

$$|\beta^R| = 2^{\omega}$$