EECS 3421 M ASSIGNMENT #01

Team members:

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Part 1

1. Cannot be expressed.

2. $\pi_{\text{datelssued, timelssued}}(\text{Ticket}) \subseteq \pi_{\text{date, time}}(\text{Match})$

3. $\pi_{TID}(Ticket) \subseteq \pi_{capacity}(Stadium)$

4. $\rho_{T1} \text{ (Team)} \bowtie_{\text{ (T1.country = T2.country }} \land_{\text{ T1.coach } \neq \text{ T2.coach)}} \rho_{T2} \text{ (Team))}$

5. Cannot be expressed.

Note: for part 2, some of the assignment statements have names constituting underscores (_) between two words since names have been chosen in accordance to their assignments.

// lines are comments in the answers below

pairs that played.

Part 2

1.

```
// A is cross-product of every stadium and country.
1) A := \pi_{country}(Team) × \pi_{SID}(Stadium)
      // making country1 and MID pairs.
2) C1 := \rho_{country1} \rightarrow country_1 MID (\pi_{country1}, MID (competes))
      // making country2 and MID pairs.
3) C2 := \rho_{country2} \rightarrow country, MID(\pi_{country2}, MID(competes))
      // all countries who played is union of all opponents in the
      competes relation
4) all countries who played := C1 U C2
      // schema is :- all countries who played(country, MID)
5) stadium country played :=
                  \pi_{country, SID}(all countries who played \bowtie Match)
      // stadium country played consists of stadium-country
```

```
6) countries_not_all_stadium :=
                           A — (stadium country played)
        // countries_all_stadium is list of all countries who
        have played in every stadium
  7) countries all stadium :=
              \pi_{country}(A) - \pi_{country}(countries\_not\_all\_stadium)
2.
        Cannot be expressed.
3.
  1) A := \pi_{country}(Team) - \pi_{country1} ->country(competes)
  2) B := \pi_{country}(Team) - \pi_{country2}->country(competes)
        // C is countries that didn't play in any matches.
  3) C := \pi_{country}(Team) - (A U B)
        // Players no match represents players that didn't play any
        match
  4) Players no match := \pi_{PID}(Player \bowtie C)
```

4.

```
    A := π<sub>SID,MID</sub>(Stadium ⋈ Match)
    // A will confirm that A.SID represents the SID of stadium where at least one match took place.
    // B and C are used for cross-product below.
    B := ρ<sub>SID,MID</sub>→SID1,MID1(A)
    C := ρ<sub>SID,MID</sub>→SID2,MID2(A)
    // D lists all stadiums with more than one match.
    D := σ<sub>SID1</sub> = SID2 ^ MID1 ≠ MID2(B × C)
    stadium_exactly_one_match := π<sub>SID</sub>(Stadium) - ρ<sub>SID1</sub>→SID(π<sub>SID1</sub>(D))
```

5. Cannot be expressed.

```
1) list_of_players := \pi_{\text{fname, Iname, position, goals}}(Team \bowtie Player)
    //schema is :- list of players(fname, lname, position, goals)
2) D position players :=
                                 \pi_{\text{fname, Iname, goals}}(\sigma_{\text{position}} = "D"(\text{list\_of\_players}))
    // schema is :- D position(fname, Iname, goals)
3) D1 := \rho_{\text{fname, lname, goals}} \rightarrow f_{1, l_1, g_1}(D_\text{position})
4) D2 := \rho_{\text{fname, lname, goals}} \rightarrow f_{2, 12, g2}(D_\text{position})
5) all except max goals :=
                         \rho_{f1, |1} \rightarrow f_{name, |name}(\pi_{f1, |1}(\sigma_{g1 < g2}(D1 \times D2)))
6) max goal player :=
```

 $\pi_{\text{fname, Iname}}(\text{player}) - \text{all_except_max_goals}$

Part 7.1: getting the first-ticket

```
1) T := \pi_{TID, dateIssued, MID}(Ticket)
```

2) T1 :=
$$\rho_{TID, dateIssued, MID} \rightarrow TID1, d1, MID1$$
(T)

// schema is T1(TID1,d1,MID1)

3) T2 :=
$$\rho_{TID, dateIssued, MID} \rightarrow TID2, d2, MID2$$
(T)

// schema is T2(TID2,d2,MID2)

4) T3 :=
$$\pi_{TID1, d1, MID1}(\sigma_{d1 > d2}(T1 X T2))$$

5) first_ticket := T
$$- \rho_{TID1, d1, MID1} \rightarrow TID, dateIssued, MID$$
(T3)

Part 7. 2: computing winner of match of first ticket

1) opponents :=

 $\pi_{country1, country2, goals1, goals2}$ (competes \bowtie first_ticket)

// winner_country will have union meaning either of two

2) winner country:=

$$(\rho_{country1} \rightarrow country)(\pi_{country1}(\sigma_{goals1} > goals2(opponent))) \ U$$

$$(\rho_{country2} \rightarrow country)(\pi_{country2}(\sigma_{goals2} > goals1(opponent)))$$

- 1) Players_Spain := π_{fname, Iname, goals}(Player ⋈ country = "Spain" Team)
 // schema is :- Players_Spain(fname, Iname, goals)
- 2) P1 := $\rho_{\text{fname, Iname, goals}} \rightarrow f1, I1, g1$ (Players_Spain)
- 3) P2 := $\rho_{\text{fname, Iname, goals}} = \rho_{\text{flame, Iname, goals}} = \rho_{\text{$
- 4) Players_Spain_except_highest := $\rho_{f1, l1, g1}$ -> fname, lname, goals $(\pi_{f1, l1, g1})$ ($\sigma_{g1 < g2}(P1 \times P2)$)
- 5) P3 := $\rho_{\text{fname, Iname, goals}} \rightarrow f_{1, I1, g1}$ (Players_Spain_except_highest)
- 6) P4 := $\rho_{\text{fname, Iname, goals}} \rightarrow f_{2, 12, g2}$ (Players_Spain_except_highest)
- 7) P5 := $\pi_{f1, l1, g1}(\sigma_{g1 < g2}(P3 X P4))$
- 8) Players_Spain_second_highest := $\pi_{\text{fname, Iname}} \text{ (Players_Spain_except_highest } - \rho_{\text{f1, I1, g1}} -> \text{fname, Iname, goals} \text{ (P5))}$

```
9.
```

1) A :=
$$\pi_{MID, date}(Match)$$

2) B :=
$$\pi_{TID, dateIssued, MID}$$
(Ticket)

3) Ticket_sold_date_match :=
$$\pi_{MID, TID}(\sigma_{date = dateIssued}(A \bowtie B))$$

4) T1 :=
$$\rho_{MID, TID} \rightarrow MID1, TID1$$
 (Ticket_sold_date_match)

5) T2 :=
$$\rho_{\text{MID, TID}} \rightarrow \text{MID2, TID2}$$
 (Ticket_sold_date_match)

6) at_least_two_tickets :=
$$\rho_{\text{MID1}-> \text{MID}}(\pi_{\text{MID1}}(\sigma_{\text{MID1} = \text{MID2}} \land_{\text{TID1} \neq \text{TID2}}(\text{T1} \times \text{T2})))$$

Part 10.1: all teams who have won at least one match

```
1) countries list := \pi_{country}(Team)
      // schema is :- countries list (country)
2) opponent_1 := \rho_{country->C1}(countries_list)
3) opponent_2 := \rho_{country-> C2} (countries list)
4) country pairs := opponent 1 X opponent 2
      //schema is :- country pairs (C1, C2)
5) Match_list := \pi_{country1, country2, goals1, goals2} (competes)
      //schema is :- Match list (country1, country2, goals1,
      goals2)
6) Countries who played :=
            country pairs \bowtie_{c1 = country1} \land_{c2 = country2} (competes)
      // schema is :- countries who played(c1, c2, country1,
      country2, goals1, goals2)
```

```
7) country lost all := \pi_{country1}(\sigma_{goals1 < goals2}(countries who played)
             // schema is :- coutnry lost all (country1)
      8) countries win at least one match :=
             \pi_{country}(Team) - \rho_{country1} -> country(country lost all)
             // schema is :- countries won at least one match
             (country)
Part 10.2:
      1) winning team players :=
                   \pi_{PID, position, goals, country} (players \bowtie
                                       countries win at least one match)
      2) W1 :=
       PPID, position, goals, country -> PID1, P1, G1,C1 (winning_team_players)
      3) W2 :=
       PPID, position, goals, country -> PID2, P2, G2, C2 (winning_team_players)
      4) players_without_highest :=
                          (\sigma_{G1 < G2}(\sigma_{C1 = C2} \land PID1 \neq PID2(W1 \times W2)))
             //schema is :- players without highest (PID1, P1, G1, C1,
```

PID2, P2, G2, C2)

5) highest_goal_players :=
$$\pi_{country, \ position, \ goals} \ (\ winning_team_players - \\ \rho_{PID1, \ P1, \ G1, \ C1} -> PID, \ position, \ goals, \ country} (\pi_{PID1, \ P1, \ G1, \ C1}$$

$$(Players_without_highest)))$$