

ALGORITHM *Backtrack*($X[1..i]$)

```
//Gives a template of a generic backtracking algorithm
```

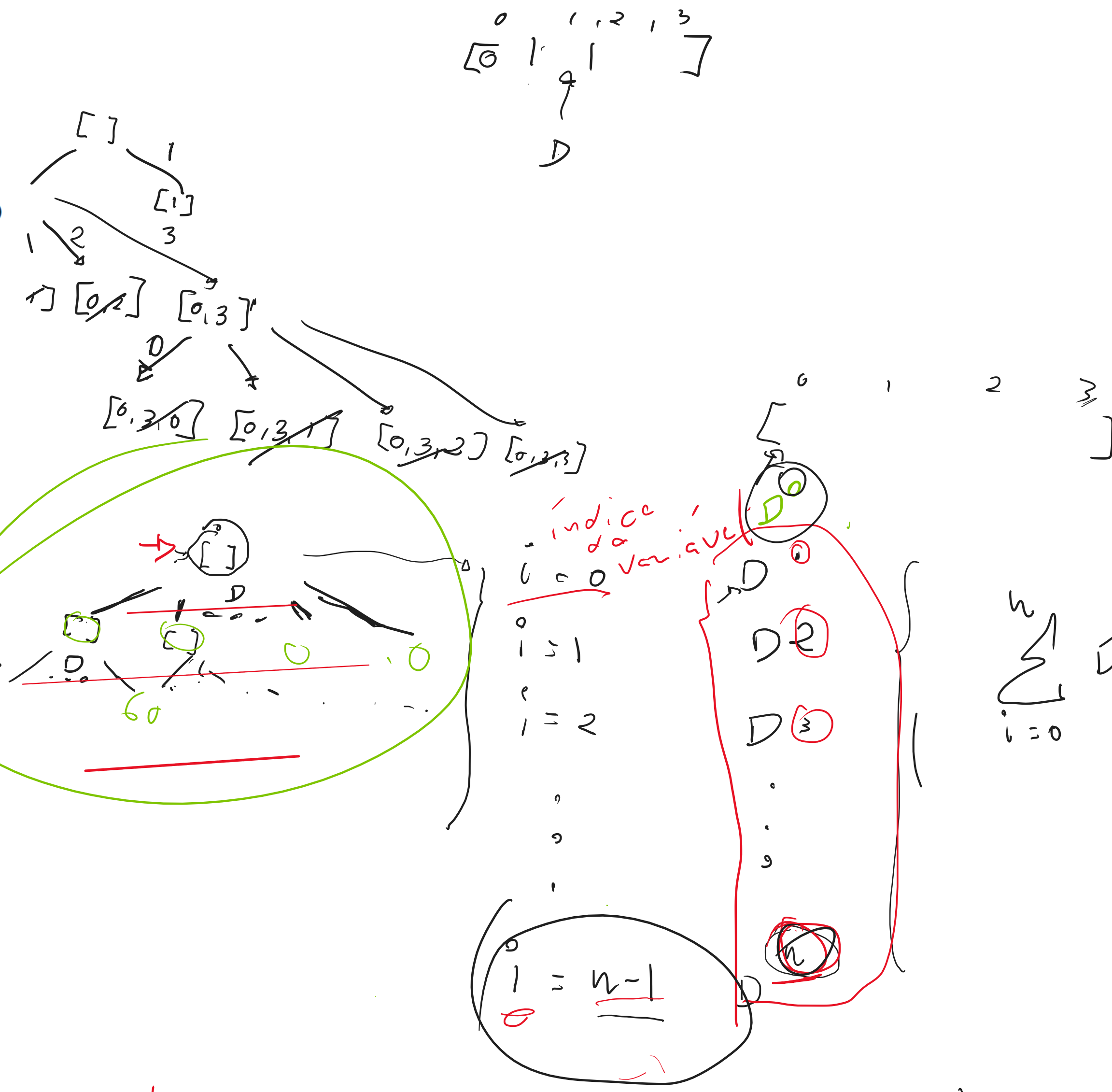
//Input: $X[1..i]$ specifies first i promising components of a solution

~~//Output: All the tuples representing the problem's solutions~~

if $X[1..i]$ is a solution **write** $X[1..i]$

```
else //see Problem 9 in this section's exercises
```

for each element $x \in S_{i+1}$ consistent with $X[1..i]$ and the constraints **do**

$$X[i + 1] \leftarrow x$$
$$\text{Backtrack}(X[1..i + 1])$$


$T(n, D) = \textcircled{D} T(n-1, D) + 1$ $T(0, D) = 1$

$$D(D^T(n - 2, p) + 1) + 1$$

$$= \underbrace{D(D(T(n-3) + 1) + 1)}_{\text{base case}} + 1$$

$$= \underbrace{D(D(D(D(T(n-4) + 1) + 1) + 1) + 1)}_{\text{base case}}$$

$$= D \left(D \left(D^2 T^{(n-4)} + D \right) + 1 \right) + 1$$

$$= D(D^3 T(n-4) + D^2 + D) + 1 + 1$$

$$= O^h T(n-4) + O^3 + O^2 + O + 1$$

$$= D^T (y - \hat{y}) + \sum_{j=0}^{n-1} D^j$$

$$= \cancel{D^n} \cancel{T(0)} + \sum_{j=0}^{n-1} D^j$$

$$= \sum_{j=0}^n D^j = \frac{1 - D^{n+1}}{1 - D}$$

$$= \frac{D^n(D+1) - D - 1}{D - 1}$$