$$\leq w(\beta(\kappa)) = 2^{\kappa} = 2^{n(\beta(\kappa))}$$