)
10
          self.add_node(node2)
11
          self.adj_list[node1].append((node2, weight))
12
13
          self.adj_list[node2].append((node1, weight))
      def remove_edge(self, node1, node2):
          for i, (node, weight) in enumerate(self.adj_list[node1]):
16
```

```
if node == node2:
17
                  del self.adj_list[node1][i]
18
19
                  break
          for i, (node, weight) in enumerate(self.adj_list[node2]):
20
              if node == node1:
21
22
                  del self.adj_list[node2][i]
                  break
23
24
      def remove_node(self, node):
25
26
          del self.adj_list[node]
          for other_node in self.adj_list:
27
              for i, (n, w) in enumerate(self.adj_list[other_node]):
28
29
                  if n == node:
                      del self.adj_list[other_node][i]
30
                      break
31
32
      def is_path(self, node1, node2):
33
34
          visited = set()
          stack = [node1]
35
          while stack:
              node = stack.pop()
37
              if node == node2:
38
39
                  return True
              if node not in visited:
40
                  visited.add(node)
41
                  stack.extend(neighbour for neighbour, weight in self.adj_list[node])
42
43
          return False
44
45 # example usage
46 g = Graph()
47 g.add_edge('A', 'B') # add an edge between nodes 'A' and 'B'
48 g.add_edge('B', 'C') # add an edge between nodes 'B' and 'C'
49 print(g.adj_list) # print the adjacency list
50 # Output: {'A': [('B', 1)], 'B': [('A', 1), ('C', 1)], 'C': [('B', 1)]}
52 g.add_edge('A', 'D') # add an edge between nodes 'A' and 'D'
53 print(g.adj_list) # print the adjacency list
54 # Output: {'A': [('B', 1), ('D', 1)], 'B': [('A', 1), ('C', 1)], 'C': [('B', 1)], 'D':
       [('A', 1)]
56 g.remove_edge('A', 'D') # remove the edge between nodes 'A' and 'D'
_{58} print(g.adj_list) # print the adjacency list
59 # Output: {'A': [], 'C': []}
61 print(g.is_path('A', 'C')) # check if a path exists between nodes 'A' and 'C'
62 # Output: False
63 print(g.is_path('A', 'D')) # check if a path exists between nodes 'A' and 'D'
64 # Output: False
^{65} print(g.is_path('D', 'A')) # check if a path exists between nodes 'D' and 'A'
66 # Output: True
```

Listing 3: Example 1 - Graph as Adjacency List Python

3.2 Adjacency matrix

```
class Graph:
def __init__(self, num_nodes):
    self.num_nodes = num_nodes
self.adj_matrix = [[0 for _ in range(num_nodes)] for _ in range(num_nodes)]

def add_node(self):
    self.num_nodes += 1
for row in self.adj_matrix:
    row.append(0)
```

```
self.adj_matrix.append([0 for _ in range(self.num_nodes)])
10
11
12
      def add_edge(self, node1, node2, weight=1):
           self.adj_matrix[node1][node2] = weight
13
           self.adj_matrix[node2][node1] = weight
14
15
      def remove_edge(self, node1, node2):
16
           self.adj_matrix[node1][node2] = 0
17
           self.adj_matrix[node2][node1] = 0
18
19
      def remove_node(self, node):
20
           self.num_nodes -= 1
21
22
           self.adj_matrix.pop(node)
           for row in self.adj_matrix:
23
               row.pop(node)
25
      def is_path(self, node1, node2):
26
           visited = [False] * self.num_nodes
27
           queue = [node1]
28
           visited[node1] = True
29
30
31
           while queue:
               current_node = queue.pop(0)
32
               if current_node == node2:
33
                   return True
34
               for neighbor, weight in enumerate(self.adj_matrix[current_node]):
35
                    if weight > 0 and not visited[neighbor]:
                        visited[neighbor] = True
37
                        queue.append(neighbor)
38
39
           return False
40
41
42
43 # example usage
44 g = Graph(3) # create a graph with 3 nodes
45 g.add_edge(0, 1) # add an edge between nodes 0 and 1
46 g.add_edge(1, 2) # add an edge between nodes 1 and 2
47 print(g.adj_matrix) # print the adjacency matrix
48 # Output: [[0, 1, 0], [1, 0, 1], [0, 1, 0]]
50 g.add_node() # add a node to the graph
{\tt 51} g.add_edge(0, 3) # add an edge between nodes 0 and 3
52 print(g.adj_matrix) # print the adjacency matrix
53 # Output: [[0, 1, 0, 1], [1, 0, 1, 0], [0, 1, 0, 0], [1, 0, 0, 0]]
55 g.remove_edge(0, 3) # remove the edge between nodes 0 and 3
56 g.remove_node(2) # remove node 2 from the graph
57 print(g.adj_matrix) # print the adjacency matrix
58 # Output: [[0, 1, 1], [1, 0, 0], [1, 0, 0]]
60 print(g.is_path(0, 2)) # check if a path exists between nodes 0 and 2
_{61} # Output: True
62 print(g.is_path(0, 1)) # check if a path exists between nodes 0 and 1
63 # Output: True
64 print(g.is_path(1, 2)) # check if a path exists between nodes 1 and 2
65 # Output: False
```

Listing 4: Example 1 - Graph as Matrix Python