

- **Row space** is span of all rows of  $A$ 
  - Equivalently,  $C(A^T)$
- **Left nullspace** is set of all vectors  $v$  such that  $v^T A = 0$ 
  - Equivalently,  $A^T v = 0$ , or  $N(A^T)$

We could calculate these by computing RREF of  $A^T$

- There is a way to calculate this all from a single RREF of  $A$  but will omit here

## Relationships

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- Both  $C(A)$  and  $N(A^T)$  live in  $\mathbb{R}^m$ 
  - Their dimensions add up to  $m$  and the subspaces are orthogonal to one another
  - That is, all vectors in  $C(A)$  are orthogonal to those in  $N(A^T)$
- Both  $C(A^T)$  and  $N(A)$  live in  $\mathbb{R}^n$ 
  - Dimensions also add to  $n$  and these are orthogonal