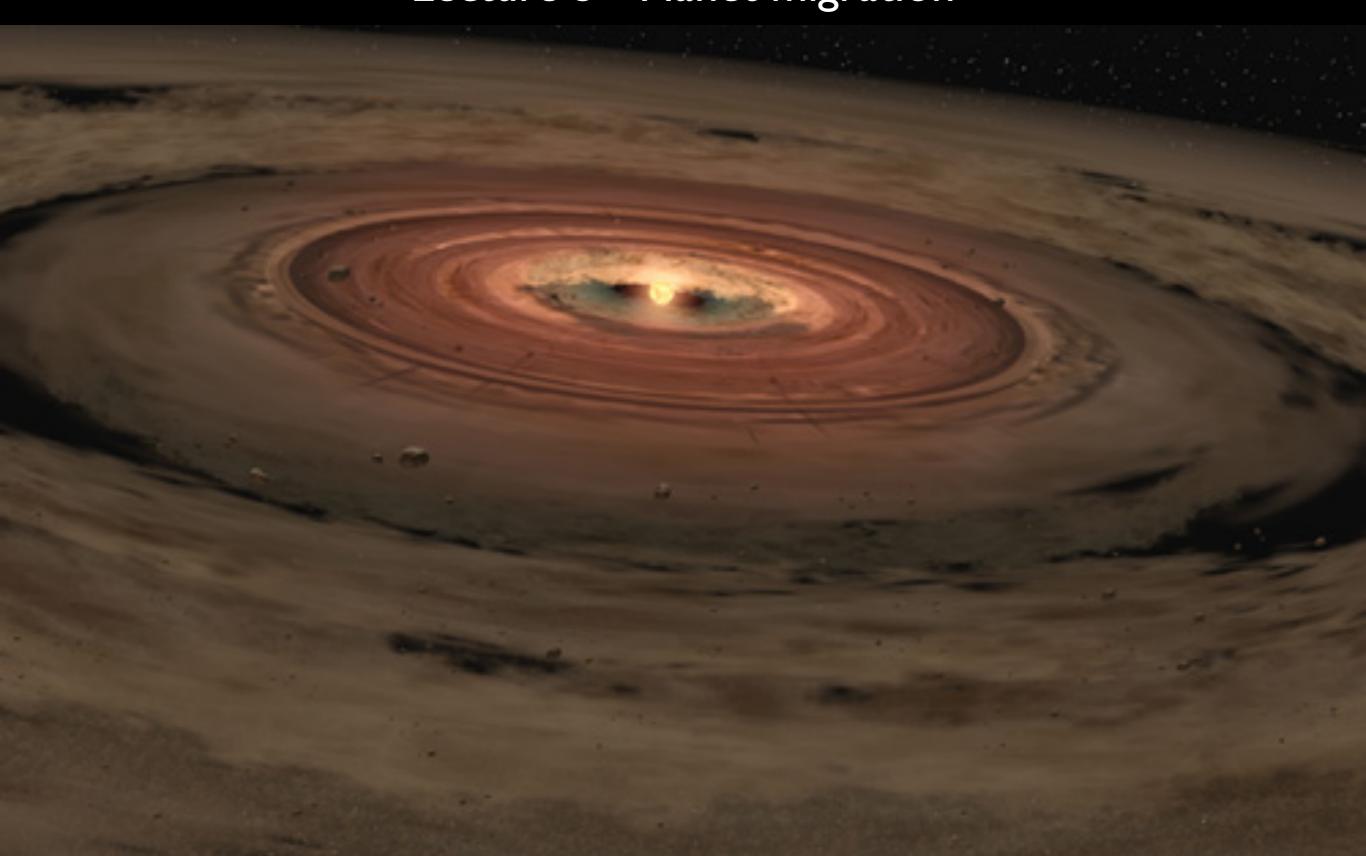
### Astrophysics of Planet Formation

Lecture 5 - Planet migration



#### Course Outline

- 5 Lectures, 2 hours each (with a break in the middle!).
  - 1) Observations of planetary systems
  - 2) Protoplanetary discs
  - 3) Dust dynamics & planetesimal formation
  - 4) Planet formation
  - 5) Planetary dynamics
- Notes for each lecture will be placed on the course home page in advance - you may find it useful to annotate these as we go.
- These slides will also be posted online.
- Textbooks: Armitage Astrophysics of planet formation (CUP).
   Protostars & Planets series (VI 2014; VII 2023)



### Resonant Torques

- Full perturbation analysis finds that the total torque is the sum of the torques at **resonances**.
- Co-rotation resonance:

$$\Omega(R) = \Omega_{\rm p}$$

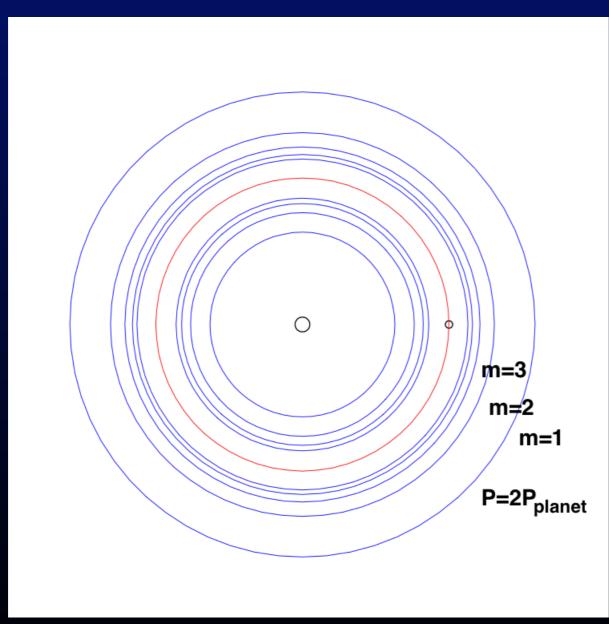
Lindblad resonances:

$$m[\Omega(R) - \Omega_{\rm p}] = \pm \kappa(R)$$

$$R_{\rm L} = \left(1 \pm \frac{1}{m}\right)^{2/3} a$$

### Resonant Torques

 Circular disc has one co-rotation resonance and a "comb" of Lindblad resonances:



$$R_{\rm L} = \left(1 \pm \frac{1}{m}\right)^{2/3} a$$

Figure from Armitage (2007)

### Resonant Torques

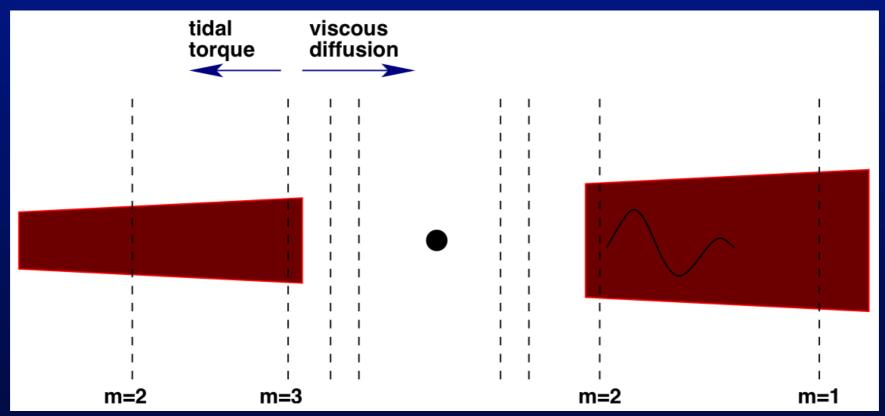
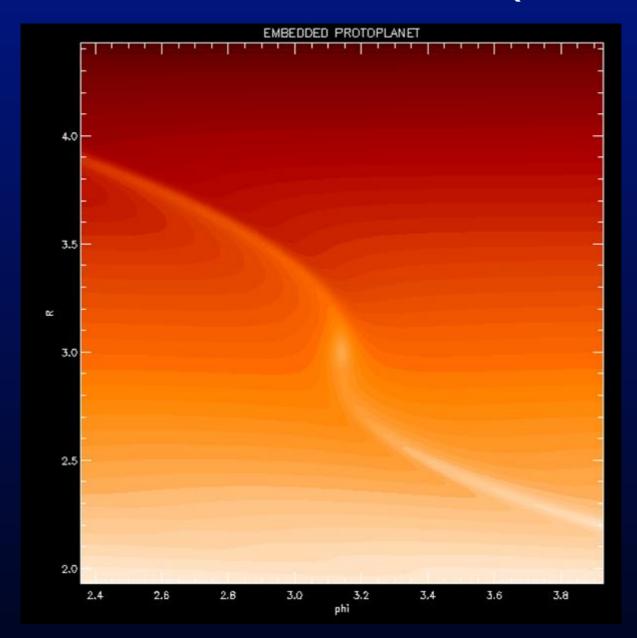


Figure from Armitage (2007)

- Torques repel disc gas from region close to planet, but viscosity opposes this. A sufficiently massive planet can open a gap in the disc.
- For typical disc parameters, the gap-opening mass is a few times the mass of Saturn.

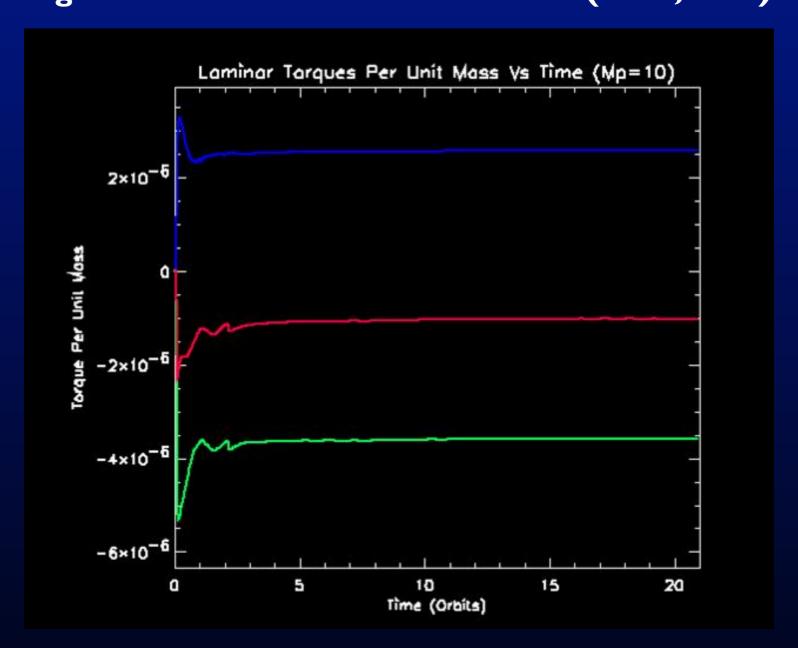
No gap = Type I migration

Gap = Type II migration



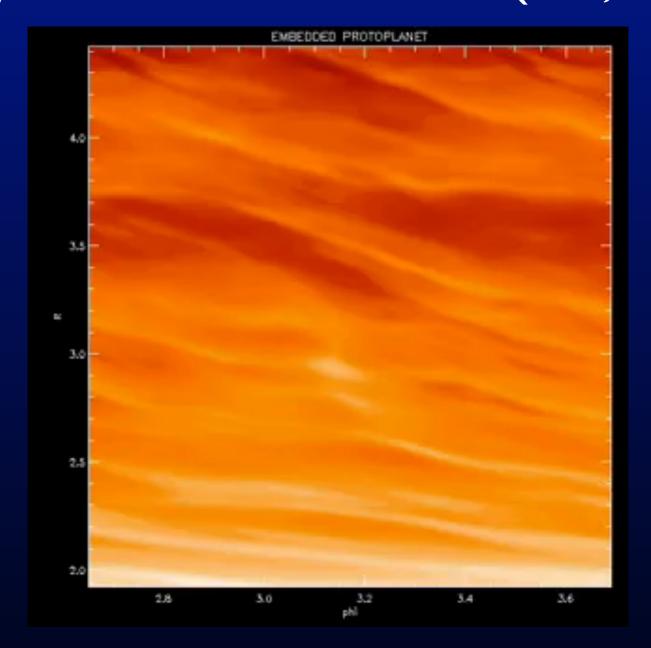
#### 10M<sub>®</sub> planet in laminar disc:

Spiral density waves launched from resonances. Well-defined, stable torques drive steady migration.



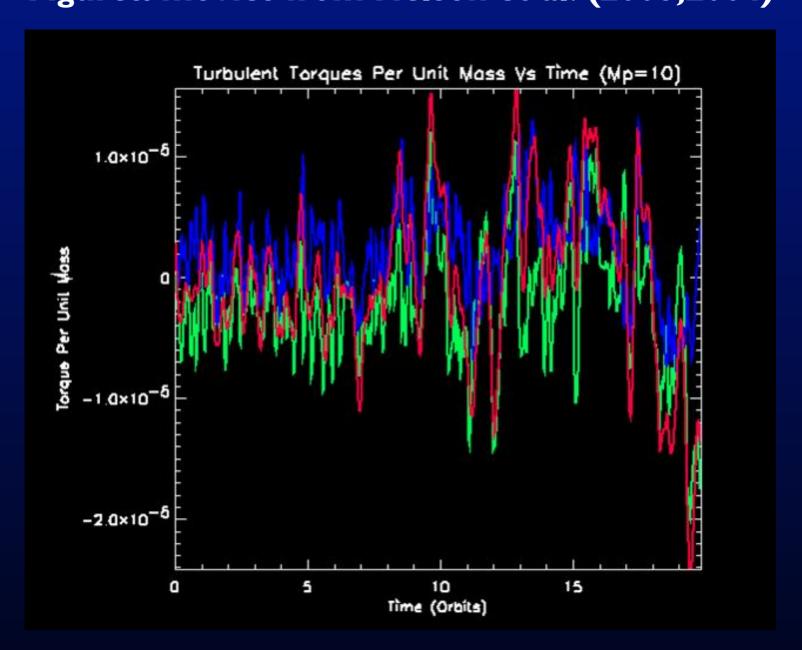
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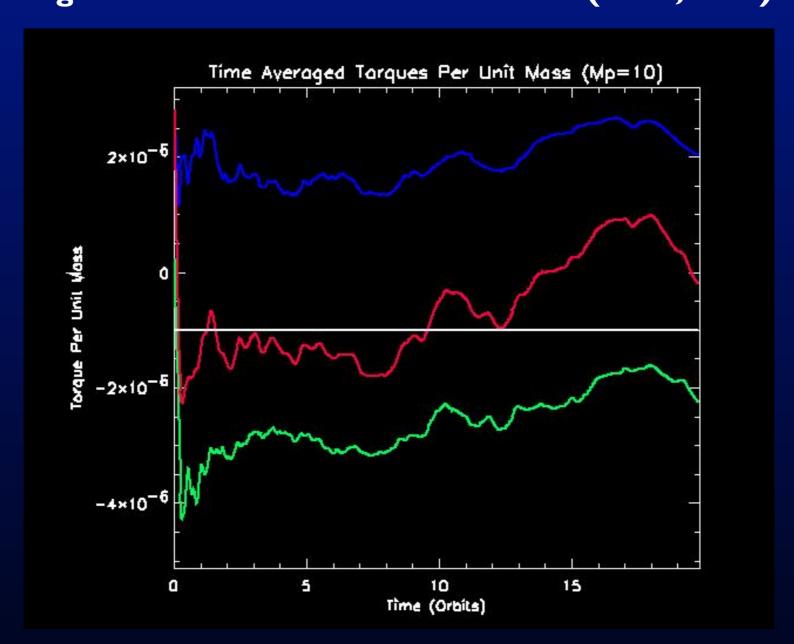
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Spiral density waves dwarfed by turbulent fluctuations. Torques are very variable, leading to stochastic migration.



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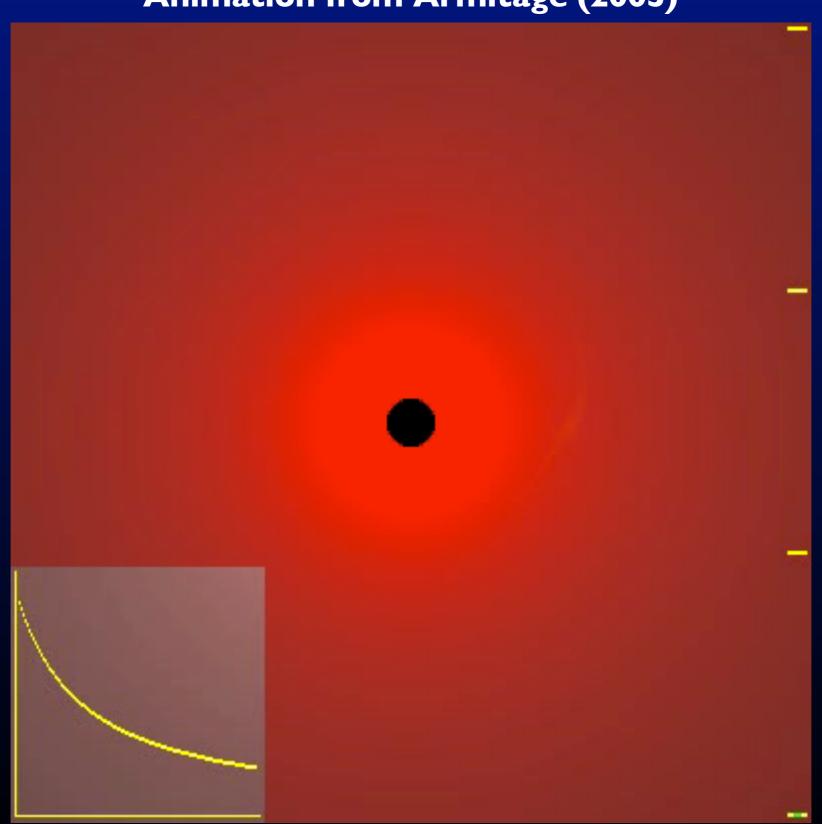


#### 10M<sub>®</sub> planet in MRI-turbulent disc:

Spiral density waves dwarfed by turbulent fluctuations. Torques are very variable, leading to stochastic migration.

### Type I/II migration

**Animation from Armitage (2005)** 



### Gap-opening conditions

Thermal condition:

$$R_{\rm h} = Rq^{1/3} \gtrsim H$$
$$q \gtrsim \left(\frac{H}{R}\right)^3$$

Viscous condition:

$$q \gtrsim \left(\frac{c_{\rm s}}{a_{\rm p}\Omega_{\rm p}}\right)^2 \alpha^{1/2}$$

Combined condition (e.g., Crida+ 2006):

$$\frac{(H/R)}{q^1/3} + \frac{50\alpha(H/R)^2}{q} \lesssim 1$$



### Resonant capture

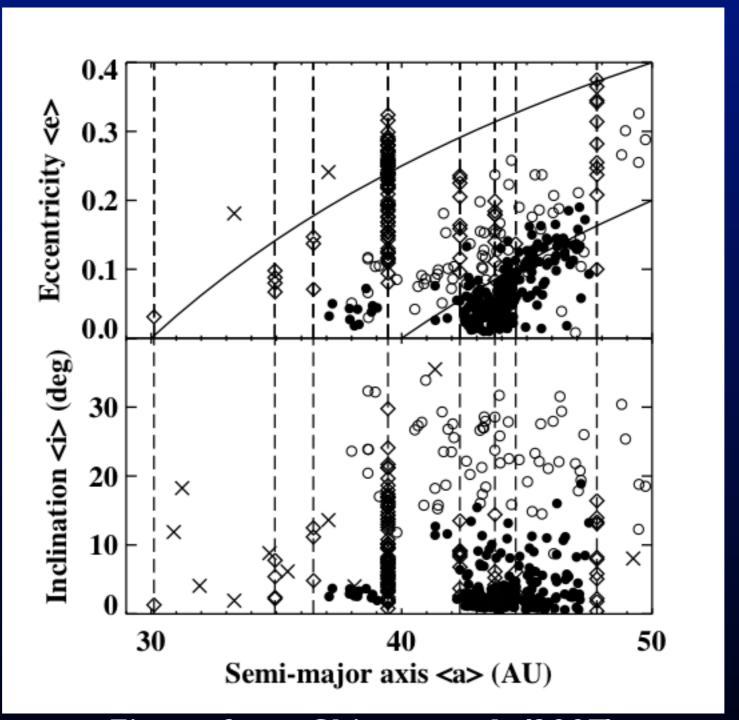
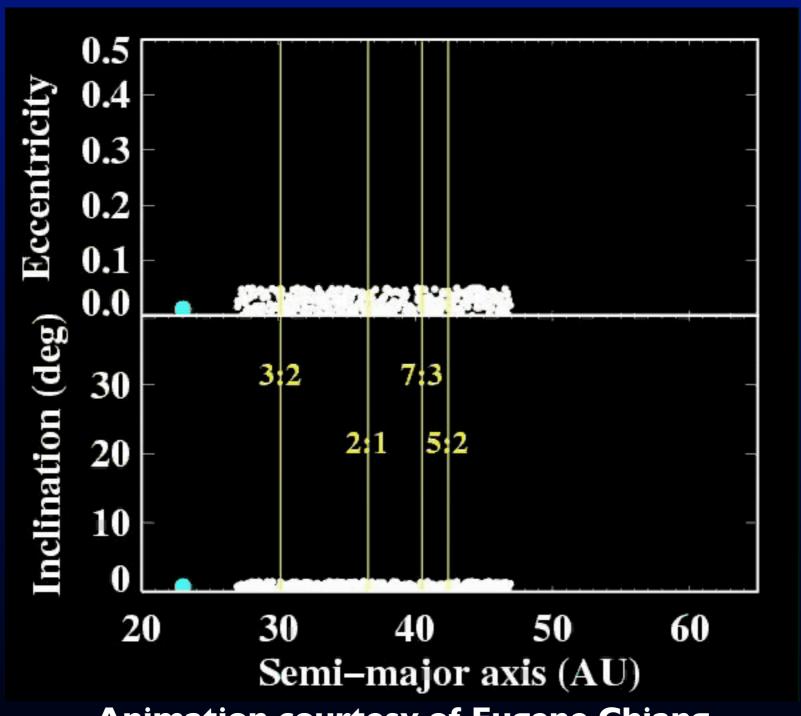


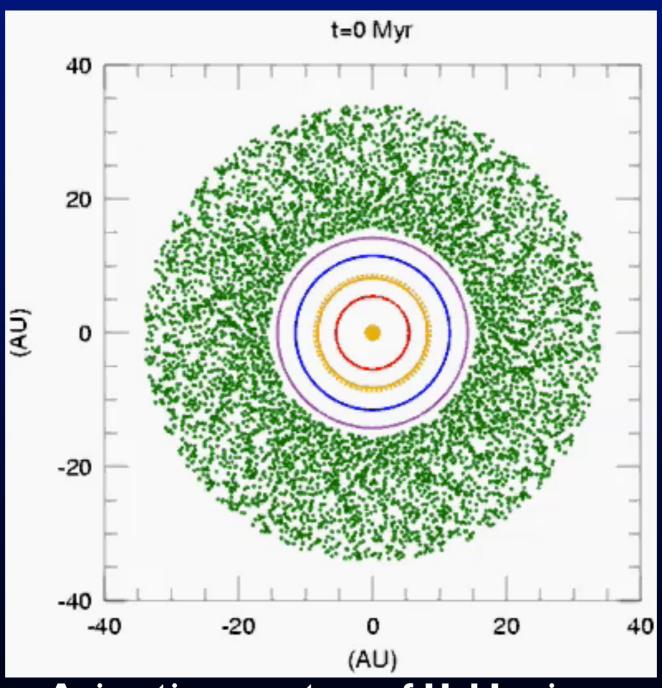
Figure from Chiang et al. (2007)

### Resonant capture



**Animation courtesy of Eugene Chiang** 

### The Nice Model



**Animation courtesy of Hal Levison** 

### The Nice Model

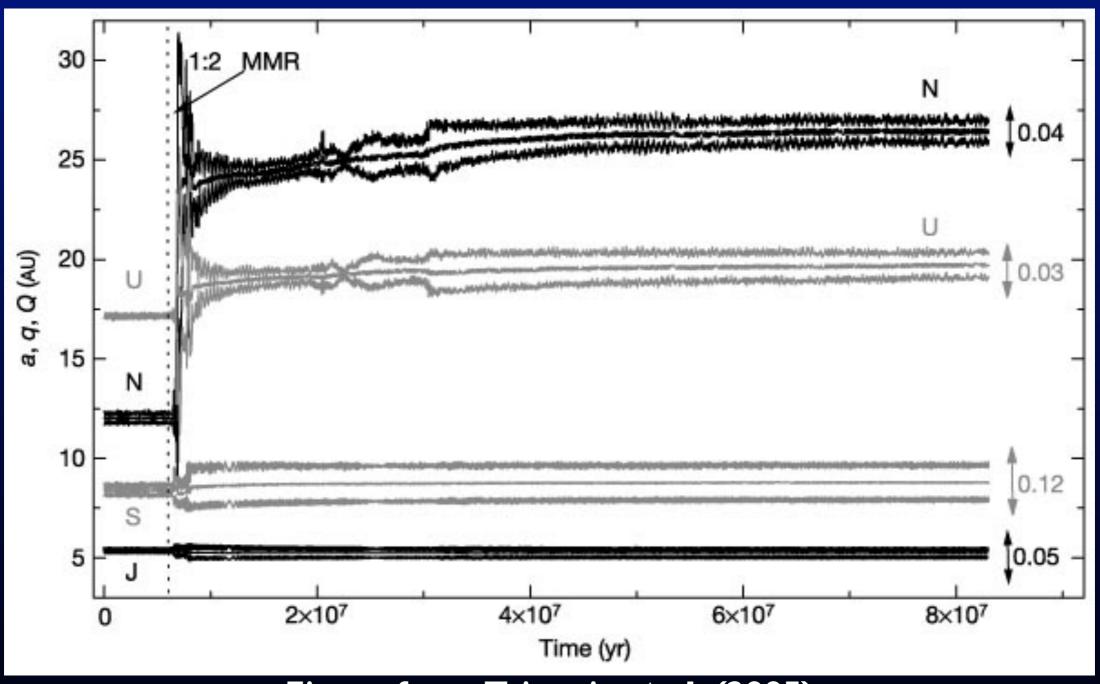


Figure from Tsiganis et al. (2005)

